

① what if  $P(x_i/y) = 0$ ?

- Smoothing - Add a constant in Numerator & Denominator

$$P(x_i / y) = \frac{\#(x_i \cap y) + 1}{\#y + 1}$$

② What if feature variables are continuous?

$$X_1 = [0, 1] \quad \text{or} \quad [0, 1, 2]$$

0, 1, 2, ..., 100

$$P(X_1 = 0 / Y = 0) \dots P(X_7 = 100 / Y = 0)$$

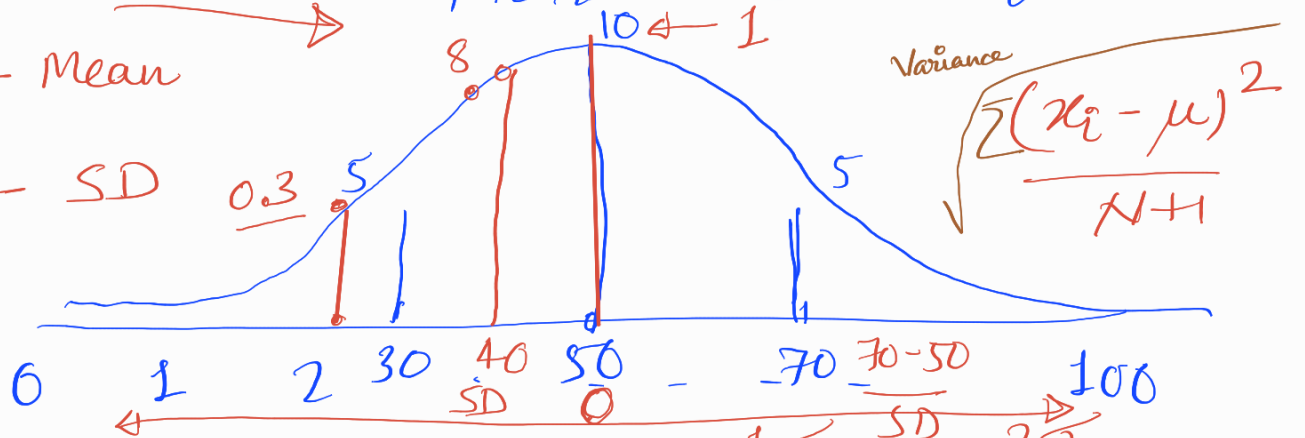
Assumption :  $X_i$  values come from

# Bell Curve

## Normal distribution

$\mu$  - Mean

$\sigma$ -SD



$$P(X_i = 40) = \frac{8}{\# \text{ examples}} = \frac{8}{10} = 0.8$$

$$P(X = \underline{25.5}) = \underline{0.3}$$

$$\frac{\sigma_i = \mu = 1}{SD = 1} = 1$$

## 7. Score

$$= \frac{x_i - \mu}{\sigma}$$

zero mean

$x_i / \sigma$  ratio

$x_i$	$x_i - \mu_{x_i}$	$\mu_{x_i} = 2$	$\frac{x_i - \mu = 2}{\sigma = 1} = 2$
1	-1		
2	0		
3	1		



$\mu, \sigma, Z\text{-Score}$

$x_i, x_i - \mu$

1 - 2.7

2 - 2.7

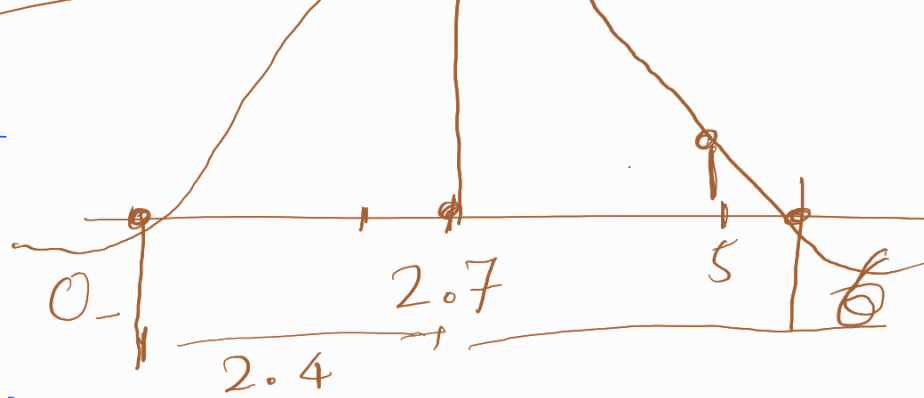
3

1 / 2.7

$P(x_i = 5)$



$$\begin{array}{r}
 2 \\
 4 \\
 2 \\
 4 \\
 6 \\
 \hline
 \text{Find } \mu \text{ \& } \sigma \\
 = 2.7 \qquad = 2.4
 \end{array}$$



What if the feature variable are continuous?

- (A) values from the feature variable come from a normal distribution
- (B) The distribution is defined by  $\mu$  &  $\sigma$   $\leftarrow$  Model parameters
- (C) Calculate  $\mu$  &  $\sigma$
- (D) Use  $\mu$  &  $\sigma$  and apply it in the formula of Gaussian Distri. to find ' $P(x_i)$ ' of an value  $x_i$  of  $X_i$

How about

$$P(x_i / y) ?$$

$$y = \{0, 1\}$$

$x_i$  = is continuous

$$P(x_i = 1.2 / y = 0) \{$$

take all examples where  $y=0$

& calculate  $\mu_{x_i}$  &  $\sigma_{x_i}$  for only those examples where ' $y=0$ '.

Use  $\mu_{x_i}$  &  $\sigma_{x_i}$  to calculate

## First sessional - Introduction

- Naive Bayes Classifier
- Bayesian Network
- Exact inference in Bayesian Network