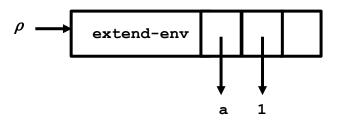
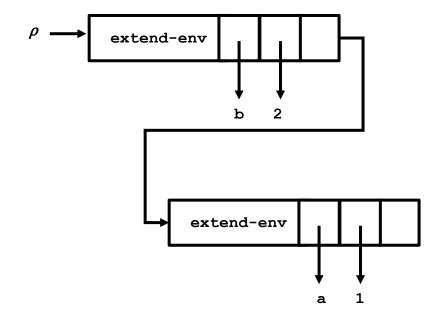
# Letrec Review

T. METIN SEZGIN

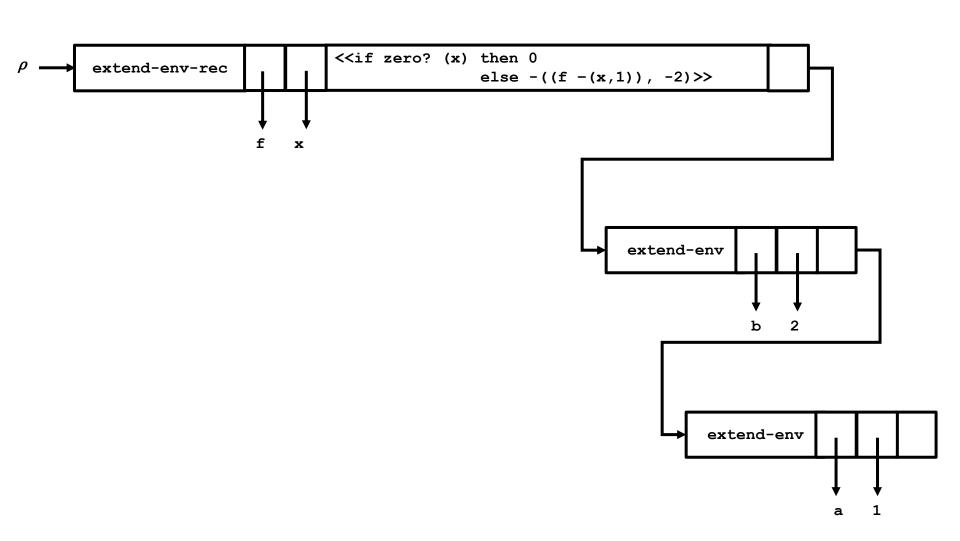
```
let a=1 in let b=2 in letrec f(x) = if zero?(x) then 0 else -((f -(x,1)),-2) in (f 2)
```



let a=1 in let b=2 in letrec f(x) = if zero?(x) then 0 else -((f -(x,1)),-2) in (f 2)



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# Scoping, Binding Lexical Addressing

T. METIN SEZGIN

#### Announcements

Midterm graded

#### Announcements

# Midterm graded

AKYÜREK	ALİ TAYLAN
BAŞOL	KEREM
SARI	GÖKHAN
IŞIK	BÜŞRA
ASLAN	HASAN CAN
KIZIL	MUHAMMED BURAK
YAMANER	ÖZKAN
ARPACI	ONUR EREN

#### Nuggets of the lecture

- Scoping controls how values are bound to variables
- Arguments to procedures always found at the expected places
- We don't need names
- We can create a new "nameless" language
- We can translate named language to the nameless one

#### Denoted values

#### Variables

References

Declarations

- Semantics
  - Binding
  - o Scope

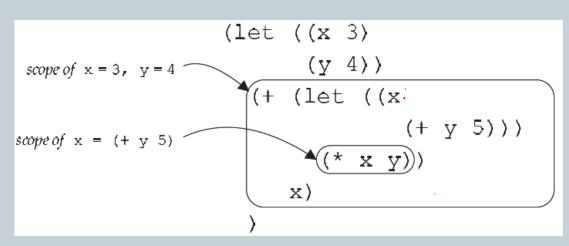
# What is the value of this expression?

#### Denoted values

#### Variables

- References
- Declarations

- Semantics
  - Binding
  - Scope



we need rules to define scoping

# Scoping

#### Static scoping

- Declarations and references can be matched without code
  - execution
- o Search "outward"

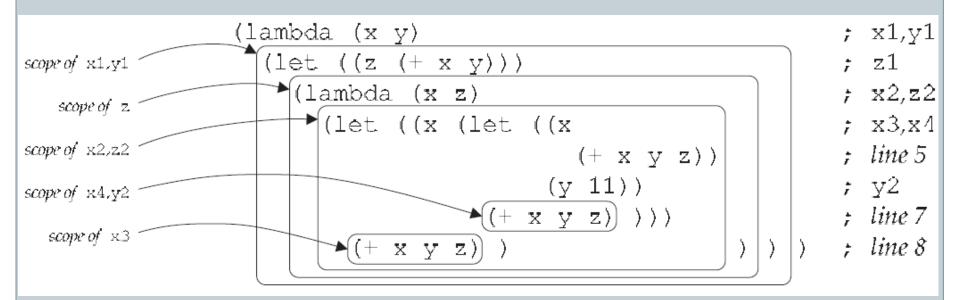
#### Dynamic scoping

- Declarations and references are matched during code execution
- o a in the proc bound to 5

#### Concepts

- Shadowing
- Holes
- Extent
  - Duration of the binding
- Contour diagram
  - Helps resolving bindings
- Lexical depth

### Another example



Where are the binding rules set/defined?

