

## HOW RSA WORKS

- select two distinct large prime numbers  $p$  and  $q$
- compute their product  $N = pq$
- Let  $T = (p-1)(q-1)$  this is called euler totient
- Choose two integers where  $(e * d) \bmod T = 1$   
Where  $e$  must be an odd number
- Now publish  $P=(e,N)$  which is the public key
- And the secret key  $S=(d,N)$
- $C = M^e \bmod N$   
Where  $M$  is the encoded message,  
 $C$  is the encrypted message
- $M = C^d \bmod N$

For example:

Lets use primes 2 and 5

$$N = 2 * 5 = 10$$

To find  $T$ ,

$$T = 1 * 4 = 4$$

Find 2 integers where  $e * d \bmod 4 = 1$

$e$  could be 3 and  $d$  could be 3

but we would use 7 .

$$3 * 7 \bmod 4 = 1 \text{ is true}$$

$$N = 10, e = 3, d = 7$$

Let  $A = 1$  ,  $B = 2$ ,  $C = 3$

And lets make  $B$  our message

$$M = 2$$

Our public key is  $P=(3,10)$

$$C = M^e \bmod N$$

$$C = 2^3 \bmod 10$$

$$C = 8$$

8 is our encrypted message

The secret key is  $S=(7,10)$

$$M = C^d \bmod N$$

$$M = 8^7 \bmod 10$$

$$M = 2097152 \bmod 10$$

$$M = 2$$

The letter B

