# COMP201

Computer Systems &

Programming

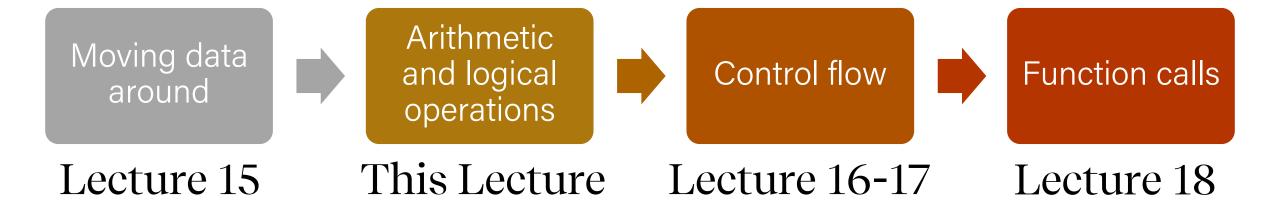
Lecture #15 - Arithmetic and Logic Operations



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# COMP201 Topic 6: How does a computer interpret and execute C programs?

# Learning Assembly



# Learning Goals

- Learn how to perform arithmetic and logical operations in assembly
- Begin to learn how to read assembly and understand the C code that generated it

# Plan for Today

- Recap: mov so far
- Data and Register Sizes
- The lea Instruction
- Logical and Arithmetic Operations
- Practice: Reverse Engineering

**Disclaimer:** Slides for this lecture were borrowed from

—Nick Troccoli's Stanford CS107 class

# Helpful Assembly Resources

#### Course textbook

Reminder: see relevant readings for each lecture on the Schedule section: <a href="https://aykuterdem.github.io/classes/comp201/index.html#div\_schedule">https://aykuterdem.github.io/classes/comp201/index.html#div\_schedule</a>

#### Other resources

See the guides on the resources section of the course website: <a href="https://aykuterdem.github.io/classes/comp201/index.html#div\_resources">https://aykuterdem.github.io/classes/comp201/index.html#div\_resources</a>

- Stanford CS107 Assembly Reference Sheet
- Stanford CS107 Guide to x86-64
- CMU 15-213 x86-64 Machine-Level Programming

#### Lecture Plan

- Recap: mov so far
- Data and Register Sizes
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#### mov

The **mov** instruction <u>copies</u> bytes from one place to another; it is similar to the assignment operator (=) in C.

mov src, dst

The **src** and **dst** can each be one of:

- Immediate (constant value, like a number) (only src)
- Register
- Memory Location
   (at most one of src, dst)

# Memory Location Syntax

Syntax	Meaning	
0x104	Address <b>0x104</b> (no \$)	
(%rax)	What's in %rax	
4(%rax)	What's in %rax, plus 4	
(%rax, %rdx)	Sum of what's in %rax and %rdx	
4(%rax, %rdx)	Sum of values in %rax and %rdx, plus 4	
(, %rcx, 4)	What's in %rcx, times 4 (multiplier can be 1, 2, 4, 8)	
(%rax, %rcx, 2)	What's in %rax, plus 2 times what's in %rcx	
8(%rax, %rcx, 2)	What's in %rax, plus 2 times what's in %rcx, plus 8	

# Operand Forms

Туре	Form	Operand Value	Name
Immediate	\$Imm	Imm	Immediate
D		D	
Register	r <sub>a</sub>	$R[r_a]$	Register
Memory	Imm	M[Imm]	Absolute
Memory	$(r_a)$	$M[R[r_a]]$	Indirect
Memory	Imm(r <sub>b</sub> )	$M[Imm + R[r_b]]$	Base + displacement
Memory	$(r_b, r_i)$	$M[R[r_b] + R[r_i]]$	Indexed
Memory	Imm(r <sub>b</sub> , r <sub>i</sub> )	$M[Imm + R[r_b] + R[r_i]]$	Indexed
Memory	$(r_i, s)$	$M[R[r_i] \cdot s]$	Scaled indexed
Memory	Imm(, r <sub>i</sub> , s)	$M[Imm + R[r_i] \cdot s]$	Scaled indexed
Memory	$(r_b, r_i, s)$	$M[R[r_b] + R[r_i] \cdot s]$	Scaled indexed
Memory	$Imm(r_b, r_i, s)$	$M[Imm + R[r_b] + R[r_i] \cdot s]$	Scaled indexed

**Figure 3.3 from the book: "Operand forms.** Operands can denote immediate (constant) values, register values, or values from memory. The scaling factor s must be either. 1, 2, 4, or 8."

