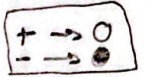


Q.1

$$\frac{1}{2} \quad \begin{matrix} 1-w \\ 1+w \end{matrix}$$



Iter: One

$$w_1 = \left[\frac{1}{8}, \frac{1}{8}, \dots \right]$$

$h_1 \rightarrow$ split at $x_1 = -0.25$

$$\text{err} = \frac{2}{8} = 0.25$$

$$\alpha_1 = \frac{1}{2} \ln \left(\frac{1-0.25}{0.25} \right) \approx 0.55 \quad I \in (0, 1)$$

$$w_2 = w_1 e^{2 \times 0.55 \times \frac{1}{2} (1-I)} = w_1 e^{\alpha_1 (1-I)}$$

$$w_2 = \left[\frac{1}{8}, \frac{1}{8}, \frac{1}{8}, \frac{1}{8}, 0.38, 0.38, \frac{1}{8}, \frac{1}{8} \right]$$

Iter: Two

$h_2 \rightarrow$ split at $x_1 = 0.75$

$$\text{err}_e = \frac{\frac{1}{8} + \frac{1}{8}}{\frac{6}{8} + 2 \times 0.38} \approx 0.167$$

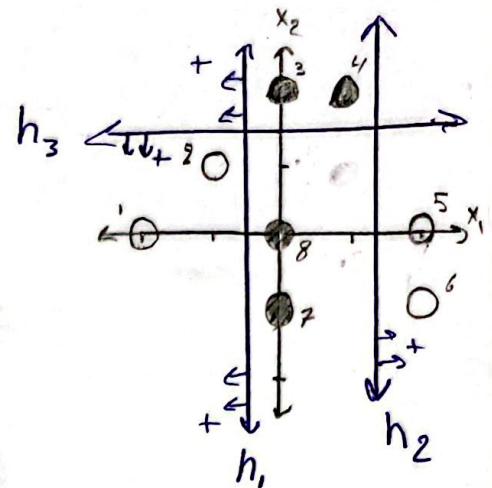
$$\alpha_2 = \frac{1}{2} \ln \left(\frac{1-\text{err}}{\text{err}} \right) = 0.8$$

$$w_3 = \left[0.62, 0.62, \frac{1}{8}, \frac{1}{8}, 0.38, 0.38, \frac{1}{8}, \frac{1}{8} \right]$$

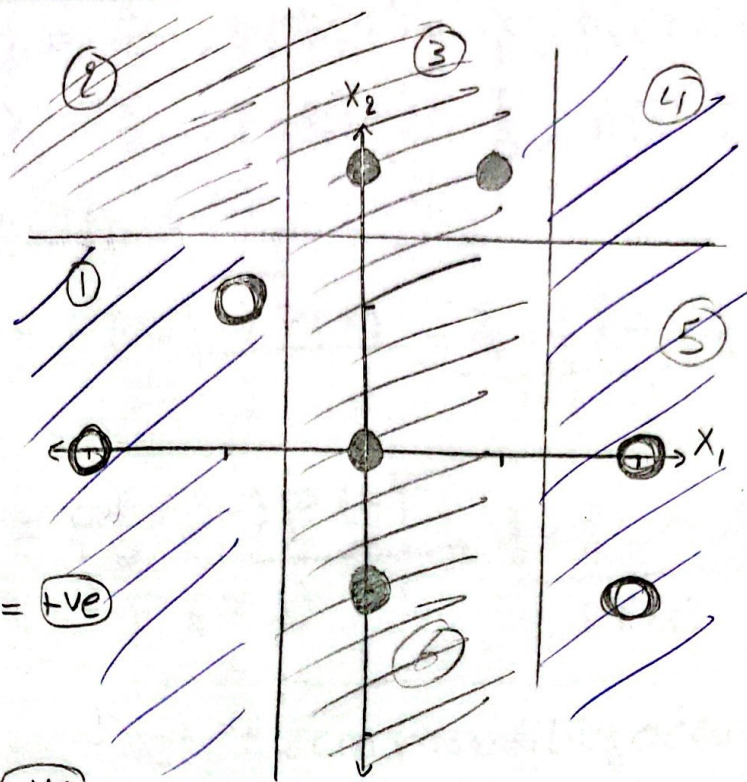
Iter: Three $h_3 \rightarrow$ at $x_2 = 0.75$

$$\text{err}_3 = \frac{2/8}{\frac{1}{8} + 2 \times 0.38 + 2 \times 0.62} = 0.1, \quad \alpha_3 = 1.098$$

$$w_4 = \left[0.62, 0.62, \frac{1}{8}, \frac{1}{8}, 0.38, 0.38, 1.12, 1.12 \right]$$



