#### 12-2 SHA-512

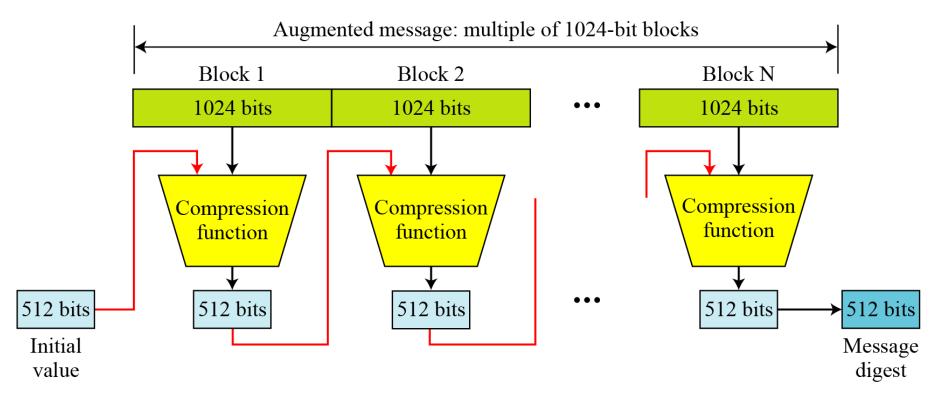
SHA-512 is the version of SHA with a 512-bit message digest. This version, like the others in the SHA family of algorithms, is based on the Merkle-Damgard scheme.

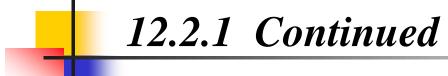
### Topics discussed in this section:

- 12.2.1 Introduction
- **12.2.2** Compression Function
- **12.2.3 Analysis**

#### 12.2.1 Introduction

Figure 12.6 Message digest creation SHA-512





### Message Preparation

SHA-512 insists that the length of the original message be less than  $2^{128}$  bits.

# Note

SHA-512 creates a 512-bit message digest out of a message less than 2<sup>128</sup>.

### Example 12.1

This example shows that the message length limitation of SHA-512 is not a serious problem. Suppose we need to send a message that is  $2^{128}$  bits in length. How long does it take for a communications network with a data rate of  $2^{64}$  bits per second to send this message?

#### **Solution**

A communications network that can send  $2^{64}$  bits per second is not yet available. Even if it were, it would take many years to send this message. This tells us that we do not need to worry about the SHA-512 message length restriction.

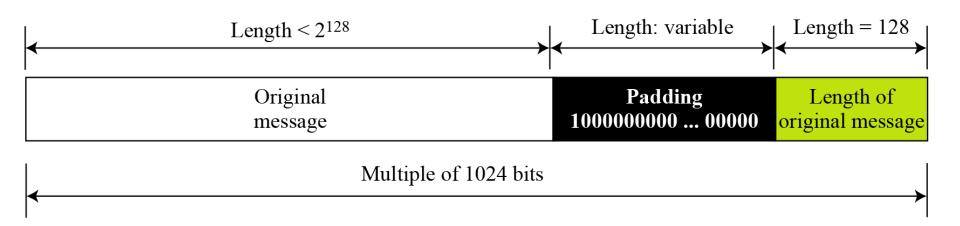
### Example 12.2

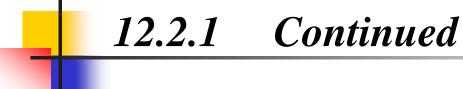
This example also concerns the message length in SHA-512. How many pages are occupied by a message of  $2^{128}$  bits?

#### **Solution**

Suppose that a character is 32, or  $2^6$ , bits. Each page is less than 2048, or approximately  $2^{12}$ , characters. So  $2^{128}$  bits need at least  $2^{128}$  /  $2^{18}$ , or  $2^{110}$ , pages. This again shows that we need not worry about the message length restriction.

#### Figure 12.7 Padding and length field in SHA-512





# Example 12.3

What is the number of padding bits if the length of the original message is 2590 bits?

#### **Solution**

We can calculate the number of padding bits as follows:

$$|P| = (-2590 - 128) \mod 1024 = -2718 \mod 1024 = 354$$

The padding consists of one 1 followed by 353 0's.

# Example 12.4

Do we need padding if the length of the original message is already a multiple of 1024 bits?

