

**Comp 410/510**

**Computer Graphics**  
Spring 2023

**Shading**

# Why do we need shading?

- Suppose we build a model of a sphere using many polygons and then color it using a fixed color. We get something like

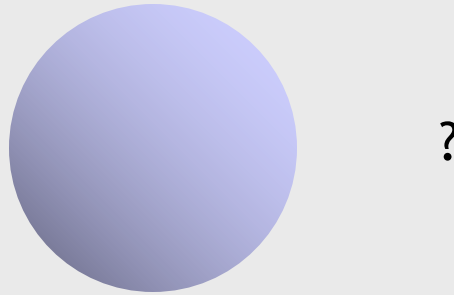


- But we rather want

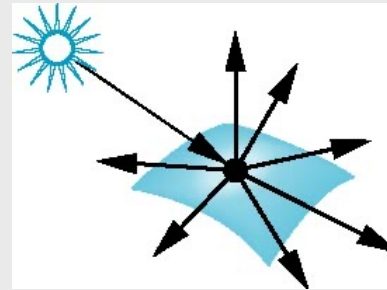


# Shading

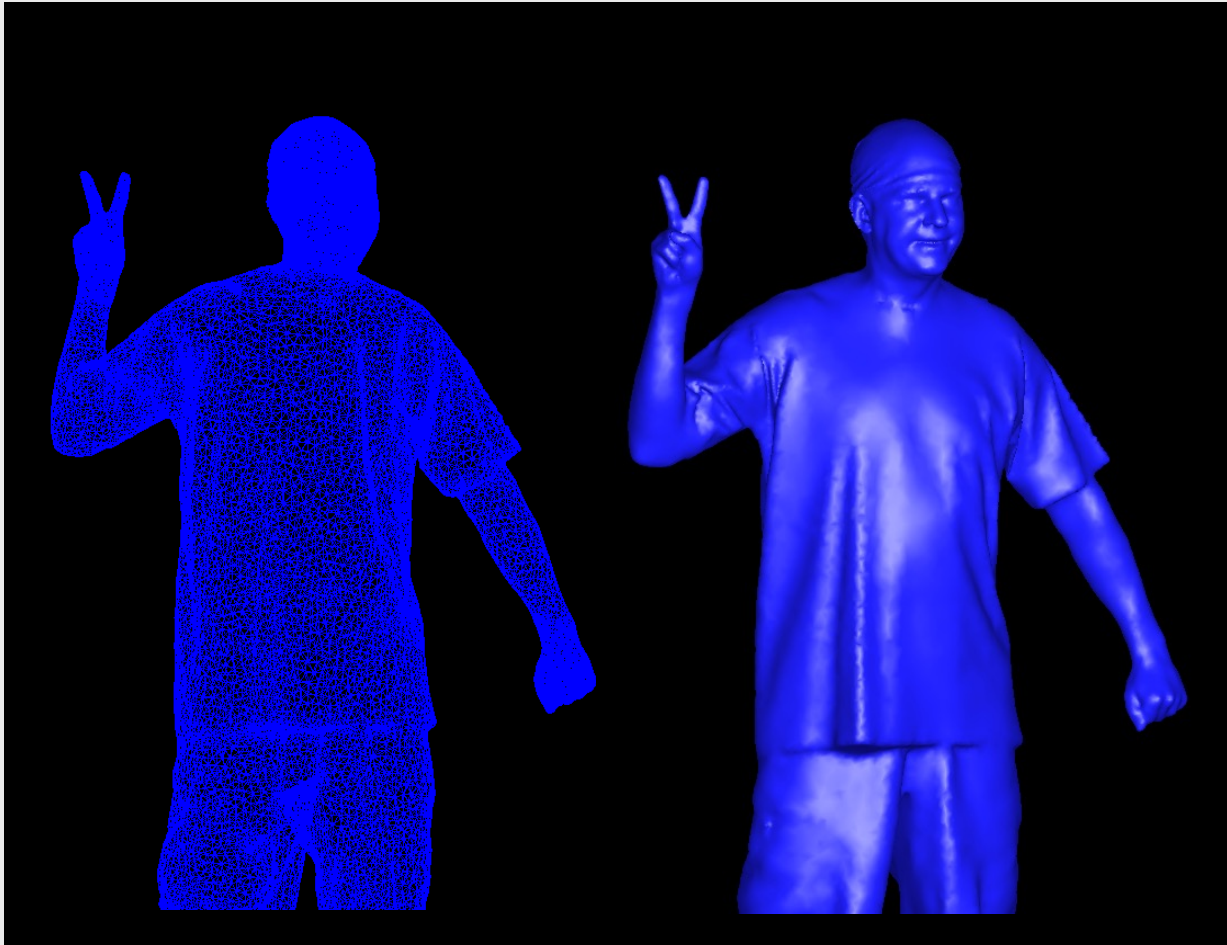
- Why does the image of a real sphere look like



