

v2/füüsika ja matemaatikaga seotud mõtted/GM eksperiment/"geometry.cfg"

v2/füüsika ja matemaatikaga seotud mõtted/GM eksperiment/"bblopts.cfg"

v2/füüsika ja matemaatikaga seotud mõtted/GM eksperiment/"english.cfg" v2/füüsika ja matemaatik-
aga seotud mõtted/GM eksperiment/"gravitomagnetismi_experiment_vana.aux"

GM eksperiment

February 23, 2022

Part I

Sissejuhatus

Eesmärk on kastseliselt demonstreerida GravitiMagneetilist nähtust. Gravitimagneetilise välja tekitamiseks kasutatakse pöörlevat silindrit.

Part II

sisu

1 G_M välja tekitamine

$B = \frac{dm^2}{dl \cdot dt} * \mu_G$ (<http://hyperphysics.phy-astr.gsu.edu/hbase/magnetic/solenoid.html> ja elektromagnetismi ja gravitomagnetismi analoogia tuginedes)

$$\frac{dm^2}{dl \cdot dt} = \int_{r_1}^{r_2} (dr * \rho * v(r)) = \int_{r_1}^{r_2} (dr * \rho * \omega * r) = \rho * \omega * \int_{r_1}^{r_2} (dr * r) = \frac{\rho * \omega * (r_2^2 - r_1^2)}{2}$$

maksimaalne GMvälja tugevus silindri kohal on $B_G = \frac{\mu_G * \omega * \rho * (r_2^2 - r_1^2)}{2} = \mu_G * \omega * \rho * \Delta l * (R - \frac{\Delta l}{2})$ kus:

- ω nurkkiirus
- μ_G on GM konstant.
- ρ on silindri tihedus.
- r_2
- Δl on silindri paksus.

Et leida maksimaalset nurkkiirust, mis silindril olla saab ilma, et see inertsiaalsete jõudude tõttu puruneks kasutan neid kahte internetist leitud valemit silindri radiaalse (keskjoonelt eemale) ja tangentsiaalse (joonkiiruse suunalise) pinge leidmiseks. valemid saad (http://www.roytech.co.uk/Useful_Tables/Cams_Springs/Flywheels.html)

$$\sigma_{radiaal\ max} = \frac{\rho * \omega^2 * (3 + \mu) * (r_2 - r_1)^2}{8}$$

$$\sigma_{tangentsiaal\ max} = \frac{\rho * \omega^2 * ((1 - \mu) * r_1^2 + (3 + \mu) * r_2^2)}{4}$$

- μ on siin aine, millest silindri tehtud on poissoni tegur.

eeeldan, et keha ei murdu kui nende ristuvate pingete ruutude summa ei ole keha pingetaluvuse ruudust suurem.

$$\sigma_{max} = \sqrt{\sigma_{radiaal\ max}^2 + \sigma_{tangentsiaal\ max}^2} = \frac{\omega * \rho * \sqrt{(\mu + 3)^2 * (r_1 - r_2)^4 + 4 * (r_1^2 * (\mu - 1) - r_2^2 * (\mu + 3))^2}}{8}$$

$$\text{avaldan siit } \omega = \frac{8 * \sigma_{max}}{\rho} \sqrt{\frac{1}{-5\mu^2 r_1^4 + 4\mu^2 r_1^3 r_2 + 2\mu^2 r_1^2 r_2^2 + 4\mu^2 r_1 r_2^3 - 5\mu^2 r_2^4 + 2\mu r_1^4 + 24\mu r_1^3 r_2 - 20\mu r_1^2 r_2^2 + 24\mu r_1 r_2^3 - 30\mu r_2^4 - 13r_1^4 + 36r_1^3 r_2 - 78r_1^2 r_2^2 + 36r_1 r_2^3 - 45r_2^4}}$$

Asendades selle B_G avaldisse saan:

$$B_G = \mu_G * \rho * (r_2^2 - r_1^2) * \frac{8 * \sigma_{max}}{\rho} \sqrt{\frac{1}{5\mu^2 r_1^4 - 4\mu^2 r_1^3 r_2 - 2\mu^2 r_1^2 r_2^2 - 4\mu^2 r_1 r_2^3 + 5\mu^2 r_2^4 - 2\mu r_1^4 - 24\mu r_1^3 r_2 + 20\mu r_1^2 r_2^2 - 24\mu r_1 r_2^3 + 30\mu r_2^4 + 13r_1^4 - 36r_1^3 r_2 + 78r_1^2 r_2^2 - 36r_1 r_2^3 + 45r_2^4}}$$