#### Solution

Yes we do, because we need to add the length field. So padding is needed to make the new block a multiple of 1024 bits.

### Example 12.5

What is the minimum and maximum number of padding bits that can be added to a message?

#### **Solution**

a. The minimum length of padding is 0 and it happens when (-M-128) mod 1024 is 0. This means that |M|=-128 mod 1024 = 896 mod 1024 bits. In other words, the last block in the original message is 896 bits. We add a 128-bit length field to make the block complete.

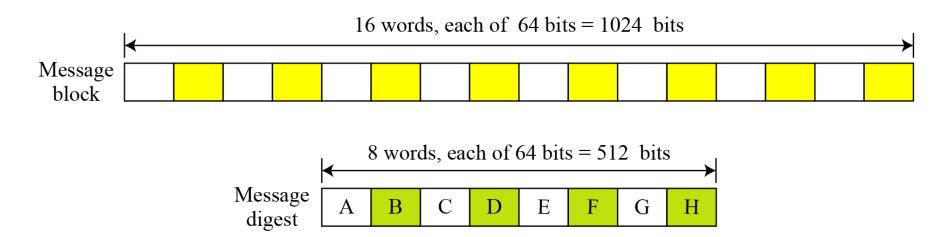
Example 12.5

**Continued** 

b) The maximum length of padding is 1023 and it happens when  $(-|M|-128) = 1023 \mod 1024$ . This means that the length of the original message is  $|M| = (-128 - 1023) \mod 1024$  or the length is  $|M| = 897 \mod 1024$ .

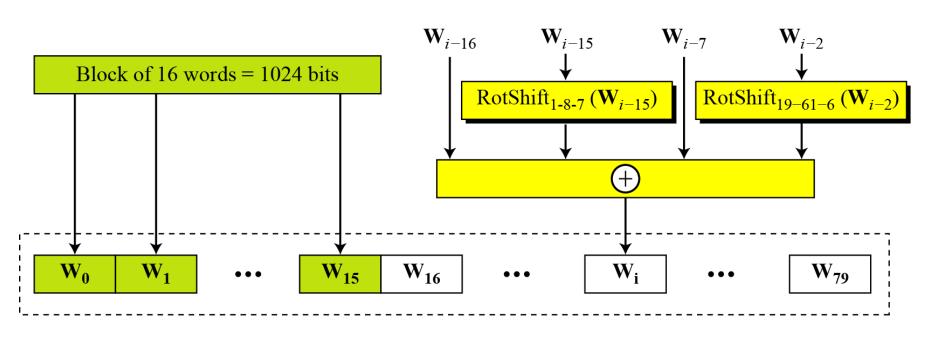
#### Words

#### Figure 12.8 A message block and the digest as words



# Word Expansion

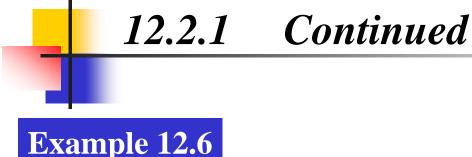
#### Figure 12.9 Word expansion in SHA-512



 $RotShift_{I-m-n}(x): RotR_I(x) \bigoplus RotR_m(x) \bigoplus ShL_n(x)$ 

 $RotR_i(x)$ : Right-rotation of the argument x by i bits

 $ShL_i(x)$ : Shift-left of the argument x by i bits and padding the left by 0's.



Show how W60 is made.

#### **Solution**

Each word in the range W16 to W79 is made from four previously-made words. W60 is made as

$$W_{60} = W_{44} \oplus RotShift_{1-8-7} (W_{45}) \oplus W_{53} \oplus RotShift_{19-61-6} (W_{58})$$