- Light-material interactions cause each point to have a different color, referred to as *shade*.
- Need to consider
  - Light sources
  - Material properties
  - Location of viewer
  - Surface orientation

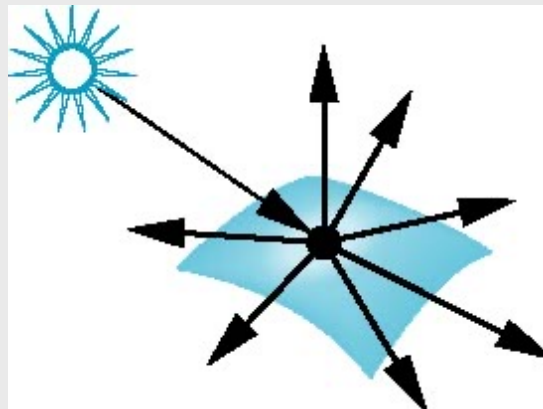


# Shading

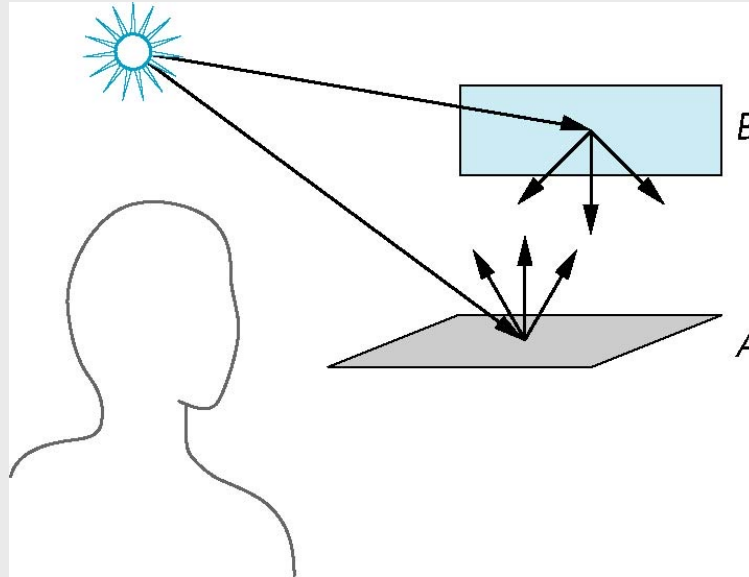


# Light-Material Interaction

- Light that strikes an object is partially absorbed and partially scattered (reflected)
- The reflected light is scattered in a manner that depends on the smoothness and orientation of the surface
- The amount of light reflected determines the color and brightness of the object
  - A surface appears red under white light because the red component of the light is reflected and the rest is absorbed

