### Relational Data

Kylie Ariel Bemis

10/10/2017

### Housekeeping

- Miniposter is due today on Piazza
- ▶ Homework 2 is due Friday (9/13) on Piazza
- ▶ The Midterm Exam is next Tuesday (9/17)
  - We will review Friday
  - Material covers everything through today
- ▶ Project groups (2-4 people) are due on the Midterm Exam
- Project guidelines will be posted on Piazza in next few days

### Introduction to Relational Data

What is relational data?

Often data analysis involve multiple tables of related data.

The data analysis steps we need to do typically depend on the *relationships* between the different tables of data.

Each relationship is defined on a pair of tables.

We need data manipulation verbs that work on pairs of tables.

### Introduction to Relational Data

dplyr provides three families of verbs for working with relational data:

- Mutating joins add new variables from one data frame to matching observations in another
- ► **Filtering joins** filter observations from one data frame based on matching observations in another
- ▶ **Set operations** treat observations (rows) as elements of a set

Most relational data live in *relational database management systems* (RDBMS) such as MySQL, SQLite, PostgreSQL, etc. and are accessed via Structured Query Language (SQL).

We will see that the names of dplyr verbs for relational data are heavily influenced by their SQL equivalents.

### Relational Data in R

#### library(nycflights13)

The nycflights13 package we have been using for examples and homework actually includes five related tables:

- airlines gives airline names based on their abbreviated code
- airports gives information about airports, identified by faa code
- ▶ flights gives the data on individual flights out of NYC airports
- planes gives information about each plane, identified by tailnum
- weather gives weather information for each NYC airport by hour

# nycflights 13 - airlines

#### airlines

##	# A	tibble:	16 x 2			
##	carrier name					
##		<chr></chr>	<chr></chr>			
##	1	9E	Endeavor Air Inc.			
##	2	AA	American Airlines Inc.			
##	3	AS	Alaska Airlines Inc.			
##	4	В6	JetBlue Airways			
##	5	DL	Delta Air Lines Inc.			
##	6	EV	ExpressJet Airlines Inc.			
##	7	F9	Frontier Airlines Inc.			
##	8	FL	AirTran Airways Corporation			
##	9	HA	Hawaiian Airlines Inc.			
##	10	MQ	Envoy Air			
##	11	00	SkyWest Airlines Inc.			
##	12	UA	United Air Lines Inc.			
##	13	US	US Airways Inc.			
##	14	VX	Virgin America			
##	15	WN	Southwest Airlines Co.			
##	16	YV	Mesa Airlines Inc.			

### nycflights13 - airports

#### airports

```
## # A tibble: 1,458 x 8
##
        faa
                                               lat
                                                           lon
                                     name
##
      <chr>>
                                     <chr>
                                             <dbl>
                                                         <dbl> <
##
   1
       04G
                        Lansdowne Airport 41.13047 -80.61958
            Moton Field Municipal Airport 32.46057 -85.68003
##
    2 06A
##
   3
       06C
                      Schaumburg Regional 41.98934 -88.10124
##
       06N
                           Randall Airport 41.43191 -74.39156
                     Jekyll Island Airport 31.07447 -81.42778
##
       09J
##
       0A9
           Elizabethton Municipal Airport 36.37122 -82.17342
       0G6
                  Williams County Airport 41.46731 -84.50678
##
##
   8
       0G7
            Finger Lakes Regional Airport 42.88356 -76.78123
##
       0P2
             Shoestring Aviation Airfield 39.79482 -76.64719
   10
       0S9
                     Jefferson County Intl 48.05381 -122.81064
##
##
   # ... with 1,448 more rows, and 2 more variables: dst <chr>,
```

### nycflights13 - flights

#### flights

```
## # A tibble: 336,776 x 19
##
       vear month
                    day dep_time sched_dep_time dep_delay arr_ti
##
      <int> <int> <int>
                            <int>
                                            <int>
                                                      <dbl>
                                                                <in
                                                                  8
##
    1
       2013
                              517
                                              515
       2013
                              533
                                              529
##
    2
                                                          4
    3 2013
                              542
                                              540
                                                                  9
##
##
       2013
                              544
                                              545
                                                         -1
                                                                 10
    4
                                                                  8
##
    5
       2013
                              554
                                              600
                                                         -6
##
    6
       2013
                              554
                                              558
                                                         -4
##
    7
       2013
                              555
                                              600
                                                         -5
       2013
                                                                  7
##
    8
                              557
                                              600
                                                         -3
                                                                  8
##
    9
       2013
                              557
                                              600
                                                         -3
##
   10
       2013
                              558
                                              600
                                                         -2
##
    ... with 336,766 more rows, and 12 more variables: sched ar
## #
       arr delay <dbl>, carrier <chr>, flight <int>, tailnum <ch
##
       origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>,
## #
       minute <dbl>, time hour <dttm>
```

