

# *DSP Final Project Report*

## MATLAB®



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## (1) Sampling and periodicity of sinusoidal signals :

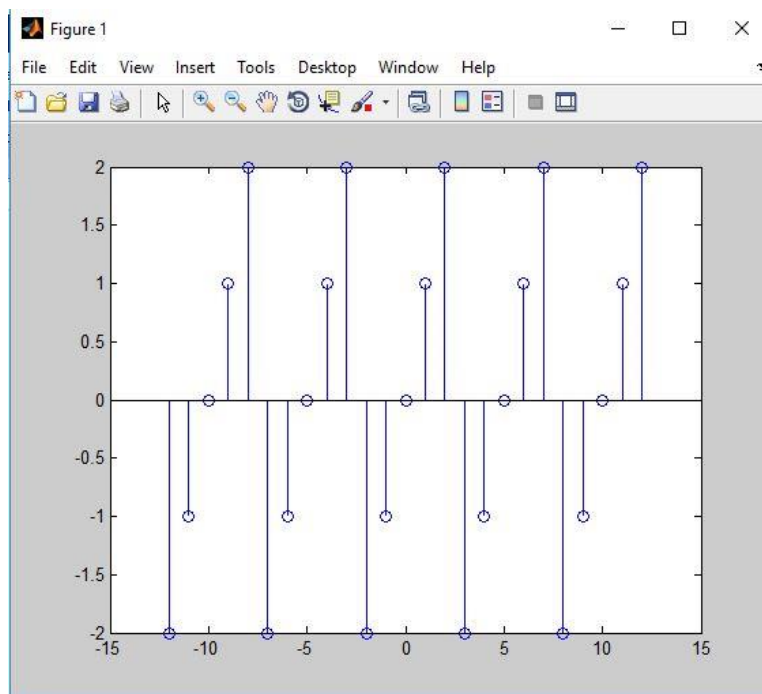
a-

1-

Code:

```
>> n=[-12:1:12];  
>> x1n=[-2:1:2,-2:1:2,-2:1:2,-2:1:2,-2:1:2];  
>> stem(n,x1n)
```

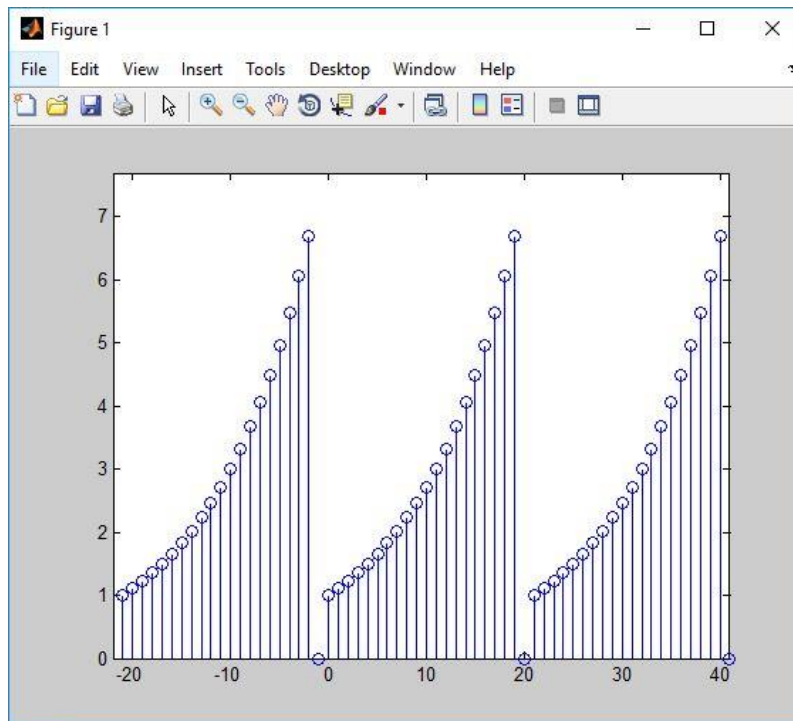
Output:



2-Code:

```
x2n=stepseq(0,0,20)-stepseq(20,0,20);  
n=[0:20];  
e=exp(0.1*n);  
x2n=e.*x2n;  
x2n=[x2n,x2n,x2n];  
np=[-21:41];  
stem(np,x2n);  
axis([min(np)-2,max(np)+2,min(x2n),max(x2n)+2]);
```

Output:

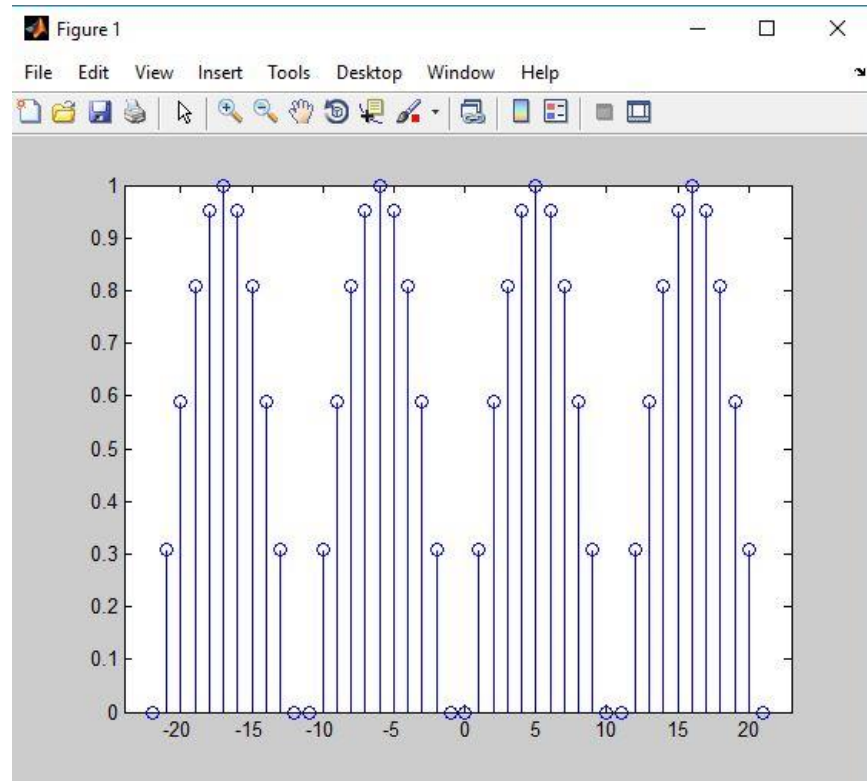


3-

Code:

```
x3n=stepseq(0,0,10)-stepseq(10,0,10);  
n=[0:10];  
s=sin(0.1*pi*n);  
x3n=s.*(x3n);  
x3n=[x3n,x3n,x3n,x3n];  
n=[-21:22];  
stem(n,x3n);  
axis([min(n)-2,max(n)+2,min(x3n),max(x3n)])
```

## Output:



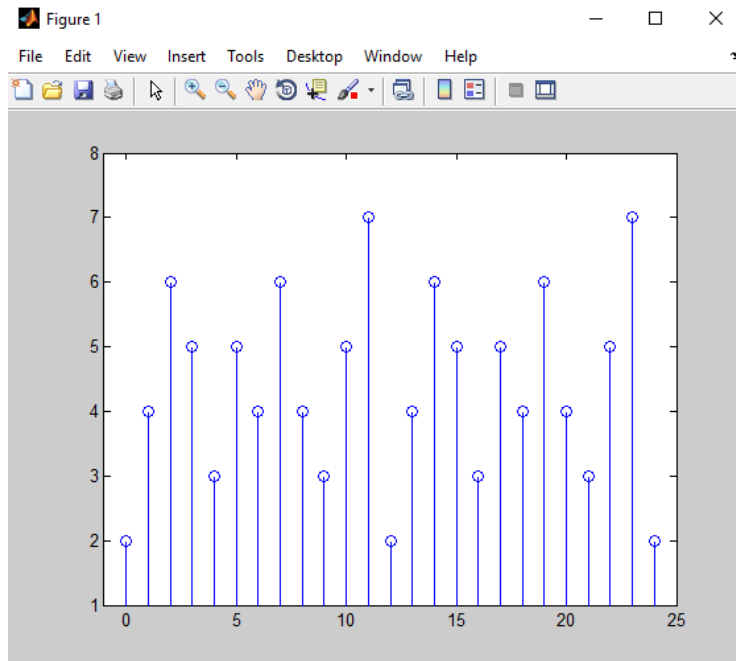
## 4-

### Code:

```
>> n=[0:24];  
>> x4a=[1 2 3];  
>> x4a= repmat(x4a,[1 9]);  
>> x4b=[1 2 3 4];  
>> x4b= repmat(x4b,[1 7]);  
>> x4=x4a(1:25)+x4b(1:25);  
>> stem(n4,x4);  
>> axis([min(n4)-1,max(n4)+1,min(x4)-1,max(x4)+1]);
```