#### Lecture Plan

- Recap: mov so far
- Data and Register Sizes
- The lea Instruction
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- Practice: Reverse Engineering

#### Data Sizes

Data sizes in assembly have slightly different terminology to get used to:

- A **byte** is 1 byte.
- A word is 2 bytes.
- A double word is 4 bytes.
- A quad word is 8 bytes.

Assembly instructions can have suffixes to refer to these sizes:

- b means byte
- w means word
- 1 means double word
- q means quad word

#### Data Sizes

Data sizes in assembly have slightly different terminology to get used to:

- A **byte** is 1 byte.
- A word is 2 bytes.
- A double word is 4 bytes.
- A quad word is 8 bytes.

C Type	Suffix	Byte	Intel Data Type
char	b	1	Byte
short	W	2	Word
int	1	4	Double word
long	q	8	Quad word
char *	q	8	Quad word
float	S	4	Single precision
double	1	8	Double precision

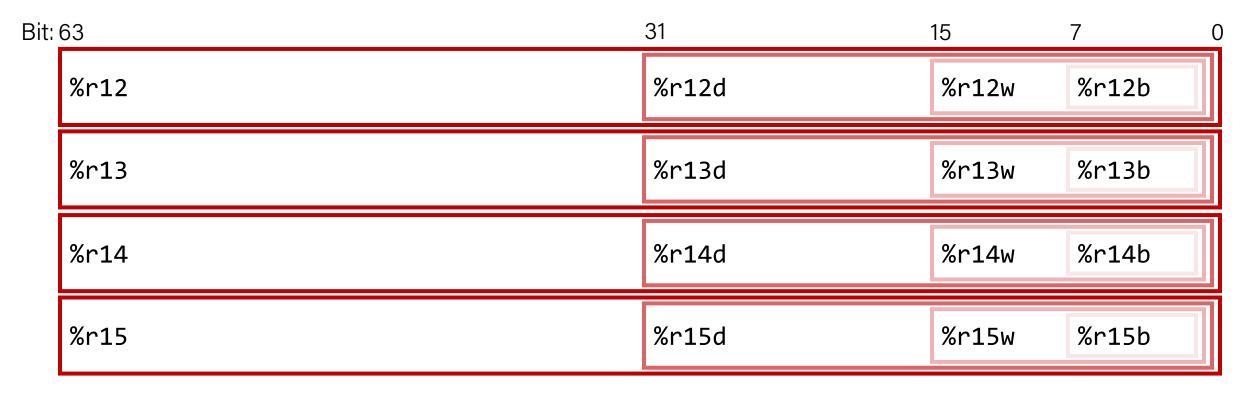
# Register Sizes

Bit:	63	31	15	7 0
	%rax	%eax	%ax	%al
	%rbx	%ebx	%bx	%bl
	%rcx	%ecx	%сх	%c1
	%rdx	%edx	%dx	%dl
	%rsi	%esi	%si	%sil
	%rdi	%edi	%di	%dil

# Register Sizes

Bit:	63	31	15	7 0
	%rbp	%ebp	%bp	%bpl
	%rsp	%esp	%sp	%spl
	%r8	%r8d	%r8w	%r8b
	%r9	%r9d	%r9w	%r9b
	%r10	%r10d	%r10w	%r10b
	%r11	%r11d	%r11w	%r11b

# Register Sizes



# Register Responsibilities

Some registers take on special responsibilities during program execution.