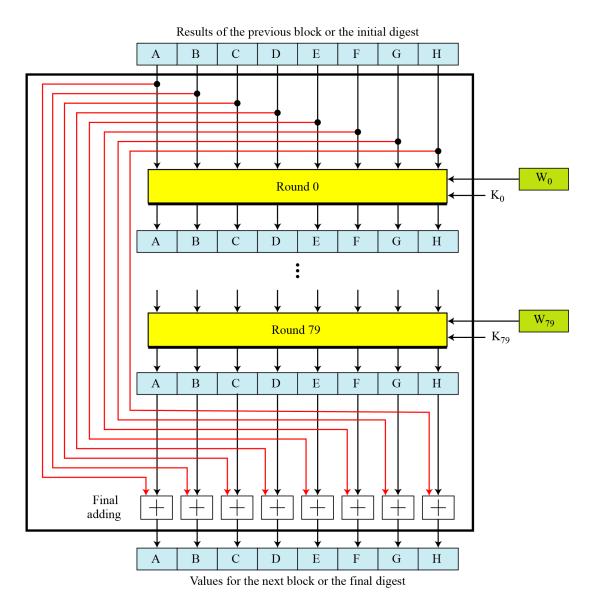
# Message Digest Initialization

**Table 12.2** Values of constants in message digest initialization of SHA-512

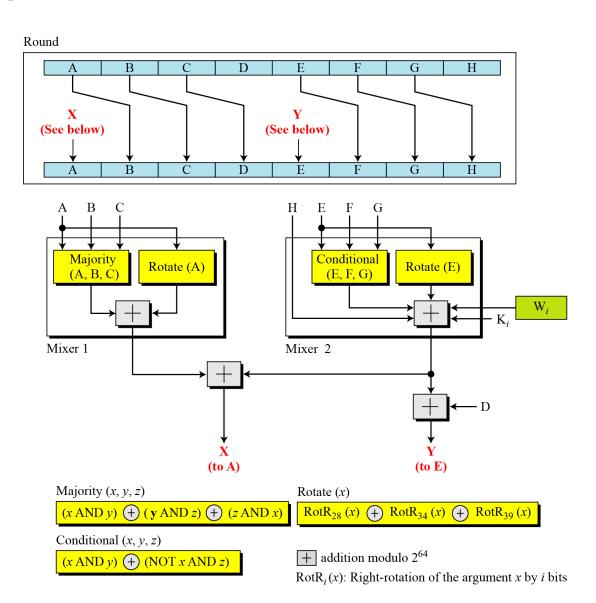
Buffer	Value (in hexadecimal)	Buffer	Value (in hexadecimal)
$A_0$	6A09E667F3BCC908	$E_0$	510E527FADE682D1
$B_0$	BB67AE8584CAA73B	$F_0$	9B05688C2B3E6C1F
$C_0$	3C6EF372EF94F828	$G_0$	1F83D9ABFB41BD6B
$D_0$	A54FE53A5F1D36F1	$H_0$	5BE0CD19137E2179

# 12.2.2 Compression Function

#### Figure 12.10 Compression function in SHA-512



#### Figure 12.11 Structure of each round in SHA-512



# Majority Function

 $(A_j AND B_j) \oplus (B_j AND C_j) \oplus (C_j AND A_j)$ 

#### **Conditional Function**

 $(\mathbf{E}_j \mathbf{AND} \mathbf{F}_j) \oplus (\mathbf{NOT} \mathbf{E}_j \mathbf{AND} \mathbf{G}_j)$ 