## Output:

*The period of  $x_4(n)$  is  $[2\ 3\ 4\ 6\ 3\ 5\ 4\ 5\ 4\ 3\ 5\ 7]$  and there is 2 periods from  $n = 0:24$ .*



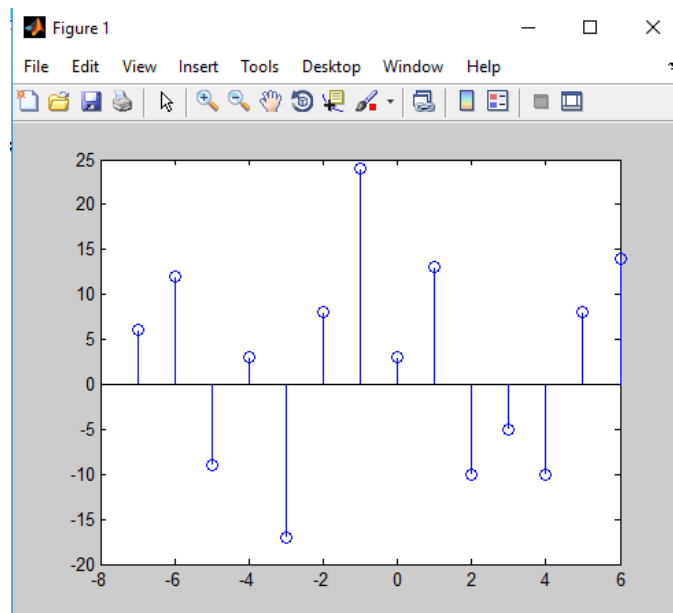
*b-*

```
>> x=[2 4 -3 1 -5 4 7];
>> n=[-3:3];
```

*1) b-Code:*

```
>> [x11,n11]=sigshift(x,n,3);
>> [x12,n12]=sigshift(x,n,-4);
>> [x1,n1]=sigadd(2*x11,n11,3*x12,n12);
>> [x1,n1]=sigadd(x1,n1,-x,n);
>> stem(n1,x1);
```

*Output:*

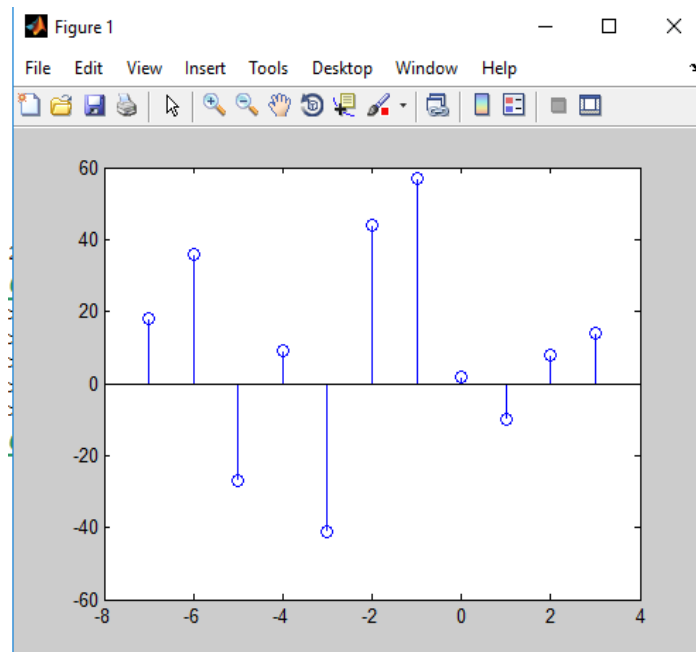


## 2) b-

### Code:

```
>> [x21,n21]=sigshift(x,n,-4);  
>> [x22,n22]=sigshift(x,n,-5);  
>> [x2,n2]=sigadd(4*x11,n11,5*x12,n12);  
>> [x2,n2]=sigadd(x2,n2,2*x,n);  
>> stem(n2,x2);
```

### Output:

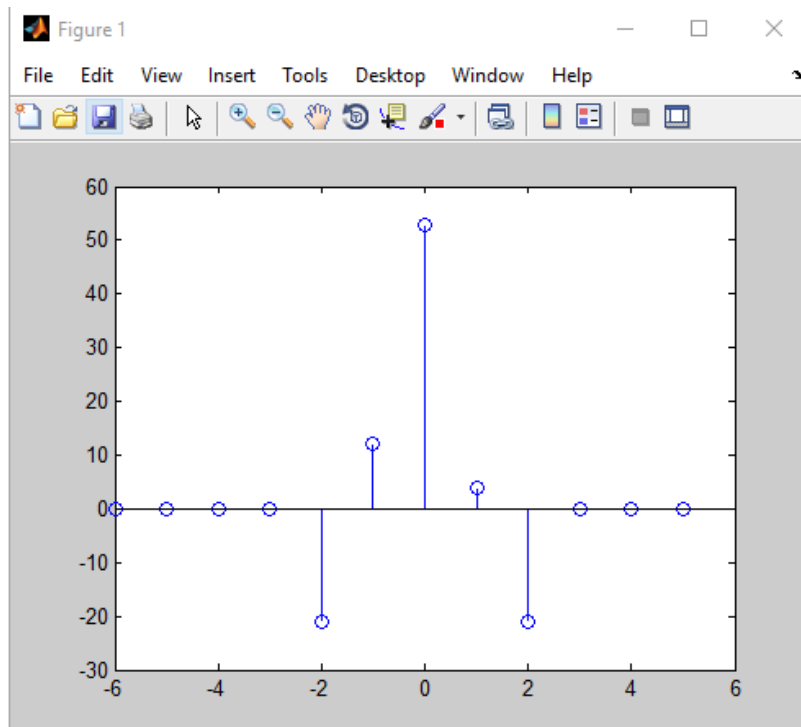


## 3) b-

### Code:

```
>> x=[2 4 -3 1 -5 4 7];  
>> n=[-3:3];  
>> [x31,n31]=sigshift(x,n,-3);  
>> [x32,n32]=sigshift(x,n,2);  
>> [x32,n32]=sigmult(x31,n31,x32,n32);  
>> [x33,n33]=sigfold(x,n);  
>> [x33,n33]=sigshift(x33,n33,1);  
>> [x34,n34]=sigshift(x,n,-1);  
>> [x33,n33]=sigmult(x33,n33,x34,n34);  
>> [x3,n3]=sigadd(x32,n32,x33,n33);  
>> stem(n3,x3);
```

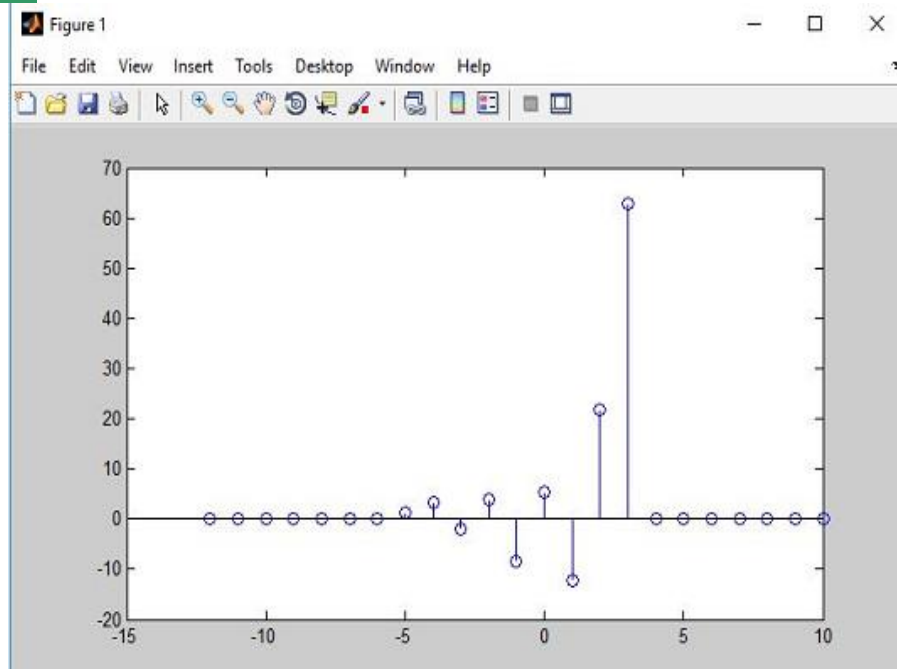
## Output:



## 4) b- Code:

```
>> x=[2 4 -3 1 -5 4 7];  
>> n=[-3:3];  
>> z=zeros(1,7);  
>> xz = horzcat(z,x,z);  
>> nz=[-10:10];  
>> e=2*exp(0.5*nz);  
>> c=cos(0.1*pi*nz);  
>> [x41,n41]=sigshift(xz,nz,-2);  
>> [x4,n4]=sigadd(e.*(xz),nz,c.*(x41),n41);  
>> stem(n4,x4);
```

