

## Chapter 4

### Syntax Analysis

#### Constructing Parsing Table – Example 5

$S \rightarrow i E t S S' \mid a$	$\text{First}(S) = \{ i, a \}$	$\text{Follow}(S) = \{ e, \$ \}$
$S' \rightarrow e S \mid \epsilon$	$\text{First}(S') = \{ e, \epsilon \}$	$\text{Follow}(S') = \{ e, \$ \}$
$E \rightarrow b$	$\text{First}(E) = \{ b \}$	$\text{Follow}(E) = \{ t \}$

## Constructing Parsing Table – Example 5

$S \rightarrow iEtSS' \mid a$	$\text{First}(S) = \{i, a\}$	$\text{Follow}(S) = \{e, \$\}$
$S' \rightarrow eS \mid \epsilon$	$\text{First}(S') = \{e, \epsilon\}$	$\text{Follow}(S') = \{e, \$\}$
$E \rightarrow b$	$\text{First}(E) = \{b\}$	$\text{Follow}(E) = \{t\}$

 $S \rightarrow iEtSS'$ 
 $S \rightarrow a$ 
 $E \rightarrow b$ 
 $\text{First}(iEtSS') = \{i\}$ 
 $\text{First}(a) = \{a\}$ 
 $\text{First}(b) = \{b\}$ 
 $S' \rightarrow eS$ 
 $S \rightarrow \epsilon$ 
 $\text{First}(eS) = \{e\}$ 
 $\text{First}(\epsilon) = \{\epsilon\}$ 
 $\text{Follow}(S') = \{e, \$\}$ 

Non-terminal	INPUT SYMBOL					
	a	b	e	i	t	\$
S	<u><math>S \rightarrow a</math></u>			<u><math>S \rightarrow iEtSS'</math></u>		
S'			<u><math>S' \rightarrow \epsilon</math></u> <u><math>S' \rightarrow eS</math></u>			<u><math>S' \rightarrow \epsilon</math></u>
E		<u><math>E \rightarrow b</math></u>				

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## LL(1) Grammars

**L** : Scan input from Left to Right

**L** : Construct a Leftmost Derivation

**1** : Use “1” input symbol as lookahead in conjunction with stack to decide on the parsing action

**LL(1) grammars** == they have no multiply-defined entries in the parsing table.

**Properties of LL(1) grammars:**

- Grammar can't be ambiguous or left recursive
- Grammar is LL(1)  $\Leftrightarrow$  when  $A \rightarrow \alpha \mid \beta$ 
  - $\alpha$  &  $\beta$  do not derive strings starting with the same terminal a
  - Either  $\alpha$  or  $\beta$  can derive  $\epsilon$ , but not both.

**Note:** It may not be possible for a grammar to be manipulated into an LL(1) grammar

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Is given grammar LL(1) ?

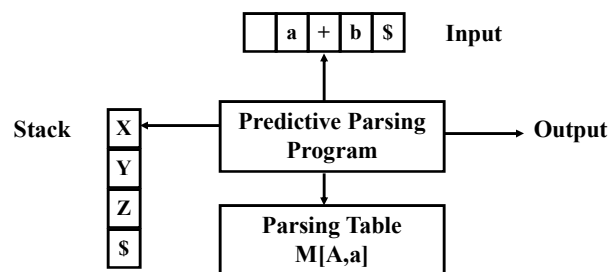
$S \rightarrow AaAb \mid BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

## Error Recovery

**When Do Errors Occur? Recall Predictive Parser Function:**



1. If `X` is a terminal and it doesn't match input.
2. If `M[X, Input]` is empty – No allowable actions

Consider two recovery techniques:

- A. Panic Mode
- B. Phrase-level Recovery

## Panic-Mode Recovery

Assume a non-terminal on the top of the stack.

1. Idea:
  - skip symbols on the input until a token in a selected set of synchronizing tokens is found.**
2. The choice for a synchronizing set is important.
  - Some ideas:**
    - a. Define the synchronizing set of A to be FOLLOW(A). then skip input until a token in FOLLOW(A) appears and then pop A from the stack. Resume parsing...
    - b. Add symbols of FIRST(A) into synchronizing set. In this case we skip input and once we find a token in FIRST(A) we resume parsing from A.
    - c. Productions that lead to  $\epsilon$  if available might be used.
3. **If a terminal appears on top of the stack and does not match to the input  $\Rightarrow$  pop it and and continue parsing (issuing an error message saying that the terminal was inserted).**

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## Panic Mode Recovery, II

**General Approach: Modify the empty cells of the Parsing Table.**

1. if  $M[A, a] = \{\text{empty}\}$  and  $a$  belongs to Follow(A) then we set  $M[A, a] = \text{"synch"}$

**Error-recovery Strategy :**

**If A=top-of-the-stack and a=current-input,**

1. **If A is NT and  $M[A, a] = \{\text{empty}\}$  then skip  $a$  from the input.**
2. **If A is NT and  $M[A, a] = \{\text{synch}\}$  then pop A.**
3. **If A is a terminal and  $A \neq a$  then pop token (essentially inserting it).**

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## Constructing Parsing Table – Example 1