1.1 leian kõige parema paksuse

- Δl on siliri paksus

$$\Delta l = r_2 - r_1 \text{ seega } r_1 = r_2 - \Delta l$$

asendan selle B_G valemisse.

$$B_G = \frac{\mu_G \cdot \rho \cdot \Delta l \cdot (2 \cdot r_2 - \Delta l) \cdot 8 \cdot \sigma_{\max}}{\rho} \sqrt{\frac{1}{5 \Delta l^4 \mu^2 - 2 \Delta l^4 \mu + 13 \Delta l^4 - 16 \Delta l^3 \mu^2 r_2 + 32 \Delta l^3 \mu r_2 - 16 \Delta l^3 r_2 + 16 \Delta l^2 \mu^2 r_2^2 - 64 \Delta l^2 \mu r_2^2 + 48 \Delta l^2 r_2^2 + 64 \Delta l \mu r_2^3 - 64 \Delta l r_2^3 + 64 r_2^4}}$$

,et leida parim paksus otsin Δl väärtuse, mille puhul tuletis Δl kaudu on 0 ja teine tuletis on negatiivne.

$$\frac{\partial B_G}{\partial \Delta l} = 0$$

$$\wedge \frac{\partial^2 B_G}{\partial \Delta l^2} < 0$$

ehk

$$\frac{\partial \left(\frac{\mu_G \cdot \rho \cdot \Delta l \cdot (2 \cdot r_2 - \Delta l) \cdot 8 \cdot \sigma_{\max}}{\rho} \sqrt{\frac{1}{5 \Delta l^4 \mu^2 - 2 \Delta l^4 \mu + 13 \Delta l^4 - 16 \Delta l^3 \mu^2 r_2 + 32 \Delta l^3 \mu r_2 - 16 \Delta l^3 r_2 + 16 \Delta l^2 \mu^2 r_2^2 - 64 \Delta l^2 \mu r_2^2 + 48 \Delta l^2 r_2^2 + 64 \Delta l \mu r_2^3 - 64 \Delta l r_2^3 + 64 r_2^4}} \right)}{\partial \Delta l} = 0$$

$$\wedge \frac{\partial^2 \left(\frac{\mu_G \cdot \rho \cdot \Delta l \cdot (2 \cdot r_2 - \Delta l) \cdot 8 \cdot \sigma_{\max}}{\rho} \sqrt{\frac{1}{5 \Delta l^4 \mu^2 - 2 \Delta l^4 \mu + 13 \Delta l^4 - 16 \Delta l^3 \mu^2 r_2 + 32 \Delta l^3 \mu r_2 - 16 \Delta l^3 r_2 + 16 \Delta l^2 \mu^2 r_2^2 - 64 \Delta l^2 \mu r_2^2 + 48 \Delta l^2 r_2^2 + 64 \Delta l \mu r_2^3 - 64 \Delta l r_2^3 + 64 r_2^4}} \right)}{\partial \Delta l^2} < 0$$

ehk

$$\frac{r_2 \sigma (-16 d l^4 \mu^2 - 96 d l^4 \mu - 144 d l^4 + 256 d l^3 \mu r_2 - 256 d l^3 r_2 - 768 d l^2 \mu r_2^2 + 768 d l^2 r_2^2 + 512 d l \mu r_2^3 - 1536 d l r_2^3 + 1024 r_2^4) \sqrt{\frac{1}{5 d l^4 \mu^2 - 2 d l^4 \mu + 13 d l^4 - 16 d l^3 \mu^2 r_2 + 32 d l^3 \mu r_2 - 16 d l^3 r_2 + 16 d l^2 \mu^2 r_2^2 - 64 d l^2 \mu r_2^2 + 48 d l^2 r_2^2 + 64 d l \mu r_2^3 - 64 d l r_2^3 + 64 r_2^4}}}{5 d l^4 \mu^2 - 2 d l^4 \mu + 13 d l^4 - 16 d l^3 \mu^2 r_2 + 32 d l^3 \mu r_2 - 16 d l^3 r_2 + 16 d l^2 \mu^2 r_2^2 - 64 d l^2 \mu r_2^2 + 48 d l^2 r_2^2 + 64 d l \mu r_2^3 - 64 d l r_2^3 + 64 r_2^4} = 0$$

$$\wedge \frac{\partial^2 B_G}{\partial \Delta l^2} < 0$$

ehk

$$-16 d l^4 \mu^2 - 96 d l^4 \mu - 144 d l^4 + 256 d l^3 \mu r_2 - 256 d l^3 r_2 - 768 d l^2 \mu r_2^2 + 768 d l^2 r_2^2 + 512 d l \mu r_2^3 - 1536 d l r_2^3 + 1024 r_2^4 = 0$$

$$\wedge \frac{\partial^2 B_G}{\partial \Delta l^2} < 0$$

Parimal juhul kui:

- $\sigma \approx -2$
- $\rho \approx 22570$
- $\sigma \approx 3.3 \cdot 10^{-10}$
- $r_1 \approx -2$
- $r_2 \approx -2$

Siis $B_G \approx 5,56488343912850 \cdot 10^{-16} \cdot s^{-1}$

Part III

Sisu 2

2 G_M välja tekitamine

$B = \frac{dm^2}{dl \cdot dt} \cdot \mu_G$ (<http://hyperphysics.phy-astr.gsu.edu/hbase/magnetic/solenoid.html> ja eletromagnetismi ja gravitomagnetismi analoogialegi tuginedes)

$$\frac{dm^2}{dl \cdot dt} = \int_{r_1}^{r_2} (dr \cdot \rho \cdot v(r)) = \int_{r_1}^{r_2} (dr \cdot \rho \cdot \omega \cdot r) = \rho \cdot \omega \cdot \int_{r_1}^{r_2} (dr \cdot r) = \frac{\rho \cdot \omega \cdot (r_2^2 - r_1^2)}{2}$$

maksimaalne GMvlja tugevus silindri kohal on $B_G = \frac{\mu_G \cdot \omega \cdot \rho \cdot (r_2^2 - r_1^2)}{2}$ kus:

- ω nurkkiirus
- μ_G on GM konstant.
- ρ on slindr tihedus.

- r_2

Et leida maksimaalsed nurkkiirust, mis silindril olla saab ilma, et see inertsiaalsete jõudude tõttu puruneks kasutan neid kahte internetist leitud valemi silindri radiaalse (keskounktist eemale) ja tangentsiaalse (joonkiiruse suunalise) pinge leidmiseks. valemid sain (http://www.roytech.co.uk/Useful_Tables/Cams_Springs/Flywheels.html)

$$\sigma_{radiaal\ max} = \frac{\rho * \omega * (3 + \mu) * (r_2 - r_1)^2}{8}$$

$$\sigma_{tangentsiaal\ max} = \frac{\rho * \omega * ((1 - \mu) * r_1^2 + (3 + \mu) * r_2^2)}{4}$$

- μ on siin aine, millest silidr tehtud on poissoni tegur.

eeldan, et keha ei murdu kui nende ristuvate pingete ruutude summa ei ole keha pingetaluvuse ruudust suurem.

$$\sigma_{max} = \sqrt{\sigma_{radiaal\ max}^2 + \sigma_{tangentsiaal\ max}^2} = \frac{\omega * \rho * \sqrt{((\mu + 3)^2 * (r_1 - r_2)^4 + 4 * (r_1^2 * (\mu - 1) - r_2^2 * (\mu + 3))^2)}}{8}$$

$$\text{avaldan siit } \omega = \frac{8 * \sigma_{max}}{\rho} \sqrt{\frac{1}{-5\mu^2 r_1^4 + 4\mu^2 r_1^3 r_2 + 2\mu^2 r_1^2 r_2^2 + 4\mu^2 r_1 r_2^3 - 5\mu^2 r_2^4 + 2\mu r_1^4 + 24\mu r_1^3 r_2 - 20\mu r_1^2 r_2^2 + 24\mu r_1 r_2^3 - 30\mu r_2^4 - 13r_1^4 + 36r_1^3 r_2 - 78r_1^2 r_2^2 + 36r_1 r_2^3 - 45r_2^4}}$$

Asendades selle B_G avaldisse saan:

$$B_G = \mu_G * \rho * (r_2^2 - r_1^2) * \frac{8 * \sigma_{max}}{\rho} \sqrt{\frac{1}{5\mu^2 r_1^4 - 4\mu^2 r_1^3 r_2 - 2\mu^2 r_1^2 r_2^2 - 4\mu^2 r_1 r_2^3 + 5\mu^2 r_2^4 - 2\mu r_1^4 - 24\mu r_1^3 r_2 + 20\mu r_1^2 r_2^2 - 24\mu r_1 r_2^3 + 30\mu r_2^4 + 13r_1^4 - 36r_1^3 r_2 + 78r_1^2 r_2^2 - 36r_1 r_2^3 + 45r_2^4}}$$