#### Rotate Functions

Rotate (A):  $RotR_{28}(A) \oplus RotR_{34}(A) \oplus RotR_{29}(A)$ 

Rotate (E):  $RotR_{28}(E) \oplus RotR_{34}(E) \oplus RotR_{29}(E)$ 

 Table 12.3
 Eighty constants used for eighty rounds in SHA-512

428A2F98D728AE22         7137449123EF65CD         B5C0FBCFEC4D3B2F         E9B5DBA58189DBBC           3956C25BF348B538         59F111F1B605D019         923F82A4AF194F9B         AB1C5ED5DA6D8118           D807AA98A3030242         12835B0145706FBE         243185BE4EE4B28C         550C7DC3D5FFB4E2           72BE5D74F27B896F         80DEB1FE3B1696B1         9BDC06A725C71235         C19BF174CF692694           E49B69C19EF14AD2         EFBE4786384F25E3         0FC19DC68B8CD5B5         240CA1CC77AC9C65           2DE92C6F592B0275         4A7484AA6EA6E483         5CB0A9DCBD41FBD4         76F988DA831153B5           983E5152EE66DFAB         A831C66D2DB43210         B00327C898FB213F         BF597FC7BEEF0EE4           C6E00BF33DA88FC2         D5A79147930AA725         06CA6351E003826F         142929670A0E6E70           27B70A8546D22FFC         2E1B21385C26C926         4D2C6DFC5AC42AED         53380D139D95B3DF           650A73548BAF63DE         766A0ABB3C77B2A8         81C2C92E47EDAEE6         92722C851482353B           A2BFE8A14CF10364         A81A664BBC423001         C24B8B70D0F89791         C76C51A30654BE30           D192E819D6EF5218         D69906245565A910         F40E35855771202A         106AA07032BBD1B8           193C0CB3C5C95A63         4ED8AA4AE3418ACB         5B9CCA4F7763E373         682E6FF3D6B2B8A3           748F82EE				
D807AA98A3030242         12835B0145706FBE         243185B4EE4B28C         550C7DC3D5FFB4E2           72BE5D74F27B896F         80DEB1FE3B1696B1         9BDC06A725C71235         C19BF174CF692694           E49B69C19EF14AD2         EFBE4786384F25E3         0FC19DC68B8CD5B5         240CA1CC77AC9C65           2DE92C6F592B0275         4A7484AA6EA6E483         5CB0A9DCBD41FBD4         76F988DA831153B5           983E5152EE66DFAB         A831C66D2DB43210         B00327C898FB213F         BF597FC7BEEF0EE4           C6E00BF33DA88FC2         D5A79147930AA725         06CA6351E003826F         142929670A0E6E70           27B70A8546D22FFC         2E1B21385C26C926         4D2C6DFC5AC42AED         53380D139D95B3DF           650A73548BAF63DE         766A0ABB3C77B2A8         81C2C92E47EDAEE6         92722C851482353B           A2BFE8A14CF10364         A81A664BBC423001         C24B8B70D0F89791         C76C51A30654BE30           D192E819D6EF5218         D69906245565A910         F40E35855771202A         106AA07032BBD1B8           19A4C116B8D2D0C8         1E376C085141AB53         2748774CDF8EEB99         34B0BCB5E19B48A8           391C0CB3C5C95A63         4ED8AA4AE3418ACB         5B9CCA4F7763E373         682E6FF3D6B2B8A3           748F82EE5DEFB2FC         78A5636F43172F60         84C87814A1F0AB72         8CC702081A6439EC           90BEFFFA2	428A2F98D728AE22	7137449123EF65CD	B5C0FBCFEC4D3B2F	E9B5DBA58189DBBC
72BE5D74F27B896F         80DEB1FE3B1696B1         9BDC06A725C71235         C19BF174CF692694           E49B69C19EF14AD2         EFBE4786384F25E3         0FC19DC68B8CD5B5         240CA1CC77AC9C65           2DE92C6F592B0275         4A7484AA6EA6E483         5CB0A9DCBD41FBD4         76F988DA831153B5           983E5152EE66DFAB         A831C66D2DB43210         B00327C898FB213F         BF597FC7BEEF0EE4           C6E00BF33DA88FC2         D5A79147930AA725         06CA6351E003826F         142929670A0E6E70           27B70A8546D22FFC         2E1B21385C26C926         4D2C6DFC5AC42AED         53380D139D95B3DF           650A73548BAF63DE         766A0ABB3C77B2A8         81C2C92E47EDAEE6         92722C851482353B           A2BFE8A14CF10364         A81A664BBC423001         C24B8B70D0F89791         C76C51A30654BE30           