

0.1 Generating Counterfactuals

The topic of counterfactual generation as explanation method was introduced by wachter *Counterfactual Explanations Opening 2018* in wachter *Counterfactual Explanations Opening 2018* [?]. The

A newer approach by dandl *MultiObjective Counterfactual Explanations 2020* incorporates four main criteria *objective fitness function* [?]. This approach strongly differs from gradient-based methods, as it does not require

0.2 Generating Counterfactual Sequences

When it comes to sequential data most researchers work on ways to generate counterfactuals for natural language. This often entails generating univariate discrete counterfactuals with the use of Deep Learning techniques. martens *Explaining data driven document 2014* and

Instead, robeer *Generating Realistic Natural 2021* showed that it is possible to generate realistic counterfactual decoder pattern in which the encoder encodes a data instance into a latent vector, which will be perturbed and then decoded

Even though, a single latent vector model can theoretically produce multivariate sequences, it may still be too restrictive to capture the combinatorial space of multivariate sequences. Hence, most of the models within Natural Language Processing (NLP) were not used to produce a sequence of vectors, but a sequence of discrete symbols. For process instances, we can assume a causal relation between state vectors in a sequential latent space. We call models that capture a sequential latent state-space, which has causal relations, *dynamic* [?]. Early models of this type of dynamic latent state-space models are the well-known *Kalman-Filter* for continuous states and Hidden Markov Model (HMM) for discrete states. In recent literature, many techniques use Deep Learning to model complex state-spaces. The first models of this type were developed by krishnan *structured Inference Networks 2017* [?, ?]. Their *Deep Kalman Filter (DKF)* and subsequent *Deep Markov space* by modelling the latent space given the data sequence and all previous latent vectors in the sequence. There are *Bound (ELBO)* of the posterior for the current Z_t given all previous $\{Z_{t-1}, \dots, Z_1\}$ and X_t [?].

0.3 Generating Counterfactual Time-Series

Within the *multivariate time-series* literature two recent approaches yield ideas worth discussing.

First, delaney *Instance Based Counterfactual Explanations 2021* introduce a case-based reasoning to generate counterfactuals [?]. Their method uses existing counterfactual instances, or prototype based approaches strongly depend on the representativeness of the prototypes [?, p. 192]. In other words, if the model based techniques will fail to provide viable counterfactuals. The likelihood of such a break-down increases due to the combinatorial explosion of possible behaviours if the true process model has cycles or continuous states. Therefore, prototype based approaches may act as a valuable baseline against other sophisticated approaches.

The second paper within the multivariate time series field by ates *Counterfactual Explanations Multivariate* based approach [?]. However, it contrasts from other approaches, as it does not specify a particular model but proposes

0.4 Generating Counterfactuals for Business Processes

So far, none of the techniques have been applied to process data.

Within Process Mining (PM), Causal Inference has long been used to analyse and model business processes. Mainly, due to the causal relationships underlying each process. However, early work has often attempted to incorporate domain-knowledge about the causality of processes in order to improve the process model itself[?, ?, ?, ?]. Among these, Narendra *Counterfactual Reasoning Process* [2019] approach is one of the first to include

Within the XAI context, Tsirtsis *Counterfactual Explanations Sequential* [2021] develop the first explanation method for learning or SARSA. However, this often requires additional assumptions such as a given reward function and an action space. For counterfactual sequence generation, there is no obvious choice for the reward function or the action space.

Nonetheless, both Tsirtsis *Counterfactual Explanations Sequential* [2021] and Oberst *Counterfactual Off Policy*

For this reason, this thesis highlights some key differences and similarities. However, to understand the differences and similarities, we first have to establish some core concepts. In this section, we only discuss their approach, briefly.

The authors recognised that some processes have critical events which govern the overall outcome. Hence, by simply avoiding the undesired outcome from critical event to critical event, it is possible to limit the search space and compute viable counterfactuals. They use an extension of DiCE[?] to generate counterfactuals. However, their approach requires concrete knowledge about these critical points. We propose a Framework that avoids this constraint.

To our knowledge, the authors are also the first authors that try to optimize their counterfactual process generation based on criteria that ensure their viability. However, in our approach, we use different operationalisations to quantify the criteria.