### nycflights13 - planes

#### planes

```
## # A tibble: 3,322 x 9
##
     tailnum year
                                     type manufacturer
##
      <chr> <int>
                                    <chr>
                                                    <chr>
##
   1 N10156 2004 Fixed wing multi engine EMBRAER EMB
   2 N102UW 1998 Fixed wing multi engine AIRBUS INDUSTRIE
##
                                                          A3
                                                           АЗ
##
   3 N103US 1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                                           АЗ
##
   4 N104UW 1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                               EMBRAER EMB
##
   5 N10575
              2002 Fixed wing multi engine
##
   6 N105UW
              1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                                           АЗ
              1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                                           АЗ
##
   7 N107US
              1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                                           АЗ
##
   8 N108UW
   9 N109UW 1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                                           АЗ
##
## 10 N110UW 1999 Fixed wing multi engine AIRBUS INDUSTRIE
                                                           A3
## # ... with 3,312 more rows, and 4 more variables: engines <in
## #
      seats <int>, speed <int>, engine <chr>
```

### nycflights13 - weather

#### weather

```
## # A tibble: 26,130 x 15
##
     origin year month
                         day hour temp dewp humid wind_dir
##
      <chr> <dbl> <dbl> <int> <int> <dbl> <dbl> <dbl> <dbl>
                                                       <dbl>
                                                         230
##
        EWR
             2013
                      1
                           1
                                 0 37.04 21.92 53.97
##
        EWR
             2013
                                 1 37.04 21.92 53.97
                                                         230
   3
        EWR.
             2013
                                 2 37.94 21.92 52.09
                                                         230
##
##
        EWR 2013
                                 3 37.94 23.00 54.51
                                                         230
##
   5
        EWR
            2013
                                 4 37.94 24.08 57.04
                                                         240
##
   6
        EWR
            2013
                                 6 39.02 26.06 59.37
                                                         270
##
   7
        EWR
             2013
                                 7 39.02 26.96 61.63
                                                         250
##
   8
        EWR
             2013
                                 8 39.02 28.04 64.43
                                                         240
##
        EWR
             2013
                                 9 39.92 28.04 62.21
                                                         250
             2013
##
   10
        EWR
                                10 39.02 28.04 64.43
                                                         260
  # ... with 26,120 more rows, and 5 more variables: wind gust
##
##
      precip <dbl>, pressure <dbl>, visib <dbl>, time hour <dtt
```

### Relations in nycflights13

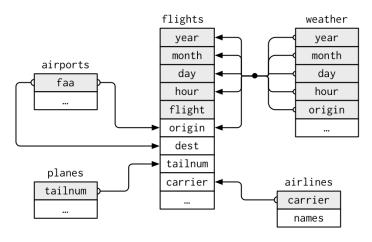


Figure 1: nycflights13

### Keys

Variables used to connect tables are called keys.

A key may be a single variable, or multiple variables.

- ▶ A **primary key** uniquely identifies an observation in its own table
  - planes has a primary key of tailnum
  - airports has a primary key of faa
  - weather has a primary key of (year, month, day, hour, origin)
- ▶ A foreign key uniquely identifies an observation in another table
  - flights has a foreign key of tailnum for planes
  - flights has a foreign key of carrier for airlines
  - flights has a foreign key of (year, month, day, hour, origin) for weather

## Checking primary keys

```
planes %>%
  count(tailnum) %>%
  filter(n > 1)
```

```
## # A tibble: 0 x 2
## # ... with 2 variables: tailnum <chr>, n <int>
```

### Checking primary keys

weather %>%

```
count(year, month, day, hour, origin) %>%
filter(n > 1)
## # A tibble: 0 x 6
```

```
## # A tibble: 0 x 6
## # ... with 6 variables: year <dbl>, month <dbl>, day <int>, h
## # origin <chr>, n <int>
```

## What is the primary key of flights?

```
flights %>%
  count(year, month, day, flight) %>%
  filter(n > 1)
```

```
## # A tibble: 29,768 x 5
##
     year month day flight
                             n
##
     <int> <int> <int> <int> <int>
## 1 2013
                             2
##
   2 2013 1
   3 2013 1
##
   4 2013 1
##
                       11
##
   5 2013 1
                       15
   6 2013 1
                       21
##
   7 2013
                       27
##
   8 2013
                       31
##
   9 2013
                       32
##
##
  10 2013
                       35
## # ... with 29,758 more rows
```

