

Entry and Priority Queue ADTs

- An **entry** stores a (key, value) pair
- Entry ADT methods:
 - **getKey()**: returns the key associated with this entry
 - **getValue()**: returns the value paired with the key associated with this entry
- Priority Queue ADT:
 - **insert(k, x)**
inserts an entry with key k and value x
 - **removeMin()**
removes and returns the entry with smallest key
 - **min()**
returns, but does not remove, an entry with smallest key
 - **size(), isEmpty()**



Example

- ❑ Online trading system where orders to purchase and sell a stock are stored in two priority queues (one for sell orders and one for buy orders) as (p, s) entries:
 - The key, p , of an order is the price
 - The value, s , for an entry is the number of shares
 - A buy order (p, s) is executed when a sell order (p', s') with price $p' \leq p$ is added (the execution is complete if $s' \geq s$)
 - A sell order (p, s) is executed when a buy order (p', s') with price $p' \geq p$ is added (the execution is complete if $s' \geq s$)
- ❑ What if someone wishes to cancel their order before it executes?
- ❑ What if someone wishes to update the price or number of shares for their order?

Methods of the Adaptable Priority Queue ADT

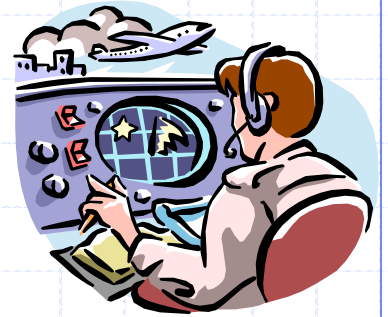
- ❑ **remove**(e): Remove from P and return entry e.
- ❑ **replaceKey**(e,k): Replace with k and return the key of entry e of P; an error condition occurs if k is invalid (that is, k cannot be compared with other keys).
- ❑ **replaceValue**(e,x): Replace with x and return the value of entry e of P.

Example

<i>Operation</i>	<i>Output</i>	<i>P</i>
insert(5,A)	e_1	(5,A)
insert(3,B)	e_2	(3,B),(5,A)
insert(7,C)	e_3	(3,B),(5,A),(7,C)
min()	e_2	(3,B),(5,A),(7,C)
key(e_2)	3	(3,B),(5,A),(7,C)
remove(e_1)	e_1	(3,B),(7,C)
replaceKey(e_2 ,9)	3	(7,C),(9,B)
replaceValue(e_3 ,D)	C	(7,D),(9,B)
remove(e_2)	e_2	(7,D)

Locating Entries

- In order to implement the operations `remove(k)`, `replaceKey(e)`, and `replaceValue(k)`, we need fast ways of locating an entry `e` in a priority queue.
- We can always just search the entire data structure to find an entry `e`, but there are better ways for locating entries.