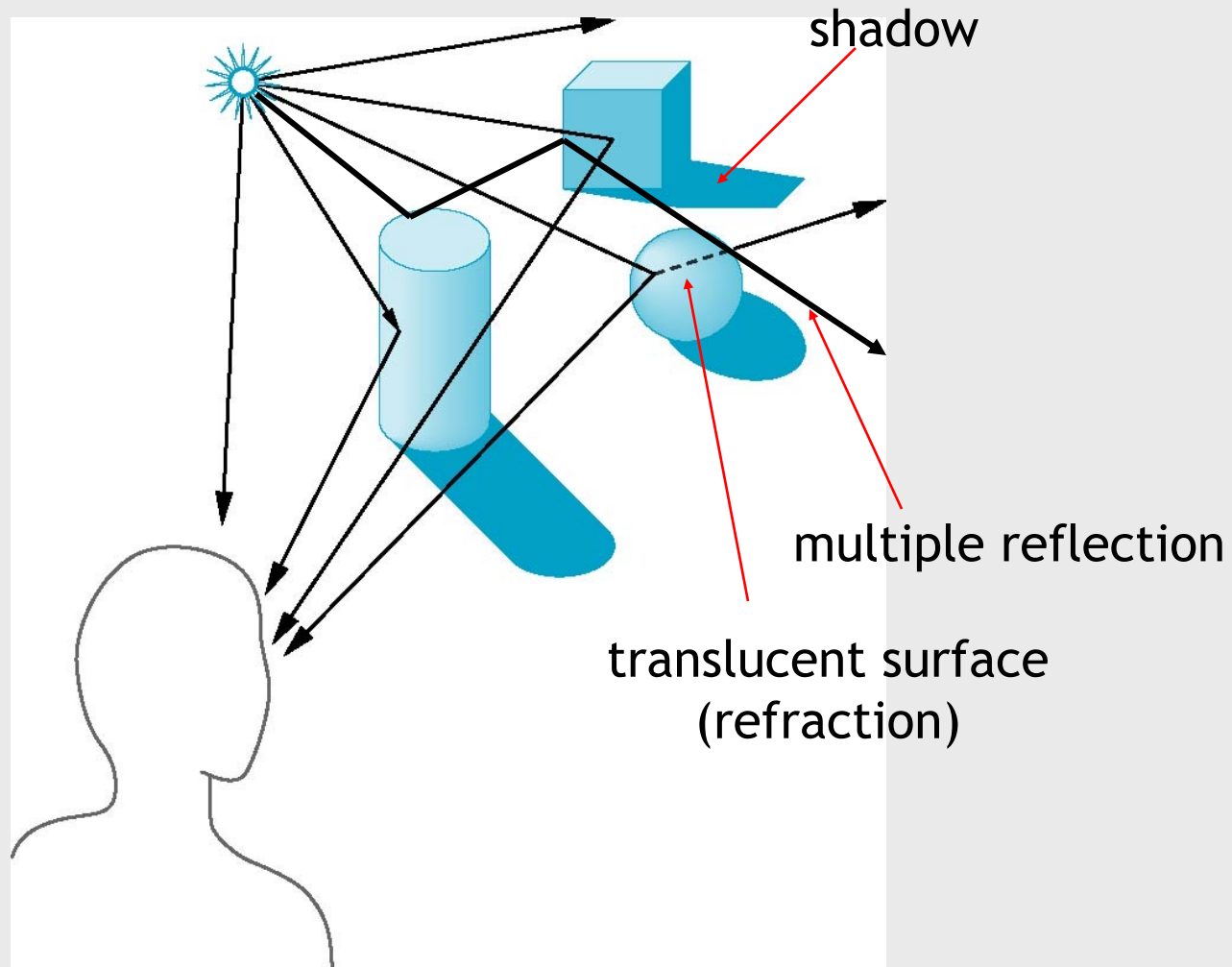


# Scattering



- Light strikes A
  - Some scattered
  - Some absorbed
- Some of scattered light strikes B
  - Some scattered
  - Some absorbed
- Some of this scattered light strikes again A and so on

# Global Effects



# Rendering Equation

- The infinite scattering and absorption of light can be described by the **rendering equation** (see Chapter 11.4 from textbook)
- Rendering equation is global and includes
  - Shadows
  - Multiple scattering from object to object
  - Refractions
- Too complex for a practical solution
- **Ray tracing** is a special case of rendering equation for perfectly reflecting surfaces, and **radiosity technique** for perfectly diffuse surfaces.

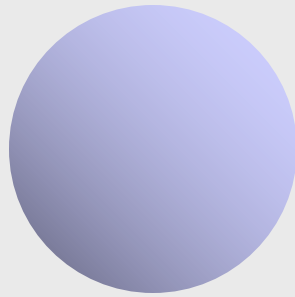


# Local vs Global Rendering

- Correct shading requires a global calculation involving all objects and light sources
  - i.e., solve rendering equation
  - which is incompatible with pipeline model that shades each polygon independently (local illumination)
- In computer graphics, especially in real time graphics, we are content if things “look right”
  - There exist many techniques for approximating global effects

# Local illumination

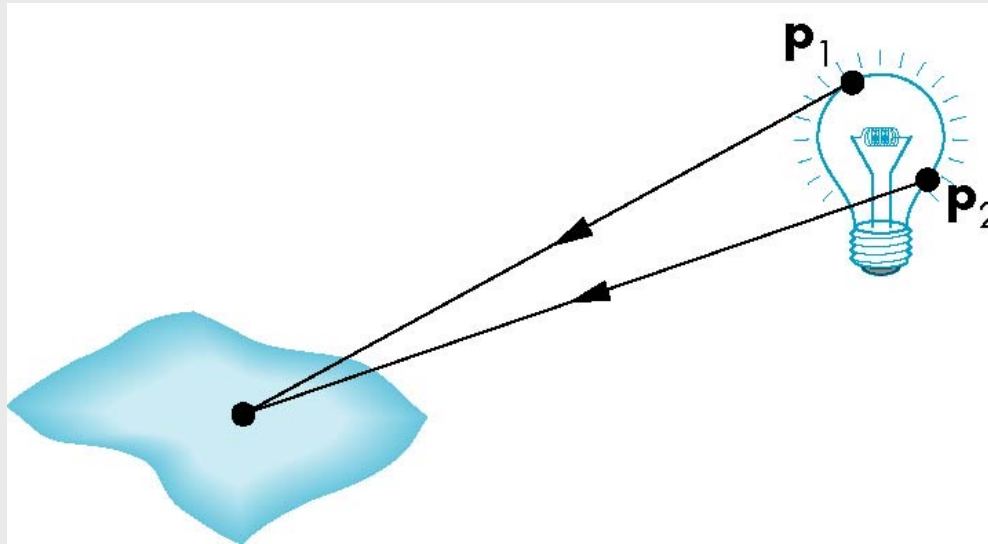
- So we need a local illumination model that will work with the pipeline approach:



