

EE5351: CONTROL SYSTEM DESIGN  
LABORATORY 03

NAME : BANDARA KMTON  
REG.NO. : EG/2021/4432  
GROUP NO. : CE 07  
DATE : 20/01/2024

Summative Laboratory Form

Semester	05
Module Code	EE5351
Module Name	Control Systems Design
Lab Number	03
Lab Name	Laboratory Session 3
Lab Conducted Date	2024.11.05
Report Submission Date	2025.01.24

Table of Contents

1 OBSERVATIONS..... 5

2 References ..... 13

## Table of Figures

Figure 1: Simulink for the Question 3	5
Figure 2: Simulink for updated version from Q3	6
Figure 3: Time domain response for Q5	6
Figure 4: Code for Root locus of closed loop	7
Figure 5: Root Locus	7
Figure 6: Root Locus after increasing Omega	9
Figure 7: Comparison of the time responses	11
Figure 8: Designing Comapesator	12
Figure 9: Time domain response [ <b><math>\theta_m(t)</math></b> ] of the closed loop position control system of DC motor	12

# 1 OBSERVATIONS

Question1)

$$\begin{aligned} \text{I. } V_m &= i_m R_m + L_m \frac{di_m}{dt} + e_b & \dots & 1 \\ e_b &= k_m \omega_m & \dots & 2 \\ T_m &= J_{eq} \frac{d\omega_m}{dt} & \dots & 3 \\ T_m &= i_m k_t & \dots & 4 \end{aligned}$$

II.

Considering the above equations t/f Given as:

$$\frac{\theta_m(S)}{V_m(S)} = \frac{k_t}{S[J_{eq}S(R_m + L_m S) + k_m k_t]}$$

By neglecting the rotor inductance (Due to the Small value)

$$\frac{\theta_m(S)}{V_m(S)} = \frac{k_t}{S[J_{eq}R_m S + k_m k_t]}$$

$$\frac{\theta_m(S)}{V_m(S)} = \frac{0.042}{1.756 \times 10^{-4} S^2 + 1.764 \times 10^{-3} S}$$

III.

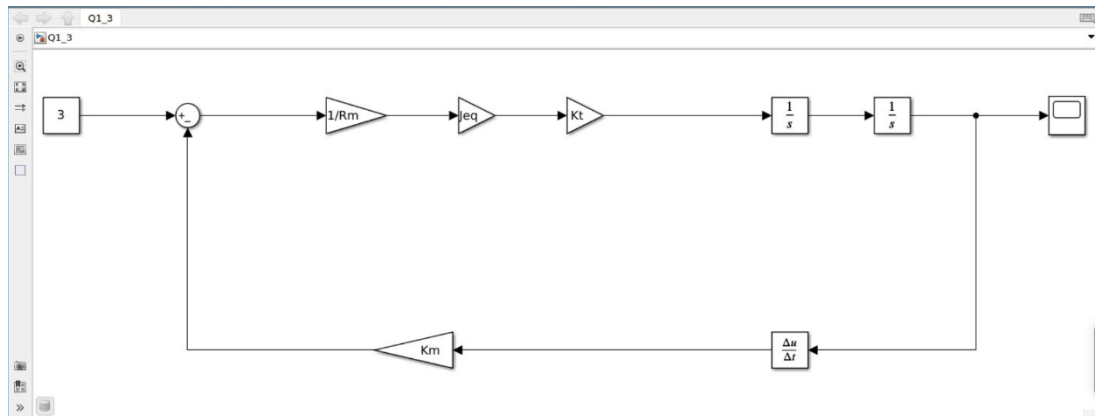


Figure 1: Simulink for the Question 3

IV. To get the closed loop transfer function

$$\begin{aligned} \frac{\theta_m(S)}{\theta_{ref}(S)} &= \frac{G(S)}{1+G(S)} \\ \frac{\theta_m(S)}{\theta_{ref}(S)} &= \frac{0.042}{1.756 \times 10^{-4} S^2 + 1.764 \times 10^{-3} S + 0.042} \end{aligned}$$

V.