### Add a primary key to flights

Called a surrogate key.

```
flights %>%
  mutate(row_id=row_number()) %>%
  select(row_id, year:dep_delay)
```

```
## # A tibble: 336,776 x 7
##
      row_id year month day dep_time sched_dep_time dep_delay
##
       <int> <int> <int> <int>
                                                             dbl>
                                   <int>
                                                  <int>
##
              2013
                                     517
                                                    515
    1
           1
                       1
                              1
              2013
                                     533
                                                    529
##
                       1
                              1
##
   3
           3 2013
                                     542
                                                    540
##
    4
           4
              2013
                                     544
                                                    545
                                                                -1
##
    5
           5
              2013
                                     554
                                                    600
##
           6 2013
                                     554
                                                    558
    7
              2013
                                     555
##
                              1
                                                    600
                                                                -5
##
    8
           8
              2013
                                     557
                                                    600
                                                                -3
                                     557
                                                                -3
##
    9
           9
              2013
                       1
                              1
                                                    600
                       1
##
   10
          10
              2013
                                     558
                                                    600
                                                                -2
    ... with 336,766 more rows
## #
```

### Why are keys important?

- ▶ A primary key and a foreign key in another table form a **relation**
- ► These relations are typically "one-to-many"
  - tailnum in planes connecting to many flights in flights
  - carrier in airlines connecting to many flights in flights
- ▶ We typically use these relations to describe how we **join** tables
- ▶ But as we will see soon, we can explicitly specify which variables are used to join tables, so why else might keys be important?

### How is relational data stored?

- ▶ Why don't we always keep all tables in memory like nycflights13?
- ▶ How do RDBMS's store the data in their tables?
- Are RDBMS's only good for accessing large data on disk?
- Why does data in a RDBMS sometimes occupy more storage space than the actual data?
- Why (as seen in the homework) are keys explicitly specified when creating tables in SQL?

## How does a RDBMS actually manage relational data?

- RBDMS's use indexing to look up data faster
- ▶ Indexes store where (in storage) to find particular rows in a table
- ▶ Indexes require additional storage space but allow faster queries
- ▶ Indexes are often a different type of data structure
  - B-trees (sorted data)
  - Hash tables (unsorted data)
- Primary and foreign keys are often indexed
- When working with data in memory, this often isn't important, but indexing can be very important when accessing data stored on disk

# Visualizing joins

	Х	У		
1	x1		1	у1
2	x2		2	y2
3	х3		4	у3

Figure 2: Two tables

## Visualizing joins

```
x <- tribble(
  ~key, ~val_x,
     1, "x1",
    2, "x2",
    3, "x3"
y <- tribble(
  ~key, ~val_y,
     1, "y1",
    2, "y2",
    4, "y3"
```

### Mutating joins

Similar to mutate(), mutating joins add new variables from one table (x) to matching observations in another (y)

- ▶ Inner joins keep only observations the appear in both x and y
- ▶ Outer joins keep observations that appear in at least one of x or y
  - ► A **left join** keeps all observations in x
  - A right join keeps all observations in y
  - A full join keeps all observations from both x and y

## Mutating joins

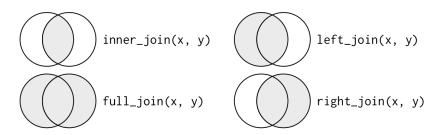


Figure 3: Types of joins as Venn diagrams

# Visualizing joins



Figure 4: Two tables with possible matches

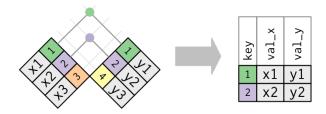


Figure 5: Keep observations that appear in both

```
inner_join(x, y)

## Joining, by = "key"

## # A tibble: 2 x 3

## key val_x val_y

## <dbl> <chr> <chr>
## 1 1 x1 y1

## 2 2 x2 y2
```

We can specify the variables used to join x and y explicitly.

```
inner_join(x, y, by = "key")
## # A tibble: 2 x 3
```

Joining by all variables that appear in both (default) is a natural join.

```
dplyr:
```

```
inner_join(x, y, by = "z")
```

base R:

```
merge(x, y, by = "z")
```

SQL:

```
SELECT * FROM x INNER JOIN y USING (z)
```

Inner joins can silently drop observations, so are rarely used for data analysis.