- Need to consider
  - Light sources
  - Material properties
  - Location of viewer
  - Surface orientation

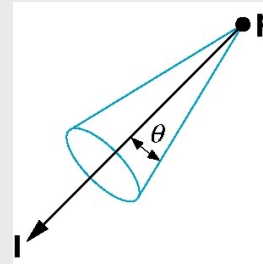
# Light Sources

Realistic light sources are difficult to work with because we must integrate light coming from all points on the source



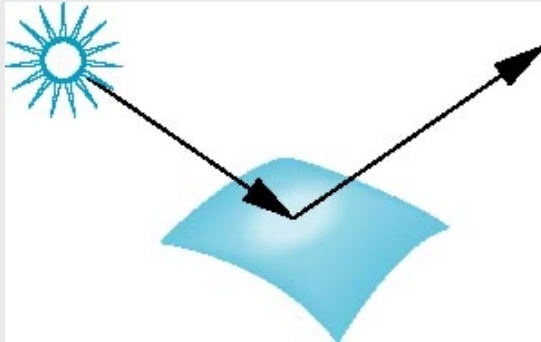
# Simple Light Sources

- Point source
  - Model with position and color
  - Distant source = infinite distance away (parallel)
- Spotlight
  - Restrict light from ideal point source
- Ambient light
  - Same amount of light everywhere in the scene
  - Can model contribution of many sources and scattering

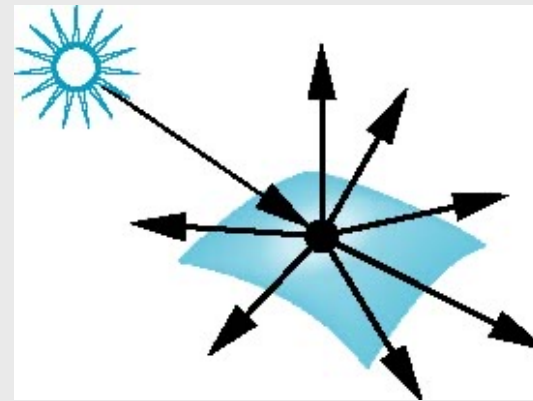


# Surface Types

- The smoother a surface, the more reflected light is concentrated in the direction that a perfect mirror would reflect the light
- A very rough surface scatters light in all directions



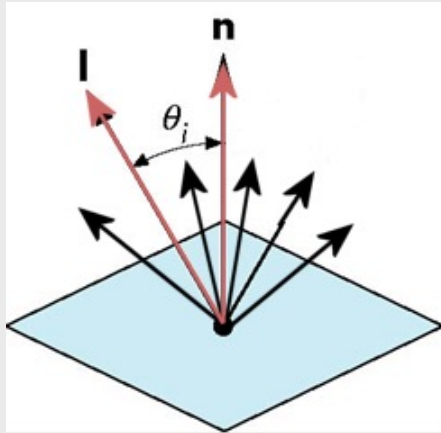
smooth surface



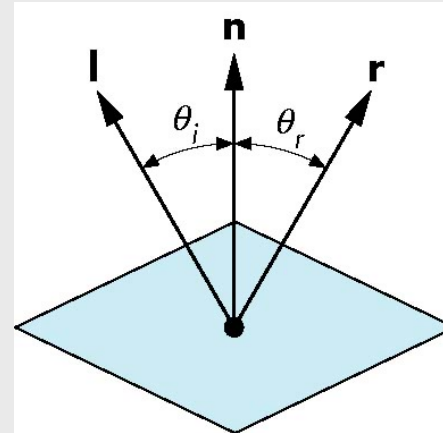
rough surface

# Two extremes (Diffuse vs Specular)

- Perfectly diffuse (Lambertian) surfaces
  - Light scattered equally in all directions
  - Amount of light reflected is proportional to the vertical component of incoming light
- Perfectly specular surfaces
  - Ideal reflectors (mirror-like)
  - Angle of incidence = Angle of reflection