- **%rax** stores the return value
- **%rdi** stores the first parameter to a function
- **%rsi** stores the second parameter to a function
- %rdx stores the third parameter to a function
- **%rip** stores the address of the next instruction to execute
- **%rsp** stores the address of the current top of the stack

See **Stanford CS107 x86-64 Reference Sheet** on Resources page of the course website! <a href="https://aykuterdem.github.io/classes/comp201/index.html#div\_resources">https://aykuterdem.github.io/classes/comp201/index.html#div\_resources</a>

#### mov Variants

- mov can take an optional suffix (b,w,1,q) that specifies the size of data to move: movb, movw, movl, movq
- **mov** only updates the specific register bytes or memory locations indicated.
  - Exception: mov1 writing to a register will also set high order 4 bytes to 0.

#### Practice #1: mov And Data Sizes

For each of the following mov instructions, determine the appropriate suffix based on the operands (e.g. movb, movw, movl or movq).

```
1. mov__ %eax, (%rsp) movl %eax, (%rsp)

2. mov__ (%rax), %dx movw (%rax), %dx

3. mov__ $0xff, %bl movb $0xff, %bl

4. mov__ (%rsp,%rdx,4),%dl movb (%rsp,%rdx,4),%dl

5. mov__ (%rdx), %rax movq (%rdx), %rax

6. mov__ %dx, (%rax) movw %dx, (%rax)
```

#### mov

- The **movabsq** instruction is used to write a 64-bit Immediate (constant) value.
- The regular **movq** instruction can only take 32-bit immediates.
- 64-bit immediate as source, only register as destination.

movabsq \$0x0011223344556677, %rax

#### Practice #2: mov And Data Sizes

For each of the following mov instructions, determine how data movement instructions modify the upper bytes of a destination register.

#### movz and movs

- There are two mov instructions that can be used to copy a smaller source to a larger destination: movz and movs.
- movz fills the remaining bytes with zeros
- **movs** fills the remaining bytes by sign-extending the most significant bit in the source.
- The source must be from memory or a register, and the destination is a register.

#### movz and movs

MOVZ S,R

R ← ZeroExtend(S)

Instruction	Description
movzbw	Move zero-extended byte to word
movzbl	Move zero-extended byte to double word
movzwl	Move zero-extended word to double word
movzbq	Move zero-extended byte to quad word
movzwq	Move zero-extended word to quad word

#### movz and movs

MOVS S,R

 $R \leftarrow SignExtend(S)$ 

Instruction	Description	
movsbw	Move sign-extended byte to word	
movsbl	Move sign-extended byte to double word	
movswl	Move sign-extended word to double word	
movsbq	Move sign-extended byte to quad word	
movswq	Move sign-extended word to quad word	
movslq	Move sign-extended double word to quad word	
cltq	Sign-extend %eax to %rax	
	%rax ← SignExtend(%eax)	

#### Lecture Plan

- Recap: mov so far
- Data and Register Sizes
- The lea Instruction
- Logical and Arithmetic Operations
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#### lea

The **lea** instruction <u>copies</u> an "effective address" from one place to another.

lea src, dst

Unlike **mov**, which copies data <u>at</u> the address src to the destination, **lea** copies the value of src *itself* to the destination.

The syntax for the destinations is the same as **mov**. The difference is how it handles the **src**.

Operands	mov Interpretation	lea Interpretation
6(%rax), %rdx	Go to the address (6 + what's in %rax), and copy data there into %rdx	Copy 6 + what's in %rax into %rdx.

Operands	mov Interpretation	lea Interpretation
6(%rax), %rdx	Go to the address (6 + what's in %rax), and copy data there into %rdx	Copy 6 + what's in %rax into %rdx.
(%rax, %rcx), %rdx	Go to the address (what's in %rax + what's in %rcx) and copy data there into %rdx	Copy (what's in %rax + what's in %rcx) into %rdx.

Operands	mov Interpretation	lea Interpretation
6(%rax), %rdx	Go to the address (6 + what's in %rax), and copy data there into %rdx	Copy 6 + what's in %rax into %rdx.
(%rax, %rcx), %rdx	Go to the address (what's in %rax + what's in %rcx) and copy data there into %rdx	Copy (what's in %rax + what's in %rcx) into %rdx.
(%rax, %rcx, 4), %rdx	Go to the address ( $%$ rax + 4 * $%$ rcx) and copy data there into $%$ rdx.	Copy (%rax + 4 * %rcx) into %rdx.