### Outer joins

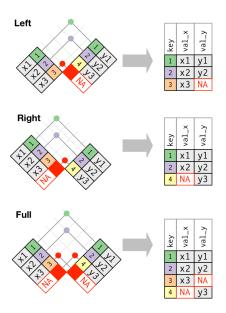


Figure 6: Keep observations that appear in at least one

## Left join

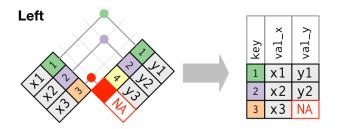


Figure 7: Keep observations that appear in  $\boldsymbol{x}$ 

## Left join

```
## Joining, by = "key"

## # A tibble: 3 x 3
## key val_x val_y
## <dbl> <chr> <chr> ## 1 1 x1 y1
## 2 2 x2 y2
## 3 3 x3 <NA>
```

left\_join(x, y)

### Left join

```
dplyr:
left_join(x, y, by = "z")
base R:
merge(x, y, all.x = TRUE, by = "z")
SQL:
SELECT * FROM x LEFT OUTER JOIN y USING (z)
Left joins are the most common type of join.
```

## Right join

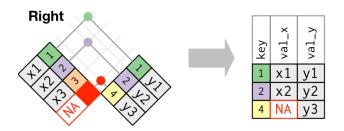


Figure 8: Keep observations that appear in y

### Right join

```
right_join(x, y)

## Joining, by = "key"

## # A tibble: 3 x 3

## key val_x val_y

## <dbl> <chr> <chr>
## 1 1 x1 y1

## 2 2 x2 y2

## 3 4 <NA> y3
```

### Right join

```
dplyr:
right_join(x, y, by = "z")
base R:
merge(x, y, all.y = TRUE, by = "z")
SQL:
SELECT * FROM x RIGHT OUTER JOIN y USING (z)
```

## Left versus right joins

What is the difference between the following calls?

left\_join(x, y)

right\_join(y, x)

```
left join(x, y)
## Joining, by = "key"
## # A tibble: 3 x 3
## key val_x val_y
## <dbl> <chr> <chr>
## 1 1 x1 y1
## 2 2 x2 y2
## 3 3 x3 <NA>
right_join(y, x)
## Joining, by = "key"
## # A tibble: 3 x 3
## key val_y val_x
## <dbl> <chr> <chr>
## 1 1 y1 x1
## 2 2 y2 x2
       3
         <NA> x3
## 3
```

- ▶ The only difference is the order of the returned columns
- ► Explicit right joins exist primarily for expressiveness
- ► Some RDBMS's do not even implement right joins (e.g., SQLite)

# Full join

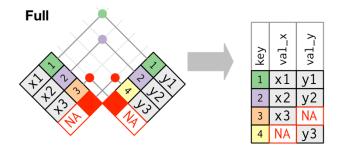


Figure 9: Keep observations that appear in either

# Full join

```
full_join(x, y)
## Joining, by = "key"
## # A tibble: 4 x 3
##
    key val_x val_y
## <dbl> <chr> <chr>
## 1
       1
         x1
               у1
## 2 2 x2 y2
## 3 3 x3 <NA>
       4 <NA> y3
## 4
```

### Full join

```
dplyr:
full_join(x, y, by = "z")
base R:
merge(x, y, all.x = TRUE, all.y = TRUE, by = "z")
SQL:
SELECT * FROM x FULL OUTER JOIN y USING (z)
```

# Duplicate keys

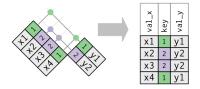


Figure 10: "One-to-many"

# Duplicate keys

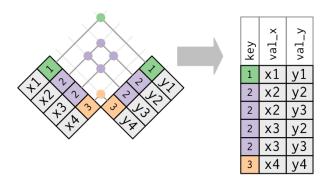


Figure 11: "Many-to-many"

### Differently-named keys

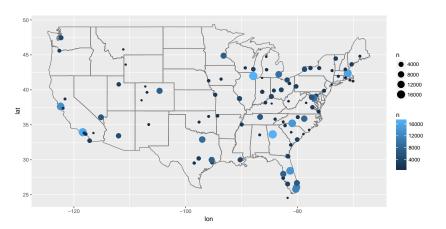
```
x2 <- x %>% rename(a = key)
y2 <- y %>% rename(b = key)
left_join(x2, y2, by = c("a" = "b"))
```

```
## # A tibble: 3 x 3
## a val_x val_y
## <dbl> <chr> <chr>
## 1 1 x1 y1
## 2 2 x2 y2
## 3 3 x3 <NA>
```