Figure 3: Time domain response for Q5

## Question2)

1.

```

Q2_1.m x
/MATLAB Drive/EE5351_L3_4432/Q2_1.m
1 % Define the open-loop transfer function for the DC motor position control system
2 % Numerator of the open-loop transfer function (system gain)
3 numerator = [0.042];
4 % Denominator of the open-loop transfer function
5 denominator = [17.556e-5, 1.764e-3, 0.042];
6 % Create the open-loop transfer function using numerator and denominator
7 G = tf(numerator, denominator);
8 % Plot the root locus to visualize how the poles move as the gain changes
9 figure;
10 rlocus(G);
11 title('Root Locus of DC Motor Position Control System');
12 grid on;

```

Figure 4: Code for Root locus of closed loop

2.

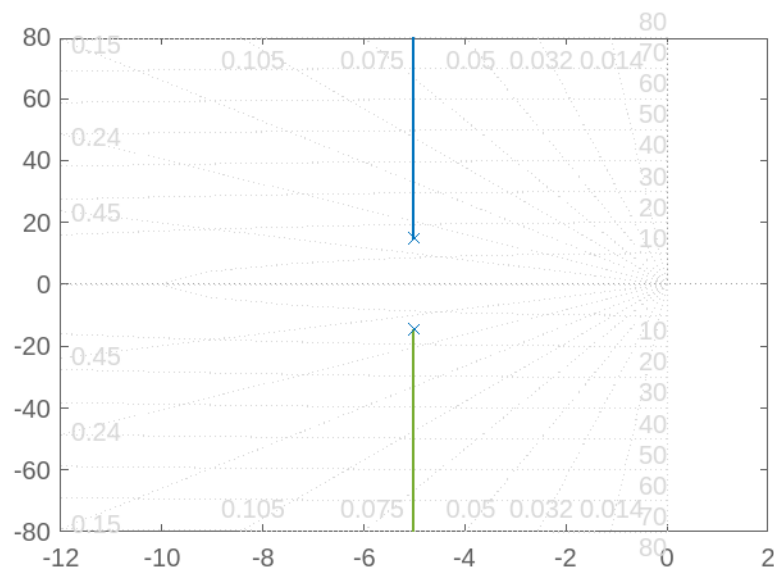


Figure 5: Root Locus

3. By considering the characteristic equation

$$2\varepsilon\omega_n = \frac{1.764 \times 10^{-3}}{1.756 \times 10^{-4}}$$

$$\underline{\omega_n} = \underline{10.045}$$

4.

```
clc; clear; close all;
```

```
%% Define the Open-Loop Transfer Function for DC Motor Position Control
```

```
numerator = [0.042]; % System gain
```

```
denominator = [17.556e-5, 1.764e-3, 0.042]; % Denominator coefficients
```

```
G = tf(numerator, denominator);
```

```
%% Plot the Root Locus of the Open-Loop System
```

```
figure;
```

```
rlocus(G);
```

```
title('Root Locus of DC Motor Position Control System');
```

```
grid on;
```

```
%% Increase Natural Frequency by 10%
```

```
omega_n = 10.045; % Current natural frequency (example value)
```

```
omega_n_new = 1.1 * omega_n; % New desired natural frequency (increase by 10%)
```

```
% Now, we will modify the system to achieve the new natural frequency.
```

```
% We need to adjust the parameters of the system such that the new  $\omega_n$  is achieved.
```

```
% Adjust the denominator to increase  $\omega_n$  by 10%
```

```
denominator_new = denominator;
```

```
denominator_new(1) = denominator_new(1) * (omega_n_new / omega_n); %
```

```
Adjust the first denominator term to scale with  $\omega_n$ 
```

```
% Create the new transfer function
```



```
G_new = tf(numerator, denominator_new);
```

```
%% Plot the Root Locus of the Modified System
```

```
figure;
```

```
rlocus(G_new);
```

```
title('Root Locus After Increasing Natural Frequency by 10%');
```

```
grid on;
```