## Output:



## 2)Time-Domain Analysis of LTI Systems

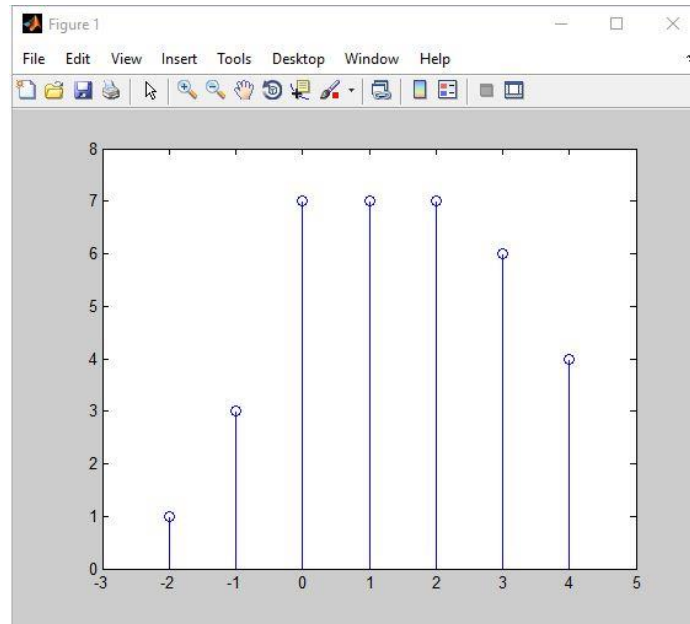
### i-Code:

```
x1=[1,2,4];  
nx=[0:2];  
h1=[ones(1,5)];  
nh=[-2:2];  
[y,ny]=conv_m(x1,nx,h1,nh)  
stem(ny,y)  
axis([min(ny)-1,max(ny)+1,min(y)-1,max(y)+1])
```

### Output:

```
y =  
    1     3     7     7     7     6     4  
  
ny =  
    -2    -1     0     1     2     3     4
```





### ii-Code:

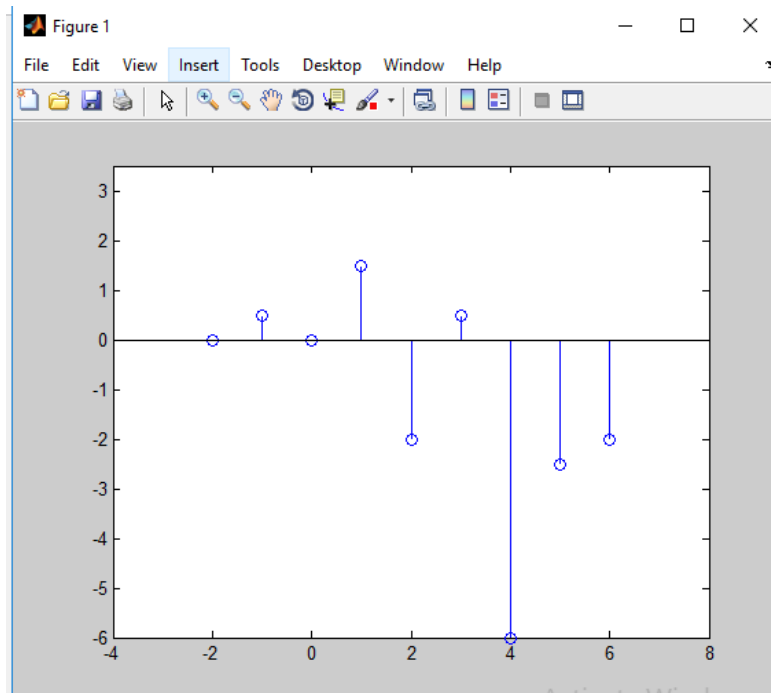
```
>> x2=[0,1,-2,3,-4];
>> nx2=[0:4];
>> h2=[0.5,1,2,1,0.5];
>> nh2=[-2:2];
>> [y2,ny2]=conv_m(x2,nx2,h2,nh2);
```

### Output:

```
y2 =
Columns 1 through 5
    0    0.5000         0    1.5000   -2.0000

Columns 6 through 9
    0.5000   -6.0000   -2.5000   -2.0000

ny2 =
-2    -1     0     1     2     3     4     5     6
```



iii-

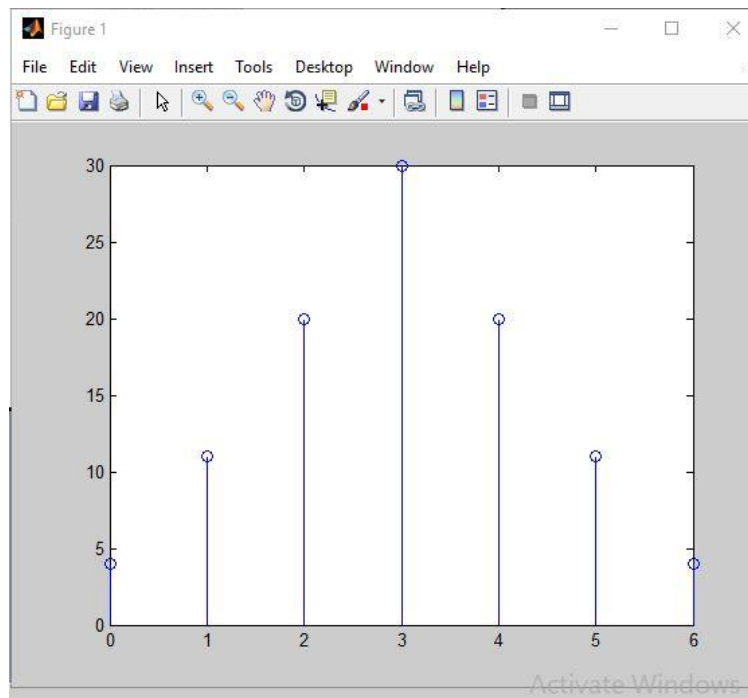
Code:

```
x3=[1,2,3,4];
nx3=[0:3];
h3=[4,3,2,1];
nh3=[0:3];
y3=conv(x3,h3);
ny3=[0:nx3(length(nx3))+nh3(length(nh3))];
stem(ny3,y3);
```

Output:

```
y3 =
     4     11     20     30     20     11     4

ny3 =
     0     1     2     3     4     5     6
```



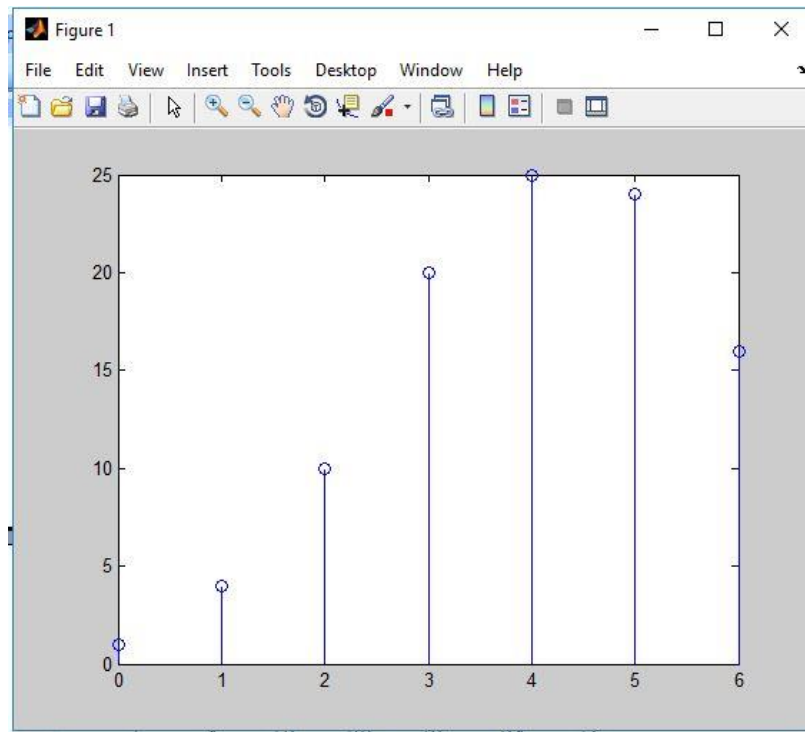
iii-

Code:

```
>> x4=[1,2,3,4];  
>> nx4=[0:3];  
>> h4=[1,2,3,4];  
>> nh4=[0:3];  
>> y4=conv(x4,h4);  
>> stem(ny4,y4);
```

Output:

```
y4 =  
     1     4    10    20    25    24    16  
  
ny4 =  
     0     1     2     3     4     5     6
```



### 3-Z-Transform analysis of discrete-systems

(a)

i.Code:

```
>> num=[1 -2 2 -1];
>> den=[1 -1.7 0.8 -0.1];
>> H=tf(num,den,0.1,'Variable','z^-1')
>> zplane(num,den)
```

