1) A Suredian is lonvex if its sciond dinviding to should be

The los likelihood is given by.

Here g(67 xi) is given by 1

Using thin vule, we got.

$$g(z) = \frac{1}{1+e^{-2}}; g'(z) = \frac{1}{(1+e^{-2})^{2}} \cdot e^{-2}$$

$$= \frac{1}{1+e^{-2}} \left(1 - \frac{1}{1+e^{-2}}\right)$$

$$= g(z) g(1-z).$$

$$\frac{\partial}{\partial 0} \left(-\log g(z) \right) = \frac{-g'(z)}{g(z)} \cdot \frac{\partial}{\partial 0} \cdot z \cdot = \left(g(z) - 1 \right) \chi.$$

$$\frac{\partial^2}{\partial o^2} = \left(-\log g\left(o^{(x)}\right)\right) = \frac{\partial}{\partial o}\left(g(z)-1\right)x.$$

$$= \frac{\partial}{\partial o}\left(g(z).x\right) = g'(z).x.$$

=
$$g(z)(1-g(z))\frac{dz}{do} \cdot x = g(z)(1-g(z))$$

$$\frac{\partial}{\partial o} \left(-\log \left(1 - g(0 \times 1) \right) \right) = -\frac{1}{1 - g(x)} \frac{\partial}{\partial o} \left(1 - g(x) \right).$$

$$\frac{1-g(z)}{1-g(z)} = \frac{g(z)\pi}{1-g(z)}.$$

$$\frac{\partial^{2} \left(-\log \left(1-9 \left(0^{\frac{1}{2} i x}\right)\right)}{\partial 0^{2}} = \frac{\partial \left(9 \left(2\right) x\right)}{\partial 0} = x 9 (2) \left(1-9 \left(2\right) x^{\frac{1}{2}} \right)$$

The XXI term in buth are squared term implying it can never be negative.

Since both the terms second dorvative have XXI and are thentre greater than O1 # the function as a whole is convex.

a). X, ord X2 ore continous.

$$\prod_{i=1}^{n} \left(\begin{bmatrix} x_i \\ x_i \end{bmatrix} \right) = \underbrace{\begin{pmatrix} x_i \\ x_i \end{pmatrix} \begin{pmatrix} x_i \\ x_i \end{pmatrix} \begin{pmatrix} x_i \\ x_i \end{pmatrix} \begin{pmatrix} x_i \\ x_i \end{pmatrix}}_{S_{2i}}$$

For three Classes and J=3, each class will have.

3x (J=1). parameters & making shot. 6

b) Assumes XI is contagorical. with 5 contegories and XZ is continous

Softmon would be.
$$\pi_{f}(x) = e^{\alpha_{f} + \beta^{T}x}$$
.

 $\frac{2}{2}e^{\alpha_{f} + \beta^{T}x}$.

There are 5 binary one hot variables, needed to represent the Categories.

Bosides that. Xz which is continous making an total of 6.

$$P(Y=1)= 4/7.$$

$$P(X_1=1)= 4/7.$$

```
In [1]:
```

```
%matplotlib inline
import matplotlib.pyplot as plt
import numpy as np
import random
from sklearn import linear_model
import scipy.stats
from sklearn.metrics import accuracy_score
np.set_printoptions(suppress=True)
```

In [2]:

```
def genData(numPoints):
    x = np.zeros(shape=(numPoints, 3))
    y = np.zeros(shape=numPoints)

x[:,0] = 1
    #x[:,1] = [i for i in range(numPoints)]
    x[:,1] = np.random.uniform(0, 3, size = numPoints)
    x[:,2] = np.random.uniform(0, 3, size = numPoints)

for i in range(0, numPoints): y[i] = 1/(1 + np.exp( - (-3 + (x[i][1]))))
    #for i in range(0, numPoints): y[i] = 1/(1 + np.exp( - (-3 + (x[i][1]))))

y = np.array([1 if i > 0.5 else 0 for i in y])
    return x, y
```

In [3]:

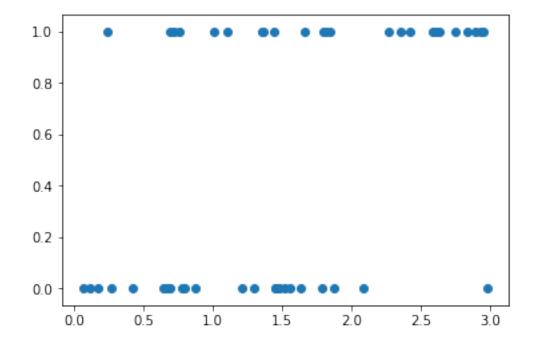
```
x,y = (genData(50))
#y_temp = np.array([1 if i > 0.5 else 0 for i in y])
```

```
In [4]:
```

```
plt.scatter(x[:,1], y)
```

Out[4]:

<matplotlib.collections.PathCollection at 0x7ff2ba97cd30>



In [5]:

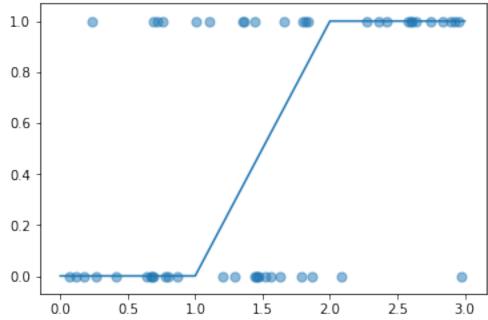
```
def gradientDescent(x, y, theta, alpha, m, numIterations):
    xTrans = x.transpose()
    for i in range(0, numIterations):
        loss = (1 / (1 + np.exp(-(1 + (np.dot(x, theta)))))) - y
        #print (np.mean(loss))
        #gradient = np.dot(xTrans, np.dot(x, theta) - y) / m #Partial derivativ
e        gradient = np.dot(xTrans, loss) / m
        theta = theta - alpha * gradient
```

