

Higher-order List Functions

Principles of Functional Programming

Recurring Patterns for Computations on Lists

The examples have shown that functions on lists often have similar structures.

We can identify several recurring patterns, like,

- transforming each element in a list in a certain way,
- retrieving a list of all elements satisfying a criterion,
- combining the elements of a list using an operator.

Functional languages allow programmers to write generic functions that implement patterns such as these using higher-order functions.

Applying a Function to Elements of a List

A common operation is to transform each element of a list and then return the list of results.

For example, to multiply each element of a list by the same factor, you could write:

Mapping

This scheme can be generalized to the method map of the List class. A simple way to define map is as follows:

```
abstract class List[T]

def map[U](f: T => U): List[U] = this match
    case Nil => this
    case x :: xs => f(x) :: xs.map(f)
```

(in fact, the actual definition of map is a bit more complicated, because it is tail-recursive, and also because it works for arbitrary collections, not just lists).

Using map, scaleList can be written more concisely.

```
def scaleList(xs: List[Double], factor: Double) =
   xs.map(x => x * factor)
```

Consider a function to square each element of a list, and return the result. Complete the two following equivalent definitions of squareList.

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Filtering

Another common operation on lists is the selection of all elements satisfying a given condition. For example:

Filter

This pattern is generalized by the method filter of the List class:

```
abstract class List[T]

def filter(p: T => Boolean): List[T] = this match
    case Nil => this
    case x :: xs => if p(x) then x :: xs.filter(p) else xs.filter(p)

Using filter, posElems can be written more concisely.

def posElems(xs: List[Int]): List[Int] =
    xs.filter(x => x > 0)
```

Variations of Filter

Besides filter, there are also the following methods that extract sublists based on a predicate:

xs.filterNot(p)	Same as $xs.filter(x \Rightarrow !p(x))$; The list consisting of those elements of xs that do not satisfy the predicate p .
xs.partition(p)	Same as (xs.filter(p), xs.filterNot(p)), but computed in a single traversal of the list xs.
xs.takeWhile(p)	The longest prefix of list xs consisting of elements that all satisfy the predicate p.
xs.dropWhile(p)	The remainder of the list xs after any leading elements satisfying p have been removed.
xs.span(p)	Same as (xs.takeWhile(p), xs.dropWhile(p)) but computed in a single traversal of the list xs.

Write a function pack that packs consecutive duplicates of list elements into sublists. For instance,

```
pack(List("a", "a", "a", "b", "c", "c", "a"))
should give
List(List("a", "a", "a"), List("b"), List("c", "c"), List("a")).
```

You can use the following template:

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You can use the following template:

Using pack, write a function encode that produces the run-length encoding of a list.

The idea is to encode n consecutive duplicates of an element x as a pair (x, n). For instance,

```
encode(List("a", "a", "a", "b", "c", "c", "a"))
```

should give

```
List(("a", 3), ("b", 1), ("c", 2), ("a", 1)).
```

Using pack, write a function encode that produces the run-length encoding of a list.

```
def encode[T](xs: List[T]): List[(T, Int)] =
  pack(xs).map(ys => (ys.head, ys.length))
```