Operands	mov Interpretation	lea Interpretation
6(%rax), %rdx	Go to the address (6 + what's in %rax), and copy data there into %rdx	Copy 6 + what's in %rax into %rdx.
(%rax, %rcx), %rdx	Go to the address (what's in %rax + what's in %rcx) and copy data there into %rdx	Copy (what's in %rax + what's in %rcx) into %rdx.
(%rax, %rcx, 4), %rdx	Go to the address (%rax + 4 * %rcx) and copy data there into %rdx.	Copy (%rax + 4 * %rcx) into %rdx.
7(%rax, %rax, 8), %rdx	Go to the address $(7 + %rax + 8 * %rax)$ and copy data there into $%rdx$ .	Copy (7 + %rax + 8 * %rax) into %rdx.

Unlike **mov**, which copies data <u>at</u> the address src to the destination, **lea** copies the value of src itself to the destination.

#### Lecture Plan

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# Unary Instructions

The following instructions operate on a single operand (register or memory):

Instruction	Effect	Description
inc D	D ← D + 1	Increment
dec D	D ← D - 1	Decrement
neg D	D ← -D	Negate
not D	D ← ~D	Complement

**Examples:** incq 16(%rax) dec %rdx

not %rcx

# **Binary Instructions**

The following instructions operate on two operands (both can be register or memory, source can also be immediate). Both cannot be memory locations. Read it as, e.g. "Subtract S from D":

Instruction	Effect	Description
add S, D	$D \leftarrow D + S$	Add
sub S, D	D ← D - S	Subtract
imul S, D	D ← D * S	Multiply
xor S, D	D ← D ^ S	Exclusive-or
or S, D	D ← D   S	Or
and S, D	D ← D & S	And

```
Examples: addq %rcx,(%rax)
xorq $16,(%rax, %rdx, 8)
subq %rdx,8(%rax)
```

# Large Multiplication

- Multiplying 64-bit numbers can produce a 128-bit result. How does x86-64 support this with only 64-bit registers?
- If you specify two operands to **imul**, it multiplies them together and truncates until it fits in a 64-bit register.

imul S, D D 
$$\leftarrow$$
 D \* S

• If you specify one operand, it multiplies that by **%rax**, and splits the product across **2** registers. It puts the high-order 64 bits in **%rdx** and the low-order 64 bits in **%rax**.

Instruction	Effect	Description
imulq S	$R[%rdx]:R[%rax] \leftarrow S \times R[%rax]$	Signed full multiply
mulq S	$R[%rdx]:R[%rax] \leftarrow S \times R[%rax]$	Unsigned full multiply

#### Division and Remainder

Instruction	Effect	Description
idivq S	R[%rdx] ← R[%rdx]:R[%rax] mod S; R[%rax] ← R[%rdx]:R[%rax] ÷ S	Signed divide
divq S	R[%rdx] ← R[%rdx]:R[%rax] mod S; R[%rax] ← R[%rdx]:R[%rax] ÷ S	Unsigned divide

- Terminology: dividend / divisor = quotient + remainder
- x86-64 supports dividing up to a 128-bit value by a 64-bit value.
- The high-order 64 bits of the dividend are in **%rdx**, and the low-order 64 bits are in **%rax**. The divisor is the operand to the instruction.
- The quotient is stored in %rax, and the remainder in %rdx.

#### Division and Remainder

Instruction	Effect	Description
idivq S	R[%rdx] ← R[%rdx]:R[%rax] mod S; R[%rax] ← R[%rdx]:R[%rax] <b>÷</b> S	Signed divide
divq S	R[%rdx] ← R[%rdx]:R[%rax] mod S; R[%rax] ← R[%rdx]:R[%rax] <b>÷</b> S	Unsigned divide
cqto	R[%rdx]:R[%rax] ← SignExtend(R[%rax])	Convert to oct word

- Terminology: dividend / divisor = quotient + remainder
- The high-order 64 bits of the dividend are in **%rdx**, and the low-order 64 bits are in **%rax**. The divisor is the operand to the instruction.
- Most division uses only 64-bit dividends. The **cqto** instruction sign-extends the 64-bit value in **%rax** into **%rdx** to fill both registers with the dividend, as the division instruction expects.