D192E819D6EF5218         D69906245565A910         F40E35855771202A         106AA07032BBD1B8           19A4C116B8D2D0C8         1E376C085141AB53         2748774CDF8EEB99         34B0BCB5E19B48A8           391C0CB3C5C95A63         4ED8AA4AE3418ACB         5B9CCA4F7763E373         682E6FF3D6B2B8A3           748F82EE5DEFB2FC         78A5636F43172F60         84C87814A1F0AB72         8CC702081A6439EC           90BEFFFA23631E28         A4506CEBDE82BDE9         EADA7DD6CDE0EB1E         F57D4F7FEE6ED178           06F067AA	3956C25BF348B538	59F111F1B605D019	923F82A4AF194F9B	AB1C5ED5DA6D8118
E49B69C19EF14AD2         EFBE4786384F25E3         0FC19DC68B8CD5B5         240CA1CC77AC9C65           2DE92C6F592B0275         4A7484AA6EA6E483         5CB0A9DCBD41FBD4         76F988DA831153B5           983E5152EE66DFAB         A831C66D2DB43210         B00327C898FB213F         BF597FC7BEEF0EE4           C6E00BF33DA88FC2         D5A79147930AA725         06CA6351E003826F         142929670A0E6E70           27B70A8546D22FFC         2E1B21385C26C926         4D2C6DFC5AC42AED         53380D139D95B3DF           650A73548BAF63DE         766A0ABB3C77B2A8         81C2C92E47EDAEE6         92722C851482353B           A2BFE8A14CF10364         A81A664BBC423001         C24B8B70D0F89791         C76C51A30654BE30           D192E819D6EF5218         D69906245565A910         F40E35855771202A         106AA07032BBD1B8           19A4C116B8D2D0C8         1E376C085141AB53         2748774CDF8EEB99         34B0BCB5E19B48A8           391C0CB3C5C95A63         4ED8AA4AE3418ACB         5B9CCA4F7763E373         682E6FF3D6B2B8A3           748F82EE5DEFB2FC         78A5636F43172F60         84C87814A1F0AB72         8CC702081A6439EC           90BEFFFA23631E28         A4506CEBDE82BDE9         BEF9A3F7B2C67915         C67178F2E372532B           CA273ECEEA26619C         D186B8C721C0C207         EADA7DD6CDE0EB1E         F57D4F7FEE6ED178           06F067AA	D807AA98A3030242	12835B0145706FBE	243185BE4EE4B28C	550C7DC3D5FFB4E2
2DE92C6F592B0275         4A7484AA6EA6E483         5CB0A9DCBD41FBD4         76F988DA831153B5           983E5152EE66DFAB         A831C66D2DB43210         B00327C898FB213F         BF597FC7BEEF0EE4           C6E00BF33DA88FC2         D5A79147930AA725         06CA6351E003826F         142929670A0E6E70           27B70A8546D22FFC         2E1B21385C26C926         4D2C6DFC5AC42AED         53380D139D95B3DF           650A73548BAF63DE         766A0ABB3C77B2A8         81C2C92E47EDAEE6         92722C851482353B           A2BFE8A14CF10364         A81A664BBC423001         C24B8B70D0F89791         C76C51A30654BE30           D192E819D6EF5218         D69906245565A910         F40E35855771202A         106AA07032BBD1B8           19A4C116B8D2D0C8         1E376C085141AB53         2748774CDF8EEB99         34B0BCB5E19B48A8           391C0CB3C5C95A63         4ED8AA4AE3418ACB         5B9CCA4F7763E373         682E6FF3D6B2BA3           748F82EE5DEFB2FC         78A5636F43172F60         84C87814A1F0AB72         8CC702081A6439EC           90BEFFFA23631E28         A4506CEBDE82BDE9         BEF9A3F7B2C67915         C67178F2E372532B           CA273ECEEA26619C         D186B8C721C0C207         EADA7DD6CDE0EB1E         F57D4F7FEE6ED178           06F067AA72176FBA         0A637DC5A2C898A6         113F9804BEF90DAE         1B710B35131C471B           28DB77F52	72BE5D74F27B896F	80DEB1FE3B1696B1	9BDC06A725C71235	C19BF174CF692694