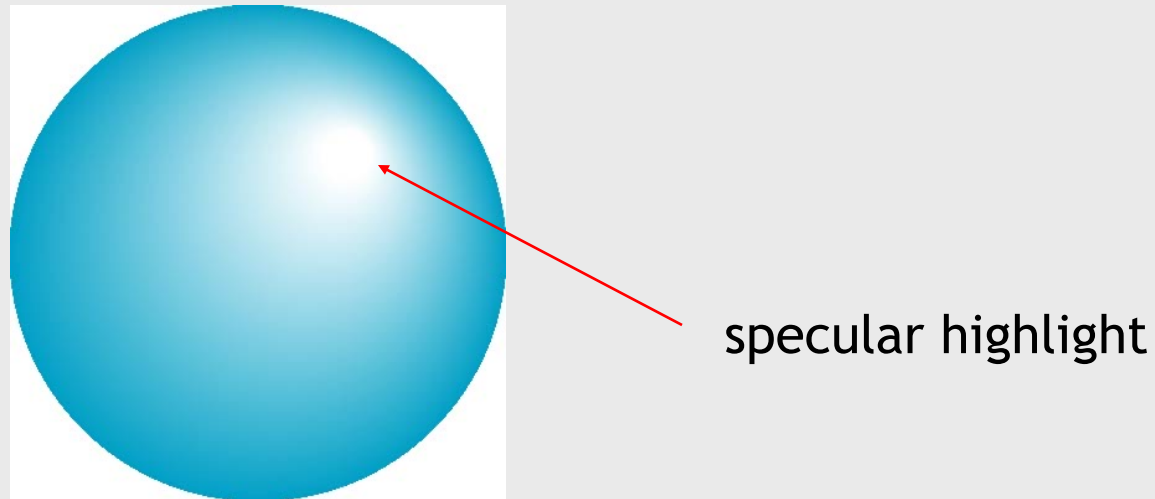
perfectly diffuse



perfectly specular

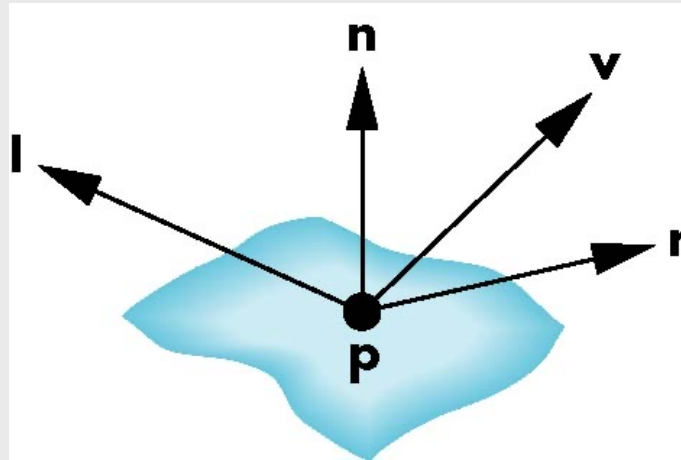
# Real Surfaces

- Most surfaces are neither ideal diffusers nor perfectly specular
- Real surfaces show specular highlights due to incoming light being reflected in directions concentrated close to the direction of a perfect reflection



# Phong Model

- A simple model that can be computed fast
- Has three components
  - Diffuse
  - Specular
  - Ambient
- Uses four vectors
  - To source ( $l$ )
  - To viewer ( $v$ )
  - Normal ( $n$ )
  - Perfect reflector ( $r$ )





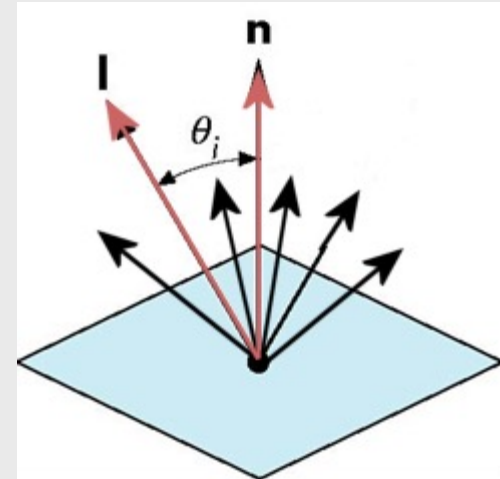
# Perfectly Diffuse Surfaces

- Light scattered equally in all directions
- Amount of light reflected is proportional to the perpendicular component of incoming light
- Normal (perpendicular) vector  $\mathbf{n}$  is determined by local orientation
  - reflected light  $\sim \cos \theta_i$
  - $\cos \theta_i = \mathbf{l} \cdot \mathbf{n}$  (if vectors are normalized to be unity)
  - There are also three coefficients,  $k_{rd}$ ,  $k_{bd}$ ,  $k_{gd}$ , that show how much of each color component is reflected

