

All evolutionary algorithms use ideas that resemble the process of evolution. There are four broad categories: A Genetic Algorithm (GA) uses bit-string representations of genes, while Genetic Programming (GP) uses binary codes to represent programs or instruction sets. Evolutionary Strategy (ES) require the use of vectors. Lastly, Evolutionary Programming (EP), which closely resembles ES, without imposing a specific data structure type [CITE](#). Our approach falls into the category of GA. The most vital concept in this category is the *gene* representation. For our purposes, the gene of a sequence consists of the sequence of events within a process instance. Hence, if an offspring inherits one gene of a parent, it inherits the activity associated with the event and all event attributes.

Our goal is to generate candidates by evaluating the sequence based on our viability measure. Our measure acts as a fitness function. The candidates that are deemed fit enough are subsequently selected to reproduce offspring. The offspring is subject to mutations. Then, we evaluate the new population repeat the procedure until a termination condition is reached. It differs from Deep Learning, because it does not require us to use differentiable functions. Hence, we can directly optimise the viability measure established in ??.

For the algorithm, we follow a rigid structure of operations as outlined in ?. As ? shows, we define 5 fundamental operations. Initiation, Selection, Crossover, Mutation and Recombination.

Algorithm 1 Shows the basic structure of an evolutionary algorithm.

Require: Hyperparameters

Ensure: The result is the final population

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population  $\leftarrow$  INIT population;
while not termination do
    parents  $\leftarrow$  SELECT population;
    offspring  $\leftarrow$  CROSSOVER parents;
    mutants  $\leftarrow$  MUTATE offspring;
    survivors  $\leftarrow$  RECOMBINE population  $\cup$  mutants;
    termination  $\leftarrow$  DETERMINE termination
    population  $\leftarrow$  survivors
end while

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Initiation

The initiation process refers to the creation of the initial set of candidates for the selection process in the first iteration of the algorithm. Often, this amounts to the random generation of individuals. In this thesis, we call

this method the *Random-Initiation*. However, choosing among a subset of the search space can allow for a faster convergence. We chose to implement three different subspaces as a starting point. First, by sampling from the data distribution of the Log (*Sampling-Based-Initiation*). Second, by picking individuals from a subset of the Log (*Case-Based-Initiation*). **And lastly, we can use the factual case itself as a reasonable starting point (*Factual-Initiation*).**

Selection

The selection process chooses a set of individuals among the population according to a selection procedure. These individuals will go on to act as material to generate new individuals. Again, there are multiple ways to accomplish this. In this thesis, we explore three methods. First, the *Roulette-Wheel-Selection*. Here, we compute the fitness of each individual in the population and choose a random sample proportionate to their fitness values. Next, the *Tournament-Selection*, which randomly selects pairs of population individuals and uses the individual with the higher fitness value to succeed. Last, we select individuals based on the elitism criterion. In other words, only a top-k amount of individuals are selected for the next operation (*Elitism-Selection*). This approach is deterministic and therefore subject to getting stuck in local minima.

Crossover

Within the crossover procedure, we select random pairing of individuals to pass on their characteristics. Again allowing a multitude of possible procedures. We can uniformly choose a fraction of genes of one individual (*Parent 1*) and overwrite the respective genes of another individual (*Parent 2*). The result is a new individual. We call that (*Uniform-Crossover*). Figure 1 shows a simple schematic example. By repeating this process towards the opposite direction, we create two new offsprings, which share characteristics of both individuals. The amount of inherited genes can be adjusted using a rate-factor. The higher the crossover-rate, the higher the risk of disrupting possible sequences. If we turn to Figure 1 again, we see how the second child has 2 repeating genes at the end. If a process does not allow the transition from *activity 8* to another *activity 8*, then the entire process instance becomes infeasible.

The second approach is suitable for sequential data of same lengths. We can choose a point in the sequence and pass on genes of *Parent 1* onto the *Parent 2* from that point onwards and backwards (*One-Point-Crossover*).

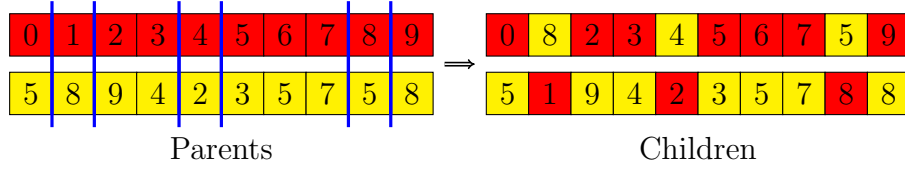


Figure 1: A figure showing the process of uniformly applying characteristics of one sequence to another.

Thus, creating two new offsprings again as depicted in Figure 2.

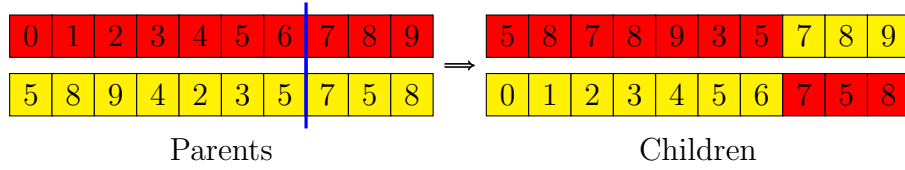


Figure 2: A figure showing the process of applying characteristics of one sequence to another using one split point

The last option is called *Two-Point-Crossover* and resembles its single-point counterpart. However, this time, we choose two points in the sequence and pass on the overlap and the disjoints to generate two new offsprings. Again, Figure 3 describes the procedure visually.