In [6]:

```
m, n = np.shape(x)
theta = gradientDescent(x,y, np.ones(n), 1, m, 70000)
```

```
theta
Out[7]:
array([-66.12729013, 20.52518735, 21.32420216])

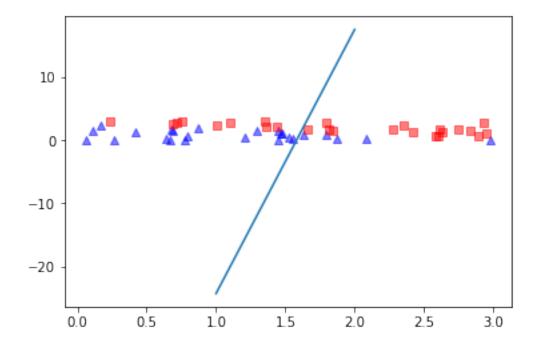
In [8]:
hypothesis = lambda x: 1 / (1 + (np.exp(-(x * theta[1] + x * theta[2]+ theta[0]))))
plt.plot([i for i in range(0,4)],[hypothesis(i) for i in range(0,4)])
plt.scatter([i[1] for i in x], y, s=50, alpha = 0.5)
plt.show()
```



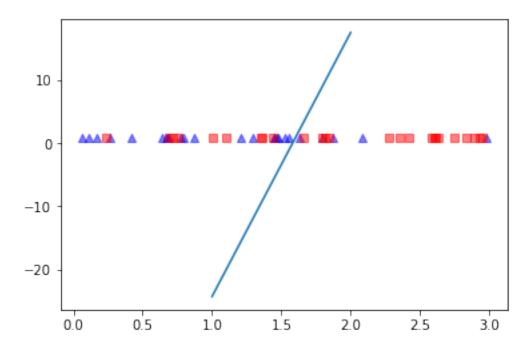
In [7]:

Decision boundaries for X[1] vs X[2] and X[1] vs X[0] respectively for Batch GD

In [9]:



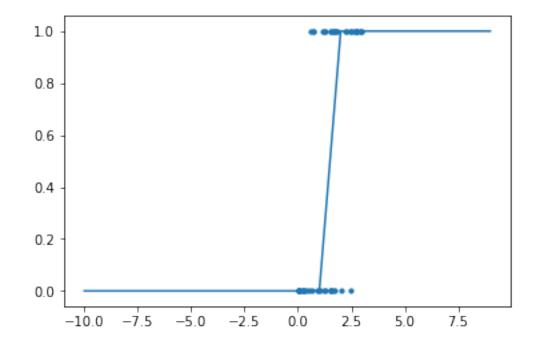
In [10]:



```
In [11]:
def gradientDescentSto(x, y, theta, alpha, m, numIterations, delta=2, conv=0.000
00001):
    xTrans = x.transpose()
    count = 0
    theta prev = theta + delta + 1
    while (count < numIterations):</pre>
            count += 1
            for i in range(m):
                hypothesis = x[i][0]*theta[0] + x[i][1]*theta[1] + x[i][2]*theta
[2]
                loss = 1/(1 + np.exp(- hypothesis)) - y[i]
                #loss = hypothesis - y[i]
                gradient1 = x[i][0] * loss
                gradient0 = x[i][1] * loss
                theta prev = theta
                theta[1] = theta[1] - alpha * gradient0
                theta[0] = theta[0] - alpha * gradient1
    return theta
In [12]:
theta = gradientDescentSto(x, y, theta, 0.08, m, 10000)
In [13]:
theta
Out[13]:
```

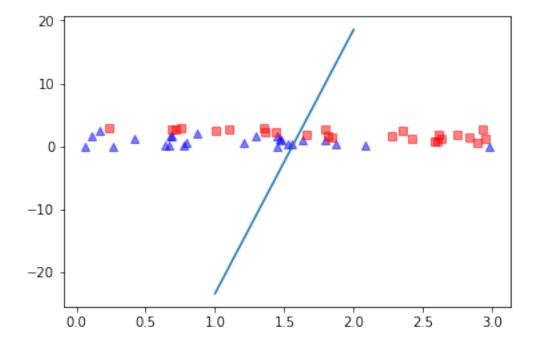
array([-65.34984189, 20.63300455, 21.32420216])

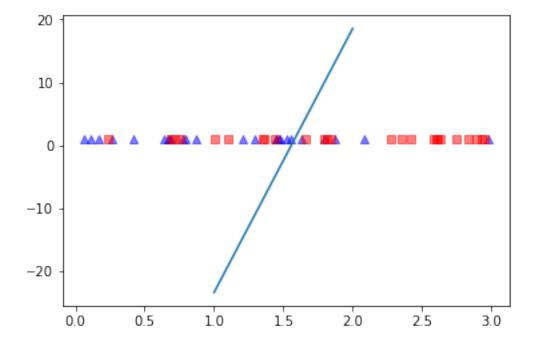
```
In [14]:
    hypothesis = lambda x: 1 / (1 + (np.exp(-(x * theta[1] + x * theta[2] + theta[0]
))))
    plt.plot([i for i in range(-10,10)],[hypothesis(i) for i in range(-10,10)])
    plt.scatter([i[2] for i in x], y, s=10)
    plt.show()
```



Decision boundaries for X[1] vs X[2] and X[1] vs X[0] respectively for Stochastic GD

In [15]:





```
In [17]:
```

```
d_boundary = lambda x: x[1]*theta[1] + x[2]*theta[2] + theta[0] * x[0] y_hat = [1 if <math>i > 0 else 0 for i in [d_boundary(i) for i in x[0]
```

```
In [18]:
accuracy_score(y, y_hat)
Out[18]:
1.0
```