$$I_d = k_d L_d \mathbf{l} \cdot \mathbf{n}$$

$$(0 \leq k_d \leq 1)$$

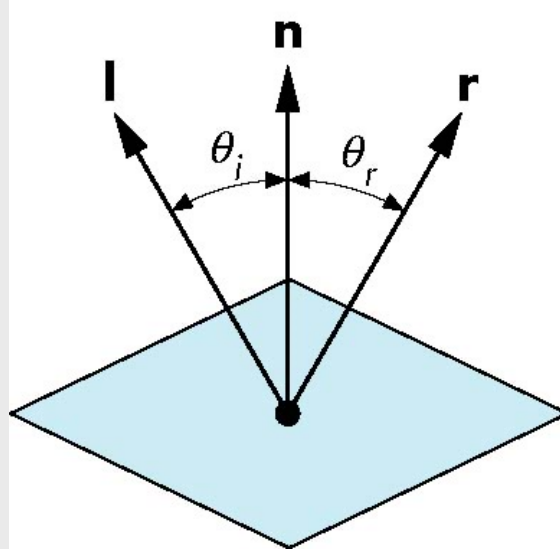
$I_d$  : diffuse component of the shade



# Perfectly Specular Surfaces

- Ideal reflectors
- Angle of incidence = Angle of reflection
- The three vectors  $\mathbf{n}$ ,  $\mathbf{l}$  and  $\mathbf{r}$  must be coplanar:

$$\mathbf{r} = 2 (\mathbf{l} \cdot \mathbf{n}) \mathbf{n} - \mathbf{l} \quad \text{(see page 275 from textbook for derivation)}$$



# Modeling Specular Reflections

- Phong proposed using a term that drops off as the angle between the viewer and the ideal reflection increases

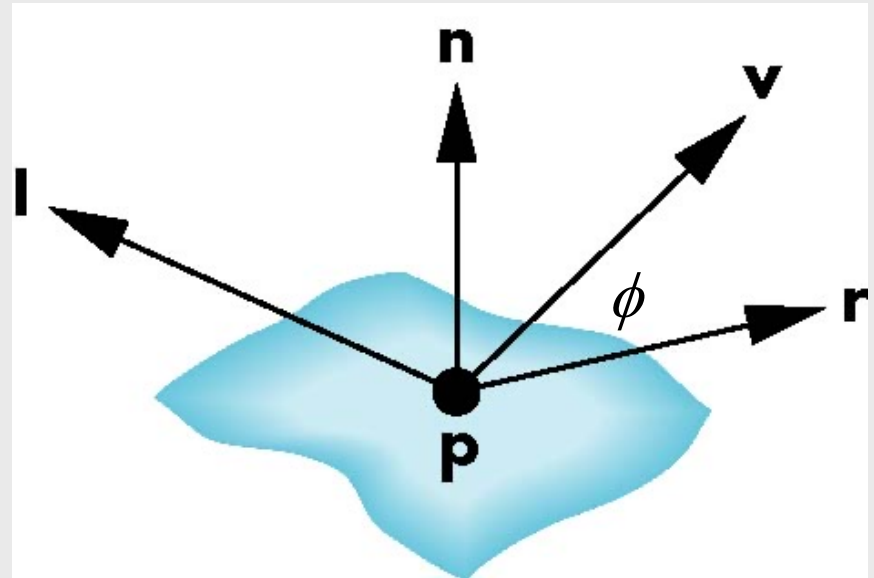
$$I_s = k_s L_s \cos^\alpha \phi$$

reflected intensity

shininess coef

incoming intensity

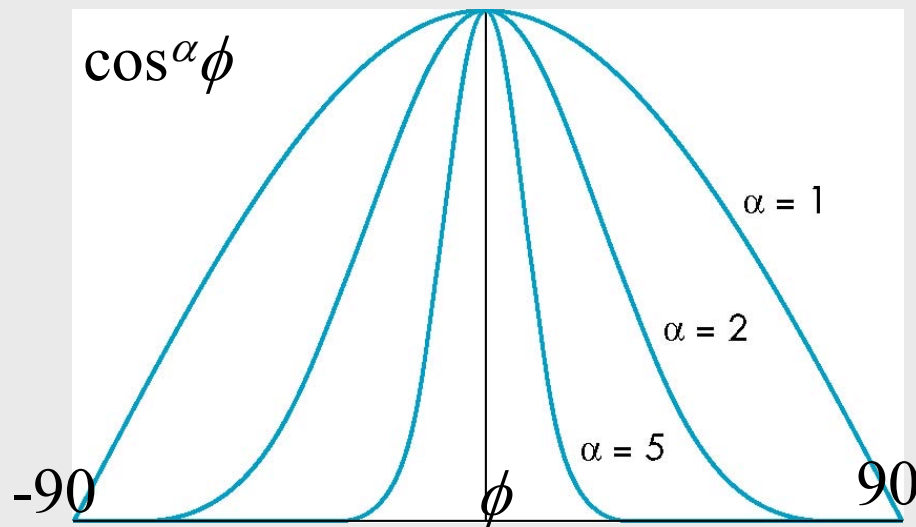
reflection coef



$I_s$  : specular component of the shade

# The Shininess Coefficient

- Values of  $\alpha$  between 100 and 200 correspond to metals
- Values between 5 and 10 give surfaces that look like plastic



$$I_s = k_s L_s \cos^\alpha \phi$$

# Ambient Light

- Ambient light is the result of multiple interactions between light sources and the objects in the environment
- Amount and color of ambient light depend on both color of the light(s) and material properties of the object
- Add  $k_a L_a$  to diffuse and specular terms