983E5152EE66DFAB A831C66D2DB43210 B00327C898FB213F BF597FC7BEEF0EE4 C6E00BF33DA88FC2 D5A79147930AA725 06CA6351E003826F 142929670A0E6E70 27B70A8546D22FFC 2E1B21385C26C926 4D2C6DFC5AC42AED 53380D139D95B3DF 650A73548BAF63DE 766A0ABB3C77B2A8 81C2C92E47EDAEE6 92722C851482353B A2BFE8A14CF10364 A81A664BBC423001 C24B8B70D0F89791 C76C51A30654BE30 D192E819D6EF5218 D69906245565A910 F40E35855771202A 106AA07032BBD1B8 19A4C116B8D2D0C8 1E376C085141AB53 2748774CDF8EEB99 34B0BCB5E19B48A8 391C0CB3C5C95A63 4ED8AA4AE3418ACB 5B9CCA4F7763E373 682E6FF3D6B2B8A3 748F82EE5DEFB2FC 78A5636F43172F60 84C87814A1F0AB72 8CC702081A6439EC 90BEFFFA23631E28 A4506CEBDE82BDE9 BEF9A3F7B2C67915 C67178F2E372532B CA273ECEEA26619C D186B8C721COC207 EADA7DD6CDE0EB1E F57D4F7FEE6ED178 06F067AA72176FBA 0A637DC5A2C898A6 113F9804BEF90DAE 1B710B35131C471B 28DB77F523047D84 32CAAB7B40C72493 3C9EBE0A15C9BEBC 431D67C49C100D4C	E49B69C19EF14AD2	EFBE4786384F25E3	0FC19DC68B8CD5B5	240CA1CC77AC9C65
C6E00BF33DA88FC2         D5A79147930AA725         06CA6351E003826F         142929670A0E6E70           27B70A8546D22FFC         2E1B21385C26C926         4D2C6DFC5AC42AED         53380D139D95B3DF           650A73548BAF63DE         766A0ABB3C77B2A8         81C2C92E47EDAEE6         92722C851482353B           A2BFE8A14CF10364         A81A664BBC423001         C24B8B70D0F89791         C76C51A30654BE30           D192E819D6EF5218         D69906245565A910         F40E35855771202A         106AA07032BBD1B8           19A4C116B8D2D0C8         1E376C085141AB53         2748774CDF8EEB99         34B0BCB5E19B48A8           391C0CB3C5C95A63         4ED8AA4AE3418ACB         5B9CCA4F7763E373         682E6FF3D6B2BA3           748F82EE5DEFB2FC         78A5636F43172F60         84C87814A1F0AB72         8CC702081A6439EC           90BEFFFA23631E28         A4506CEBDE82BDE9         BEF9A3F7B2C67915         C67178F2E372532B           CA273ECEEA26619C         D186B8C721C0C207         EADA7DD6CDE0EB1E         F57D4F7FEE6ED178           06F067AA72176FBA         0A637DC5A2C898A6         113F9804BEF90DAE         1B710B35131C471B           28DB77F523047D84         32CAAB7B40C72493         3C9EBE0A15C9BEBC         431D67C49C100D4C	2DE92C6F592B0275	4A7484AA6EA6E483	5CBOA9DCBD41FBD4	76F988DA831153B5
27B70A8546D22FFC2E1B21385C26C9264D2C6DFC5AC42AED53380D139D95B3DF650A73548BAF63DE766A0ABB3C77B2A881C2C92E47EDAEE692722C851482353BA2BFE8A14CF10364A81A664BBC423001C24B8B70D0F89791C76C51A30654BE30D192E819D6EF5218D69906245565A910F40E35855771202A106AA07032BBD1B819A4C116B8D2D0C81E376C085141AB532748774CDF8EEB9934B0BCB5E19B48A8391C0CB3C5C95A634ED8AA4AE3418ACB5B9CCA4F7763E373682E6FF3D6B2B8A3748F82EE5DEFB2FC78A5636F43172F6084C87814A1F0AB728CC702081A6439EC90BEFFFA23631E28A4506CEBDE82BDE9BEF9A3F7B2C67915C67178F2E372532BCA273ECEEA26619CD186B8C721C0C207EADA7DD6CDE0EB1EF57D4F7FEE6ED17806F067AA72176FBA0A637DC5A2C898A6113F9804BEF90DAE1B710B35131C471B28DB77F523047D8432CAAB7B40C724933C9EBE0A15C9BEBC431D67C49C100D4C	983E5152EE66DFAB	A831C66D2DB43210	B00327C898FB213F	BF597FC7BEEF0EE4
650A73548BAF63DE       766A0ABB3C77B2A8       81C2C92E47EDAEE6       92722C851482353B         A2BFE8A14CF10364       A81A664BBC423001       C24B8B70D0F89791       C76C51A30654BE30         D192E819D6EF5218       D69906245565A910       F40E35855771202A       106AA07032BBD1B8         19A4C116B8D2D0C8       1E376C085141AB53       2748774CDF8EEB99       34B0BCB5E19B48A8         391C0CB3C5C95A63       4ED8AA4AE3418ACB       5B9CCA4F7763E373       682E6FF3D6B2B8A3         748F82EE5DEFB2FC       78A5636F43172F60       84C87814A1F0AB72       8CC702081A6439EC         90BEFFFA23631E28       A4506CEBDE82BDE9       BEF9A3F7B2C67915       C67178F2E372532B         CA273ECEEA26619C       D186B8C721C0C207       EADA7DD6CDE0EB1E       F57D4F7FEE6ED178         06F067AA72176FBA       0A637DC5A2C898A6       113F9804BEF90DAE       1B710B35131C471B         28DB77F523047D84       32CAAB7B40C72493       3C9EBE0A15C9BEBC       431D67C49C100D4C	C6E00BF33DA88FC2	D5A79147930AA725	06CA6351E003826F	142929670A0E6E70
