

Q3

$$X = \begin{bmatrix} X^{(1)} \\ X^{(2)} \\ X^{(3)} \\ \vdots \\ X^{(m)} \end{bmatrix}, Y = \begin{bmatrix} Y^{(1)} \\ \vdots \\ Y^{(m)} \end{bmatrix}$$

$(n+1)$ indicates we have an extra feature containing only '1's.

Parameters

$$\Theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

θ_0

~~This ~~removes the~~~~
This ensures that $\hat{Y} = X\Theta$ works (instead of $Y = w^T X + b$)

In BGD

$$\theta_j \leftarrow \theta_j - \alpha \frac{\partial J(\theta)}{\partial \theta_j}, \text{ where } J(\theta) = \frac{1}{2} \sum_{i=1}^m (X^{(i)}\theta - y)^2$$

Repeat
 $\Rightarrow \theta_j \leftarrow \theta_j - \alpha \sum_{i=1}^m (X^{(i)}\Theta - Y^{(i)}) X_j^{(i)}, j = 1, 2, \dots, n+1$
until $J(\Theta)$ stops ~~improving~~ reducing.

SGD

Repeat
 $\theta_j \leftarrow \theta_j - \alpha (X^{(i)}\Theta - Y^{(i)}), j = 1, 2, \dots, n+1$
until $J(\Theta) = (X^{(i)}\Theta - Y^{(i)})^2$ stops reducing

Repeat this ←
for each training example
i.e $i = 1, 2, \dots, m$.

For complex (large) datasets, SGD is better as it provides ~~better~~ faster convergence.

~~Math~~ A mathematical proof is

~~Entail~~

Intuition

In BGD, we have to calculate ~~the~~ $\sum_{i=1}^m X^{(i)}\Theta - Y^{(i)}$ by iterating over all training examples before updating θ_j .

Whereas in SGD, an ~~update~~ optimization is made for each training example. This makes ~~sense~~ It is highly likely that ~~the~~ optimizing Θ for each training example is ~~the~~ "close" to the ~~dirn~~ when we optimize entire cost fn.