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Formale Grundlagen der Informatik I -Assignment 1

Hand out: 21.02.2019 - Due to: 07.03.2019

Please upload your solutions to the Olat system.

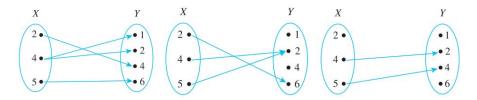
1.1 Sets and Subsets

- a) Write in your own words how to read the following sets:
 - i. $\{x \in \mathbb{R} \mid x \notin \mathbb{Q}\}$
 - ii. $\{n \in \mathbb{Z}^- \mid n > -6\}$
- **b)** Answer the following questions with a short explanation:
 - i. Is $\emptyset \in \{\}$?
 - ii. How many elements contains the set $\{1, 1, 2, 2\}$?
 - iii. How many elements contains the set $\{0, \{0\}, \{\{0\}\}\}\}$?
 - iv. Is $2 \in \{\{1\}, \{2\}\}$?
 - v. Is $\{0\} \in \{\{0\}, \{1\}\}\$?
 - vi. Is $2 \in \{\{1, 2\}\}$?

1.2 Relations and Functions

- a) What is the difference between a function and a relation?
- b) Let $A = \{2, 4\}$ and $B = \{1, 3, 5\}$. Define the nonempty and pairwise different relations $U, V, W \subseteq A \times B$ as follows:
 - $(x,y) \in U$ implies $x * y \ge 7$.
 - $(x,y) \in V$ implies x > y.
 - x > y implies $(x, y) \in W$.
 - i. For wich of the above tasks would the empty set be a valid solution (if the "non-empty" wasn't given in the task)?
 - ii. Determine if the relations U, V and W are functions and reason in a few words.

c) Give a label for each of the following three figures. Do they show a relation, function, or something else? Please give a (short) reason for your decision?



1.3 Logical Equivalence

a) Please determine (in a plausible way) which of the statement forms are tautologies and which are contradictions.

i.
$$((p \land \neg q \land \neg r) \lor (p \land \neg q \land r)) \Leftrightarrow \neg (p \lor q)$$

ii.
$$(p \lor q) \lor \neg (p \land q)$$

- **b)** With a few word of explanation, determine if the following statements are mutually excluding.
 - Susan speaks German and English. Oliver speaks English.
 - It is not the case that Oliver and Susan both speak German and English.

1.4 Conditional Statements

- a) Write each of the following three statements in symbolic form and determine which pairs are logically equivalent. Include a few words of explanation.
 - i. If it walks like a duck and it talks like a duck, then it is a duck.
 - ii. Either it does not walk like a duck or it does not talk like a duck, or it is a duck.
 - iii. If it does not walk like a duck and it does not talk like a duck, then it is not a duck.
- b) The following statement is given: "If compound X is boiling, then its temperature must be at least 150°C". Assuming that this statement is true, which of the following must also be true? Argument with respect to a necessary and sufficient condition.
 - i. Compound X will boil only if its temperature is at least 150°C.
 - ii. If compound X is not boiling, then its temperature is less than 150°C.
 - iii. A necessary condition for compound X to boil is that its temperature be at least 150°C.

 \mathbf{or}

A sufficient condition for compound X to boil is that its temperature be at least 150 °C.