

1) Same size (n, n)

1) Merge Sort

- Maintain the count while merging
- if count becomes n, we have reached the median

```
int getMedian(int ar1[], int ar2[], int n)
{
    int i = 0; /* Current index of i/p array ar1[] */
    int j = 0; /* Current index of i/p array ar2[] */
    int count;
    int m1 = -1, m2 = -1;

    /* Since there are 2n elements, median will be average
       of elements at index n-1 and n in the array obtained after
       merging ar1 and ar2 */
    for (count = 0; count <= n; count++)
    {
        /*Below is to handle case where all elements of ar1[] are
           smaller than smallest(or first) element of ar2[]*/
        if (i == n)
        {
            m1 = m2;
            m2 = ar2[0];
            break;
        }

        /*Below is to handle case where all elements of ar2[] are
           smaller than smallest(or first) element of ar1[]*/
        else if (j == n)
        {
            m1 = m2;
            m2 = ar1[0];
            break;
        }

        /* equals sign because if two
           arrays have some common elements */
        if (ar1[i] <= ar2[j])
        {
            m1 = m2; /* Store the prev median */
            m2 = ar1[i];
            i++;
        }
        else
        {
            m1 = m2; /* Store the prev median */
            m2 = ar2[j];
            j++;
        }
    }

    return (m1 + m2)/2;
}
```

Time Complexity  $\Rightarrow O(n)$

## 2) Compare Medians of 2 Arrays $O(\log n)$

1) Calculate median of both the arrays  $m_1$  &  $m_2$

2) If  $m_1 \leq m_2$  return  $m_1$

3) If  $m_1 > m_2$ , then search in

a)  $\text{array1}[0] - m_1$

b)  $m_2 - \text{array}[n-1]$

4) Similarly for  $m_2 > m_1$

5) If size of Arrays is 2 then

$$\text{Median} = \frac{\max(a1_0, a2_0) + \min(a1_1, a2_1)}{2}$$

```
int getMedian(int ar1[], int ar2[], int n)
{
    /* return -1 for invalid input */
    if (n <= 0)
        return -1;
    if (n == 1)
        return (ar1[0] + ar2[0])/2;
    if (n == 2)
        return (max(ar1[0], ar2[0]) + min(ar1[1], ar2[1])) / 2;

    int m1 = median(ar1, n); /* get the median of the first array */
    int m2 = median(ar2, n); /* get the median of the second array */

    /* If medians are equal then return either m1 or m2 */
    if (m1 == m2)
        return m1;

    /* if m1 < m2 then median must exist in ar1[m1....] and
       ar2[....m2] */
    if (m1 < m2)
    {
        if (n % 2 == 0)
            return getMedian(ar1 + n/2 - 1, ar2, n - n/2 + 1);
        return getMedian(ar1 + n/2, ar2, n - n/2);
    }

    /* if m1 > m2 then median must exist in ar1[....m1] and
       ar2[m2....] */
    if (n % 2 == 0)
        return getMedian(ar2 + n/2 - 1, ar1, n - n/2 + 1);
    return getMedian(ar2 + n/2, ar1, n - n/2);
}
```

2) Different Sizes ( $m, n$ )

1) Similar to method 1 in same size  
Count in Merge Sort.

$$O(n+m)$$

2) Divide and Conquer  $O(\log(m+n))$

$$A \Rightarrow [a_1 | a_2 | a_3 | a_4 | a_5]$$

$$B \Rightarrow [b_1 | b_2 | b_3 | b_4 | b_5 | b_6 | b_7]$$

$$\text{total length} \Rightarrow \underline{m+n}$$

$$\text{length of left half of sorted array} = \frac{m+n}{2}$$

same for right half

$\Rightarrow$  Let's say we take  $x$  elements from A  
 $a_1 \dots a_x$

$\Rightarrow$  Now we have to take  $y = \frac{m+n}{2} - x$  elements  
from B

$\Rightarrow$  Now, we have

$$\begin{array}{c|c} a_1 \dots a_x & a_{x+1} \dots a_n \\ b_1 \dots b_y & b_{y+1} \dots b_m \end{array}$$

→ Checking if split has been made at the correct point

Eg: →

1	3	4	:	7	10	12
		2	:	6	15	

For correct split

$$4 \leq 6 \quad \&\& \quad 3 \leq 7$$

All elements in the left half should be smaller than all elements on the right

→ We know that  $a_x < a_{x+1}$  &  $b_y < b_{y+1}$

→ We only need to make sure

$$a_x \leq b_{y+1} \quad \& \quad b_y \leq a_{x+1}$$

Finally our median is

$$\Rightarrow \frac{\text{Max of left} + \text{Min of right}}{2}$$

$$\Rightarrow \frac{\text{Max}(a_x, b_y) + \text{Min}(a_{x+1}, b_{y+1})}{2}$$

→ We can use binary search to find the correct position



→ We can use binary search to find the correct position

→ Let's say  $a_x \leq b_{y+1}$ , but

$$b_y > a_{x+1}$$

In this case, we need to decrease  $x$  and increase  $y$

- Same for other case

low  $\Rightarrow$  least no. of elements that can be taken from A to form left half

$\Rightarrow 0$  if  $l_2 > \text{size of left half}$

$\Rightarrow \text{left half} - l_2$  if  $l_2 < \text{left half}$

high  $\Rightarrow$  max no. of elements that can be taken from right half

$\Rightarrow l_1$  if  $l_1 < \text{size of left half}$

$\Rightarrow \text{left half}$  if  $l_1 > \text{size of left half}$

→ if  $l_1 + l_2$  is odd, then either left or right half (whichever has more elements) contains the answer