

Chapter 4

Syntax Analysis

What is Follow of Non-Terminal ?

Given the production rules:

$S \rightarrow aABb$

$A \rightarrow c \mid \epsilon$

$B \rightarrow d \mid \epsilon$

$\text{First}(S) = \{a\}$

$\text{First}(A) = \{c, \epsilon\}$

$\text{First}(B) = \{d, \epsilon\}$

$\text{Follow}(S) = \{\$ \}$

$\text{Follow}(A) = \{d, b\}$

$\text{Follow}(B) = \{b\}$

Let's Derive 'ab'

SS
 $aABb\$$
 $aAb\$$
 $ab\$$

Let's Derive
 'adb'

SS
 $aABb\$$
 $aAdb\$$
 $ab\$$

Computing Follow(A) : All Non-Terminals

1. Place \$ in Follow(S), where S is the start symbol and \$ signals end of input
2. If there is a production $A \rightarrow \alpha B \beta$, then everything in First(β) is in Follow(B) except for ϵ .
3. If $A \rightarrow \alpha B$ is a production, or $A \rightarrow \alpha B \beta$ and $\beta \xRightarrow{*} \epsilon$ (First(β) contains ϵ), then everything in Follow(A) is in Follow(B)

Whatever followed A must follow B, since nothing follows B from the production rule.

$S \rightarrow AP$
 $A \rightarrow cB$
 $B \rightarrow d \mid \epsilon$
 $P \rightarrow f$

$S\$$
 $AP\$$
 $cBP\$$
 $cBf\$$

$S \rightarrow AP$
 $A \rightarrow cBQ$
 $B \rightarrow d \mid \epsilon$
 $P \rightarrow f$
 $Q \rightarrow \epsilon$

$S\$$
 $AP\$$
 $cBQP\$$
 $cBP\$$
 $cBf\$$

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Computing Follow : 1st Example

Recall:

$S \rightarrow i E t SS' \mid a$

$S' \rightarrow eS \mid \epsilon$

$E \rightarrow b$

First(S) = { i, a }

First(S') = { e, ϵ }

First(E) = { b }

Follow(S) – Contains \$, since S is start symbol

Since $S \rightarrow i E t SS'$, put in First(S') – not ϵ

Here $S' \Rightarrow \epsilon$

Since $S' \rightarrow eS$, put 'e' in Follow(S')

So.... Follow(S) = { e, \$ }

Follow(S') = Follow(S) **HOW?**

Follow(E) = { t }

$S\$$
 $iEtSS'\$$
 $iEtSeS\$$

$S\$$
 $iEtSS'\$$
 $iEtS\$$

$S\$$
 $iEtSS'\$$
 $iEtiEtSS'S'\$$
 $iEtiEtSS'eS\$$

$S\$$
 $iEtSS'\$$
 $iEtiEtSS'S'\$$
 $iEtiEtSS'\$$

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Example 2

Compute Follow for:

$E \rightarrow TE'$
 $E' \rightarrow + TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow * FT' \mid \epsilon$
 $F \rightarrow (E) \mid id$

	First
E	(id
E'	ϵ +
T	(id
T'	ϵ *
F	(id

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Example 2

Compute Follow for:

$E \rightarrow TE'$
 $E' \rightarrow + TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow * FT' \mid \epsilon$
 $F \rightarrow (E) \mid id$

Follow (E) $\rightarrow \{), \$ \}$

Follow(E') \rightarrow Follow(E) $\rightarrow \{), \$ \}$

	First
E	(id
E'	ϵ +
T	(id
T'	ϵ *
F	(id

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Example 2

Compute Follow for:

$E \rightarrow TE'$
 $E' \rightarrow + TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow * FT' \mid \epsilon$
 $F \rightarrow (E) \mid id$

Follow(E) $\rightarrow \{), \$ \}$

Follow(E') \rightarrow Follow(E) $\rightarrow \{), \$ \}$

Follow(T) \rightarrow First(E') $\rightarrow \{ +, \epsilon \}$

Follow(T) $\rightarrow \{ +, \epsilon \} - \{ \epsilon \} \cup$ Follow(E)
 $\rightarrow \{ +,), \$ \}$

