

A.A. 2021-2022

Elementi di Elettronica (INF)

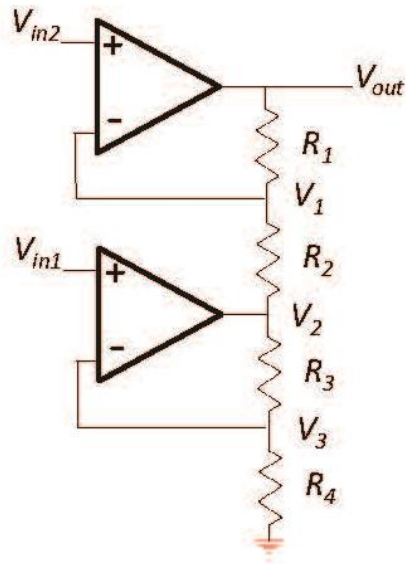
Prof. Paolo Crippa

Esercizi – P2

Esercizi su Circuiti con Amplificatori Operazionali da compiti del:

14 Gennaio 2014
4 Febbraio 2014
17 Giugno 2014
20 Luglio 2014
16 Settembre 2014
3 Febbraio 2015
17 Aprile 2015
17 Gennaio 2016

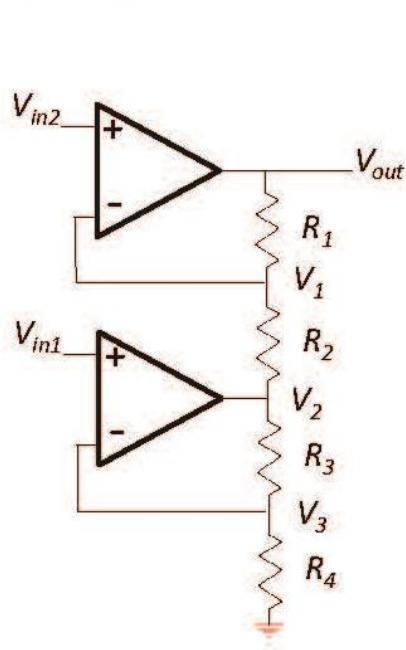
- . Dato il circuito ($V_{in1} = 1 \text{ V}$, $V_{in2} = 3 \text{ V}$, $R_1 = 1 \text{ k}\Omega$, $R_2 = 2 \text{ k}\Omega$, $R_3 = 3 \text{ k}\Omega$, $R_4 = 4 \text{ k}\Omega$), determinare:
i) l'espressione simbolica che lega V_{out} a V_{in1} e V_{in2} ; ii) i valori numerici indicati.



$$V_{out} =$$

V_1	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
V_2	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
V_3	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
V_{out}	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V

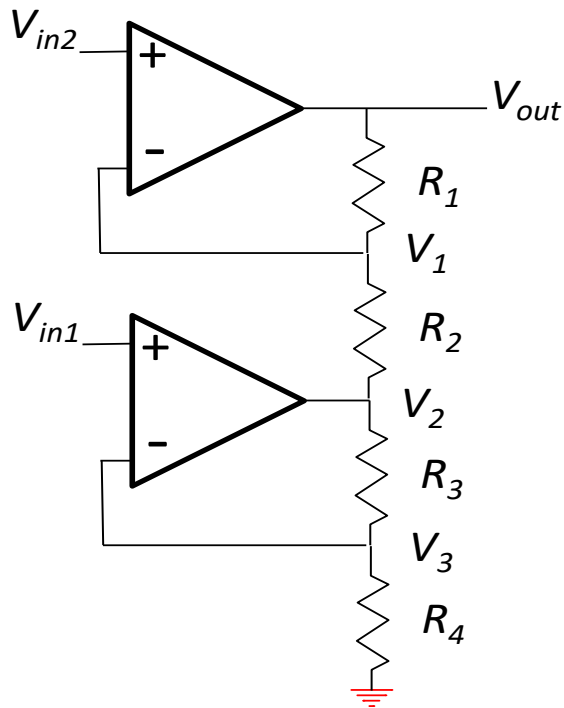
- . Dato il circuito ($V_{in1} = 1 \text{ V}$, $V_{in2} = 3 \text{ V}$, $R_1 = 1 \text{ k}\Omega$, $R_2 = 2 \text{ k}\Omega$, $R_3 = 3 \text{ k}\Omega$, $R_4 = 4 \text{ k}\Omega$), determinare:
i) l'espressione simbolica che lega V_{out} a V_{in1} e V_{in2} ; ii) i valori numerici indicati.



$$V_{out} = V_{in2} \left(1 + \frac{R_1}{R_2} \right) - V_{in1} \left(1 + \frac{R_3}{R_4} \right) \frac{R_1}{R_2}$$

V_1	=	+				3	.	0	0	0	V
V_2	=	+				1	.	7	5	0	V
V_3	=	+				1	.	0	0	0	V
V_{out}	=	+				2	.	1	2	5	V