## Shift Instructions

The following instructions have two operands: the shift amount **k** and the destination to shift, **D**. **k** can be either an immediate value, or the byte register **%c1** (and only that register!)

Instruction	Effect	Description
sal k, D	D ← D << k	Left shift
shl k, D	D ← D << k	Left shift (same as sal)
sar k, D	$D \leftarrow D >>_A k$	Arithmetic right shift
shr k, D	D ← D >> <sub>L</sub> k	Logical right shift

## Shift Amount

Instruction	Effect	Description
sal k, D	D ← D << k	Left shift
shl k, D	D ← D << k	Left shift (same as sal)
sar k, D	$D \leftarrow D >>_A k$	Arithmetic right shift
shr k, D	D ← D >> <sub>L</sub> k	Logical right shift

- When using **%c1**, the width of what you are shifting determines what portion of **%c1** is used.
- For w bits of data, it looks at the low-order log2(w) bits of %cl to know how much to shift.
  - If **%c1** = 0xff (0b11111111), then: **shlb** shifts by 7 because it considers only the low-order log2(8) = 3 bits, which represent 7. **shlw** shifts by 15 because it considers only the low-order log2(16) = 4 bits, which represent 15.

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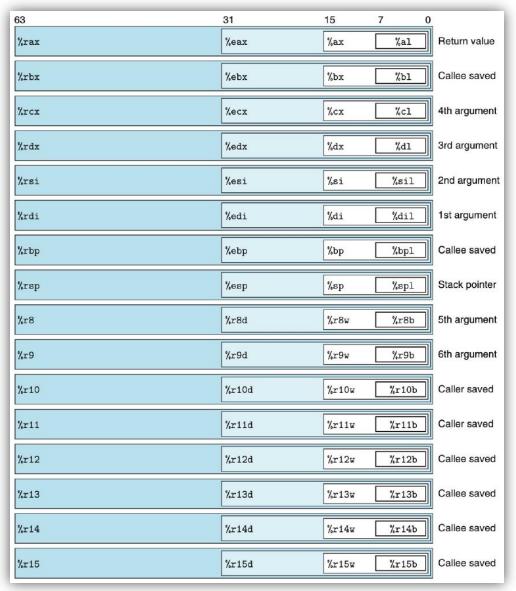
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## Assembly Exploration

- Let's pull these commands together and see how some C code might be translated to assembly.
- Compiler Explorer is a handy website that lets you quickly write C code and see its assembly translation. Let's check it out!
- https://godbolt.org/z/NLYhVf

# Code Reference: add\_to\_first

```
// Returns the sum of x and the first
// element in arr
int add to first(int x, int arr[]) {
    int sum = x;
    sum += arr[0];
    return sum;
add to first:
  movl %edi, %eax
  addl (%rsi), %eax
  ret
```



# Code Reference: full\_divide

```
// Returns x/y, stores remainder in location stored in remainder_ptr
long full divide(long x, long y, long *remainder ptr) {
     long quotient = x / y;
     long remainder = x % y;
                                                       %rax
                                                                                                  Return value
                                                                                              %al
                                                                             %eax
     *remainder ptr = remainder;
                                                                                       %bx
                                                                                             %b1
                                                                                                  Callee saved
                                                       %rbx
                                                                             %ebx
     return quotient;
                                                        %rcx
                                                                             %ecx
                                                                                              %cl
                                                                                                  4th argument
                                                        %rdx
                                                                             %edx
                                                                                       %dx
                                                                                              %d1
                                                                                                  3rd argument
                                                        %rsi
                                                                             %esi
                                                                                       %si
                                                                                             %sil
                                                                                                  2nd argument
                                                       %rdi
                                                                             %edi
                                                                                             %dil
                                                                                                  1st argument
full divide.
```