Follow(T') \rightarrow Follow(T) $\rightarrow \{ +,), \$ \}$

$E\$$
 $TE'\$$
 $T+TE'\$$

$E\$$
 $TE'\$$
 $FT'E'\$$
 $(E)T'E'\$$
 $(TE')T'E'\$$
 $(T)T'E'\$$

	First
E	(id
E'	ϵ +
T	(id
T'	ϵ *
F	(id

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Example 2

Compute Follow for:

$E \rightarrow TE'$
 $E' \rightarrow + TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow * FT' \mid \epsilon$
 $F \rightarrow (E) \mid id$

Follow(E) $\rightarrow \{), \$ \}$

Follow(E') \rightarrow Follow(E) $\rightarrow \{), \$ \}$

Follow(T) \rightarrow First(E') $\rightarrow \{ +, \epsilon \}$

Follow(T) $\rightarrow \{ +, \epsilon \} - \{ \epsilon \} \cup$ Follow(E)
 $\rightarrow \{ +,), \$ \}$

Follow(T') \rightarrow Follow(T) $\rightarrow \{ +,), \$ \}$

Follow(F) \rightarrow First(T') $\rightarrow \{ *, \epsilon \}$

Follow(F) $\rightarrow \{ *, \epsilon \} - \{ \epsilon \} \cup$ Follow(T)
 $\rightarrow \{ *, +,), \$ \}$

$E\$$
 $TE'\$$
 $FT'E'\$$
 $F*FT'E'\$$
 $F*FE'\$$
 $F*F+TE'\$$

	First
E	(id
E'	ϵ +
T	(id
T'	ϵ *
F	(id

$E\$$
 $TE'\$$
 $FT'E'\$$
 $(E)T'E'\$$
 $(TE')T'E'\$$
 $(FT'E')T'E'\$$
 $(F)T'E'\$$

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Example 3

$E \rightarrow TX$
 $X \rightarrow +E$
 $X \rightarrow \epsilon$
 $T \rightarrow \text{int } Y$
 $T \rightarrow (E)$
 $Y \rightarrow *T$
 $Y \rightarrow \epsilon$

Symbol	First
((
))
+	+
*	*
int	int
Y	$\epsilon, *$
X	$\epsilon, +$
T	int, (
E	int, (

Example 3

$E \rightarrow TX$
 $X \rightarrow +E$
 $X \rightarrow \epsilon$
 $T \rightarrow \text{int } Y$
 $T \rightarrow (E)$
 $Y \rightarrow *T$
 $Y \rightarrow \epsilon$

Symbol	First	Follow
((N/A
))	
+	+	
*	*	
int	int), \$, +
Y	$\epsilon, *$	
X	$\epsilon, +$	
T	int, (
E	int, (

Example 4

1. $S \rightarrow A a$
2. $A \rightarrow B D$
3. $B \rightarrow b$
4. $B \rightarrow \epsilon$
5. $D \rightarrow d$
6. $D \rightarrow \epsilon$

$\text{First}(S) = \{b, d, a\}$
 $\text{First}(A) = \{b, d, \epsilon\}$
 $\text{First}(B) = \{b, \epsilon\}$
 $\text{First}(D) = \{d, \epsilon\}$

Example 4

1. $S \rightarrow A a$
2. $A \rightarrow B D$
3. $B \rightarrow b$
4. $B \rightarrow \epsilon$
5. $D \rightarrow d$
6. $D \rightarrow \epsilon$

$\text{Follow}(S) = \{\$ \}$
 $\text{Follow}(A) = \{a\}$
 $\text{Follow}(B) = \{d, a\}$
 $\text{Follow}(D) = \{a\}$

$\text{First}(S) = \{b, d, a\}$
 $\text{First}(A) = \{b, d, \epsilon\}$
 $\text{First}(B) = \{b, \epsilon\}$
 $\text{First}(D) = \{d, \epsilon\}$