Linear discriminant analysis

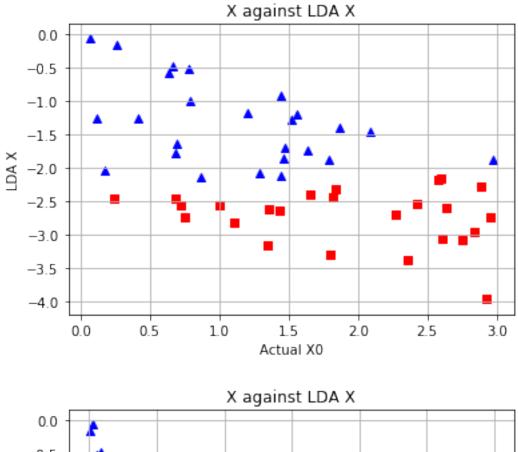
```
In [19]:
x_old = x
x = x[:, 1:]
```

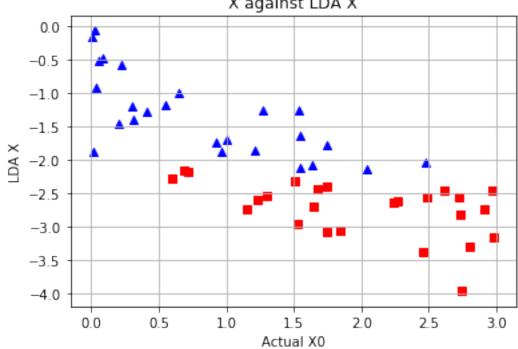
```
In [20]:
mean vs = []
y_{temp} = np.array([1 if i > 0.5 else 0 for i in y])
for i in range(0,2):mean_vs.append(np.mean(x[y_temp==i], axis = 0))
print(mean vs)
[array([1.11687638, 0.83202265]), array([1.90450382, 1.97216123])]
In [21]:
within class = np.zeros((2,2))
for cl,mv in zip(range(0,2), mean vs):
    class scatter matrix = np.zeros((2,2))
    for row in x[y temp == cl]:
        row, mv = row.reshape(2,1), mv.reshape(2,1)
        class scatter matrix += (row-mv).dot((row-mv).T)
    within class += class scatter matrix
within class
Out[21]:
array([[ 28.46191249, -14.49320429],
       [-14.49320429, 26.81805413]])
In [22]:
mean = np.mean(x, axis=0)
between class = np.zeros((2,2))
for i,mean vec in enumerate(mean vs):
    n = x[y temp==i+1,:].shape[0]
    mean vec = mean vec.reshape(2,1)
    overall_mean = mean.reshape(2,1)
    between class += n * (mean vec - mean).dot((mean vec - mean).T)
between class
Out[22]:
```

array([[5.91092904, 10.74652962],

[10.74652962, 19.63921255]])

```
In [23]:
eig vals, eig vecs = np.linalg.eig(np.linalg.inv(within class).dot(between class
for i in range(len(eig_vals)): eigvec_sc = eig_vecs[:,i].reshape(2,1)
print(eig vals, eig vecs)
[0.00058142 1.85935676] [[-0.87693265 -0.6255713 ]
 [ 0.48061328 -0.780167 ]]
In [29]:
eig_pairs = sorted([(np.abs(eig_vals[i]), eig_vecs[:,i]) for i in range(len(eig_
vals))]
                   , key=lambda k: k[0], reverse=True)
eig pairs
Out[29]:
[(1.859356764932039, array([-0.6255713, -0.780167])),
 (0.0005814232087433258, array([-0.87693265, 0.48061328]))]
In [33]:
W = eig pairs[0][1].reshape(2,1)
x lda = x.dot(W)
In [41]:
from matplotlib import pyplot as plt
def plot step lda(feature):
    ax = plt.subplot(111)
    for label, marker, color in zip(range(0,2),('^', 's', 'o'),('blue', 'red', 'gr
een')):
        plt.scatter(x=x[:,feature].real[y == label],
                y=x lda[:,0].real[y == label],
                marker=marker, color=color)
    plt.xlabel('Actual X0')
    plt.ylabel('LDA X')
    plt.title('X against LDA X')
    plt.grid()
    plt.tight_layout
    plt.show()
plot_step_lda(0)
plot_step_lda(1)
```





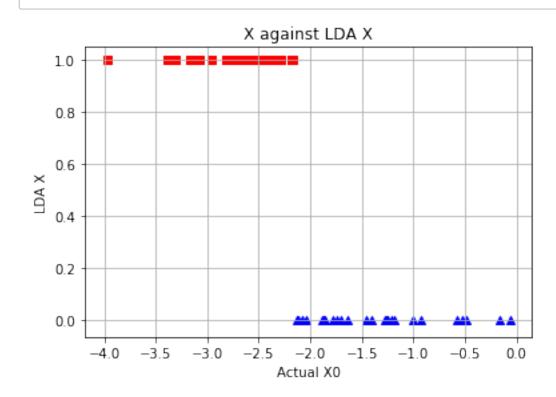
The above plot shows the relationship between actual X and LDA transformed X. Both X0 and X1 are shown to be linearly seperated at $X \sim 2.0$

```
In [42]:

ax = plt.subplot(111)
for label,marker,color in zip(range(0,2),('^', 's'),('blue', 'red')): plt.scatte
r(x=x_lda[:,0].real[y == label],y=y.real[y == label],marker=marker,color=color)

plt.xlabel('Actual X0')
plt.ylabel('LDA X')
plt.title('X against LDA X')

plt.grid()
plt.tight_layout
plt.show()
```



There is a clean seperation once LDA is applied to X

```
In [584]:

y_hat = [1 if i>=2 else 0 for i in x_lda]
accuracy_score(y, y_hat)

Out[584]:
```

0.96

Histograms of the three methods

```
In [609]:
```

```
accuracies_gd = []

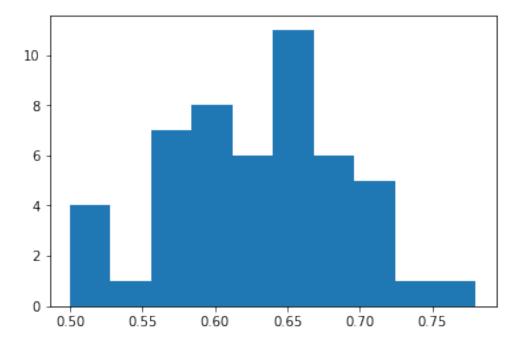
for run in range(50):
    x,y = (genData(50))
    m, n = np.shape(x)
    theta = gradientDescent(x,y, np.ones(n), 1, m, 70000)

d_boundary = lambda x: x[0]*theta[1] + x[1]*theta[2] + x[2]*theta[0]

y_hat = [0 if i > 0 else 1 for i in [d_boundary(i) for i in x]]
    accuracies_gd.append(accuracy_score(y, y_hat))

plt.hist(np.array(accuracies_gd), label = 'GD')
```

Out[609]:



```
In [620]:
```

```
accuracies_sto = []

for run in range(20):
    print (run)
    x,y = (genData(50))
    m, n = np.shape(x)
    theta = gradientDescentSto(x,y, np.ones(n), 1, m, 10000)

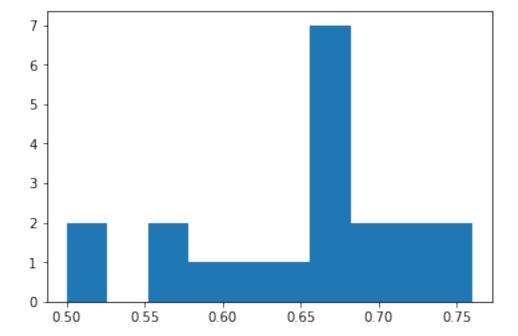
    d_boundary = lambda x: x[0]*theta[1] + x[1]*theta[2] + x[2]*theta[0]

    y_hat = [0 if i > 0 else 1 for i in [d_boundary(i) for i in x]]
    accuracies_sto.append(accuracy_score(y, y_hat))

plt.hist(np.array(accuracies_sto), label = 'GD')
```

```
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
Out[620]:
```