Tarr_arvrac.	
movq %rdx,	%rcx
movq %rdi,	%rax
cqto	
idivq %rsi	
movq %rdx,	(%rcx)
ret	

Instruction	Effect	Description
idivq S	$R[%rdx] \leftarrow R[%rdx]:R[%rax] \mod S;$ $R[%rax] \leftarrow R[%rdx]:R[%rax] = S$	Signed divide
divq S	R[%rdx] ← R[%rdx]:R[%rax] mod S; R[%rax] ← R[%rdx]:R[%rax] ÷ S	Unsigned divide
cqto	$R[%rdx]:R[%rax] \leftarrow SignExtend(R[%rax])$	Convert to oct word

## Assembly Exercise 1



```
00000000004005ac <sum_example1>:
    4005bd:
            8b 45 e8
                           mov %esi,%eax
    4005c3: 01 d0
                           add %edi,%eax
    4005cc: c3
                           retq
```

Which of the following is most likely to have generated the \_\_\_\_ssembly?

```
// A)
void sum_example1() {
    int x;
    int y;
    int sum = x + y;
// C)
void sum_example1(int x, int y) {
    int sum = x + y;
```

```
B)
int sum_example1(int x, int y)
    return x + y;
```

## Assembly Exercise 2



```
00000000000400578 <sum_example2>:
    400578: 8b 47 0c mov 0xc(%rdi),%eax
    40057b: 03 07 add (%rdi),%eax
    40057d: 2b 47 18 sub 0x18(%rdi),%eax
    400580: c3 retq
```

```
int sum_example2(int arr[]) {
    int sum = 0;
    sum += arr[0];
    sum += arr[3];
    sum -= arr[6];
    return sum;
}
```

What location or value in the assembly above represents the C code's **sum** variable?

%eax

## Assembly Exercise 3



```
00000000000400578 <sum_example2>:
        400578: 8b 47 0c mov 0xc(%rdi),%eax
        40057b: 03 07 add (%rdi),%eax
        40057d: 2b 47 18 sub 0x18(%rdi),%eax
        400580: c3 retq
```

```
int sum_example2(int arr[]) {
    int sum = 0;
    sum += arr[0];
    sum += arr[3];
    sum -= arr[6];
    return sum;
}
```

What location or value in the assembly code above represents the C code's 6 (as in arr[6])?

0x18

## Our First Assembly

```
int sum_array(int arr[], int nelems) {
  int sum = 0;
  for (int i = 0; i < nelems; i++) {
    sum += arr[i];
  }
  return sum;
}</pre>
We're 1/2 of the way to understanding assembly!
What looks understandable right now?
```

#### 00000000004005b6 <sum\_array>:

```
4005b6:
           ba 00 00 00 00
                                       $0x0,%edx
                                mov
                                       $0x0,%eax
4005bb:
       b8 00 00 00 00
                                mov
                                       4005cb <sum_array+0x15>
       eb 09
4005c0:
                                jmp
                                movslq %edx,%rcx
4005c2:
       48 63 ca
                                        (%rdi,%rcx,4),%eax
          03 04 8f
                                add
4005c5:
                                       $0x1,%edx
          83 c2 01
4005c8:
                                add
4005cb:
           39 f2
                                       %esi,%edx
                                \mathsf{cmp}
                                j1
                                       4005c2 <sum_array+0xc>
4005cd:
       7c f3
4005cf:
           f3 c3
                                repz retq
```



## A Note About Operand Forms

- Many instructions share the same address operand forms that mov uses.
  - Eg. 7(%rax, %rcx, 2).
- These forms work the same way for other instructions, e.g. sub:
  - sub 8(%rax,%rdx),%rcx -> Go to 8 + %rax + %rdx, subtract what's there from %rcx
- The exception is **lea**:
  - It interprets this form as just the calculation, not the dereferencing
  - lea 8(%rax,%rdx),%rcx -> Calculate 8 + %rax + %rdx, put it in %rcx