Final classifier:



region 1:

$$\alpha_1 + \alpha_3 - \alpha_2 = +ve$$

reg 2

$$\alpha_1 - \alpha_2 - \alpha_3 = -ve$$

$$\text{reg 3: } -\alpha_1 - \alpha_2 - \alpha_3 = -ve, \text{ reg 4: } -\alpha_1 + \alpha_2 + \alpha_3 = +ve$$

$$\text{reg 5: } -\alpha_1 + \alpha_2 + \alpha_3 = +ve, \text{ reg 6: } -\alpha_1 - \alpha_2 + \alpha_3 = -ve$$

$$\text{err}_y = \frac{0}{\sum W} = 0$$

Q.2

$X_{11} = (\text{red}, \text{surv}, \text{Dom})$

$$P(X_{11} | \text{stolen} = \text{yes}) = \frac{P(\text{red} | \text{yes}) P(\text{surv} | \text{yes}) P(\text{Dom} | \text{yes}) P(c)}{P(\text{red}) P(\text{surv}) P(\text{Dom}) = P(X_{11})}$$

$$P(X_{11} | \text{yes}) = \frac{3/5 \times 1/5 \times 2/5 \times 5/10}{P(X_{11})} = \frac{0.024}{P(X_{11})}$$

$$P(X_{11} | \text{No}) = \frac{2/5 \times 3/5 \times 3/5 \times 5/10}{P(X_{11})} = \frac{0.072}{P(X_{11})}$$

Pred = NO

✱

Q.3

$$a) P(A|+) = \frac{3}{5}, P(B|+) = \frac{1}{5}, P(C|+) = \frac{4}{5}$$
$$P(A|-) = \frac{2}{5}, P(B|-) = \frac{2}{5}, P(C|-) = \frac{5}{5}$$

$$b) X_{11} = 0, 1, 0$$

$$P(+|X_{11}) = \frac{P(X_{11}|+)P(+)}{P(X_{11})} = \frac{\frac{2}{5} \times \frac{1}{5} \times \frac{1}{5} \times \frac{5}{10}}{P(X_{11})} = \frac{0.008}{P(X_{11})}$$

$$P(-|X_{11}) = \frac{P(X_{11}|-)P(-)}{P(X_{11})} = \frac{\frac{3}{5} \times \frac{2}{5} \times 0 \times \frac{5}{10}}{P(X_{11})} = 0$$

Pref = +

Note: zero probability occurred which is not accurate and should be avoided by using MAP

Q.4

a) 2 Dim b) all integers

$$c) = \sqrt{20^2 + 10^2 + 20^2 + 50^2} = 10\sqrt{34}$$

$$d) = \sqrt{20^2 + 50^2 + 40^2 + 70^2} = 10\sqrt{94}$$

$$e) \cos \theta = \frac{x_2 \cdot x_4}{\|x_2\| \|x_4\|} = \frac{20^2 + 50^2 + 40 \times 20 + 70 \times 60}{\sqrt{20^2 + 50^2 + 20^2 + 60^2} \times 10\sqrt{94}} = 0.98$$

Q. 5

ID	a1	a2	a4
x1	10	60	96
x2	20	50	70
x3	30	50	40
x4	20	50	60
x5	10	60	10

c) [18, 54, 54]

d)
$$\begin{bmatrix} -8 & 6 & 36 \\ 2 & -4 & 16 \\ 12 & -4 & -14 \\ 2 & -4 & 6 \\ -8 & 6 & -44 \end{bmatrix}$$

e)
$$= \begin{bmatrix} 56 & 0 & 0 \\ 0 & 24 & 0 \\ 0 & 0 & 744 \end{bmatrix}$$

$$V(x) = \frac{\sum_{i=1}^n (x_i - \mu)^2}{n}$$

$$V(a_1) = \frac{8^2 + 2^2 + 12^2 + 2^2 + 8^2}{5} = 56 = 11.2$$

$$\begin{bmatrix} V(a_1) & \text{cov}(a_1, a_2) & \text{cov}(a_1, a_3) \\ \text{cov}(a_1, a_2) & V(a_2) & \text{cov}(a_2, a_3) \\ \text{cov}(a_1, a_3) & \text{cov}(a_2, a_3) & V(a_3) \end{bmatrix}$$

$$V(a_2) = 24$$

$$V(a_3) =$$

$$\text{cov}(a_1, a_2) = \frac{-8 + 2 + 12 + 2 - 8 + 6 - 4 - 11 - 4 + 6}{5} = 0$$

$$\text{cov}(a_1, a_3) = \frac{0 + 36 + 16 - 14 + 6 - 44}{5} = 0$$

$$\text{cov}(a_2, a_3) = \frac{0}{5}$$