2.1 leian kõige parema täidetuse

- p on, et kui suure osa kogu raadiusest on täitmata osa raadiud

$p = r_1 / r_2$ seega $r_1 = p * r_2$.

asendan selle B_G valemisse.

$$B_G = 4v_g \sigma \sqrt{\frac{1}{-5\mu^2 p^4 + 4\mu^2 p^3 + 2\mu^2 p^2 + 4\mu^2 p - 5\mu^2 + 2\mu p^4 + 24\mu p^3 - 20\mu p^2 + 24\mu p - 30\mu - 13p^4 + 36p^3 - 78p^2 + 36p - 45}} * (1 - p^2)$$

, et leida parim täidetuse otsin p väärtuse, mille puhul tuletis p kaudu on 0 ja teine tuletis on negatiivne.

$$\frac{\partial B_G}{\partial p} = 0$$

$$\wedge \frac{\partial^2 B_G}{\partial p^2} < 0$$

ehk

$$\frac{\partial (\frac{\mu_G * \rho * \Delta l * (2 * r_2 - \Delta l) * 8 * \sigma_{max}}{\rho} \sqrt{\frac{1}{5\Delta l^4 \mu^2 - 2\Delta l^4 \mu + 13\Delta l^4 - 16\Delta l^3 \mu^2 r_2 + 32\Delta l^3 \mu r_2 - 16\Delta l^3 r_2 + 16\Delta l^2 \mu^2 r_2^2 - 64\Delta l^2 \mu r_2^2 + 48\Delta l^2 r_2^2 + 64\Delta l \mu r_2^3 - 64\Delta l r_2^3 + 64r_2^4}})}{\partial \Delta l} = 0$$

$$\wedge \frac{\partial^2 (\frac{\mu_G * \rho * \Delta l * (2 * r_2 - \Delta l) * 8 * \sigma_{max}}{\rho} \sqrt{\frac{1}{5\Delta l^4 \mu^2 - 2\Delta l^4 \mu + 13\Delta l^4 - 16\Delta l^3 \mu^2 r_2 + 32\Delta l^3 \mu r_2 - 16\Delta l^3 r_2 + 16\Delta l^2 \mu^2 r_2^2 - 64\Delta l^2 \mu r_2^2 + 48\Delta l^2 r_2^2 + 64\Delta l \mu r_2^3 - 64\Delta l r_2^3 + 64r_2^4}})}{\partial \Delta l^2} < 0$$

ehk

$$\frac{v_g \sigma \sqrt{\frac{1}{-5\mu^2 p^4 + 4\mu^2 p^3 + 2\mu^2 p^2 + 4\mu^2 p - 5\mu^2 + 2\mu p^4 + 24\mu p^3 - 20\mu p^2 + 24\mu p - 30\mu - 13p^4 + 36p^3 - 78p^2 + 36p - 45}}}{\frac{8\mu^2 p^4 - 32\mu^2 p^3 + 48\mu^2 p^2 - 32\mu^2 p + 8\mu^2 + 48\mu p^4 - 64\mu p^3 + 288\mu p^2 - 320\mu p + 48\mu + 72p^4 - 416p^3 + 432p^2 - 672p + 72}}{5\mu^2 p^4 - 4\mu^2 p^3 - 2\mu^2 p^2 - 4\mu^2 p + 5\mu^2 - 2\mu p^4 - 24\mu p^3 + 20\mu p^2 - 24\mu p + 30\mu + 13p^4 - 36p^3 + 78p^2 - 36p + 45}} (8\mu^2 p^4 - 32\mu^2 p^3 + 48\mu^2 p^2 - 32\mu^2 p + 8\mu^2 + 48\mu p^4 - 64\mu p^3 + 288\mu p^2 - 320\mu p + 48\mu + 72p^4 - 416p^3 + 432p^2 - 672p + 72) = 0$$

$$\wedge \frac{\partial^2 B_G}{\partial \Delta l^2} < 0$$

ehk

$$8\mu^2 p^4 - 32\mu^2 p^3 + 48\mu^2 p^2 - 32\mu^2 p + 8\mu^2 + 48\mu p^4 - 64\mu p^3 + 288\mu p^2 - 320\mu p + 48\mu + 72p^4 - 416p^3 + 432p^2 - 672p + 72 = 0$$

