

ELEN-0060: Information and Coding Theory

Project 2 - Source coding, data compression and
channel coding

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1 Implementation

1.1 Binary Huffman code (question 1)

Our implementation is based on a data structure representing a Node of the tree which has 4 fields:

- the symbol of the Node which is 'None' if the Node is not a leaf.
- the probability of the Node
- a pointer to the left child of the Node which is 'None' if the Node is a leaf.
- a pointer to the right child of the Node which is 'None' if the Node is a leaf.

We first create a node for each letter in which we store its symbol, its probability, and 'None' for both children. Then, we build the tree as seen in class: we iteratively link the two nodes with the lowest probabilities until the tree is complete with a node having 1 as probability as root. Each new node born from the birth of two nodes has for probability the sum of the probabilities of these nodes. It also maintains a link to these two nodes becoming its children, and has for symbol 'None'. Finally, we recursively build the Huffman code on the basis of the previously built tree and a choice to represent a left child by a 0 and a right child by a 1.

The output of our code for this question is: {'A': '000', 'B': '001', 'E': '01', 'C': '100', 'D': '101', 'F': '11'} which is not the same as the one found during the exercise session. It is not a problem because the Huffman code is not unique: our code is acceptable and its tree can be observed in the figure 1.

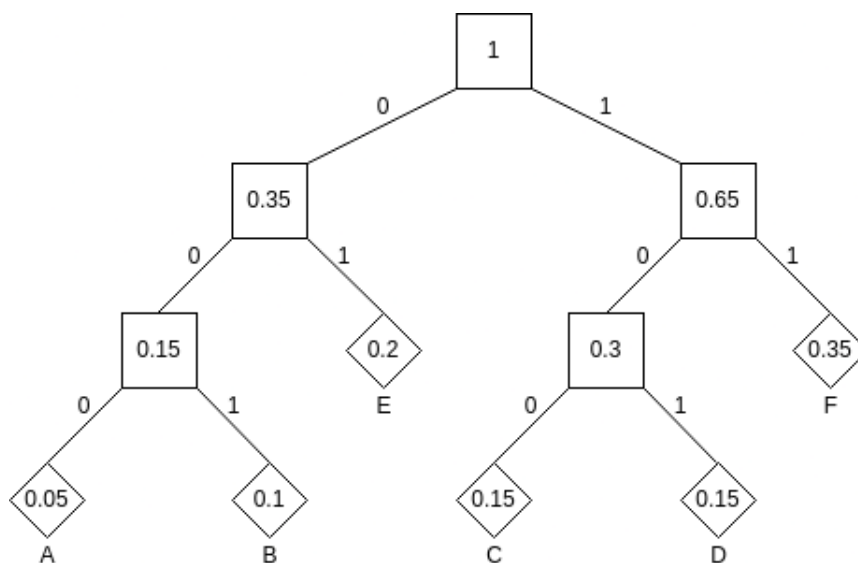


Figure 1: Huffman tree corresponding to the output code

To generate a Huffman code of any (output) alphabet size, several changes would be necessary both in our data structure and in our algorithm:

- Data structure
 - We would need to add a field to store the alphabet size N which was implicitly set to 2 in the binary Huffman code.

- We would need to store the N children of each node which is not a leaf instead of the two children in the binary Huffman code.
- Algorithm
 - We would need to take the N lowest probability and link them to create new nodes instead of the two nodes with the lowest probability in the binary Huffman code.
 - We would need to assign a given unique symbol of the code to each child of a node when recursively building the Huffman code instead of 1 and 0 in the binary Huffman code where there were only 2 children per node.
 - We might have to deal with problems of number of symbols and size of the alphabet not compatible unlike in the binary Huffman code where it is always possible to merge the two lowest probable nodes.

1.2 On-line Lempel-Ziv algorithm (question 2)

The example given in the course about state of the art in data compression on slide 50/53 where the sequence 1011010100010 is encoded gives this output our `LZ_online` function:

- Dictionary: {": (0, "), '1': (1, '1'), '0': (2, '00'), '11': (3, '011'), '01': (4, '101'), '010': (5, '1000'), '00': (6, '0100'), '10': (7, '0010')}
- Encoded sequence: 100011101100001000010