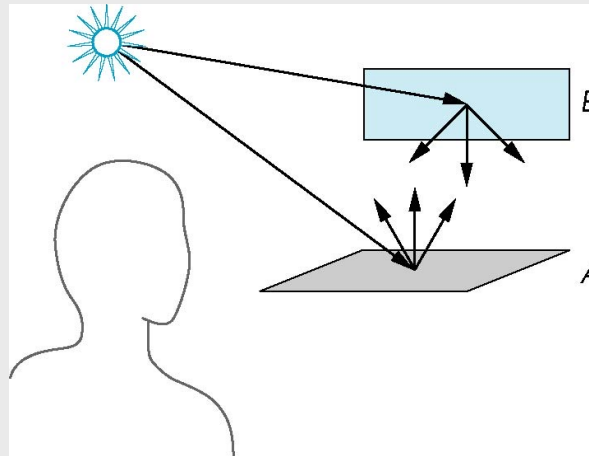
reflection coef

intensity of ambient light



# Distance Terms

- The light from a point source that reaches a surface is inversely proportional to the square of the distance between them.
- We can add a factor of the form  $1/(a + bd + cd^2)$  to the diffuse and specular terms.
- The constant and linear terms soften the effect of the point source.



# Light Sources

- In the Phong Model, we add the contributions from each light source.
- Each light source has separate diffuse, specular, and ambient terms to allow for maximum flexibility, even though this form does not have a physical justification.
- Separate red, green and blue components.
- Hence, 9 coefficients for each point light source
  - $L_{dr}, L_{dg}, L_{db}, L_{sr}, L_{sg}, L_{sb}, L_{ar}, L_{ag}, L_{ab}$

# Material Properties

- Material properties match light source properties
  - Nine reflection coefficients
    - $k_{dr}, k_{dg}, k_{db}, k_{sr}, k_{sg}, k_{sb}, k_{ar}, k_{ag}, k_{ab}$
  - Shininess coefficient  $\alpha$

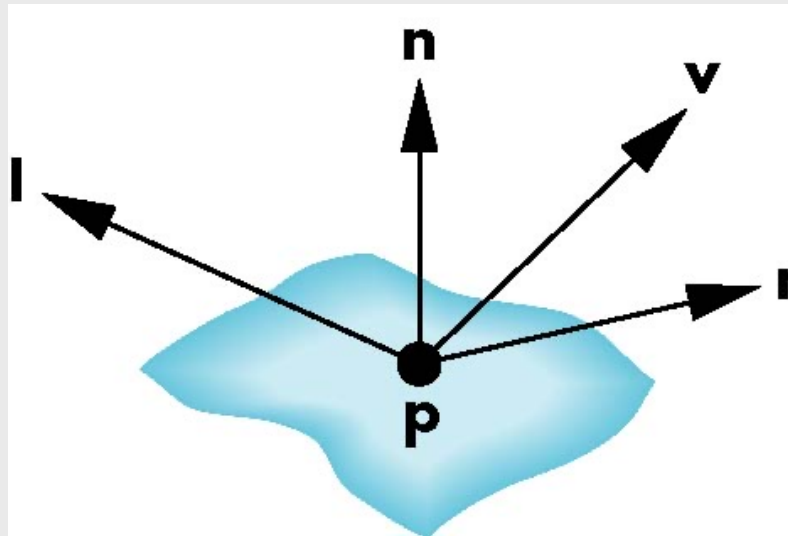


# Adding up the Components

For each light source and each color component, the **Phong** model can then be written as

$$I = \frac{1}{a + bd + cd^2} (k_d L_d \mathbf{l} \cdot \mathbf{n} + k_s L_s (\mathbf{v} \cdot \mathbf{r})^\alpha) + k_a L_a$$

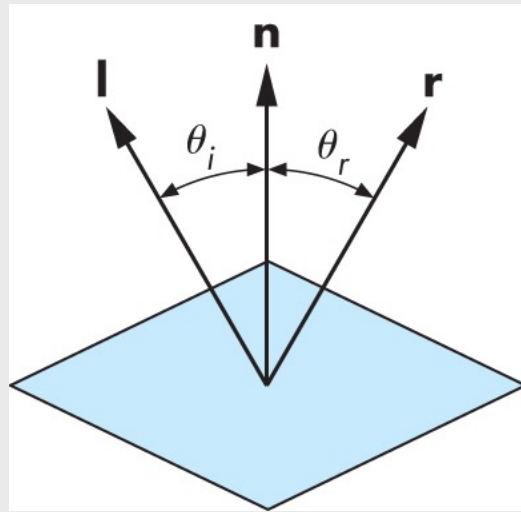
For each color component we add contributions from all light sources.



