

Elements of Programming

Principles of Functional Programming

Elements of Programming

Every non-trivial programming language provides:

- primitive expressions representing the simplest elements
- ways to *combine* expressions
- ways to abstract expressions, which introduce a name for an expression by which it can then be referred to.

The Read-Eval-Print Loop

Functional programming is a bit like using a calculator

An interactive shell (or REPL, for Read-Eval-Print-Loop) lets one write expressions and responds with their value.

The Scala REPL can be started by simply typing

> scala

Expressions

Here are some simple interactions with the REPL

```
scala> 87 + 145
res0: Int = 232
```

Functional programming languages are more than simple calcululators because they let one define values and functions:

```
scala> def size = 2
size: Int

scala> 5 * size
res1: Int = 10
```

Evaluation

A non-primitive expression is evaluated as follows.

- 1. Take the leftmost operator
- 2. Evaluate its operands (left before right)
- 3. Apply the operator to the operands

A name is evaluated by replacing it with the right hand side of its definition

The evaluation process stops once it results in a value

A value is a number (for the moment)

Later on we will consider also other kinds of values

```
def pi = 3.14159
def radius = 10
(2 * pi) * radius
```

```
(2 * pi) * radius
```

```
(2 * 3.14159) * radius
```

```
(2 * pi) * radius
```

```
6.28318 * radius
```

```
(2 * pi) * radius
```

```
6.28318 * 10
```

Here is the evaluation of an arithmetic expression:

```
(2 * pi) * radius
```

6.28318 * radius

6.28318 * 10

62.8318

Parameters

Definitions can have parameters. For instance: scala > def square(x: Double) = x * xsquare: (x: Double)Double scala> square(2) 4.0 scala > square(5 + 4)81.0 scala> square(square(4)) 256.0 scala> def sumOfSquares(x: Double, y: Double) = square(x) + square(y) sumOfSquares: (x: Double, y: Double)Double

Parameter and Return Types

Function parameters come with their type, which is given after a colon

```
def power(x: Double, y: Int): Double = ...
```

If a return type is given, it follows the parameter list.

Primitive types are as in Java, but are written capitalized, e.g:

```
Int 32-bit integers
```

Double 64-bit floating point numbers

Boolean boolean values true and false

Evaluation of Function Applications

Applications of parameterized functions are evaluated in a similar way as operators:

- 1. Evaluate all function arguments, from left to right
- 2. Replace the function application by the function's right-hand side, and, at the same time
- 3. Replace the formal parameters of the function by the actual arguments.

sumOfSquares(3, 2+2)

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
9 + 4 * 4
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
9 + 4 * 4
9 + 16
```

```
sumOfSquares(3, 2+2)
sumOfSquares(3, 4)
square(3) + square(4)
3 * 3 + square(4)
9 + square(4)
9 + 4 * 4
9 + 16
25
```

The substitution model

This scheme of expression evaluation is called the *substitution model*.

The idea underlying this model is that all evaluation does is *reduce an expression to a value*.

It can be applied to all expressions, as long as they have no side effects.

The substitution model is formalized in the λ -calculus, which gives a foundation for functional programming.

Termination

► Does every expression reduce to a value (in a finite number of steps)?

Termination

- ► Does every expression reduce to a value (in a finite number of steps)?
- ► No. Here is a counter-example

```
def loop: Int = loop
loop
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
```

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```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
9 + 4 * (2+2)
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
9 + 4 * (2+2)
9 + 4 * 4
```

The interpreter reduces function arguments to values before rewriting the function application.

One could alternatively apply the function to unreduced arguments.

```
sumOfSquares(3, 2+2)
square(3) + square(2+2)
3 * 3 + square(2+2)
9 + square(2+2)
9 + (2+2) * (2+2)
9 + 4 * (2+2)
9 + 4 * 4
```

Call-by-name and call-by-value

The first evaluation strategy is known as *call-by-value*, the second is is known as *call-by-name*.

Both strategies reduce to the same final values as long as

- the reduced expression consists of pure functions, and
- both evaluations terminate.

Call-by-value has the advantage that it evaluates every function argument only once.

Call-by-name has the advantage that a function argument is not evaluated if the corresponding parameter is unused in the evaluation of the function body.

Call-by-name vs call-by-value

Question: Say you are given the following function definition:

```
def test(x: Int, y: Int) = x * x
```

For each of the following function applications, indicate which evaluation strategy is fastest (has the fewest reduction steps)

CBV	CBN	same	
fastest	fastest	#steps	
0	0	0	test(2, 3)
0	0	0	test(3+4, 8)
0	0	0	test(7, 2*4)
0	0	0	test(3+4, 2*4)

Call-by-name vs call-by-value

```
def test(x: Int, y: Int) = x * x
test(2, 3)
test(3+4, 8)
test(7, 2*4)
test(3+4, 2*4)
```