

1. **Differentiation**:

- If $f(x) = \ln(x^2 + 1)$, then the second derivative $f''(x)$ is...
- A) $(2 - 2x^2)/(x^2 + 1)^2$ [Correct]
- B) $(2x^2 - 2)/(x^2 + 1)^2$
- C) $(2x)/(x^2 + 1)$
- D) $(2x^2 + 2)/(x^2 + 1)^2$

2. **Limits**:

- Evaluate the limit: $\lim_{x \rightarrow 0} (\sin(2x)/x) = \dots$
- A) 2 [Correct]
- B) 1
- C) 0
- D) ∞

3. **Differentiation**:

- If $y = \tan^{-1}(x^2)$, find dy/dx when $x = 1$.
- A) 1 [Correct]
- B) 2
- C) $1/2$
- D) 0

4. **Integration**:

- Evaluate the integral: $\int_0^{\pi/2} \sin^3(x) \cos^2(x) dx$.
- A) $1/12$ [Correct]
- B) $1/6$
- C) $1/8$
- D) $1/10$

5. **Differentiation**:

- If $f(x) = e^{(3x)}$ and $g(x) = \ln(x)$, find $(f \circ g)'(x)$.
- A) $3x$ [Correct]
- B) $3/x$
- C) $3x^2$
- D) $e^{(3x)}/x$

6. **Differentiation**:

- If $y = x^x$, find dy/dx .

- A) $x^x(\ln(x) + 1)$ [Correct]
- B) $x^x \ln(x)$
- C) $x^{(x-1)}$
- D) $\ln(x) + 1$

7. **Differentiation**:

- If the function f is continuous on $[0, 2]$ and differentiable on $(0, 2)$, and $f(0) = 1$, $f(2) = 3$, find $f'(c)$ for some c in $(0, 2)$.
- A) 1 [Correct]
- B) 2
- C) 0
- D) 3

8. **Differentiation**:

- If $y = \ln(\sec(x))$, find dy/dx .
- A) $\tan(x)$ [Correct]
- B) $\sec(x)$
- C) $1/\cos(x)$
- D) $\sin(x)$

9. **Integration**:

- Solve for x : $\int (1 \text{ to } x) (1/t) dt = 2$.
- A) e^2 [Correct]
- B) 2
- C) e
- D) $1/e^2$

10. **Functions**:

- If the function $g(x) = x^3 - 3x + 2$ has a local maximum at $x = a$, find the value of a .
- A) -1 [Correct]
- B) 1
- C) 0
- D) 2

11. **Differentiation**:

- If $f(x) = x^2 + 2x + 1$, find the inverse function $f^{-1}(x)$.
- A) $\sqrt{x} - 1$ [Correct]
- B) $-\sqrt{x} - 1$

- C) $x - 1$
- D) $x^2 - 1$

12. ****Differentiation****:

- If $y = \cos(x) + \sin(x)$, find the maximum value of y on the interval $[0, \pi]$.
- A) $\sqrt{2}$ [Correct]
- B) 1
- C) 2
- D) $\sqrt{3}$

13. ****Integration****:

- Determine the area enclosed by the curves $y = x^2$ and $y = 2x$.
- A) $4/3$ [Correct]
- B) 2
- C) $8/3$
- D) 1

14. ****Differentiation****:

- If $y = x^2 + 1/x$, find the asymptotes of the curve.
- A) Vertical asymptote at $x = 0$ [Correct]
- B) Horizontal asymptote at $y = 0$
- C) Oblique asymptote at $y = x$
- D) No asymptotes

15. ****Hard Question - Functions****:

- If $f(x) = x^4 - 4x^3 + 6x^2 - 4x + 1$, find the critical points and determine their nature.
- A) $x = 1$, point of inflection [Correct]
- B) $x = 1$, local minimum
- C) $x = 1$, local maximum
- D) No critical points

16. ****Limits****:

- Evaluate the limit: $\lim_{x \rightarrow \infty} (x^2 - 3x + 2)/(2x^2 + 5)$.
- A) $1/2$ [Correct]
- B) 1
- C) 0
- D) ∞

17. **Differentiation**:

- Determine the Taylor series expansion of $f(x) = e^x$ centered at $x = 0$ up to the fourth degree.

- A) $1 + x + x^2/2 + x^3/6 + x^4/24$ [Correct]
- B) $1 + x + x^2/2 + x^3/3 + x^4/4$
- C) $1 + x + x^2 + x^3 + x^4$
- D) $1 + x^2/2 + x^3/6 + x^4/24$

18. **Differentiation**:

- If $f(x) = \sin(x)$ and $g(x) = \cos(x)$, find the points where $f(x) = g(x)$ on the interval $[0, 2\pi]$.

- A) $\pi/4, 5\pi/4$ [Correct]
- B) $\pi/4, 3\pi/4$
- C) $\pi/2, 3\pi/2$
- D) $0, \pi$

19. **Functions**:

- If $f(x) = |x - 1|$, find the derivative $f'(x)$ at $x = 1$.

- A) Does not exist [Correct]
- B) 0
- C) 1
- D) -1

20. **Differential Equations**:

- Solve the initial value problem: $dy/dx = 3y$, $y(0) = 2$.

- A) $y = 2e^{(3x)}$ [Correct]
- B) $y = 3e^{(2x)}$
- C) $y = 2e^{(x)}$
- D) $y = e^{(3x)}$

21. **Geometry**:

- If the function $h(x) = x^5 - 5x^3 + 4x$ has an inflection point at $x = b$, find b .

- A) $\sqrt{3}/2$ [Correct]
- B) 0
- C) 1
- D) $\sqrt{2}/3$

22. **Geometry**:

- Evaluate the integral: $\int_0^1 e^{-x^2} dx$.

- A) 0.7468 [Correct]

- B) 0.5

- C) 1

- D) 0.25