

Sheet (4)

Question (1) :-

$$R = \sqrt[4]{\frac{P_t G^2 \lambda^2 \sigma}{P_E (4\pi)^3}} = \sqrt[4]{\frac{1.5 \times (20000)^2 \times \left(\frac{3 \times 10^8}{24 \times 10^9}\right)^2 \times 200}{2 \times 10^{-10} \times (4\pi)^3}} = 2622 \text{ m}$$

Question (2) :-

$$f_D = \frac{2v_r}{\lambda} \quad v_r = \frac{f_D \lambda}{2} = \frac{f_D c}{2f_R}$$

$$1) v_r = \frac{3 \times 10^3 \times 3 \times 10^8}{2 \times 30 \times 10^9} = 15 \text{ m/s} = 54 \text{ Km/h}$$

$$2) v_r = 81 \text{ Km/h}$$

$$3) v_r = 198 \text{ Km/h}$$

$$4) v_r = 54 \text{ Km/h}$$

∴ Targets (2, 3) will get a line, because their speed is above the speed limit.

(Note) The $(-1/2)$ sign indicates that their directions are towards the radar.

Question (3) :-

$$A] \text{ Bandwidth} = \frac{C}{2R} = \frac{C}{2 \times 0.5} = C = 3 \times 10^8 \text{ Hz} = 0.3 \text{ GHz}$$

$$B] \text{ Chip time} = 5.5 \times 2 \times \frac{R_{\max}}{C} = \frac{5.5 \times 2 \times 100}{3 \times 10^8} = 3.67 \times 10^{-6} \text{ sec}$$

$$\begin{aligned} C] \text{ Transmitted signal} &= A \cos(2\pi f t) \\ &= A \cos\left(2\pi \left[77 \times 10^9 + \frac{B}{T} t\right] t\right) \\ &= A \cos\left[2\pi \left(77 \times 10^9 t + 8.17 \times 10^{13} t^2\right)\right] \end{aligned}$$

$$D] \text{ Sampling Rate} = 2B_{\text{sweep}} = 0.6 \text{ GHz}$$

E] 2 targets only

→ (0) is a replicate of the transmitted signal

→ (100 MHz) is out of range

$$F] \text{ Range} = \frac{CT_c f}{2B_{\text{sweep}}}$$

$$\rightarrow 2 \text{ MHz} \rightarrow 3.67 \text{ m}$$

$$\rightarrow 11 \text{ MHz} \rightarrow 20.2 \text{ m}$$

$$\rightarrow 100 \text{ MHz} \rightarrow 183.5 \text{ m (out of range)}$$

$$G] \text{ Received signal} = A \cos(2\pi f t)$$

$$= A \cos\left[2\pi \left(77 \times 10^9 t + \frac{B}{T} t^2 + \frac{f}{B_{\text{beat}}} (t - \tau)\right)\right]$$

$$= A \cos\left[2\pi \left(77 \times 10^9 t + 8.17 \times 10^{13} t^2 + 2 \times 10^6 \left(t - \frac{2 \times 3.67}{3 \times 10^8}\right)\right)\right]$$

$$+ A \cos\left[2\pi \left(77 \times 10^9 t + 8.17 \times 10^{13} t^2 + 11 \times 10^6 \left(t - \frac{2 \times 20.2}{3 \times 10^8}\right)\right)\right]$$

Question (4) :-

B] To apply the CFAR :-

1] Determine the first cell under test (CUT), which is cell number $[T+G+1 = 6]$

2] Get noise level = Sum of the leading training cells.

3] Threshold = $\frac{\text{Noise level}}{T} \times \text{offset} = \frac{2}{3} \times \text{Noise level}$

4] If signal value at CUT $<$ Threshold, then assign (0) to CUT

(Note) as we have 15 received points

as Number of points after applying CFAR = $N - (T+G) = 15 - 5 = 10$

CUTs = [2.32 18 1.98 3.8 27 0.52 22 0.78 3.47 0.89]

NLs = [5.31 7.84 21.65 22.54 36.32 22.3 23.78 32.78 31.32 49.52]

Threshold = [3.54 5.23 14.43 15.03 24.21 14.87 15.85 21.85 20.88 33.01]

CUTs] = [0 18 0 0 27 0 22 0 0 0]

After
CFAR

D] 3 Targets are detected