Soluzione :



$$V_1 = V_{in2} = 3 \text{ V}; \quad V_3 = V_{in1} = 1 \text{ V}$$

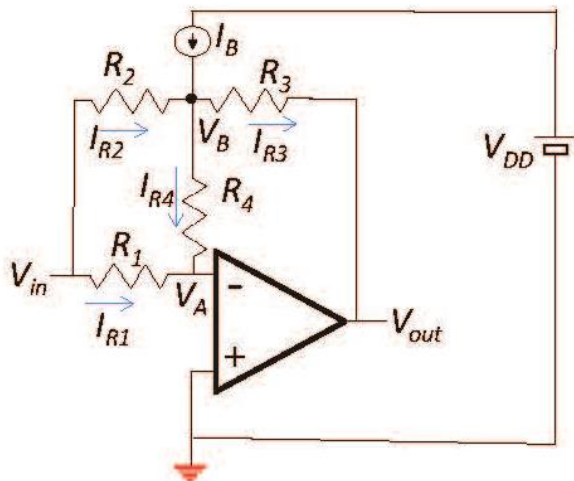
$$\frac{V_{out} - V_1}{R_1} = \frac{V_1 - V_2}{R_2} \quad ; \quad \frac{V_2 - V_3}{R_3} = \frac{V_3}{R_4}$$

$$V_2 = V_{in1} \frac{R_3 + R_4}{R_4} = 1.75 \text{ V}$$

$$\begin{aligned} V_{out} &= V_{in2} \frac{R_1 + R_2}{R_2} - V_{in1} \frac{R_3 + R_4}{R_4} \frac{R_1}{R_2} = \\ &= 3 \frac{1+2}{2} - 1 \frac{3+4}{4} \frac{1}{2} = 2.125 \text{ V} \end{aligned}$$

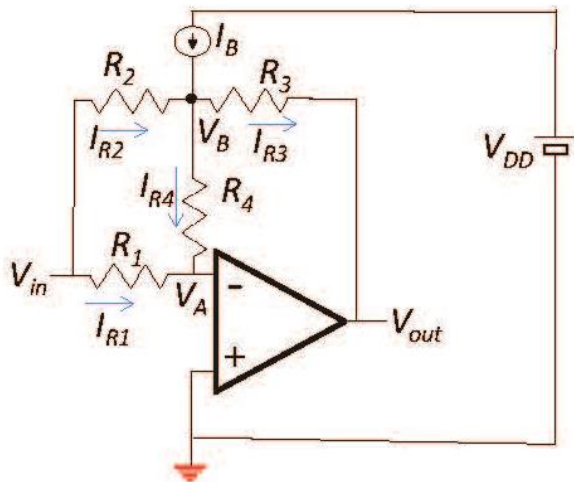
Dato il circuito ($V_{in} = 1\text{ V}$, $I_B = 1\text{ mA}$, $R_1 = 1\text{ k}\Omega$, $R_2 = 2\text{ k}\Omega$, $R_3 = 2\text{ k}\Omega$, $R_4 = 1\text{ k}\Omega$), determinare:
i) l'espressione simbolica che lega V_{out} a V_{in} ; ii) i valori numerici delle grandezze indicate.

$$V_{out} =$$



V_A	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
V_B	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
I_{R1}	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	mA
I_{R2}	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	mA
I_{R3}	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	mA
I_{R4}	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	mA
V_{out}	=	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V

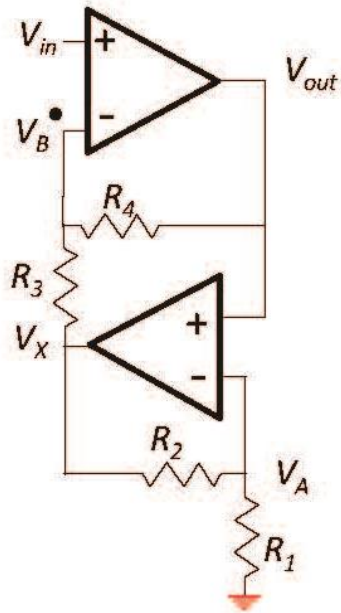
Dato il circuito ($V_{in} = 1\text{ V}$, $I_B = 1\text{ mA}$, $R_1 = 1\text{ k}\Omega$, $R_2 = 2\text{ k}\Omega$, $R_3 = 2\text{ k}\Omega$, $R_4 = 1\text{ k}\Omega$), determinare:
i) l'espressione simbolica che lega V_{out} a V_{in} ; ii) i valori numerici delle grandezze indicate.



$$V_{out} = -R_3 I_B - V_{in} R_3 \left(\frac{1}{R_2} + \frac{R_4}{R_1 R_2} + \frac{R_4}{R_1 R_3} + \frac{1}{R_1} \right)$$

V_A	=				0	.	0	0	0	V
V_B	=	-			1	.	0	0	0	V
I_{R1}	=	+			1	.	0	0	0	mA
I_{R2}	=	+			1	.	0	0	0	mA
I_{R3}	=	+			3	.	0	0	0	mA
I_{R4}	=	-			1	.	0	0	0	mA
V_{out}	=	-			7	.	0	0	0	V