0./34, 0./6]),
<a list of 10 Patch objects>)



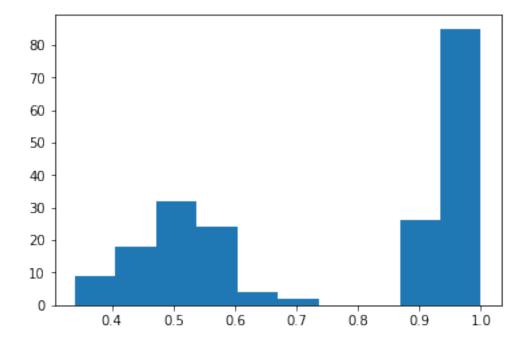
```
In [45]:
accuracies lda = []
for run in range(200):
    x,y = (genData(50))
    x = x[:, 1:]
    mean vs = []
    y temp = np.array([1 if i > 0.5 else 0 for i in y])
    for i in range(0,2):mean_vs.append(np.mean(x[y_temp==i], axis = 0))
    print(mean vs)
    within class = np.zeros((2,2))
    for cl,mv in zip(range(0,2), mean vs):
        class_scatter_matrix = np.zeros((2,2))
        for row in x[y temp == cl]:
            row, mv = row.reshape(2,1), mv.reshape(2,1)
            class scatter matrix += (row-mv).dot((row-mv).T)
        within class += class scatter matrix
    overall mean = np.mean(x, axis=0)
    mean = np.mean(x, axis=0)
    between class = np.zeros((2,2))
    for i,mean vec in enumerate(mean vs):
        n = x[y temp==i+1,:].shape[0]
        mean_vec = mean_vec.reshape(2,1)
        overall mean = mean.reshape(2,1)
        between class += n * (mean vec - mean).dot((mean vec - mean).T)
    eig vals, eig vecs = np.linalg.eig(np.linalg.inv(within class).dot(between c
lass))
    for i in range(len(eig vals)): eigvec sc = eig vecs[:,i].reshape(2,1)
    eig pairs = sorted([(np.abs(eig vals[i]), eig vecs[:,i]) for i in range(len(
eig vals))]
                   , key=lambda k: k[0], reverse=True)
    W = eig pairs[0][1].reshape(2,1)
    x lda = x.dot(W)
    y_hat = [1 if i>=2 else 0 for i in x_lda]
    accuracies lda.append(accuracy_score(y, y_hat))
plt.hist(np.array(accuracies_lda), label = 'GD')
```

```
[array([0.83929/04, 1.00614434]), array([2.26066898, 1.98306645])]
[array([1.06232932, 1.05398051]), array([1.69221586, 2.20116009])]
[array([0.8595049 , 1.12125005]), array([1.90860151, 2.04333948])]
[array([0.66273389, 1.12640724]), array([2.0469637, 1.79945824])]
[array([1.39749888, 0.72031956]), array([1.97557825, 1.95054578])]
[array([1.16347381, 1.01042746]), array([2.07469372, 1.86183587])]
[array([0.98200943, 0.92036327]), array([1.80268477, 2.2628307 ])]
[array([1.13439717, 1.09243617]), array([2.17336398, 2.28375346])]
[array([1.25256252, 0.97733217]), array([1.93141848, 2.28168542])]
[array([0.84419823, 0.91675769]), array([2.26498206, 1.89756332])]
[array([0.73760576, 1.41559017]), array([2.01185166, 1.8043372])]
[array([1.19567031, 0.6815785 ]), array([2.25383607, 1.77951421])]
[array([1.13134132, 1.07579967]), array([1.98603291, 1.97414516])]
[array([1.08014185, 0.9773905]), array([2.1687166, 2.05693904])]
[array([0.92437414, 1.27888806]), array([1.77244258, 2.20451583])]
[array([0.94577157, 0.82670936]), array([2.10106905, 1.89203975])]
[array([1.04056687, 0.86694862]), array([1.84393481, 2.1233452])]
[array([1.1376197 , 1.01674285]), array([1.95185591, 1.80288235])]
[array([0.79833992, 1.04388146]), array([1.99347243, 2.13186886])]
[array([1.11348563, 0.92840595]), array([2.16059205, 1.77703197])]
[array([1.17397058, 0.7901681 ]), array([2.05593733, 1.98202127])]
[array([1.02757846, 1.06142999]), array([2.05920861, 1.95480949])]
[array([1.09639654, 0.80886487]), array([1.92884076, 1.97198275])]
[array([1.03332626, 0.88547872]), array([2.0162863, 2.060518])]
[array([1.01642599, 0.94183089]), array([1.96869499, 2.05641464])]
[array([0.8334427 , 0.79823615]), array([2.21331414, 1.83948053])]
[array([1.0974606 , 0.92377971]), array([2.01187447, 2.04512918])]
[array([0.90334048, 1.13076672]), array([2.11443585, 1.97782092])]
[array([0.94844166, 0.98771563]), array([2.23343228, 1.69019859])]
[array([1.02636027, 1.28305872]), array([1.97338957, 2.02634463])]
[array([1.00490103, 0.99833925]), array([1.96769705, 1.75880355])]
[array([1.04004681, 0.98802631]), array([1.90451316, 2.00244706])]
[array([0.8371501 , 1.10444209]), array([1.84189095, 2.16167476])]
[array([1.14778684, 0.95436929]), array([2.13162302, 1.83861561])]
[array([0.76344194, 1.33282895]), array([1.96857004, 1.95690778])]
[array([0.93710826, 1.15980332]), array([1.88983318, 2.02440109])]
[array([1.07358488, 1.07455568]), array([1.95049053, 2.13105952])]
[array([0.99597244, 1.20381687]), array([1.91977011, 2.21975561])]
[array([0.98242316, 0.89770331]), array([2.11831111, 2.1170304])]
[array([0.81203613, 1.10178435]), array([1.94710593, 1.90929428])]
[array([0.89721168, 1.0803754 ]), array([1.9731049, 1.9711887])]
[array([0.95514714, 0.96270942]), array([2.05381239, 1.7455297 ])]
[array([1.01984562, 0.9033315 ]), array([1.91527404, 2.12371993])]
[array([0.94577072, 1.02794188]), array([1.72712178, 2.23386794])]
[array([1.16062009, 0.79901388]), array([1.8363361 , 2.17504166])]
[array([0.93329937, 0.97759638]), array([2.11606276, 1.78148375])]
[array([0.9986055 , 1.07649602]), array([2.24285238, 1.70709711])]
[array([0.86272636, 0.99789699]), array([2.16081022, 1.87144328])]
[array([0.98013833, 1.04247989]), array([2.15355015, 1.82210936])]
[array([1.04280776, 1.00771868]), array([2.02068867, 1.91002787])]
[array([1.02507636, 0.87423156]), array([2.01317073, 2.0864678 ])]
[array([0.80640918, 1.04962882]), array([2.12106105, 1.8754633 ])]
[array([1.05425878, 0.90262161]), array([1.96071607, 2.10267842])]
[array([0.78469714, 1.1424283 ]), array([1.9980087, 2.19465726])]
```

```
[array([1.0187896 , 0.95930482]), array([2.03487846, 2.00838616])]
[array([0.94920769, 1.09558346]), array([2.04181521, 1.96686198])]
[array([0.9850755 , 1.05782142]), array([2.05664234, 1.96258126])]
[array([0.97467426, 0.92362596]), array([1.95959361, 2.22828744])]
[array([1.01354359, 0.88067864]), array([1.7399228 , 2.15377644])]
[array([1.03096888, 0.95656048]), array([2.01971526, 2.27358889])]
[array([0.83884659, 1.00104054]), array([2.2737725 , 1.81754569])]
[array([0.93150606, 1.01448678]), array([1.87034135, 1.88970036])]
[array([0.98982547, 1.12657339]), array([1.75187528, 2.14249861])]
[array([1.08722262, 1.12176508]), array([1.76054122, 2.22835194])]
[array([0.89317817, 1.32315068]), array([2.14885953, 1.81801011])]
[array([0.96495706, 1.05547138]), array([2.06152634, 1.98093605])]
[array([1.06401855, 0.91694693]), array([1.94244596, 1.99419318])]
[array([1.1576754 , 0.77499116]), array([1.74686025, 2.20172313])]
[array([0.8644793 , 0.87279762]), array([1.89238983, 1.98834183])]
[array([0.77768114, 1.20253381]), array([1.99136713, 1.95884892])]
[array([1.13023102, 0.91269429]), array([2.17933597, 1.7709569 ])]
[array([0.98295646, 1.03465817]), array([2.04238763, 2.01288952])]
[array([0.94075902, 1.11511166]), array([2.01883025, 2.02861991])]
[array([0.8374107, 0.8967099]), array([2.22148945, 1.72178718])]
[array([0.74149054, 1.23793015]), array([2.29515958, 2.05398902])]
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```