Example 5

- | | |
|--|--|
| 1. $C \rightarrow P F \text{ class id } X Y$ | |
| 2. $P \rightarrow \text{public}$ | |
| 3. $P \rightarrow \epsilon$ | |
| 4. $F \rightarrow \text{final}$ | $\text{First}(C) = \{\text{public, final, class}\}$ |
| 5. $F \rightarrow \epsilon$ | $\text{First}(P) = \{\text{public, } \epsilon\}$ |
| 6. $X \rightarrow \text{extends id}$ | $\text{First}(F) = \{\text{final, } \epsilon\}$ |
| 7. $X \rightarrow \epsilon$ | $\text{First}(X) = \{\text{extends, } \epsilon\}$ |
| 8. $Y \rightarrow \text{implements I}$ | $\text{First}(Y) = \{\text{implements, } \epsilon\}$ |
| 9. $Y \rightarrow \epsilon$ | $\text{First}(I) = \{\text{id}\}$ |
| 10. $I \rightarrow \text{id J}$ | $\text{First}(J) = \{\text{'', ' ', } \epsilon\}$ |
| 11. $J \rightarrow \text{'', ' ', I}$ | |
| 12. $J \rightarrow \epsilon$ | |

Example 5

- | | |
|--|--|
| 1. $C \rightarrow P F \text{ class id } X Y$ | $\text{First}(C) = \{\text{public, final, class}\}$ |
| 2. $P \rightarrow \text{public}$ | $\text{First}(P) = \{\text{public, } \epsilon\}$ |
| 3. $P \rightarrow \epsilon$ | $\text{First}(F) = \{\text{final, } \epsilon\}$ |
| 4. $F \rightarrow \text{final}$ | $\text{First}(X) = \{\text{extends, } \epsilon\}$ |
| 5. $F \rightarrow \epsilon$ | $\text{First}(Y) = \{\text{implements, } \epsilon\}$ |
| 6. $X \rightarrow \text{extends id}$ | $\text{First}(I) = \{\text{id}\}$ |
| 7. $X \rightarrow \epsilon$ | $\text{First}(J) = \{\text{'', ' ', } \epsilon\}$ |
| 8. $Y \rightarrow \text{implements I}$ | $\text{Follow}(C) = \{\text{\$}\}$ |
| 9. $Y \rightarrow \epsilon$ | $\text{Follow}(P) = \{\text{final, class}\}$ |
| 10. $I \rightarrow \text{id J}$ | $\text{Follow}(F) = \{\text{class}\}$ |
| 11. $J \rightarrow \text{'', ' ', I}$ | $\text{Follow}(X) = \{\text{implements, \$}\}$ |
| 12. $J \rightarrow \epsilon$ | $\text{Follow}(Y) = \{\text{\$}\}$ |
| | $\text{Follow}(I) = \{\text{\$}\}$ |
| | $\text{Follow}(J) = \{\text{\$}\}$ |

Example - 6

$$S \rightarrow ABC \mid CbB \mid Ba$$

$$A \rightarrow da \mid BC$$

$$B \rightarrow g \mid \epsilon$$

$$C \rightarrow h \mid \epsilon$$

$$\text{First}(S) \rightarrow \{a, b, d, g, h, \epsilon\}$$

$$\text{First}(A) \rightarrow \{d, g, h, \epsilon\}$$

$$\text{First}(B) = \{g, \epsilon\}$$

$$\text{First}(C) = \{h, \epsilon\}$$

Example - 6

$$S \rightarrow ABC \mid CbB \mid Ba$$

$$A \rightarrow da \mid BC$$

$$B \rightarrow g \mid \epsilon$$

$$C \rightarrow h \mid \epsilon$$

$$\text{First}(S) \rightarrow \{a, b, d, g, h, \epsilon\}$$

$$\text{First}(A) \rightarrow \{d, g, h, \epsilon\}$$

$$\text{First}(B) = \{g, \epsilon\}$$

$$\text{First}(C) = \{h, \epsilon\}$$

$$\text{Follow}(S) \rightarrow \{\$ \}$$

$$\text{Follow}(A) \rightarrow \{g, h, \$ \}$$

$$\text{Follow}(B) \rightarrow \{a, g, h, \$ \}$$

$$\text{Follow}(C) \rightarrow \{b, g, h, \$ \}$$