



John called, Mary didn't, is it Earthquake?

$$P(E=1 | J=1, M=0) ?$$

$$= \frac{P(E=1, J=1, M=0)}{P(J=1, M=0)} = \frac{P(A|B)}{P(B)}$$

Convenient Notation

$$P(e/j, \sim m) = \frac{P(e, j, \sim m)}{P(j, \sim m)}$$

$$= \frac{\sum_b \sum_a P(e, j, \sim m, b, a)}{\sum_b \sum_a P(j, \sim m, e, b, a)}$$

margi-
nalize
missing
variables

$$\textcircled{A} = P(e, j, \sim m, \sim b, \sim a) + P(e, j, \sim m, \sim b, a) + P(e, j, \sim m, b, \sim a) + P(e, j, \sim m, b, a)$$

$$\textcircled{B} = P(\sim e, j, \sim m, \sim b, \sim a) + P(\sim e, j, \sim m, \sim b, a) + P(\sim e, j, \sim m, b, \sim a) + P(\sim e, j, \sim m, b, a)$$

$$P(e, j, \sim m, \sim b, \sim a) = P(j/\sim a) \cdot P(\sim m/\sim a) \cdot P(\sim a/\sim b, e) \cdot P(\sim b) \cdot P(e) = 0.00007021$$

$$P(e, j, \sim m, \sim b, a) = P(j/a) \cdot P(\sim m/a) \cdot P(a/\sim b, e) \cdot P(\sim b) \cdot P(e) = 0.0001564$$

$$P(e, j, \sim m, b, \sim a) = P(j/\sim a) \cdot P(\sim m/\sim a) \cdot P(\sim a/b, e) \cdot P(b) \cdot P(e) = 4.95 \times 10^{-9}$$

$$P(e, j, \sim m, b, a) = P(j/a) \cdot P(\sim m/a) \cdot P(a/b, e) \cdot P(b) \cdot P(e) = 5.13 \times 10^{-7}$$

$$P(\sim e, j, \sim m, \sim b, \sim a) = P(j/\sim a) \cdot P(\sim m/\sim a) \cdot P(\sim a/\sim b, \sim e) \cdot P(\sim b) \cdot P(\sim e) = 0.0493$$

$$P(\sim e, j, \sim m, \sim b, a) = P(j/a) \cdot P(\sim m/a) \cdot P(a/\sim b, \sim e) \cdot P(\sim b) \cdot P(\sim e) = 0.00026919$$

$$P(\sim e, j, \sim m, b, \sim a) = P(j/\sim a) \cdot P(\sim m/\sim a) \cdot P(\sim a/b, \sim e) \cdot P(b) \cdot P(\sim e) = 2.9641 \times 10^{-6}$$

$$P(\sim e, j, \sim m, b, a) = P(j/a) \cdot P(\sim m/a) \cdot P(a/b, \sim e) \cdot P(b) \cdot P(\sim e) = 0.00025329$$

$$P(e/j, \sim m) = \frac{P(e, j, \sim m)}{P(j, \sim m)}$$

$$= \frac{\sum_b \sum_a P(e, j, \sim m, b, a)}{\sum_b \sum_a P(j, \sim m, e, b, a)}$$

margi-
nalize
missing
variables

$$= \frac{(A)}{(B)}$$

$$= \frac{(0.0000702 + 0.0001564 + 4.95 \times 10^{-9} + 5.13 \times 10^{-7})}{[0.0000702 + 0.0001564 + 4.95 \times 10^{-9} + 5.13 \times 10^{-7} + 0.0493 + 0.00026919 + 2.9641 \times 10^{-6} + 0.000253]}$$

$$= \frac{0.00022718}{0.0501}$$

$$= 0.0045345$$

$$p(\sim e | j; \sim m) =$$