#### Plot most popular flight destinations

```
flights %>%
  filter(dest != "HNL", dest != "ANC") %>%
  count(dest) %>%
  left_join(airports, by = c("dest" = "faa")) %>%
  ggplot(aes(lon, lat, size=n, color=n)) +
  borders("state") +
  geom_point() +
  coord_quickmap()
```

## Warning: Removed 4 rows containing missing values (geom\_point



#### Get total number of flights flown by each type of plane

```
flights %>%
  left_join(planes, by = "tailnum") %>%
  count(type)
```

```
## # A tibble: 4 x 2
##
                          type
                                    n
##
                         <chr> <int>
      Fixed wing multi engine 282074
##
   2 Fixed wing single engine
                                 1686
##
## 3
                   Rotorcraft
                                  410
## 4
                          <NA> 52606
```

#### Mutating joins

Similar to filter(), filtering joins do not add new variables, but instead subset the observations from one table (x) based on observations in another (y)

- ▶ **Semi joins** *keep* all observations in x that have a match in y
- ▶ Anti joins drop all observations in x that have a match in y

# Semi joins

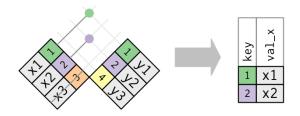


Figure 12: Keeps all observations that match

### Semi joins

```
## Joining, by = "key"
## # A tibble: 2 x 2
## key val_x
## <dbl> <chr>
## 1  1  x1
## 2  2  x2
```

### Semi joins with duplicate keys

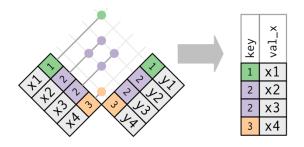


Figure 13: Keeps all observations that match

Semi joins never duplicate rows (unlike mutating joins).

#### Keep only flights from most popular destinations

```
top_dest <- flights %>%
  count(dest) %>%
  filter(n > 10000)
semi_join(flights, top_dest)
## Joining, by = "dest"
## # A tibble: 131,440 x 19
##
       year month day dep_time sched_dep_time dep_delay arr_time
##
      <int> <int> <int>
                             <int>
                                             <int>
                                                        dbl>
                                                                 <int>
       2013
                               542
                                               540
                                                                   923
##
    1
##
       2013
                               554
                                               600
                                                           -6
                                                                   812
##
    3
       2013
                               554
                                               558
                                                           -4
                                                                   740
##
    4
       2013
                               555
                                               600
                                                           -5
                                                                   913
                               557
                                                                   838
##
    5
       2013
                                               600
                                                           -3
##
       2013
                               558
                                               600
                                                           -2
                                                                   753
                               558
##
    7
       2013
                                               600
                                                           -2
                                                                   924
       2013
                               558
                                               600
                                                           -2
                                                                   923
##
    8
       2013
                               559
                                               559
                                                                   702
##
                                                            0
```

## 10 2013 1 1 600 600 0 851 ## # ... with 131,430 more rows, and 12 more variables: sched\_arr\_time

# Anti joins

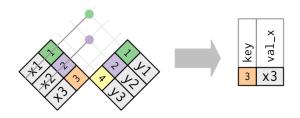


Figure 14:

#### Anti joins

```
## Joining, by = "key"

## # A tibble: 1 x 2
## key val_x
## <dbl> <chr>
## 1 3 x3
```

Why did we have missing values when plotting destination airports?

```
flights %>%
  anti_join(airports, by = c("dest" = "faa")) %>%
  count(dest)
```

```
## # A tibble: 4 x 2
## dest n
## <chr> <int>
## 1 BQN 896
## 2 PSE 365
## 3 SJU 5819
## 4 STT 522
```

#### Set operations

Set operations take two tables with the same variables and compare whole rows (i.e., every variable in each row), to treat observations like members of sets.

- intersect(x, y) returns observations in both x and y
- ▶ union(x, y) returns all unique observations in x and y
- ▶ setdiff(x, y) returns the observations in x that aren't in y

These are less commonly used for data analysis than the joins.

# Set operations

#### Intersection

```
intersect(df1, df2)
```

```
## # A tibble: 1 x 2
## x y
## <dbl> <dbl>
## 1 1 1
```

#### Union

```
union(df1, df2)
```

#### Difference

```
## # A tibble: 1 x 2
## x y
## <dbl> <dbl>
## 1 2 1
```

setdiff(df1, df2)