# Extra Practice

https://godbolt.org/z/QQj77g

```
int add to(int x, int arr[], int i) {
   int sum = ____;
   sum += arr[ ? ];
   return ___?__;
add to ith:
 movslq %edx, %rdx
 movl %edi, %eax
 addl (%rsi,%rdx,4), %eax
 ret
```

```
int add to(int x, int arr[], int i) {
   int sum = ? ;
   sum += arr[ ? ];
   return ___?__;
// x in %edi, arr in %rsi, i in %edx
add to ith:
 movslq %edx, %rdx
                  // sign-extend i into full register
 movl %edi, %eax
                  // copy x into %eax
 addl (%rsi,%rdx,4), %eax // add arr[i] to %eax
 ret
```

```
int add to(int x, int arr[], int i) {
   int sum = x;
   sum += arr[i];
   return sum;
// x in %edi, arr in %rsi, i in %edx
add to ith:
 movslq %edx, %rdx
                            // sign-extend i into full register
 movl %edi, %eax
                    // copy x into %eax
 addl (%rsi,%rdx,4), %eax // add arr[i] to %eax
 ret
```

```
int elem arithmetic(int nums[], int y) {
   int z = nums[___?__] * ___?__;
   z >>= ____;
   return ? -:
elem arithmetic:
 movl %esi, %eax
 imull (%rdi), %eax
 subl 4(%rdi), %eax
 sarl $2, %eax
 addl $2, %eax
  ret
```

```
int elem arithmetic(int nums[], int y) {
   int z = nums[___?__] * ___?__;
   z >>= <u>?</u>;
   return ? -:
// nums in %rdi, y in %esi
elem arithmetic:
 movl %esi, %eax // copy y into %eax
 imull (%rdi), %eax  // multiply %eax by nums[0]
 subl 4(%rdi), %eax // subtract nums[1] from %eax
 sarl $2, %eax
              // shift %eax right by 2
 addl $2, %eax
              // add 2 to %eax
 ret
```

```
int elem_arithmetic(int nums[], int y) {
   int z = nums[0] * y;
   z \rightarrow nums[1];
   z >>= 2;
   return z + 2;
// nums in %rdi, y in %esi
elem arithmetic:
 movl %esi, %eax // copy y into %eax
 imull (%rdi), %eax  // multiply %eax by nums[0]
 subl 4(%rdi), %eax // subtract nums[1] from %eax
               // shift %eax right by 2
 sarl $2, %eax
 addl $2, %eax
               // add 2 to %eax
 ret
```

```
long func(long x, long *ptr) {
    *ptr = ___?___ + 1;
    long result = x % ____?___;
   return ___?__;
func:
  leaq 1(%rdi), %rcx
 movq %rcx, (%rsi)
 movq %rdi, %rax
  cqto
 idivq %rcx
  movq %rdx, %rax
  ret
```

```
long func(long x, long *ptr) {
   *ptr = ____?___ + 1;
   long result = x % ____?___;
   return ? ;
// x in %rdi, ptr in %rsi
func:
 leaq 1(%rdi), %rcx // put x + 1 into %rcx
 movq %rcx, (%rsi) // copy %rcx into *ptr
 movq %rdi, %rax
                 // copy x into %rax
                         // sign-extend x into %rdx
 cqto
 idivq %rcx
                         // calculate x / (x + 1)
                         // copy the remainder into %rax
 movq %rdx, %rax
 ret
```

```
long func(long x, long *ptr) {
   *ptr = x + 1;
   long result = x \% *ptr; // or x + 1
   return result;
// x in %rdi, ptr in %rsi
func:
 leaq 1(%rdi), %rcx // put x + 1 into %rcx
 movq %rcx, (%rsi) // copy %rcx into *ptr
                  // copy x into %rax
 movq %rdi, %rax
                         // sign-extend x into %rdx
 cqto
 idivq %rcx
                         // calculate x / (x + 1)
                         // copy the remainder into %rax
 movq %rdx, %rax
 ret
```

## Recap

- Recap: mov so far
- Data and Register Sizes
- The lea Instruction
- Logical and Arithmetic Operations
- Practice: Reverse Engineering

**Next Time:** control flow in assembly (while loops, if statements, and more)