# How are the binding rules defined?

```
(apply-procedure (procedure var body \rho) val)
= (value-of body (extend-env var val \rho))
(value-of (let-exp var\ val\ body)\ \rho)
= (value-of body (extend-env var val \rho))
(value-of
  (letrec-exp proc-name bound-var proc-body letrec-body)
  \rho)
= (value-of
    letrec-body
     (extend-env-rec proc-name bound-var proc-body \rho))
```

Nugget

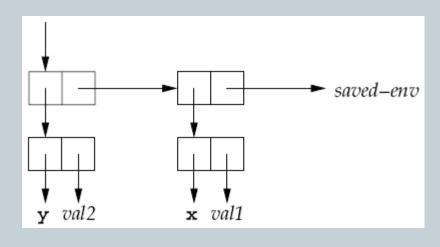
# Arguments to procedures always found at the expected places

# **Evaluating expressions**



```
let x = exp_1
in let y = exp_2
in -(x,y)
```





### Consider another example

• The expression: let a = 5 in proc (x) - (x, a)

• Its value:

Application:

```
(apply-procedure
  (procedure x <<-(x,a)>> [a=[5]] ρ)
  [7])
= (value-of <<-(x,a)>>
  [x=[7]] [a=[5]] ρ)
```

Things are found at the expected lexical depth!

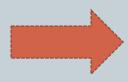
Nugget

# We don't need names

#### We don't need names

We can create a new "nameless" language

```
(lambda (x)
((lambda (a)
(x a))
x))
```



```
(nameless-lambda
    ((nameless-lambda
          (#1 #0))
    #0))
```

# Implementing lexical addressing

The Idea: rewrite value-of (i.o.w. write a translator)

```
let x = 37
in proc (y)
    let z = -(y,x)
    in -(x,y)
```

Nugget

# We can create a new "nameless" language

# The translator: the target language

Nugget

# We can translate the named language to the nameless one

# The translator: Exp x Senv → NamelessExp

#### **Static Environment**

```
Senv = Listof(Sym)
Lexaddr = N
empty-senv : () \rightarrow Senv
(define empty-senv
  (lambda ()
     ′()))
extend-senv : Var \times Senv \rightarrow Senv
(define extend-senv
  (lambda (var senv)
     (cons var senv)))
apply-senv : Senv \times Var \rightarrow Lexaddr
(define apply-senv
  (lambda (senv var)
     (cond
       ((null? senv)
        (report-unbound-var var))
       ((eqv? var (car senv))
        0)
       (else
         (+ 1 (apply-senv (cdr senv) var)))))
```

#### Translator 1

```
translation-of-program : Program → Nameless-program
(define translation-of-program
  (lambda (pgm)
    (cases program pgm
       (a-program (exp1)
         (a-program
           (translation-of exp1 (init-senv)))))))
init-senv : () \rightarrow Senv
(define init-senv
  (lambda ()
    (extend-senv 'i
       (extend-senv 'v
         (extend-senv 'x
           (empty-senv))))))
```

#### Translator 2

```
translation-of : Exp \times Senv \rightarrow Nameless-exp
(define translation-of
  (lambda (exp senv)
    (cases expression exp
      (const-exp (num) (const-exp num)
       (diff-exp (exp1 exp2)
         (diff-exp
           (translation-of exp1 senv)
           (translation-of exp2 senv)))
       (zero?-exp (exp1)
         (zero?-exp
           (translation-of exp1 senv)))
       (if-exp (exp1 exp2 exp3)
         (if-exp
           (translation-of exp1 senv)
           (translation-of exp2 senv)
           (translation-of exp3 senv)))
```

```
(var-exp (var)
  (nameless-var-exp
    (apply-senv senv var)))
(let-exp (var exp1 body)
  (nameless-let-exp
    (translation-of expl senv)
    (translation-of body
      (extend-senv var senv))))
(proc-exp (var body)
  (nameless-proc-exp
    (translation-of body
      (extend-senv var senv))))
(call-exp (rator rand)
  (call-exp
    (translation-of rator senv)
    (translation-of rand senv)))
(else
  (report-invalid-source-expression exp)))))
```