$E \rightarrow TE'$	$\text{First}(E, F, T) = \{ (, id \}$	$\text{Follow}(E, E') = \{ ), \$ \}$
$E' \rightarrow + TE' \mid \epsilon$	$\text{First}(E') = \{ +, \epsilon \}$	$\text{Follow}(F) = \{ *, +, ), \$ \}$
$T \rightarrow FT'$	$\text{First}(T') = \{ *, \epsilon \}$	$\text{Follow}(T, T') = \{ +, ), \$ \}$
$T' \rightarrow * FT' \mid \epsilon$		
$F \rightarrow ( E ) \mid id$		

$E \rightarrow TE'$   
 $E' \rightarrow + TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow * FT' \mid \epsilon$   
 $F \rightarrow ( E ) \mid id$

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## Revised Parsing Table / Example

Non-terminal	INPUT SYMBOL					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$	_____	_____	$E \rightarrow TE'$	_____	_____
E'	_____	$E' \rightarrow + TE'$	_____	_____	$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	_____	_____	$T \rightarrow FT'$	_____	_____
T'	_____	$T' \rightarrow \epsilon$	$T' \rightarrow * FT'$	_____	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$	_____	_____	$F \rightarrow ( E )$	_____	_____

From Follow sets. Pop top  
 of stack NT  
 “synch” action

Skip input symbol

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### Revised Parsing Table / Example(2)

STACK	INPUT	Remark
SE	+ id * + id\$	error, skip +
SE	id * + id\$	
SE'T	id * + id\$	
SE'T'F	id * + id\$	
SE'T'id	id * + id\$	
SE'T'	* + id\$	
SE'T'F*	* + id\$	
SE'T'F	+ id\$	error, M[F,+] = synch
SE'T'	+ id\$	F has been popped
SE'	+ id\$	
SE'T+	+ id\$	
SE'T	id\$	
SE'T'F	id\$	
SE'T'id	id\$	
SE'T'	\$	
SE'	\$	
S	\$	

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### Writing Error Messages

1. **Keep input counter(s)**
2. **Recall: every non-terminal symbolizes an abstract language construct.**
3. **Examples of Error-messages for our usual grammar**

**E = means expression.**

  - top-of-stack is E, input is +  
“Error at location i, expressions cannot start with a ‘+’” or “error at location i, invalid expression”
  - Similarly for E, \*

**E' = expression ending.**

  1. Top-of-stack is E', input is \* or id  
“Error: expression starting at j is badly formed at location i”

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## Writing Error-Messages, II

### **T = summation term.**

- Top-of-stack is T, input is \*  
“error at location i, invalid term.”

### **T' = term ending**

- Top-of-stack is T', input is (  
“error: term starting at k is badly formed at location i”

### **F = summation/multiplication term**

#### **4. Messages for Synch Errors.**

Top-of-stack is F input is +

- “error at location i, expected summation/multiplication term missing”

Top-of-stack is E input is )

- “error at location i, expected expression missing”

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## Writing Error Messages, III

#### **5. When the top-of-the stack is a terminal that does not match...**

E.g. top-of-stack is id and the input is +

- “error at location i: identifier expected”

Top-of-stack is ) and the input is terminal other than )

- Every time you match an ‘(’  
push the location of ‘(’ to a “left parenthesis” stack.  
— this can also be done with the symbol stack.
- When the mismatch is discovered look at the left parenthesis stack to recover the location of the parenthesis.
- “error at location i: left parenthesis at location m has no closing right parenthesis”  
— E.g. consider ( id \* + (id id) \$

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## Phrase-Level Recovery

1. Fill in blanks entries of parsing table with error handling routines
2. These routines
  - a) Modify stack and / or input stream
  - b) Issue error message
3. Problems:
  - a) Modifying stack has to be done with care, so as to not create possibility of derivations that aren't in language
  - b) Infinite loops must be avoided
4. Can be used in conjunction with panic mode to have more complete error handling

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$T' \rightarrow * FT' \mid \epsilon$		
$F \rightarrow ( E ) \mid id$		

$E \rightarrow TE'$   
 $E' \rightarrow + TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow * FT' \mid \epsilon$   
 $F \rightarrow ( E ) \mid id$

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## How Would You Implement TD Parser

- Stack – Easy to handle.
- Input Stream – Responsibility of lexical analyzer
- Key Issue – How is parsing table implemented ?

**One approach: Assign unique IDS**

Non-terminal	INPUT SYMBOL					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$	synch	synch
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$	synch		$T \rightarrow FT'$	synch	synch
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$	synch	synch	$F \rightarrow (E)$	synch	synch

All rules have unique IDs

synch actions

Also for blanks which handle errors

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## Revised Parsing Table:

Non-terminal	INPUT SYMBOL					
	id	+	*	(	)	\$
E	1	18	19	1	9	10
E'	20	2	21	22	3	3
T	4	11	23	4	12	13
T'	24	6	5	25	6	6
F	8	14	15	7	16	17

1  $E \rightarrow TE'$

2  $E' \rightarrow +TE'$

3  $E' \rightarrow \epsilon$

4  $T \rightarrow FT'$

5  $T' \rightarrow *FT'$

6  $T' \rightarrow \epsilon$

7  $F \rightarrow (E)$

8  $F \rightarrow id$

9 – 17 :  
Sync  
Actions

18 – 25 :  
Error  
Handlers

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