```
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[array([0.95414165, 0.83551079]), array([2.05350838, 2.15319374])]
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```

```
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[array([0.88152574, 1.03048357]), array([1.85380017, 2.13225989])]
[array([0.83457479, 1.0717429 ]), array([2.03430186, 1.99407116])]
Out[45]:
(array([ 9., 18., 32., 24., 4., 2., 0., 0., 26., 85.]),
array([0.34 , 0.406, 0.472, 0.538, 0.604, 0.67 , 0.736, 0.802, 0.86
8,
        0.934, 1.
<a list of 10 Patch objects>)
```



Problem 6

```
In [626]:
```

```
hw3 = pd.read_csv("hw3_dataset.txt", delim_whitespace=True, names = ['id', 'fund
ing', 'fv', 'shares', 'l_buyout'])
```

6 A

Trying out EDA

In [630]:

```
hw3.describe()
```

Out[630]:

	funding	fv	shares	I_buyout
count	482.000000	4.820000e+02	4.820000e+02	482.000000
mean	0.439834	2.651672e+07	2.227942e+06	0.093361
std	0.496883	2.632174e+07	1.413872e+06	0.291240
min	0.000000	1.200000e+06	3.000000e+05	0.000000
25%	0.000000	1.025000e+07	1.300000e+06	0.000000
50%	0.000000	1.950000e+07	2.000000e+06	0.000000
75%	1.000000	3.250000e+07	2.700000e+06	0.000000
max	1.000000	2.346000e+08	1.101862e+07	1.000000

The fv and shares features have really large values compared to I_buyout and funding columns.

```
In [627]:
```

```
hw3.head()
```

Out[627]:

	id	funding	fv	shares	l_buyout
0	1	0	1200000	3000000	0
1	2	0	1454000	1454000	1
2	3	0	1500000	300000	0
3	4	0	1530000	510000	0
4	5	0	2000000	800000	0

In [628]:

```
we know that id is not giving any useful information
also, we'll check for missing values here
"""
hw3 = hw3.drop('id', axis=1)
nas = hw3.isnull().sum()
print(nas)
```

funding 0 fv 0 shares 0 l_buyout 0 dtype: int64

There are no missing values in this dataset

In [632]:

```
features = hw3.drop('funding', axis=1)
target = hw3['funding']
```

In [633]:

```
X_train, X_test, y_train, y_test = train_test_split(features, target, test_size=
0.33, random_state=42)
```

```
In [634]:
```

```
X_train.info()
```

<class 'pandas.core.frame.DataFrame'>
Int64Indov. 222 ontries 157 to 102

Int64Index: 322 entries, 157 to 102

Data columns (total 3 columns):

fv 322 non-null int64 shares 322 non-null int64

1_buyout 322 non-null int64

dtypes: int64(3)

memory usage: 10.1 KB

In [635]:

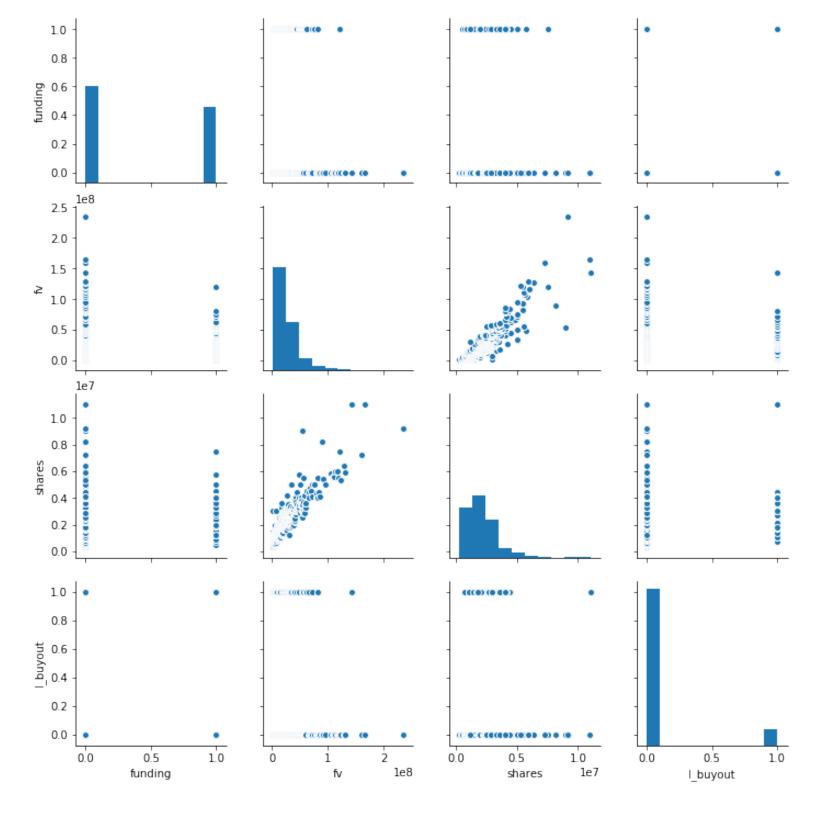
```
X_train.head()
```

Out[635]:

	fv	shares	I_buyout
157	13000000	1300000	0
449	63000000	4500000	1
118	10103125	1325000	0
114	9625000	1375000	0
439	55000000	2500000	0

In [653]:

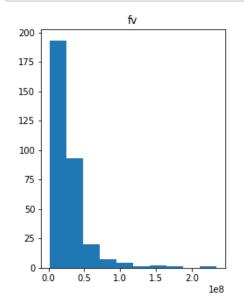
```
sns.pairplot(hw3, vars=hw3.columns)
plt.show()
```

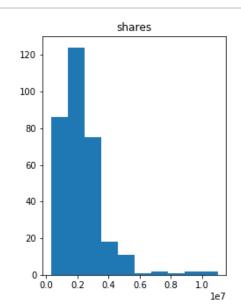


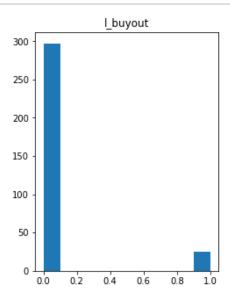
```
In [644]:
```

```
fig, axs = plt.subplots(1,3, figsize=(15, 5), facecolor='w', edgecolor='k')
fig.subplots_adjust(hspace = .5, wspace=.5)

for i,j in enumerate(X_train.columns):
    axs[i].hist(X_train[j])
    axs[i].set_title(j)
```



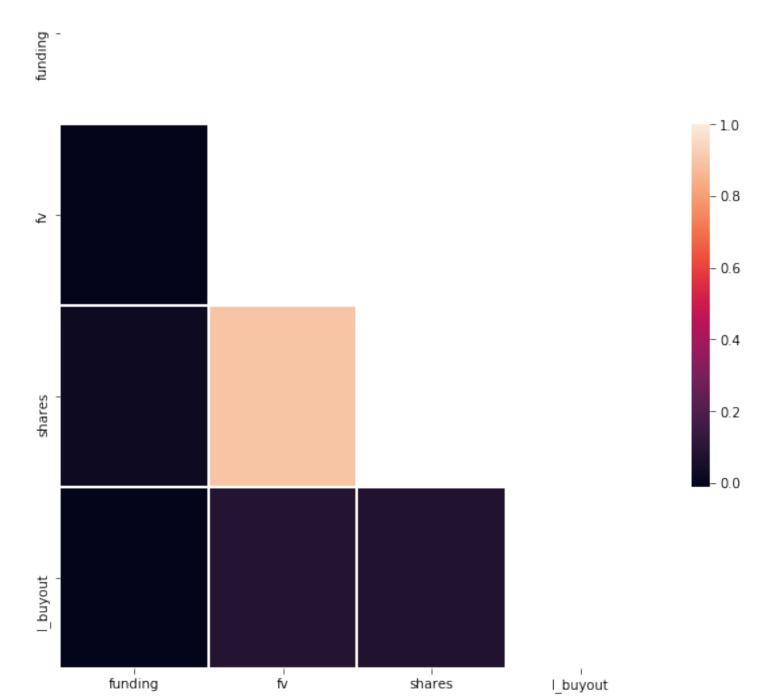




In [649]:

Out[649]:

<matplotlib.axes._subplots.AxesSubplot at 0x7f01443329b0>



shares

fν

Inference

funding

```
In [654]:
```

```
X_train.head()
```

Out[654]:

	fv	shares	I_buyout
157	13000000	1300000	0
449	63000000	4500000	1
118	10103125	1325000	0
114	9625000	1375000	0
439	55000000	2500000	0

6 B

```
In [ ]:
```

```
X_train['capital'] = np.log(X_train['face_value'] * X_train['n_shares'])
X_validate['capital'] = np.log(X_validate['face_value'] * X_validate['n_shares'])
X_test['capital'] = np.log(X_test['face_value'] * X_test['n_shares'])

X_train['fvl'] = np.log(X_train.face_value)
X_train['nsl'] = np.log(X_train.n_shares)

X_validate['fvl'] = np.log(X_validate.face_value)
X_validate['nsl'] = np.log(X_validate.n_shares)

X_test['fvl'] = np.log(X_test.face_value)
X_test['nsl'] = np.log(X_test.n_shares)
```

The first thing to try is the log value of the two features which have a positively skewed distr.

```
In [660]:
X train['fv log'] = np.log(X train['fv'])
X test['fv log'] = np.log(X test['fv'])
X_train['shares_log'] = np.log(X_train['shares'])
X test['shares log'] = np.log(X test['shares'])
/opt/conda/lib/python3.6/site-packages/ipykernel launcher.py:4: Sett
ingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row indexer,col indexer] = value instead
See the caveats in the documentation: http://pandas.pydata.org/panda
s-docs/stable/indexing.html#indexing-view-versus-copy
  after removing the cwd from sys.path.
/opt/conda/lib/python3.6/site-packages/ipykernel launcher.py:5: Sett
ingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row indexer,col indexer] = value instead
See the caveats in the documentation: http://pandas.pydata.org/panda
s-docs/stable/indexing.html#indexing-view-versus-copy
In [710]:
# method to print basic metrics of a classifier
def print metrics(y test, y hat):
    print("Accuracy of model is ", metrics.accuracy score(y test, y hat))
    print("Precision of model is ", metrics.precision_score(y_test, y_hat))
    print("Recall of model is ", metrics.recall_score(y_test, y_hat))
    print("Confusion matrix\n", metrics.confusion matrix(y test, y hat))
# method to plot AUC
def plot roc_auc(model, X_test):
    y hat probabilities = model.predict proba(X test)[::,1]
    fpr, tpr, _ = metrics.roc_curve(y_test, y_hat_probabilities)
    auc = metrics.roc auc score(y test, y hat probabilities)
    plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
```