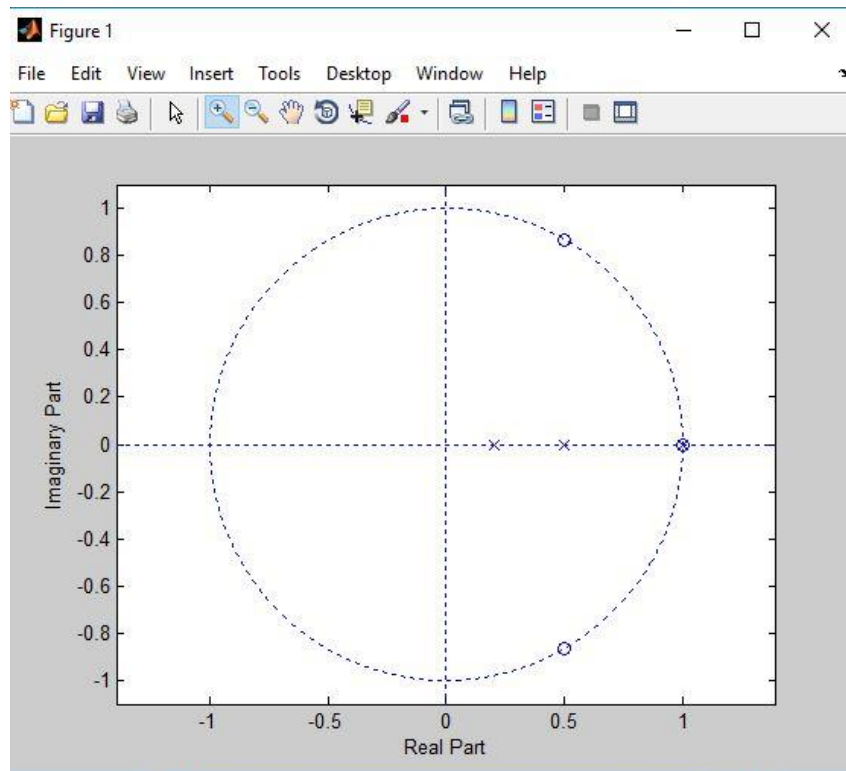
Output:

H =

$$\frac{1 - 2 z^{-1} + 2 z^{-2} - z^{-3}}{1 - 1.7 z^{-1} + 0.8 z^{-2} - 0.1 z^{-3}}$$

Sample time: 0.1 seconds  
Discrete-time transfer function.

*1<sup>st</sup>-Method to check Stability  $\rightarrow$  `zplane(num,den)`*

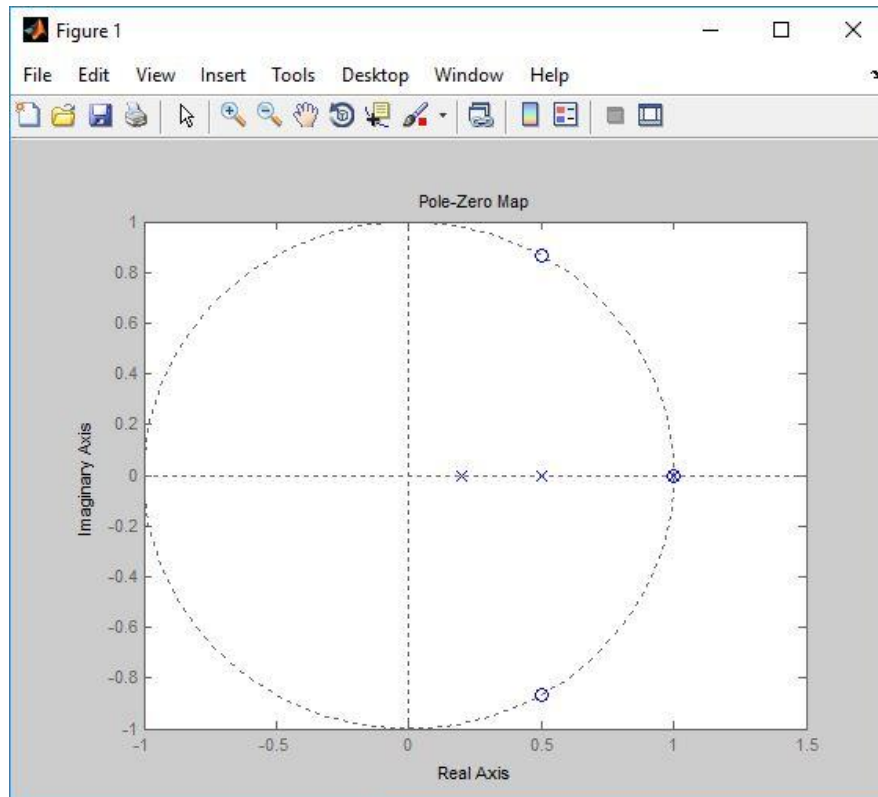


*Marginally Stable  $\rightarrow$  as there is one pole on the unit circle  $|P| = 1$*

*2<sup>nd</sup> Method to check Stability  $\rightarrow$  `[p,z]=pzmap(H)`*

**Code :** `>> [p, z]=pzmap (H)`

Output:



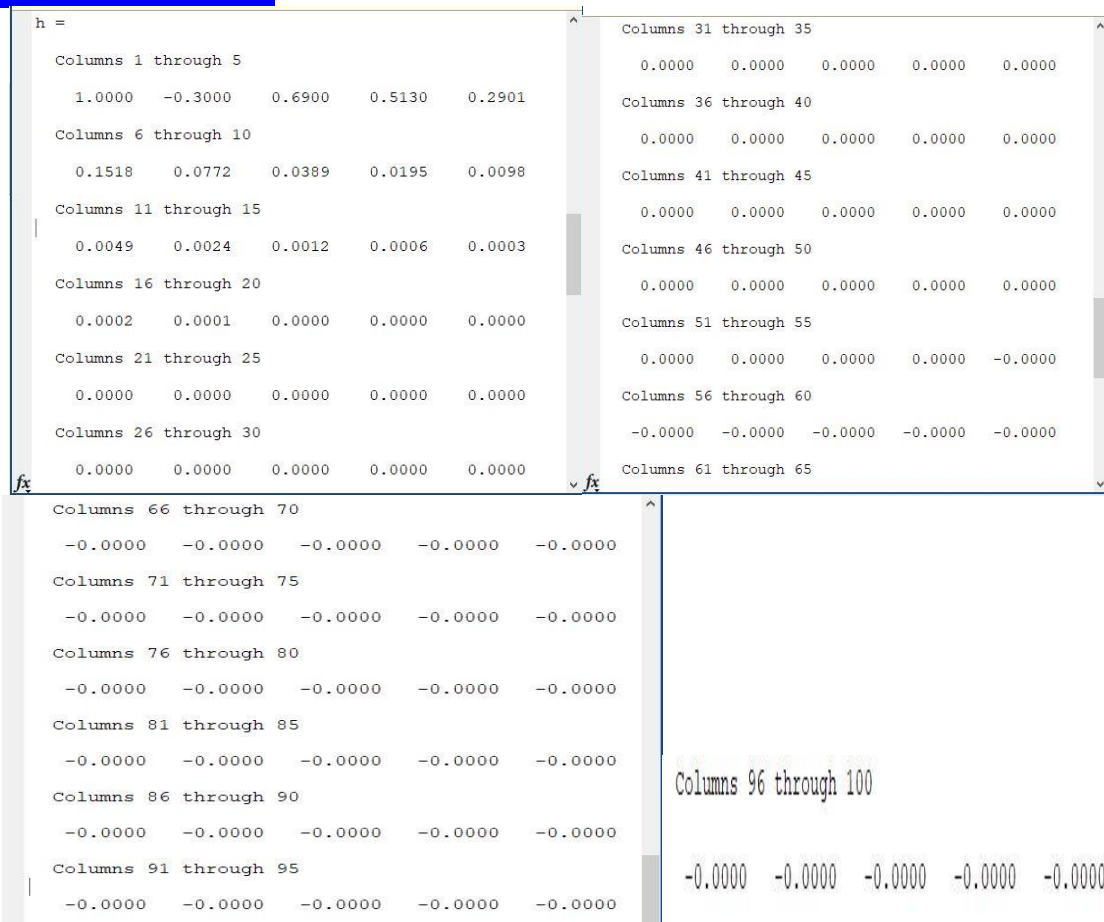
Marginally Stable  $\rightarrow$  as there is one pole on the unit circle  $|P| = 1$

```
p =  
    1.0000  
    0.5000  
    0.2000  
  
z =  
    1.0000 + 0.0000i  
    0.5000 + 0.8660i  
    0.5000 - 0.8660i  
  
>> abs(p)  
  
ans =  
    1.0000  
    0.5000  
    0.2000
```

## ii-Impulse Response

Code: `>> h=filter(num,den,[1 zeros(1,N-1)])`

Output:



(b).Code:

```
>> num=[0.03 -0.02 0.01];  
>> den=[1 -2.8 3.02 -1.468 0.27];  
>> H=tf(num,den,0.1,'Variable','z^-1')
```

Output:

H =

$$\frac{0.03 - 0.02 z^{-1} + 0.01 z^{-2}}{1 - 2.8 z^{-1} + 3.02 z^{-2} - 1.468 z^{-3} + 0.27 z^{-4}}$$

Sample time: 0.1 seconds  
Discrete-time transfer function.