$$\wedge \frac{\partial^2 B_G}{\partial \Delta l^2} < 0$$

###

lasilk asendus: $r_1 = p * r_2$. lihtsam parim p leida kui parim _Delta l leida

$$\frac{1v_g \sigma \sqrt{\frac{1}{-5\mu^2 p^4 + 4\mu^2 p^3 + 2\mu^2 p^2 + 4\mu^2 p - 5\mu^2 + 2\mu p^4 + 24\mu p^3 - 20\mu p^2 + 24\mu p - 30\mu - 13p^4 + 36p^3 - 78p^2 + 36p - 45}}}{\frac{8\mu^2 p^4 - 32\mu^2 p^3 + 48\mu^2 p^2 - 32\mu^2 p + 8\mu^2 + 48\mu p^4 - 64\mu p^3 + 288\mu p^2 - 320\mu p + 48\mu + 72p^4 - 416p^3 + 432p^2 - 672p + 72}}{5\mu^2 p^4 - 4\mu^2 p^3 - 2\mu^2 p^2 - 4\mu^2 p + 5\mu^2 - 2\mu p^4 - 24\mu p^3 + 20\mu p^2 - 24\mu p + 30\mu + 13p^4 - 36p^3 + 78p^2 - 36p + 45}} (8\mu^2 p^4 - 32\mu^2 p^3 + 48\mu^2 p^2 - 32\mu^2 p + 8\mu^2 + 48\mu p^4 - 64\mu p^3 + 288\mu p^2 - 320\mu p + 48\mu + 72p^4 - 416p^3 + 432p^2 - 672p + 72) = 0$$

3 GM välja detekteerimise meetodid

3.1 neutronite kõrvalekaldumine

$$F = 4 * B \times v$$

3.2 keerleva ketta keeramine

Sekundaarse ketta pöörlemistelg on primaarse silindriga 90 kraadi kaldus. $F = 4 * \frac{\partial m}{\partial r} * B_G * l_{juhe} =$

3.3 teise suure inertsimomendiga silndrile jõumomendi tekitamine.

$$\tau = \int (dr * (2\pi * r) * h * \rho_2 * E_G * r * 4) = - \int (dr * (2\pi * r) * h * \rho_2 * \frac{r * \frac{\partial B_G}{\partial t}}{2} * r * 4) = - \frac{2\pi * h * \rho_2 * \frac{\partial B_G}{\partial t} * (r_{2,2}^4 - r_{2,1}^4)}{2} = - \frac{2\pi * h * \rho_2 * B_G * (r_{2,2}^4 - r_{2,1}^4)}{2 * \Delta t}$$

3.4 teise silndri pöörlema panemine

- roo_2 on teise silindri tihedus
- r_2.1 on teise õõnes silindri välimine raadius.
- r_2.2 on teise õõnes silindri sisemine raadius.
- E_G on gravitatsiooni väli.
- E_G on gravitimagneetilineväli.
- tau on jõumoment.
- I on inertsimoment.

GEM võrrand: $rot(E_G) = - \frac{\partial B_G}{\partial t}$

$$2 * \pi * r * E_G = - \pi * r^2 * \frac{\partial B_G}{\partial t}$$

$$E_G = - \frac{r * \frac{\partial B_G}{\partial t}}{2}$$

$$\tau = \int (dr * (2\pi * r) * h * \rho_2 * E_G * r * 4) = - \int (dr * (2\pi * r) * h * \rho_2 * \frac{r * \frac{\partial B_G}{\partial t} * 4}{2} * r) = - \frac{2\pi * h * \rho_2 * \frac{\partial B_G}{\partial t} * (r_{2,2}^4 - r_{2,1}^4)}{2}$$

$$I = \frac{m * (r_{2,2}^2 - r_{2,1}^2)}{2} = \frac{\pi * h * \rho_2 * (r_{2,2}^2 - r_{2,1}^2)^2}{2}$$

$$\omega = \int \left(\frac{\tau * dt}{I} \right) = \int \left(\frac{2\pi * h * \rho_2 * \frac{\partial B_G}{\partial t} * (r_{2,2}^4 - r_{2,1}^4) * dt}{4 * \pi * h * \rho_2 * (r_{2,2}^2 - r_{2,1}^2)^2} \right) = \int \left(\frac{\frac{\partial B_G}{\partial t} * (r_{2,2}^4 - r_{2,1}^4) * dt}{2 * (r_{2,2}^2 - r_{2,1}^2)^2} \right) = \frac{\Delta B_G * (r_{2,2}^4 - r_{2,1}^4)}{2 * (r_{2,2}^2 - r_{2,1}^2)^2}$$