Obviously, we can increase the number of crossover points even further. However, this increase comes at the risk of disrupting sequential dependencies.

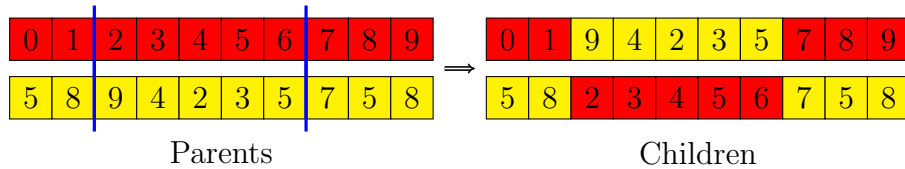


Figure 3: A figure showing the process of applying characteristics of one sequence to another using two split points.

Mutation

Mutations introduce random perturbations to the offsprings. Here, we apply only one major operation. However, the extend in which these mutations are applicable can still vary.

Before elaborating on the details, we have to briefly discuss four modification types that we can apply to sequences of data. Reminiscent of edit distances, which were introduced earlier in this thesis, we can either insert,

delete or change a step. These edit-types are the fundamental edits we use to modify sequences. For a visual explanation of each edit-type we refer to ?? in ??.

However, we can change the rate to which each operation is applied over the sequence. We call these parameters *mutation-rates*. In other words, if the delete-rate equals 1 every individual experiences a modification which results in the deletion of a step. Same applies to other edit types. Further, we modify the amount to which each modification applies to the sequence. We call this rate *edit-rate* and keep it constant across every edit-type. Meaning, if the edit-rate is 0.5 and the delete-rate is 1, then each individual will have 50% of their sequence deleted.

There are still three noteworthy topics to discuss.

First, these edit-types are disputable. One can argue, that change and transpose are just restricted versions of delete-insert compositions. For instance, if we want to change the activity *Buy-Order* with *Postpone-Order* at timestep 4, we can first, delete *Buy-Order* and insert *Postpone-Order* at the same place. Similar holds for transpositions, albeit more complex. Hence, these operations would naturally occur over repeated iterations in an evolutionary algorithm.

However, these operations follow the structure of established edit-distances like the Damerau-Levenshtein distance. Furthermore, they allow for efficient restrictions with respect to the chosen data encoding. For instance, we can restrict delete operations to steps that are not padding steps. In contrast insert operations can be restricted to padding steps only.

Second, we could introduce different edit-rates for each edit-type. However, this adds additional complexity and needlessly increases the search space for hyperparameters.

Third, as we chose the hybrid encoding scheme, we have to define what an insert or a change means for the data. Aside from changing the activity, we also have to choose reasonable data attributes. This necessity requires to define two ways to produce them. We can either choose the features randomly, or choose to sample from a distribution which depends on the previous activities. We name the former approach *Default-Mutation*. We can simplify the latter approach by invoking the markov assumption and sample the feature attributes given the activity in question (*Sample-Based-Mutation*).

Recombination

This process refers to the creation of a new population for the next iteration¹. Here, we use introduce two variants.

We name the strict selection of the best individuals among the offsprings and the previous population *Fittest-Survivor-Recombination*. In contrast, we name the addition of the top-k best offsprings to the initial population *Best-of-Breed-Recombination*. The former will guarantee, that the population size remains the same across all iterations but is prone to local optima. The latter keeps suboptimal individuals, while adding a constant pool of better individuals to select.

Furthermore, we propose two additional recombination operators.

First, one that does not select the new population based on the viability function, but rather defines a cut-off point and sorts each individual by every viability component separately. This approach allows us to select regardless of the scales of every individual viability measure. We refer to this method as *Ranked-Recombination*.

The second approach is similar. However, this time we sort each individual by their pairwise-pareto dominance. In other words, we decide selecting individuals by selecting the individuals first, who have the highest delta without reducing the feasibility. Then, those with the highest feasibility, without reducing sparsity and so on. All individuals that fall through the cut-off point are discarded [Change num survivors to cut-off point.]. We refer to this approach as *Ranked-Pareto-Recombination*.

The difference between *Ranked-Pareto-Recombination* and *Ranked-Recombination* is subtle. We show this in Figure 4.

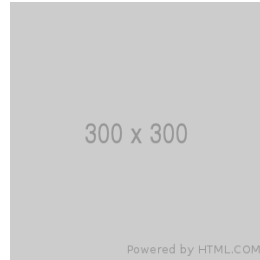


Figure 4: Shows difference between both approaches on two arbitrary dimensions. It shows the number that are selected on the pareto frontier and those selected by sorting. The selected individuals are marked by a cross.

¹We have to point out that in the literature, recombination is often synonymous with crossover. However, in this thesis recombination refers to the update process which generates the next population.