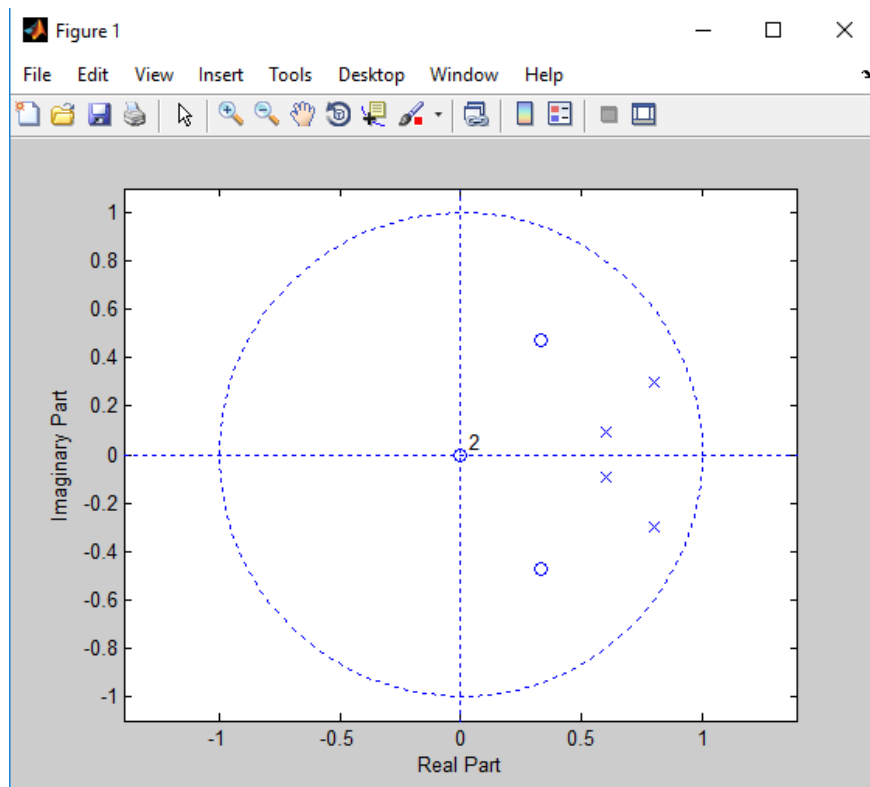
Discussing Stability:

Code:

>> zplane(num,den)

[p,z]=pzmap(H)

Output:



Stable System since all the poles lies inside the unit circle.  **$|P| < 1$**

```
>> zplane(num,den)
>> [p,z]=pzmap(H)

p =

    0.7988 + 0.3004i
    0.7988 - 0.3004i
    0.6012 + 0.0962i
    0.6012 - 0.0962i

z =

    0.0000 + 0.0000i
    0.0000 + 0.0000i
    0.3333 + 0.4714i
    0.3333 - 0.4714i

>> abs(p)

ans =

    0.8534
    0.8534
    0.6089
    0.6089
```



Code : "  $x(n)=5u(n)$  "

```
>> N=100;  
>> x=5*ones(1,N)  
>> y=filter(num,den,x)
```

Output :

```
y =  
Columns 1 through 6  
0.1500    0.4700    0.9630    1.5972    2.3134    3.0406  
Columns 7 through 12  
3.7121    4.2760    4.7012    4.9784    5.1165    5.1386  
Columns 13 through 18  
5.0750    4.9584    4.8190    4.6814    4.5634    4.4751  
Columns 19 through 24  
4.4200    4.3963    4.3986    4.4195    4.4512    4.4866  
Columns 25 through 30  
4.5201    4.5478    4.5677    4.5793    4.5833    4.5812  
Columns 31 through 36  
4.5751    4.5667    4.5579    4.5498    4.5433    4.5389  
Columns 37 through 42  
4.5365    4.5360    4.5368    4.5386    4.5407    4.5429  
Columns 43 through 48  
4.5448    4.5463    4.5473    4.5478    4.5478    4.5475  
Columns 49 through 54  
4.5470    4.5465    4.5460    4.5455    4.5452    4.5449  
Columns 55 through 60  
4.5449    4.5449    4.5450    4.5451    4.5452    4.5454  
Columns 61 through 66  
4.5455    4.5455    4.5456    4.5456    4.5456    4.5456  
Columns 67 through 72  
4.5455    4.5455    4.5455    4.5454    4.5454    4.5454  
Columns 73 through 78  
4.5454    4.5454    4.5454    4.5454    4.5454    4.5455  
Columns 79 through 84  
4.5455    4.5455    4.5455    4.5455    4.5455    4.5455  
Columns 85 through 90  
4.5455    4.5455    4.5455    4.5455    4.5455    4.5455  
Columns 91 through 96  
4.5455    4.5455    4.5455    4.5455    4.5455    4.5455  
Columns 97 through 100  
4.5455    4.5455    4.5455    4.5455
```

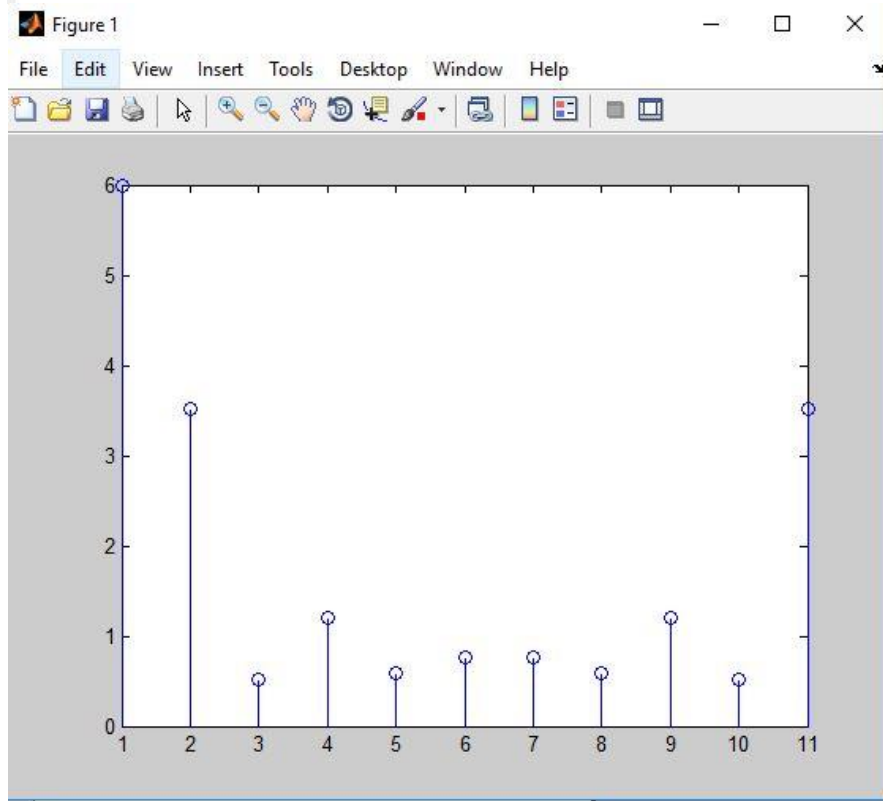
## (4) Fourier-transform analysis of discrete systems

a. Code :

```
na=[0:10];  
xa=stepseq(0,0,10)-stepseq(6,0,10);  
xa=fft(xa);  
xaMag=abs(xa);  
stem(xaMag);  
xaPhase=angle(xa);  
stem(xaPhase);
```

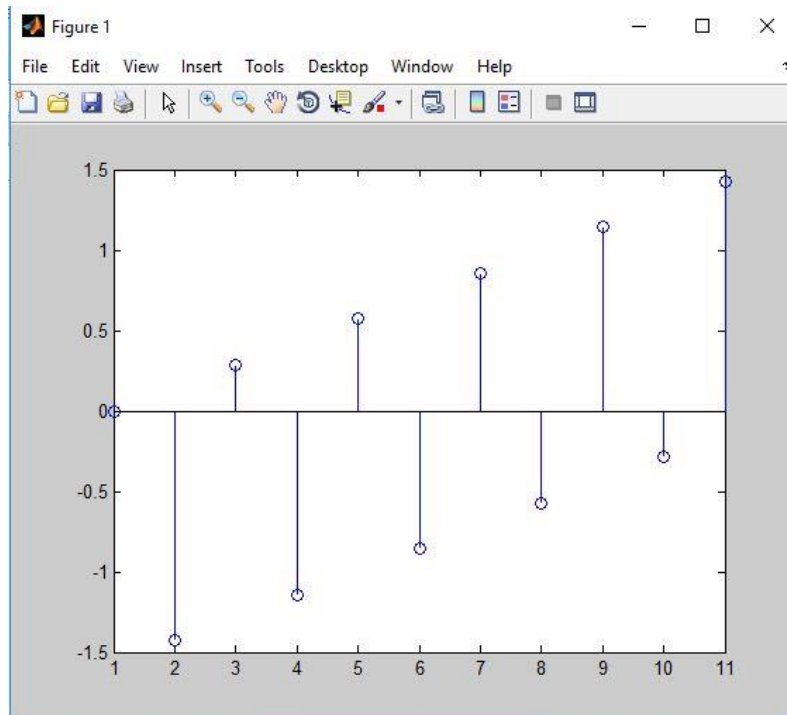
## Output: Magnitude:

```
xaMag =  
  
Columns 1 through 6  
    6.0000    3.5133    0.5211    1.2036    0.5944    0.7635  
  
Columns 7 through 11  
    0.7635    0.5944    1.2036    0.5211    3.5133
```



