## **Load Balancing**

Problem Input: m identical machines, n jobs with ith job having processing time ti

Goal: Schedule jobs to computers such that

- Jobs run contiguously on a machine
- A machine processes only one job a time
- Makespan or maximum load on any machine is minimized

Definition Let A(i) be the set of jobs assigned to machine i. The load on i is Ti = Summation of time of every job executed on i. The makespan of A is T = maxi Ti

Load Balancing is NP-Complete.

- 1. Greedy Algorithm
  - Consider the jobs in some fixed order
  - Assign job j to the machine with lowest load so far

Consider 6 jobs whose processing times is given as follows Jobs 1 2 3 4 5 6

```
ti 2 3 4 6 2 2
```

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1 job 1(2) -- job 4(6) -----: 8
2 job 2(3) --- job 5(2) ---: 5
3 job 3(4) ---- job 6 (2) ---: 6
```

The loads are: T1 = 8, T2 = 5, and T3 = 6. So makespan of schedule is 8

Is the greedy algorithm optimal?

Modified Greedy Sort the jobs in descending order of processing time, and process jobs using greedy algorithm

Consider 6 jobs whose processing times is given as follows

Jobs 1 2 3 4 5 6

ti 2 3 4 6 2 2

Jobs 4 3 2 1 5 6 time 6 4 3 2 2 2

Machine 1 J4 - - - - : 6 Machine 2 J3 - - - J2 - : 6 Machine 3 J2 - - - J1 - - J3 - : 7

Makespan: 7

Is the modified greedy algorithm always optimal?

Greedy algorithm:

9 1 3 8 Jobs Time 5 5 7 8 1 J1 - - - - J4 - - - - - J8 - - - - - -Machine 1 : 20 Machine 2 J2 - - - - - J6 – J7 - - - -: 14 J3 - - - - J3 - - - - - J9 -Machine 3 : 13

Makespan: 20

Modified greedy algorithm:

Jobs 2 8 4 5 1 3 7 6 9 Time 8 8 7 7 5 5 5 1 1

Makespan: 18

 Machine 1
 5
 5
 7
 : 17

 Machine 2
 8
 7
 1
 1
 : 17

 Machine 3
 8
 5
 : 13

Machine 1 8 7 1: 16 Machine 2 8 7 1: 16 Machine 3 5 5 5: 15