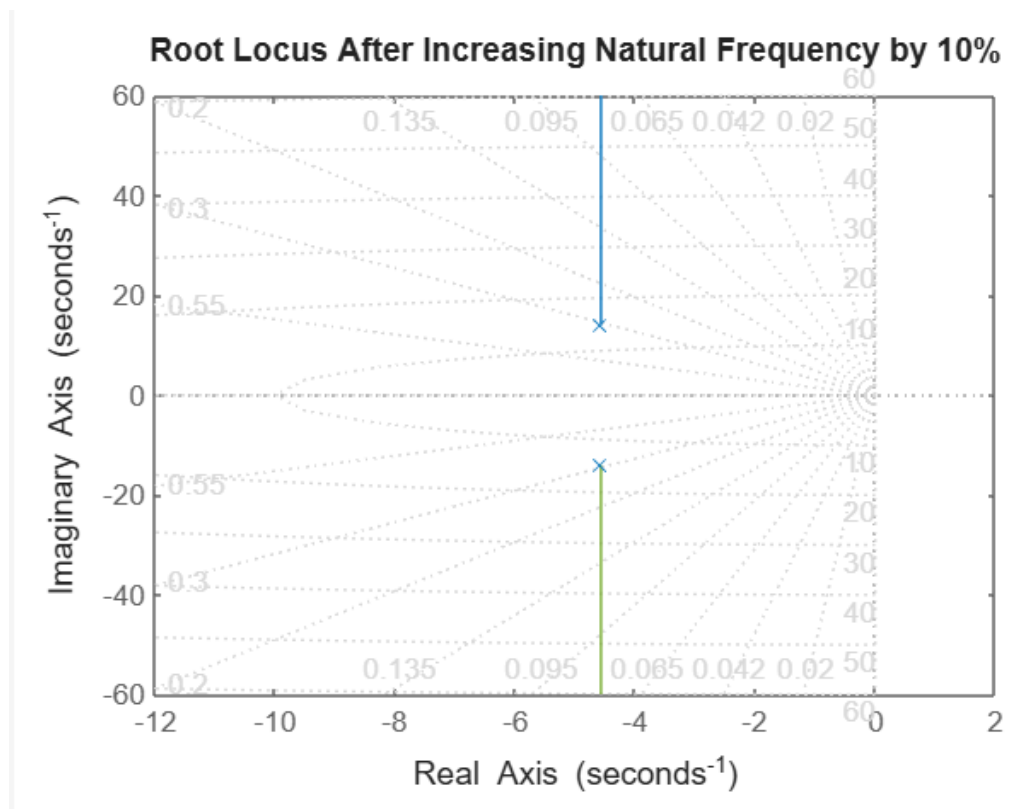


Figure 6: Root Locus after increasing Omega

5.

```
clc; clear; close all;
```

```
%% Define the Open-Loop Transfer Function for DC Motor Position Control
```

```
numerator = [0.042]; % System gain
```

```
denominator = [17.556e-5, 1.764e-3, 0.042]; % Denominator coefficients
```

```
G = tf(numerator, denominator);
```

```
%% Plot the Root Locus of the Open-Loop System
```

```

figure;
rlocus(G);
title('Root Locus of DC Motor Position Control System');
grid on;

%% Increase Natural Frequency by 10%

omega_n = 10.045; % Current natural frequency (example value)
omega_n_new = 1.1 * omega_n; % New desired natural frequency (increase by 10%)

% Now, we will modify the system to achieve the new natural frequency.
% We need to adjust the parameters of the system such that the new  $\omega_n$  is achieved.

% Adjust the denominator to increase  $\omega_n$  by 10%
denominator_new = denominator;
denominator_new(1) = denominator_new(1) * (omega_n_new / omega_n); %
Adjust the first denominator term to scale with  $\omega_n$ 

% Create the new transfer function
G_new = tf(numerator, denominator_new);

%% Plot the Root Locus of the Modified System
figure;
rlocus(G_new);
title('Root Locus After Increasing Natural Frequency by 10%');
grid on;

% Calculate and plot the time response of both systems
figure;
step(G, 'b', G_new, 'r'); % Original in blue, Modified in red
title('Comparison of Time Responses: Original vs Modified System');
legend('Original System', 'Modified System');
grid on;

