

	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$
1	6	2	2	1	100	
2	5	3	4	1	1	
3	4	4	6	1	2	
4	3	5	8	1	1	
5	2	6	10	1	2	
6	1	7	12	1	1	

Outlier

\* Standard Deviation

\* Variance

$$\frac{\sum (x_i - \bar{x})^2}{n-1}$$

Covariance  
Any one of  $x_1$  &  $x_2$

Remove keep  $x_1$   
 $x_4 = 2x_1$   
No new info

Not Useful  
Remove

$$\frac{\sum (x_i - \bar{x}_i)(x_j - \bar{x}_j)}{n}$$

$$\sum_{i=1}^n (x_{1i} - \bar{x}_1)(x_{2i} - \bar{x}_2)$$

Variance, Standard Deviation,  
Co-variance

(1)

## Vectors & Matrices

"If vectors are super heroes,  
Matrix is Thanos"

← In some random marvel  
book

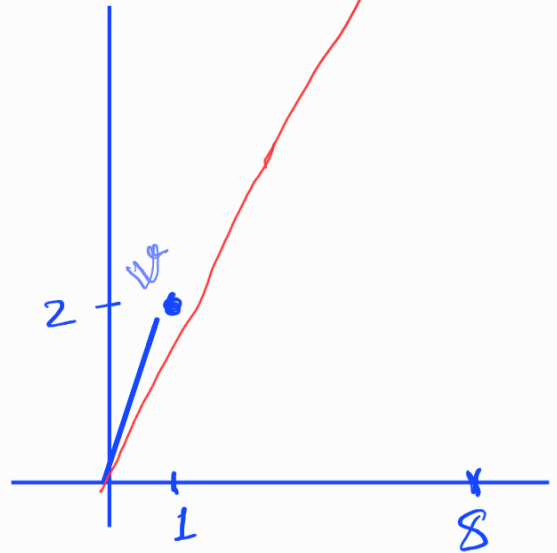
world of a geek.

$$V = [1, 2]$$

$$A = \begin{bmatrix} 2 & 3 \\ 3 & 4 \end{bmatrix}$$

$$A \times V =$$

$$\begin{bmatrix} 2 & 3 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix} = \begin{bmatrix} 8 \\ 11 \end{bmatrix}$$



"There is always a vector who will not be affected by the matrix"

"For every Thanos there is an Iron man"

"Eigen Vector"

$$A \cdot v = \lambda \cdot v$$

matrix                      vector  
Eigen vector

Scalar  
Eigen value

$$A = \begin{bmatrix} -6 & 3 \\ 4 & 5 \end{bmatrix}$$

$$A \cdot v - \lambda \cdot v = 0$$

$$(A - \lambda I) \cdot v = 0$$

$$A - \lambda I = 0$$

$$\begin{bmatrix} -6 & 3 \\ 4 & 5 \end{bmatrix} - \begin{bmatrix} \lambda & 0 \\ 0 & \lambda \end{bmatrix} = 0$$

$$\begin{bmatrix} -6-\lambda & 3 \\ 4 & 5-\lambda \end{bmatrix} = 0$$

$$(-6-\lambda)(5-\lambda) - 12 = 0$$

$$\lambda^2 + \lambda - 42 = 0$$

$$\boxed{\lambda_1 = -7, \quad \lambda_2 = 6}$$

$$A \cdot v = \lambda_1 \cdot v$$

$$\begin{bmatrix} -6 & 3 \\ 4 & 5 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = -7 \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$

$$-6v_1 + 3v_2 = -7v_1$$

$$4v_1 + 5v_2 = -7v_2$$

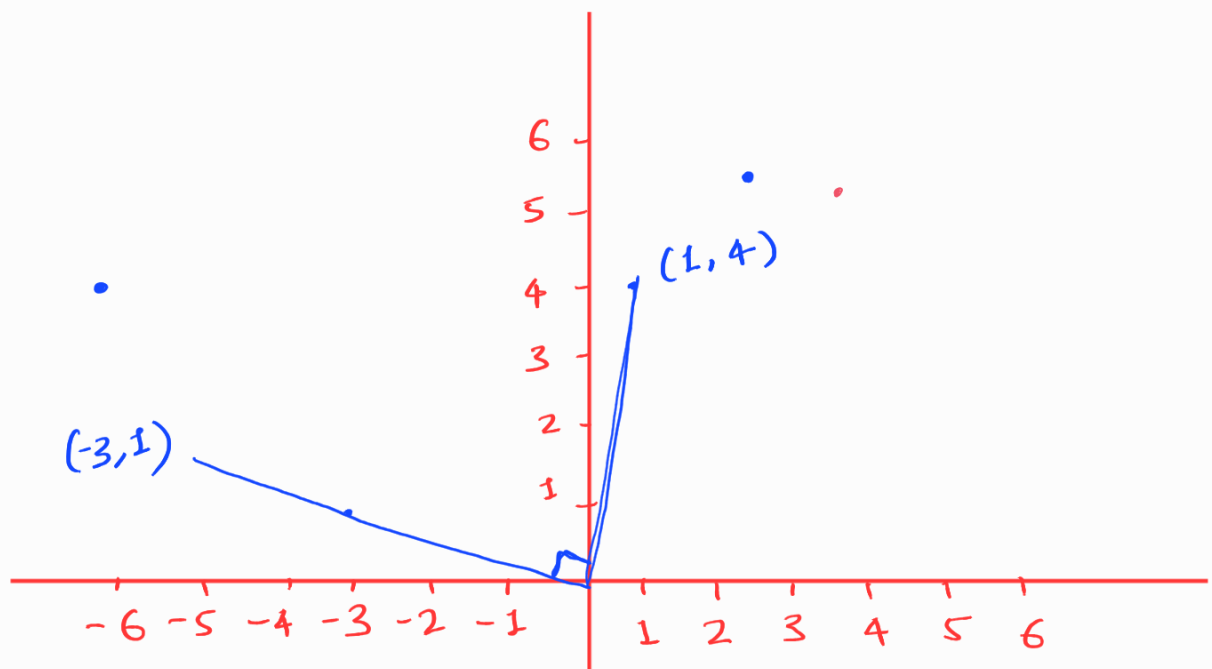
$$\boxed{v_1 = -3v_2}$$

$$V_1 = \begin{bmatrix} -3 \\ 1 \end{bmatrix}, \quad \lambda_1 = -7$$

$$V_2 = \begin{bmatrix} 1 \\ 4 \end{bmatrix}, \quad \lambda_2 = 6$$

$$A \times V = \begin{bmatrix} -6 & 3 \\ 4 & 5 \end{bmatrix} \begin{bmatrix} 1 \\ 4 \end{bmatrix} \checkmark$$

$$= \begin{bmatrix} 6 \\ 24 \end{bmatrix} = 6 \begin{bmatrix} 1 \\ 4 \end{bmatrix} \checkmark$$



- ① Eigen Vectors can serve as axis to study datapoints
- ② Along Eigen Vectors data points are not distorted

- ③ Eigen Vectors point to the direction along which the variance is maximum

Covariance + Eigen Vector

↳ Principal Component Analysis (PCA)