

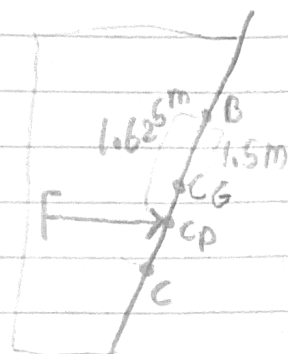
$$1a) F = \gamma h_{CG} A = (9790)(4.5) \sin 50^\circ (\pi)(1.5)^2$$

$$= 239 \text{ kN}$$

FBD

$$b) |y_{cp} - y_{CG}| = \frac{I_{xx} \sin \theta}{h_{CG} A} = \frac{\frac{\pi}{4} r^4 \sin \theta}{h_{CG} \pi r^2}$$

$$= \frac{\frac{\pi}{4} (1.5)^4 \sin 50^\circ}{4.5 \sin 50^\circ (\pi)(1.5)^2} = 0.125 \text{ m}$$



$\therefore y_{cp}$ is 1.625 m from B

AND $y_{cp} = |y_{cp} - y_{CG}| + h_{CG} = 0.125 + 4.5 = 4.625 \text{ m}$

$\therefore y_{cp}$ is 4.625 m from free surface

$$c) M_B = (238550)(1.625) = 388 \text{ kN}\cdot\text{m}$$

\therefore The hydrostatic force is 239 kN

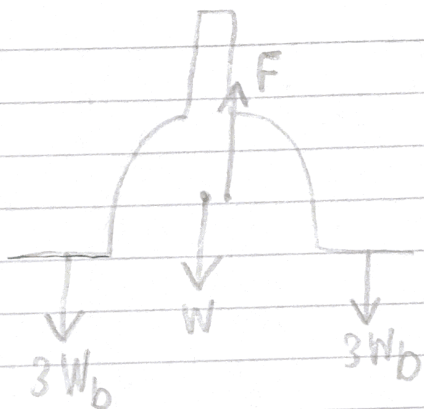
\therefore The center of pressure is 4.625 m from free surface

\therefore The moment about B is 388 kN·m

$$2) F = W_{\text{cylinder}} - W_{\text{hemisphere}} - W_{\text{pipe}}$$

$$= (9790) \pi (2)^2 (6) - (9790) \left(\frac{2\pi}{3} \right) (2)^3 - (9790) \frac{\pi}{4} (0.03)^2 (4)$$

$$= 738144 - 164033 - 28 = 574088 \text{ N}$$



$$\sum F_y = 0$$

$$F - W - 6W_b = 0$$

$$W_b = \frac{F - W}{6} = \frac{574088 - 30000}{6}$$

$$W_b = 90700 \text{ N} = 90.7 \text{ kN}$$

FBD

\therefore The force in each bolt is 90.7 kN

$$3) 7.85 \gamma (a+b) L W = \gamma a L W + 13.56 \gamma b L W \quad \div \gamma L W$$

$$\therefore 7.85a + 7.85b = a + 13.56b$$

$$\frac{a}{b} = \frac{13.56 - 7.85}{7.85 - 1} = 0.834$$

\therefore The ratio of the distances a and b is 0.834

$$4) h = \frac{p}{\gamma} = \frac{150000}{9790} = 15.32 \text{ m above gate}$$

$$F = \gamma V = (9790) \left[\frac{\pi}{4} (2)^2 (8.32) + \frac{1}{3} \frac{\pi}{4} (2)^2 (4) \right]$$

$$= 297000 \text{ N} = 297 \text{ kN}$$

\therefore The net hydrostatic force on ABC is 297 kN