A2BFE8A14CF10364 A81A664BBC423001 C24B8B70D0F89791 C76C51A30654BE30 D192E819D6EF5218 D69906245565A910 F40E35855771202A 106AA07032BBD1B8 19A4C116B8D2D0C8 1E376C085141AB53 2748774CDF8EEB99 34B0BCB5E19B48A8 391C0CB3C5C95A63 4ED8AA4AE3418ACB 5B9CCA4F7763E373 682E6FF3D6B2B8A3 748F82EE5DEFB2FC 78A5636F43172F60 84C87814A1F0AB72 8CC702081A6439EC 90BEFFFA23631E28 A4506CEBDE82BDE9 BEF9A3F7B2C67915 C67178F2E372532B CA273ECEEA26619C D186B8C721C0C207 EADA7DD6CDE0EB1E F57D4F7FEE6ED178 06F067AA72176FBA 0A637DC5A2C898A6 113F9804BEF90DAE 1B710B35131C471B 28DB77F523047D84 32CAAB7B40C72493 3C9EBE0A15C9BEBC 431D67C49C100D4C	27B70A8546D22FFC	2E1B21385C26C926	4D2C6DFC5AC42AED	53380D139D95B3DF
D192E819D6EF5218 D69906245565A910 F40E35855771202A 106AA07032BBD1B8 19A4C116B8D2D0C8 1E376C085141AB53 2748774CDF8EEB99 34B0BCB5E19B48A8 391C0CB3C5C95A63 4ED8AA4AE3418ACB 5B9CCA4F7763E373 682E6FF3D6B2B8A3 748F82EE5DEFB2FC 78A5636F43172F60 84C87814A1F0AB72 8CC702081A6439EC 90BEFFFA23631E28 A4506CEBDE82BDE9 BEF9A3F7B2C67915 C67178F2E372532B CA273ECEEA26619C D186B8C721C0C207 EADA7DD6CDE0EB1E F57D4F7FEE6ED178 06F067AA72176FBA 0A637DC5A2C898A6 113F9804BEF90DAE 1B710B35131C471B 28DB77F523047D84 32CAAB7B40C72493 3C9EBE0A15C9BEBC 431D67C49C100D4C	650A73548BAF63DE	766A0ABB3C77B2A8	81C2C92E47EDAEE6	92722C851482353B
19A4C116B8D2D0C8       1E376C085141AB53       2748774CDF8EEB99       34B0BCB5E19B48A8         391C0CB3C5C95A63       4ED8AA4AE3418ACB       5B9CCA4F7763E373       682E6FF3D6B2B8A3         748F82EE5DEFB2FC       78A5636F43172F60       84C87814A1F0AB72       8CC702081A6439EC         90BEFFFA23631E28       A4506CEBDE82BDE9       BEF9A3F7B2C67915       C67178F2E372532B         CA273ECEEA26619C       D186B8C721C0C207       EADA7DD6CDE0EB1E       F57D4F7FEE6ED178         06F067AA72176FBA       0A637DC5A2C898A6       113F9804BEF90DAE       1B710B35131C471B         28DB77F523047D84       32CAAB7B40C72493       3C9EBE0A15C9BEBC       431D67C49C100D4C	A2BFE8A14CF10364	A81A664BBC423001	C24B8B70D0F89791	C76C51A30654BE30
391C0CB3C5C95A63	D192E819D6EF5218	D69906245565A910	F40E35855771202A	106AA07032BBD1B8
748F82EE5DEFB2FC       78A5636F43172F60       84C87814A1F0AB72       8CC702081A6439EC         90BEFFFA23631E28       A4506CEBDE82BDE9       BEF9A3F7B2C67915       C67178F2E372532B         CA273ECEEA26619C       D186B8C721C0C207       EADA7DD6CDE0EB1E       F57D4F7FEE6ED178         06F067AA72176FBA       OA637DC5A2C898A6       113F9804BEF90DAE       1B710B35131C471B         28DB77F523047D84       32CAAB7B40C72493       3C9EBEOA15C9BEBC       431D67C49C100D4C	19A4C116B8D2D0C8	1E376C085141AB53	2748774CDF8EEB99	34B0BCB5E19B48A8
90BEFFFA23631E28       A4506CEBDE82BDE9       BEF9A3F7B2C67915       C67178F2E372532B         CA273ECEEA26619C       D186B8C721C0C207       EADA7DD6CDE0EB1E       F57D4F7FEE6ED178         06F067AA72176FBA       OA637DC5A2C898A6       113F9804BEF90DAE       1B710B35131C471B         28DB77F523047D84       32CAAB7B40C72493       3C9EBE0A15C9BEBC       431D67C49C100D4C	391C0CB3C5C95A63	4ED8AA4AE3418ACB	5B9CCA4F7763E373	682E6FF3D6B2B8A3
CA273ECEEA26619C D186B8C721COC207 EADA7DD6CDE0EB1E F57D4F7FEE6ED178 06F067AA72176FBA 0A637DC5A2C898A6 113F9804BEF90DAE 1B710B35131C471B 3C9EBE0A15C9BEBC 431D67C49C100D4C	748F82EE5DEFB2FC	78A5636F43172F60	84C87814A1F0AB72	8CC702081A6439EC
06F067AA72176FBA         0A637DC5A2C898A6         113F9804BEF90DAE         1B710B35131C471B           28DB77F523047D84         32CAAB7B40C72493         3C9EBE0A15C9BEBC         431D67C49C100D4C	90BEFFFA23631E28	A4506CEBDE82BDE9	BEF9A3F7B2C67915	C67178F2E372532B
28DB77F523047D84 32CAAB7B40C72493 3C9EBE0A15C9BEBC 431D67C49C100D4C	CA273ECEEA26619C	D186B8C721C0C207	EADA7DD6CDE0EB1E	F57D4F7FEE6ED178
	06F067AA72176FBA	0A637DC5A2C898A6	113F9804BEF90DAE	1B710B35131C471B
4CC5D4BECB3E42B6	28DB77F523047D84	32CAAB7B40C72493	3C9EBEOA15C9BEBC	431D67C49C100D4C
	4CC5D4BECB3E42B6	4597F299CFC657E2	5FCB6FAB3AD6FAEC	6C44198C4A475817