# Computation of Vectors

$$I = \frac{1}{a + b d + c d^2} ( k_d L_d \mathbf{l} \cdot \mathbf{n} + k_s L_s (\mathbf{v} \cdot \mathbf{r})^\alpha ) + k_a L_a$$

- $\mathbf{l}$  and  $\mathbf{v}$  are specified by the application
- Can compute  $\mathbf{r}$  from  $\mathbf{l}$  and  $\mathbf{n}$
- But how to compute  $\mathbf{n}$ ?
- OpenGL leaves computation of  $\mathbf{n}$  to application

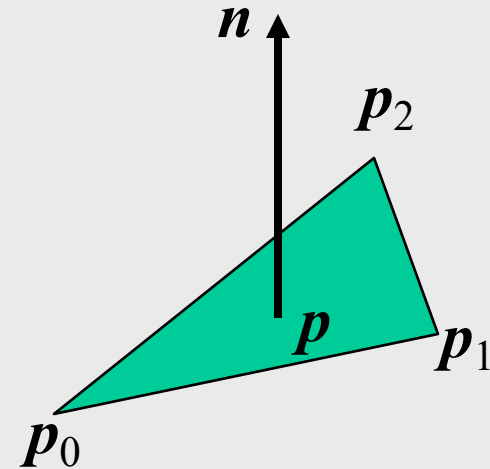


All vectors to be  
unit length

$$\mathbf{r} = 2 (\mathbf{l} \cdot \mathbf{n}) \mathbf{n} - \mathbf{l}$$

# Computation of Normal for Triangles

- Right-hand rule determines outward face
- Normal:  $\mathbf{n} = (\mathbf{p}_1 - \mathbf{p}_0) \times (\mathbf{p}_2 - \mathbf{p}_0)$
- Normalize by  $\mathbf{n} \leftarrow \mathbf{n} / |\mathbf{n}|$



# Modified Phong Model

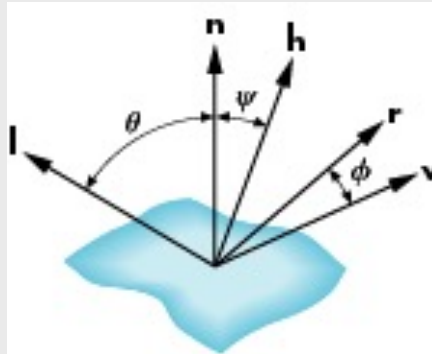
$$I = (k_d L_d \mathbf{l} \cdot \mathbf{n} + k_s L_s (\mathbf{v} \cdot \mathbf{r})^\alpha) + k_a L_a$$

- The specular term in the Phong model above is problematic because it requires for each vertex the calculation of a new reflection vector  $\mathbf{r}$  (along with view vector  $\mathbf{v}$ )
- *Blinn* suggested an approximation using the halfway vector that is more efficient

# The Halfway Vector

- $\mathbf{h}$  is normalized vector halfway between  $\mathbf{l}$  and  $\mathbf{v}$

$$\mathbf{h} = (\mathbf{l} + \mathbf{v}) / |\mathbf{l} + \mathbf{v}|$$



$$I = (k_d L_d \mathbf{l} \cdot \mathbf{n} + k_s L_s (\mathbf{n} \cdot \mathbf{h})^\beta) + k_a L_a$$

Hence we replace  $(\mathbf{v} \cdot \mathbf{r})^\alpha$  by  $(\mathbf{n} \cdot \mathbf{h})^\beta$

Note that  $\mathbf{n} \cdot \mathbf{h}$  depends on the angle between normal vector  $\mathbf{n}$  and halfway vector  $\mathbf{h}$

# Using the halfway vector

- Replace  $(\mathbf{v} \cdot \mathbf{r})^\alpha$  by  $(\mathbf{n} \cdot \mathbf{h})^\beta$

$$I = (k_d L_d \mathbf{l} \cdot \mathbf{n} + k_s L_s (\mathbf{n} \cdot \mathbf{h})^\beta) + k_a L_a$$

- $\beta$  is chosen so as to match shininess  $\alpha$
- Resulting model is known as the **modified Phong** or Blinn lighting model

# OpenGL Example

Differences in these  
teapots are only due to  
the parameters in the  
modified Phong model