## Phase:

```
xaPhase =  
  
Columns 1 through 6  
    0    -1.4280    0.2856   -1.1424    0.5712   -0.8568  
  
Columns 7 through 11  
    0.8568   -0.5712    1.1424   -0.2856    1.4280
```



## b-Code:

```
>> nb=[0:10];
>> cb=2.^nb;
>> xb=stepseq(0,0,10);
>> [xb,nb]=sigfold(cb.^(xb),nb);
>> xbF=fft(xb);
>> xbMag=abs(xbF);
>> xbPhase=phase(xbF);
```

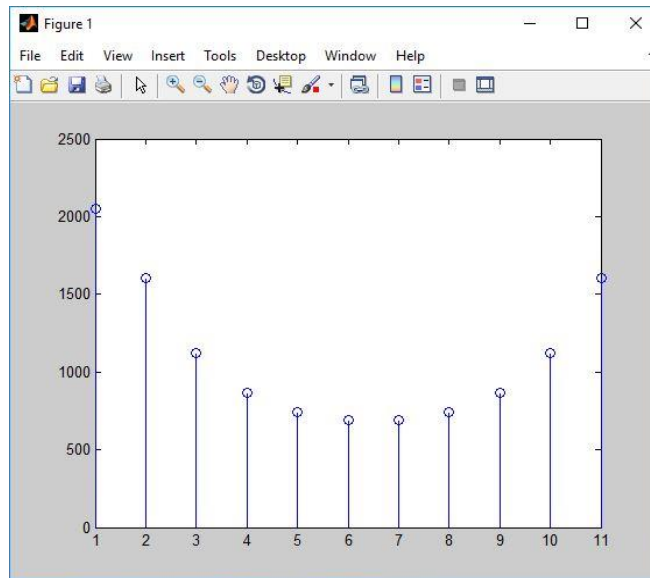
## Output:

### Magnitude:

xbMag =

1.0e+03 \*

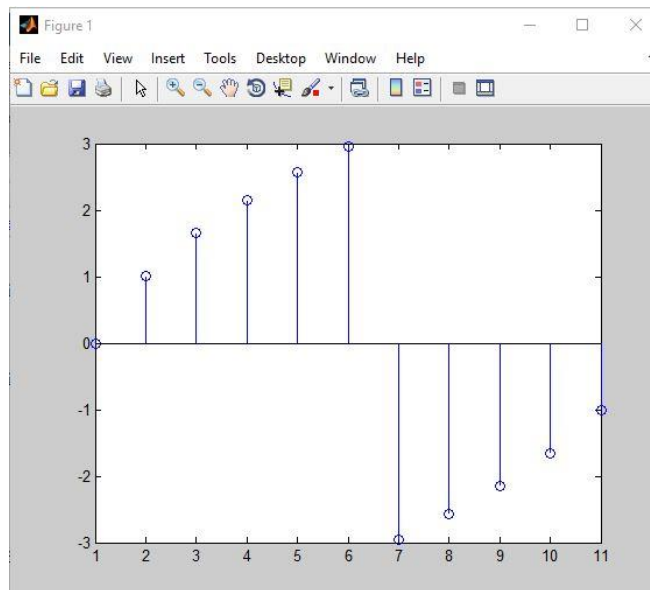
2.0470 1.6009 1.1203 0.8674 0.7416 0.6886 0.6886 0.7416 0.8674 1.1203 1.6009



## Phase:

xbPhase =

0 1.0077 1.6635 2.1464 2.5621 2.9509 -2.9509 -2.5621 -2.1464 -1.6635 -1.0077



## c-Code:

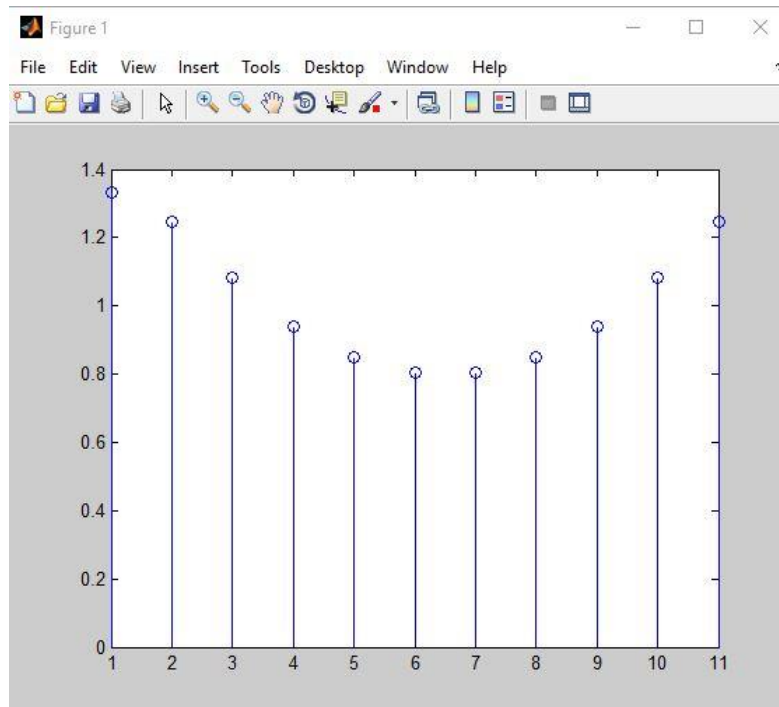
```
>> nc=[0:10];
>> cc=(1/4).^nc;
>> xc=stepseq(0,0,10);
>> xc=cc.^xc;
>> xcF=fft(xc);
>> stem(xcPhase);
>> stem(xcMag);
```

## Output:

## Magnitude:

xcMag =

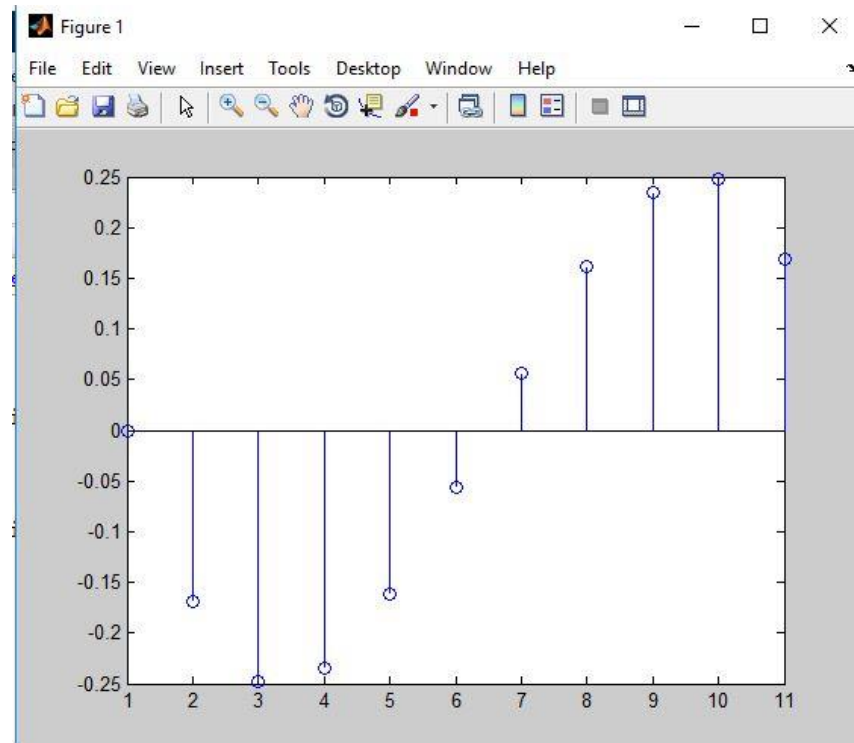
1.3333 1.2482 1.0816 0.9392 0.8482 0.8052 0.8052 0.8482 0.9392 1.0816 1.2482