There are 80 constants,  $K_0$  to  $K_{79}$ , each of 64 bits. Similar These values are calculated from the first 80 prime numbers (2, 3,..., 409). For example, the 80th prime is 409, with the cubic root  $(409)^{1/3} = 7.42291412044$ . Converting this number to binary with only 64 bits in the fraction part, we get

 $(111.0110\ 1100\ 0100\ 0100\ \dots\ 0111)_2 \ \to \ (7.6\text{C}44198\text{C}4\text{A}475817)_{16}$ 

The fraction part: (6C44198C4A475817)<sub>16</sub>

### Example 12.7

We apply the Majority function on buffers A, B, and C. If the leftmost hexadecimal digits of these buffers are 0x7, 0xA, and 0xE, respectively, what is the leftmost digit of the result?

#### **Solution**

The digits in binary are 0111, 1010, and 1110.

- a. The first bits are 0, 1, and 1. The majority is 1.
- b. The second bits are 1, 0, and 1. The majority is 1.
- c. The third bits are 1, 1, and 1. The majority is 1.
- d. The fourth bits are 1, 0, and 0. The majority is 0.

The result is 1110, or 0xE in hexadecimal.

#### Example 12.8

We apply the Conditional function on E, F, and G buffers. If the leftmost hexadecimal digits of these buffers are 0x9, 0xA, and 0xF respectively, what is the leftmost digit of the result?

#### **Solution**

The digits in binary are 1001, 1010, and 1111.

- a. The first bits are 1, 1, and 1. The result is  $F_1$ , which is 1.
- b. The second bits are 0, 0, and 1. The result is  $G_2$ , which is 1.
- c. The third bits are 0, 1, and 1. The result is  $G_3,$  which is 1.
- d. The fourth bits are 1, 0, and 1. The result is  $F_4$ , which is 0.

The result is 1110, or 0xE in hexadecimal.

# 12.2.3 Analysis

With a message digest of 512 bits, SHA-512 expected to be resistant to all attacks, including collision attacks.