```

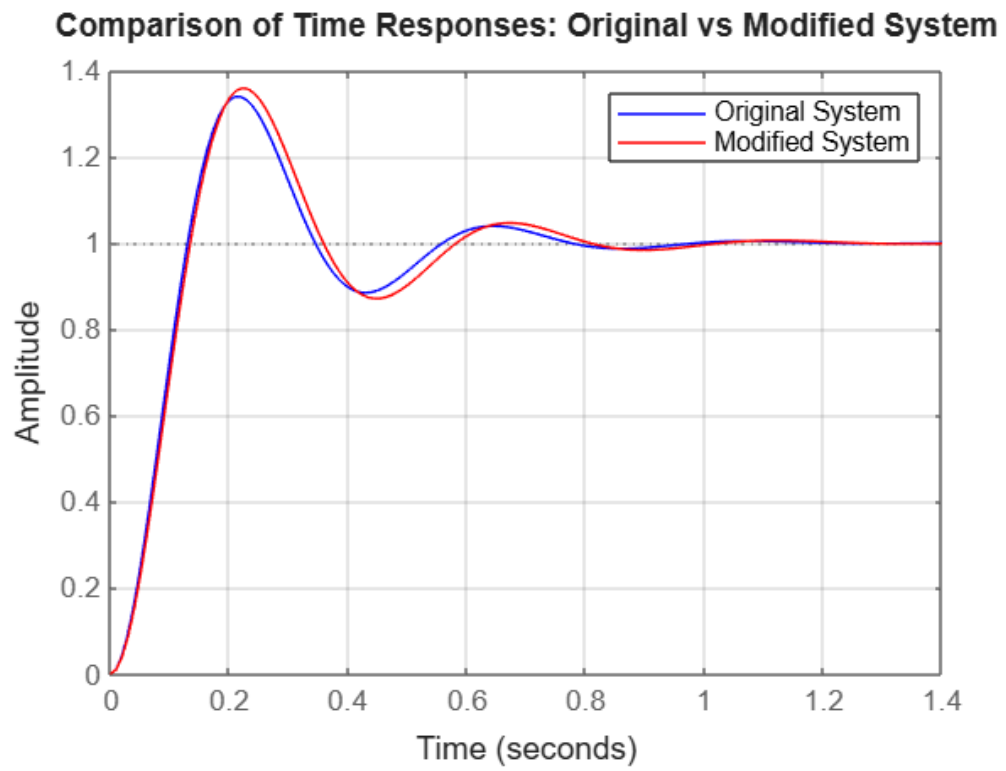


Figure 7: Comparison of the time responses

Question3)

1.

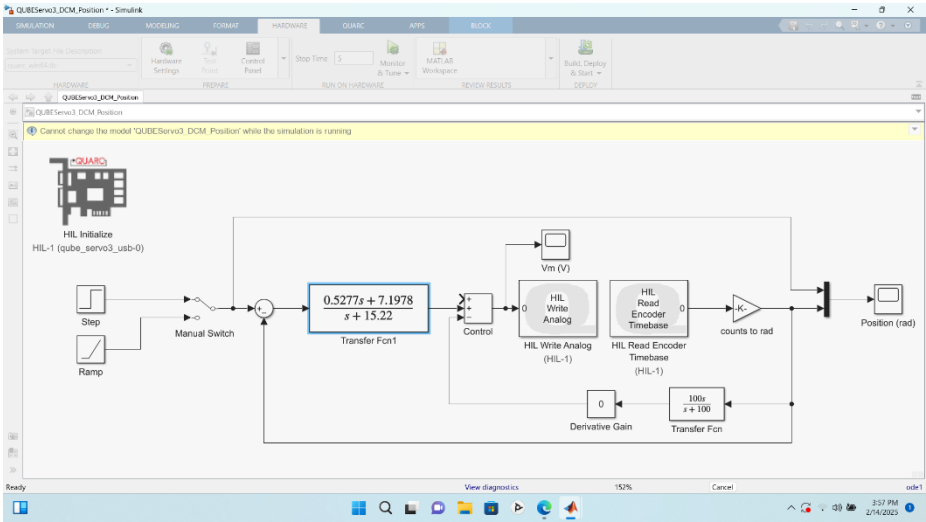


Figure 8:Designing Comapesator

2.



Figure 9: Time domain response  $[\theta_m(t)]$  of the closed loop position control system of DC motor

## 2 References

- [1] “Tutorials Point,” [Online]. Available:  
[https://www.tutorialspoint.com/control\\_systems/control\\_systems\\_construction\\_root\\_locus.htm](https://www.tutorialspoint.com/control_systems/control_systems_construction_root_locus.htm).
- [2] “Mathworks,” [Online]. Available:  
<https://in.mathworks.com/help/control/ref/dynamicsystem.rlocus.html>.
- [3] [Online]. Available: <https://www.geeksforgeeks.org/control-systems-controllers/>.