## Phase:

xcPhase =

0 -0.1695 -0.2485 -0.2346 -0.1610 -0.0567 0.0567 0.1610 0.2346 0.2485 0.1695



## d-Code:

```
nd=[0:10];
cd= (0.25).^nd;
cs=cd.*sin(2*pi*0.25*nd);
xd=stepseq(0,0,10);
xd=cs.^xd;
xdF=fft(xd);
xdMag=abs(xdF);
xdPhase=phase(xdF);
```

## Output:

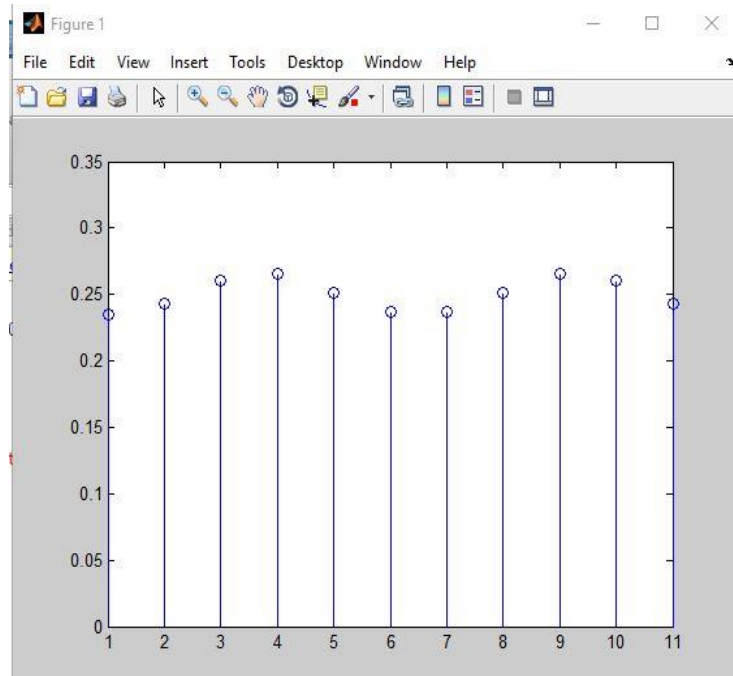
### Magnitude

Columns 1 through 6

```
0.2353    0.2433    0.2604    0.2659    0.2518    0.2374
```

Columns 7 through 11

```
0.2374    0.2518    0.2659    0.2604    0.2433
```



## Phase:

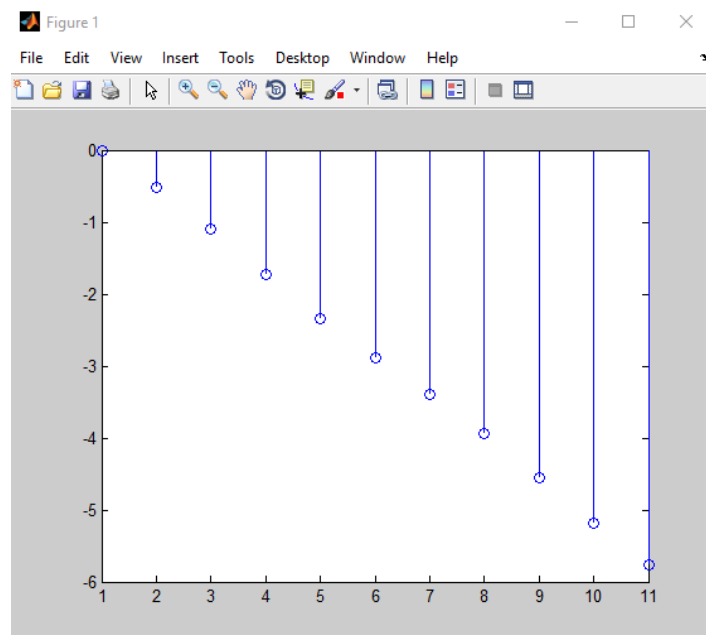
xdPhase =

Columns 1 through 6

0   -0.5158   -1.0932   -1.7323   -2.3471   -2.8881

Columns 7 through 11

-3.3951   -3.9361   -4.5509   -5.1900   -5.7673



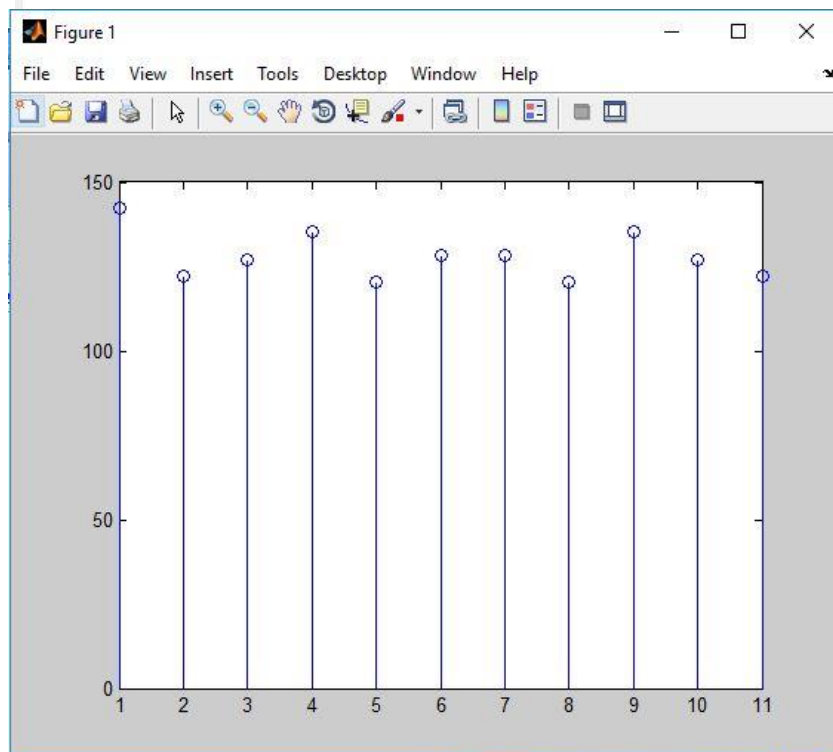
## e-Code:

```
>> ne=[0:10];  
>> ce=(0.5).^ne;  
>> xe=sin(2*pi*0.25*ne) ;  
>> xe=ce.^xe;  
>> xeF=fft(xe) ;  
>> xeMag=abs(xeF) ;  
>> xePhase=angle(xeF) ;  
>> stem(xeMag) ;  
>> stem(xePhase) ;
```

## Output:

### Magnitude:

```
xeMag =  
  
Columns 1 through 6  
142.5332 122.2006 127.0740 135.1672 120.3649 128.4595  
  
Columns 7 through 11  
128.4595 120.3649 135.1672 127.0740 122.2006
```





## Phase:

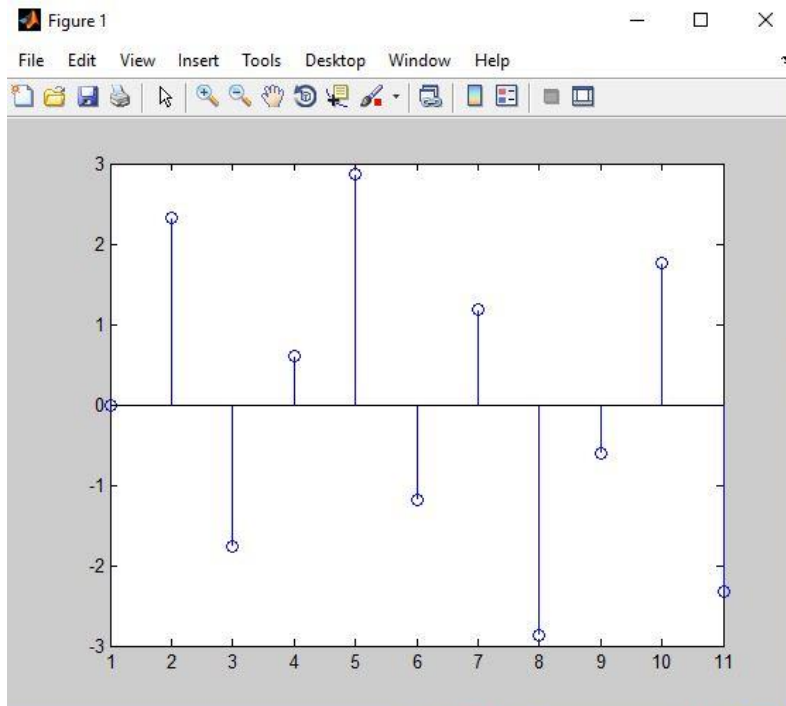
```
xePhase =
```

```
Columns 1 through 6
```

```
0    2.3295   -1.7701    0.6019    2.8684   -1.1883
```

```
Columns 7 through 11
```

```
1.1883   -2.8684   -0.6019    1.7701   -2.3295
```