plt.legend(loc=4)

plt.show()

```
In [711]:

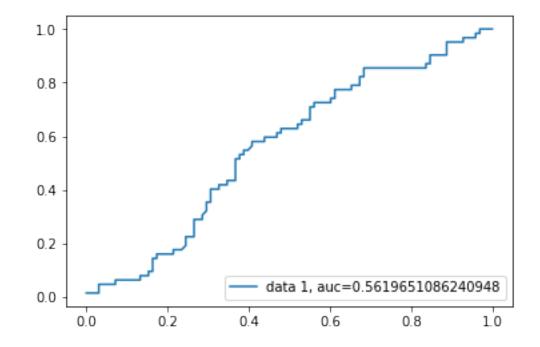
lr = LogisticRegression()
lr.fit(X_train[['fv_log', 'shares_log', 'l_buyout']], y_train)

y_hat = lr.predict(X_test[['fv_log', 'shares_log', 'l_buyout']])
print_metrics(y_test, y_hat)
```

So, that's an okayish accuracy. We just tried all variables we thought would work. Let's try plotting the Area under curve.

```
In [712]:
```

```
plot_roc_auc(lr, X_test[['fv_log', 'shares_log', 'l_buyout']])
```



Let's try more feature transformation. Since face_value and number of shares are highly correlated in stock market, it's worth trying. Moreover, there's no point in using two highly correlated features in building a model. the correlation between them is greater than 0.8. I will multiply them and then take a log over the multiplied quantity.

```
In [713]:
# All the values are greater than 0 so no need to do log(p+1) as shown in class.
X_train['stock_value'] = np.log((X_train['fv'] * X_train['shares']))
X test['stock value'] = np.log((X test['fv'] * X test['shares']))
/opt/conda/lib/python3.6/site-packages/ipykernel launcher.py:4: Sett
ingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row indexer,col indexer] = value instead
See the caveats in the documentation: http://pandas.pydata.org/panda
s-docs/stable/indexing.html#indexing-view-versus-copy
  after removing the cwd from sys.path.
In [714]:
lr = LogisticRegression()
lr.fit(X train[['stock value', 'l buyout']], y train)
y_hat = lr.predict(X_test[['stock_value', 'l_buyout']])
print_metrics(y_test, y_hat)
Accuracy of model is 0.55625
Precision of model is 0.0
Recall of model is 0.0
Confusion matrix
 [[8 9]]
 [62 0]]
In [715]:
plot roc auc(lr, X test[['stock value', 'l buyout']])
1.0
0.8
0.6
0.4
```

Didn't give a significant improvement. Logistic regression has different solver so will try a different solver.

1.0

data 1, auc=0.5354674127715602

0.8

0.6

0.2

0.0

0.0

0.2

0.4

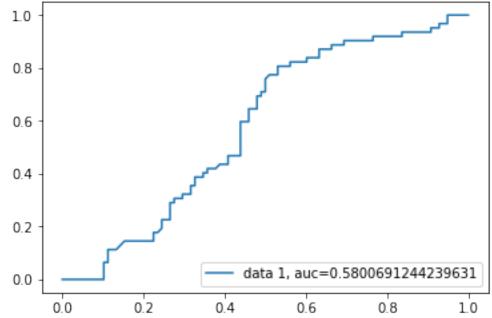
```
lr = LogisticRegression(solver='lbfgs')
lr.fit(X_train[['stock_value', 'l_buyout']], y_train)

y_hat = lr.predict(X_test[['stock_value', 'l_buyout']])
print_metrics(y_test, y_hat)

Accuracy of model is 0.55
Precision of model is 0.4074074074074
Recall of model is 0.3548387096774194
Confusion matrix
[[66 32]
[40 22]]

In [717]:

plot_roc_auc(lr, X_test[['stock_value', 'l_buyout']])
```



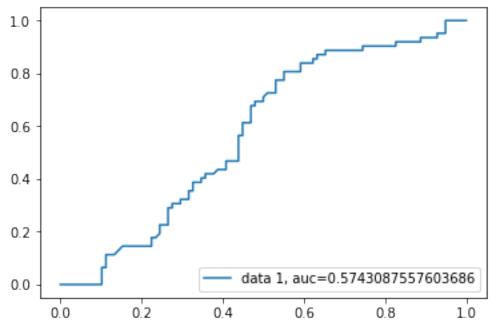
Though it didn't improve significantly, it is definitely better than the previous model.

6 C

In [736]:

Now, we try another kind of classifier- LDA. Again following a similar approach, let's start with all features and slowly narrow down to the ones which we found useful from our logistic regression model.

```
In [718]:
lda = sklearn lda()
lda.fit(X train[['fv log', 'shares log', 'l buyout']], y train)
y_hat = lda.predict(X_test[['fv_log', 'shares_log', 'l_buyout']])
print_metrics(y_test, y_hat)
Accuracy of model is 0.575
Precision of model is 0.45
Recall of model is 0.43548387096774194
Confusion matrix
 [[65 33]
 [35 27]]
Now, trying the enhanced version:
In [719]:
lda = sklearn lda()
lda.fit(X_train[['stock_value', 'l_buyout']], y_train)
y_hat = lda.predict(X_test[['stock_value', 'l_buyout']])
print metrics(y_test, y_hat)
Accuracy of model is 0.55
Precision of model is 0.4074074074074
Recall of model is 0.3548387096774194
Confusion matrix
 [[66 32]
 [40 22]]
In [720]:
plot_roc_auc(lda, X_test[['stock_value', 'l_buyout']])
1.0
0.8
```



```
In [731]:

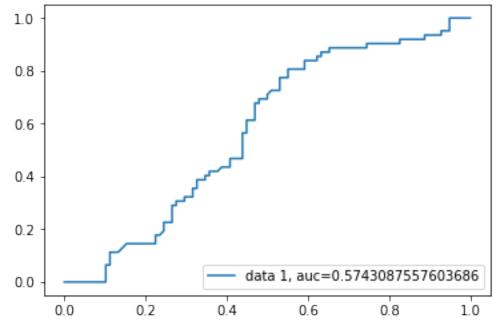
lda = sklearn_lda(solver='svd')
lda.fit(X_train[['stock_value', 'l_buyout']], y_train)

y_hat = lda.predict(X_test[['stock_value', 'l_buyout']])
print_metrics(y_test, y_hat)

Accuracy of model is 0.55
Precision of model is 0.4074074074074
Recall of model is 0.3548387096774194

Confusion matrix
[[66 32]
[40 22]]

In [732]:
plot_roc_auc(lda, X_test[['stock_value', 'l_buyout']])
```



