

$$2) \frac{du}{dt} = u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y}$$

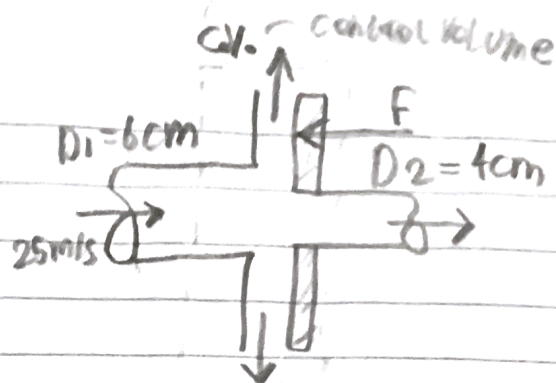
$$= \left( U_0 \frac{x}{L} \right) \left( \frac{U_0}{L} \right) +$$

$$\left( -U_0 \frac{y}{L} \right) (0) = \frac{U_0^2}{L^2} x$$

$$\frac{dv}{dt} = u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y}$$

$$= \left( U_0 \frac{x}{L} \right) (0) +$$

$$\left( -U_0 \frac{y}{L} \right) \left( -\frac{U_0}{L} \right) = \frac{U_0^2}{L^2} y$$



$$Q_{in} = \frac{\pi}{4} (0.06)^2 (25) = 0.0707 \frac{m^3}{s}$$

$$Q_{hole} = \frac{\pi}{4} (0.04)^2 (25) = 0.0314 \frac{m^3}{s}$$

$$\sum F_x = -F_{plate} = \dot{m}_{hole} U_{hole}$$

$$+ \dot{m}_{upper} U_{upper} + \dot{m}_{lower} U_{lower} - \dot{m}_{in} U_{in}$$

$$= (998)(0.0314)(25) - (998 \times 25 \times 0.0707)$$

$$= 784 - 1764 \quad \therefore F = -980 N$$

a) ∴ The acceleration

Vector is  $\vec{\alpha}$

$$\left( \frac{U_0^2}{L^2} \right) (x\hat{i} + y\hat{j})$$

$$\text{or } |\vec{\alpha}| \text{ is } \left( \frac{U_0^2}{L^2} \right) r$$

$$|\alpha| = 25 = \frac{U_0^2}{L^2} |r|$$

$$U_0 = \sqrt{\frac{25(1.5)^2}{\sqrt{2}}} = 6.3 \frac{m}{s}$$

$$b) \therefore U_0 = 6.3 \text{ m/s}$$

∴ The horizontal force required to hold the Plate is 980 N (left)

3) Assumptions:

at  $t=10s$  &  $x=1m$

1. Flow is steady

$$\frac{dT}{dt} = -0.08 \times 10 + 0.84 + 0.24 \times (5-1)$$

2. Flow is incompressible

$$= 1^\circ C/m$$

3. Flow is two-dimensional

$$\frac{dP}{dt} = \cancel{\frac{\partial P}{\partial t}} + u \frac{\partial P}{\partial x} + v \frac{\partial P}{\partial y}$$

∴ The temperature change is  $1^\circ C/m$

$$+ w \cancel{\frac{\partial P}{\partial z}} = (U_0 + bx)$$

$$(-P U_0 b - P b^2 x) + (-b y)$$

$$(-P b^2 y)$$

$$\therefore \frac{dP}{dt} = P[-U_0^2 b - 2U_0 b^2 x + b^3(y^2 - x^2)]$$

$$4) \frac{dT}{dt} = -0.4 \frac{dy}{dt} - 0.6 \frac{dz}{dt}$$

$$-0.2 \times 2 \times (-1)(5-x) \frac{dx}{dt}$$

$$= -0.4 V_y - 0.6 V_z + 0.4(5-x)V_x$$

$$= -0.086 + 0.84 + 0.24x(5-x)$$