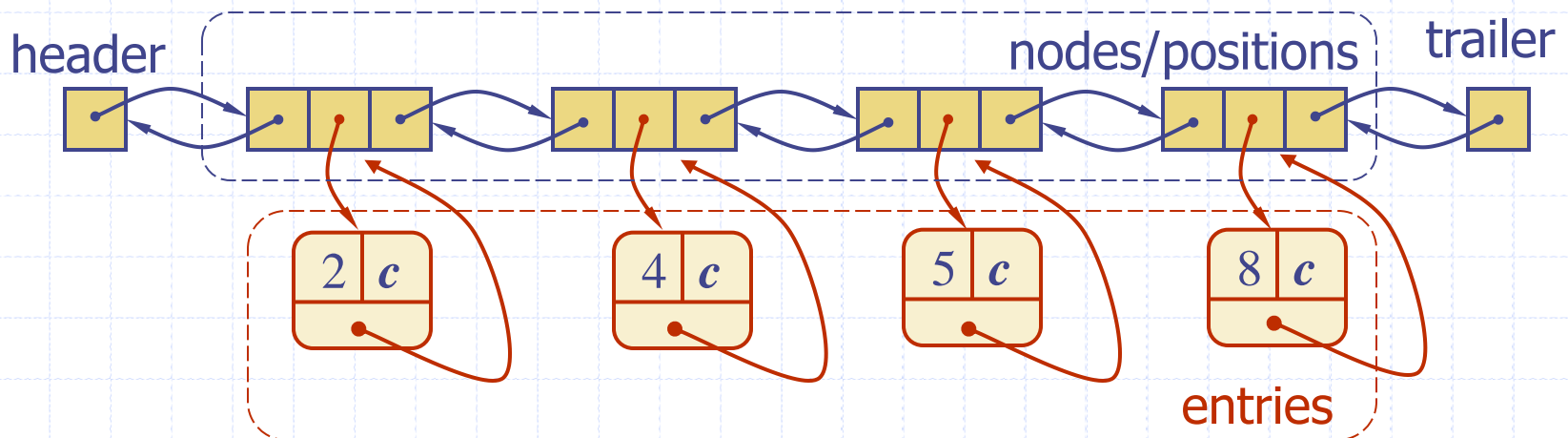


Location-Aware Entries

- ❑ A location-aware entry identifies and tracks the location of its (key, value) object within a data structure
- ❑ Intuitive notion:
 - Coat claim check
 - Valet claim ticket
 - Reservation number
- ❑ Main idea:
 - Since entries are created and returned from the data structure itself, it can return location-aware entries, thereby making future updates easier

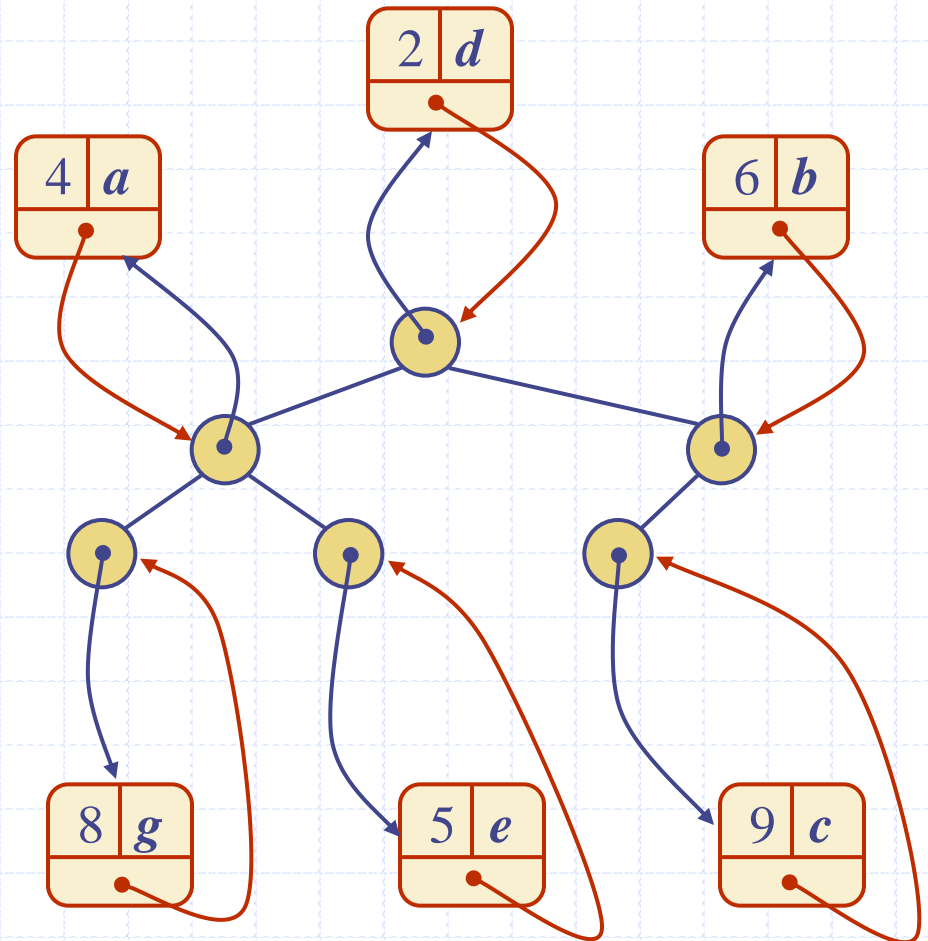
List Implementation

- A location-aware list entry is an object storing
 - key
 - value
 - position (or rank) of the item in the list
- In turn, the position (or array cell) stores the entry
- Back pointers (or ranks) are updated during swaps



Heap Implementation

- ❑ A location-aware heap entry is an object storing
 - key
 - value
 - position of the entry in the underlying heap
- ❑ In turn, each heap position stores an entry
- ❑ Back pointers are updated during entry swaps



Performance

- Improved times thanks to location-aware entries are highlighted in red

Method	Unsorted List	Sorted List	Heap
size, isEmpty	$O(1)$	$O(1)$	$O(1)$
insert	$O(1)$	$O(n)$	$O(\log n)$
min	$O(n)$	$O(1)$	$O(1)$
removeMin	$O(n)$	$O(1)$	$O(\log n)$
remove	$O(1)$	$O(1)$	$O(\log n)$
replaceKey	$O(1)$	$O(n)$	$O(\log n)$
replaceValue	$O(1)$	$O(1)$	$O(1)$