Let's even test the training accuracy of our model

```
In [723]:
```

```
y_hat_train = lda.predict(X_train[['stock_value', 'l_buyout']])
print_metrics(y_train, y_hat_train)
```

Here, we observe again that feature transformation provides better AUC compared to fitting the model on the original features. However, changing solver here didn't make any difference.

6 D

Let's try finding training accuracies:

a) Logistic regression

```
In [725]:
```

```
lr = LogisticRegression(solver='lbfgs')
lr.fit(X_train[['stock_value', 'l_buyout']], y_train)

y_hat_train = lr.predict(X_train[['stock_value', 'l_buyout']])
print_metrics(y_train, y_hat_train)

y_hat_probabilities = lr.predict_proba(X_train[['stock_value', 'l_buyout']])[::,
1]
fpr, tpr, _ = metrics.roc_curve(y_train, y_hat_probabilities)
auc = metrics.roc_auc_score(y_train, y_hat_probabilities)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
```

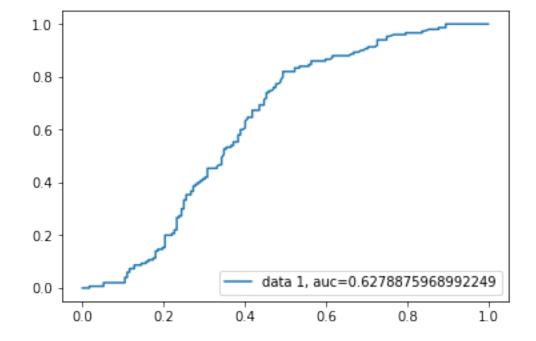
```
Accuracy of model is 0.5745341614906833

Precision of model is 0.5546218487394958

Recall of model is 0.44

Confusion matrix

[[119 53]
[84 66]]
```

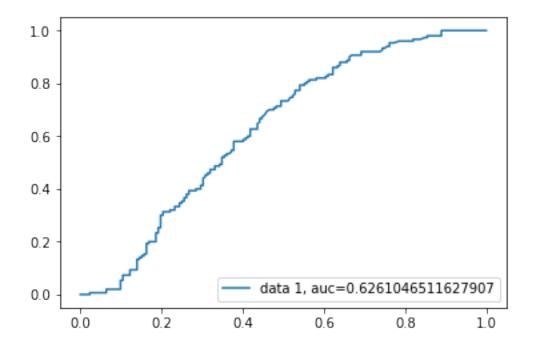


```
In [727]:

lr = LogisticRegression(solver='lbfgs')
lr.fit(X_train[['fv_log', 'l_buyout', 'shares_log']], y_train)

y_hat_train = lr.predict(X_train[['fv_log', 'l_buyout', 'shares_log']])
print_metrics(y_train, y_hat_train)

y_hat_probabilities = lr.predict_proba(X_train[['fv_log', 'l_buyout', 'shares_log']])[::,1]
fpr, tpr, _ = metrics.roc_curve(y_train, y_hat_probabilities)
auc = metrics.roc_auc_score(y_train, y_hat_probabilities)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
```



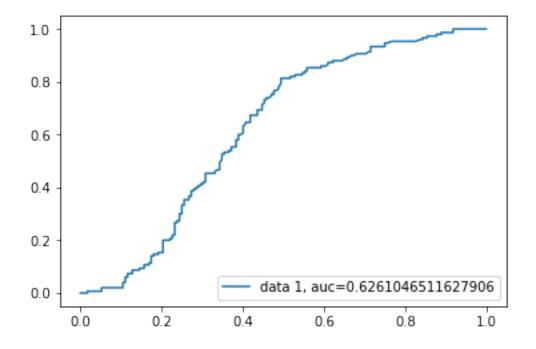
b) Linear Discriminant Analysis

```
In [737]:
```

```
lda = sklearn_lda(solver='svd')
lda.fit(X_train[['stock_value', 'l_buyout']], y_train)

y_hat_train = lda.predict(X_train[['stock_value', 'l_buyout']])
print_metrics(y_train, y_hat_train)

y_hat_probabilities = lda.predict_proba(X_train[['stock_value', 'l_buyout']])[::
,1]
fpr, tpr, _ = metrics.roc_curve(y_train, y_hat_probabilities)
auc = metrics.roc_auc_score(y_train, y_hat_probabilities)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
```



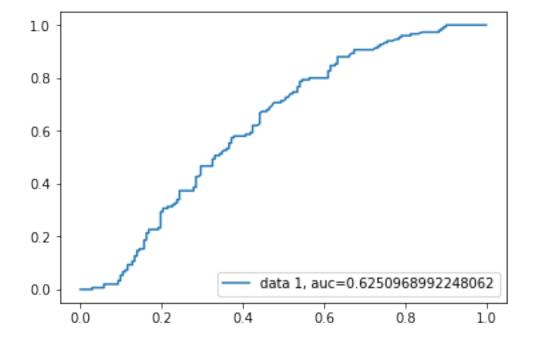
```
In [738]:
```

```
lda = sklearn_lda(solver='svd')
lda.fit(X_train[['fv_log', 'l_buyout', 'shares_log']], y_train)

y_hat_train = lda.predict(X_train[['fv_log', 'l_buyout', 'shares_log']])
print_metrics(y_train, y_hat_train)

y_hat_probabilities = lda.predict_proba(X_train[['fv_log', 'l_buyout', 'shares_log']])[::,1]
fpr, tpr, _ = metrics.roc_curve(y_train, y_hat_probabilities)
auc = metrics.roc_auc_score(y_train, y_hat_probabilities)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
```

```
Accuracy of model is 0.5900621118012422
Precision of model is 0.5671641791044776
Recall of model is 0.5066666666667
Confusion matrix
[[114 58]
[ 74 76]]
```



Here I tested out traning accuracies in my model.