## f-Code:

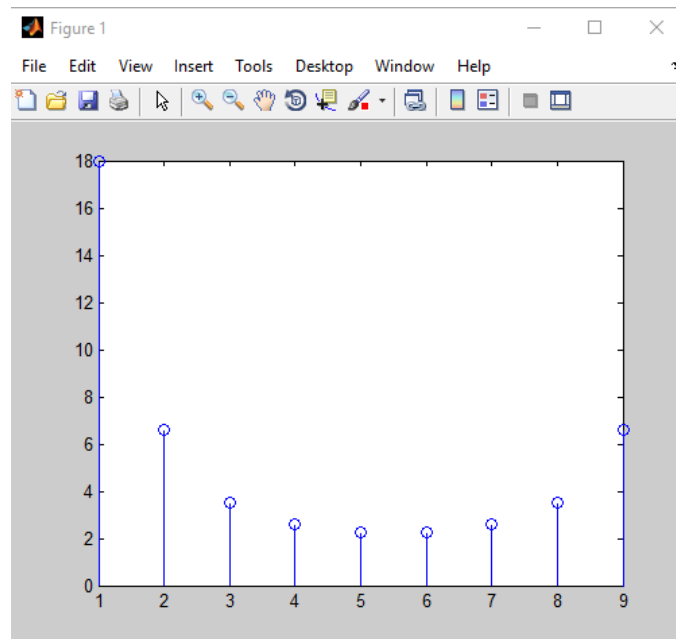
```
>> nf=[-4:4];  
>> xf=2-(0.5*nf);  
>> xfF=fft(xf);  
>> xfMag=abs(xf);  
>> xfMag=abs(xfF);  
>> xfPhase=phase(xfF);  
>> stem(xfMag);
```

## Output:

## Magnitude:

xfMag =

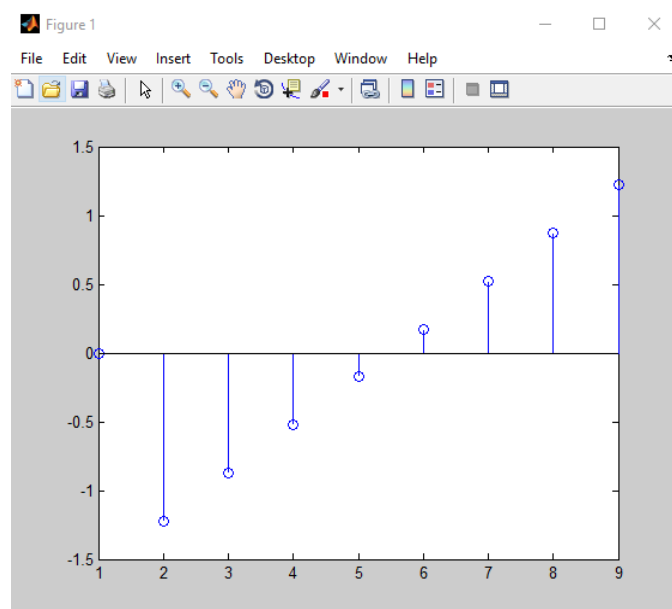
18.0000    6.5786    3.5004    2.5981    2.2847    2.2847    2.5981    3.5004    6.5786



## Phase:

xfPhase =

0   -1.2217   -0.8727   -0.5236   -0.1745    0.1745    0.5236    0.8727    1.2217



g.

Code:

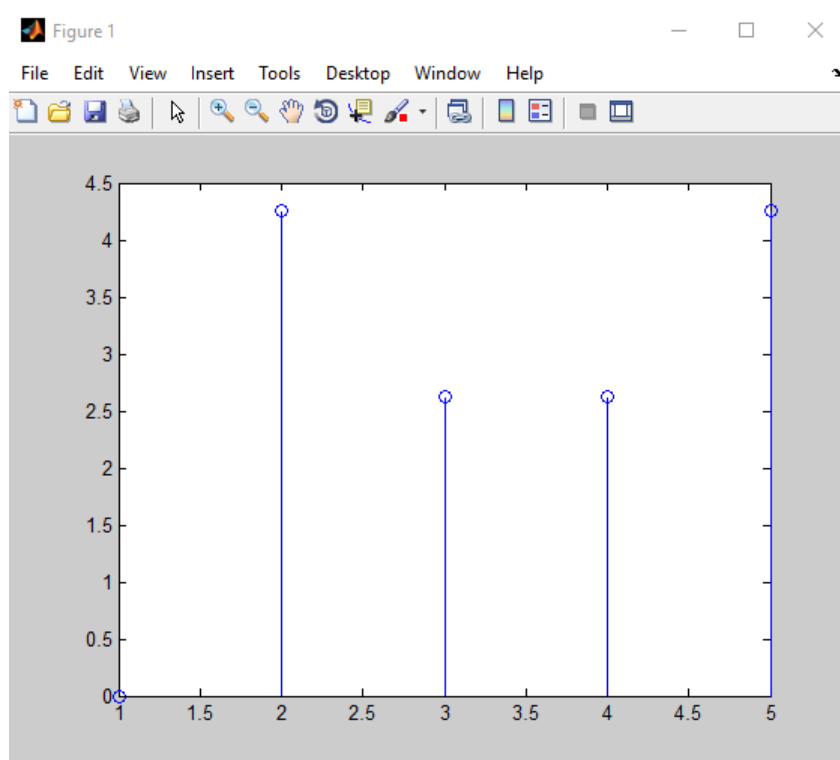
```
>> ng=[-2:2];  
>> xg=[-2 -1 0 1 2];  
>> xgF=fft(xg);  
>> xgMag=abs(xgF);  
>> xgPhase=phase(xgF);  
>> stem(xgMag);  
>> stem(xgPhase);
```

Output:

Magnitude:

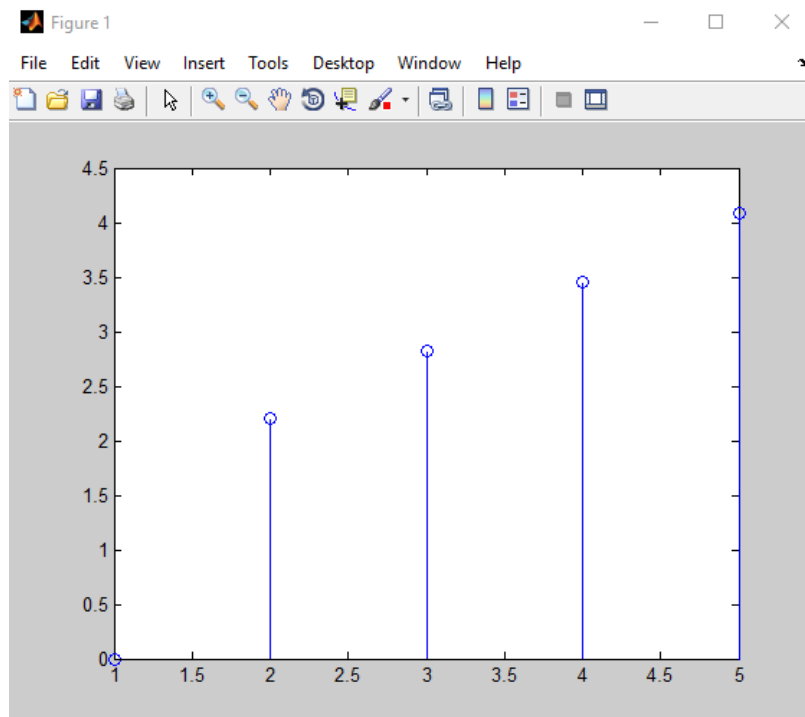
xgMag =

0      4.2533      2.6287      2.6287      4.2533

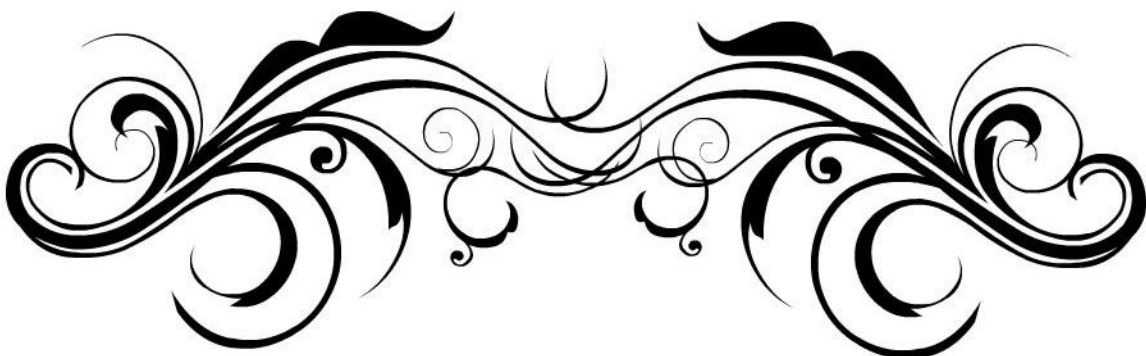


## Phase:

```
xgPhase =  
0      2.1991      2.8274      3.4558      4.0841
```



# End of Report



*DSP Final MATLAB Project*