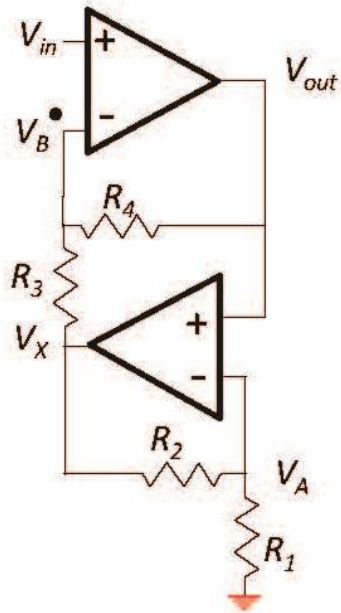
Dato il circuito ($V_{in} = 3\text{ V}$, $R_1 = 1\text{ k}\Omega$, $R_2 = 2\text{ k}\Omega$, $R_3 = 2\text{ k}\Omega$, $R_4 = 4\text{ k}\Omega$), determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori di V_A , V_B , V_X , V_{out} .



$$V_{out} =$$

$$\begin{array}{lcl} V_A & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \text{ V} \\ V_B & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \text{ V} \\ V_X & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \text{ V} \\ V_{out} & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \text{ V} \end{array}$$

Dato il circuito ($V_{in} = 3 \text{ V}$, $R_1 = 1 \text{ k}\Omega$, $R_2 = 2 \text{ k}\Omega$, $R_3 = 2 \text{ k}\Omega$, $R_4 = 4 \text{ k}\Omega$), determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori di V_A , V_B , V_X , V_{out} .

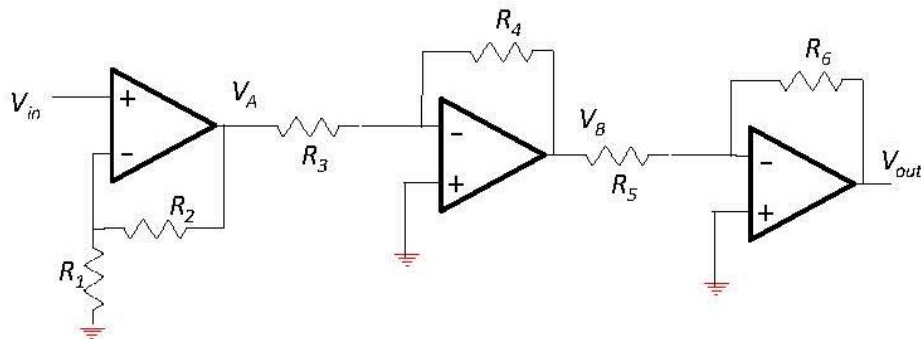


$$V_{out} = V_{in} \frac{R_3 + R_4}{R_3 + R_4 \left(1 + \frac{R_2}{R_1} \right)}$$

V_A	=	+				1	.	2	8	6	V
V_B	=	+				3	.	0	0	0	V
V_X	=	+				3	.	8	5	7	V
V_{out}	=	+				1	.	2	8	6	V

Dato il circuito in figura ($V_{in} = 1\text{ V}$, $R_1 = R_3 = R_5 = 10\text{ k}\Omega$, $R_2 = R_4 = R_6 = 20\text{ k}\Omega$), determinare:
i) i valori di V_A , V_B , V_{out} ; ii) l'espressione simbolica che lega V_{out} a V_{in} .

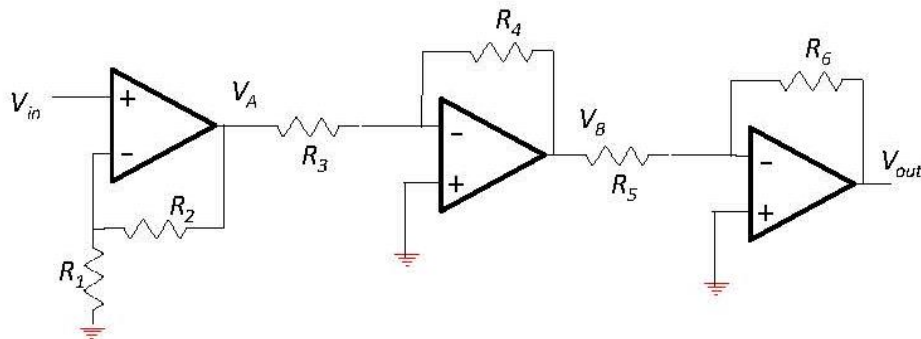
$$V_{out} =$$



$$\begin{array}{lcl} V_A & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \cdot \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \\ V_B & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \cdot \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \\ V_{out} & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \cdot \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \end{array}$$

Dato il circuito in figura ($V_{in} = 1 \text{ V}$, $R_1 = R_3 = R_5 = 10 \text{ k}\Omega$, $R_2 = R_4 = R_6 = 20 \text{ k}\Omega$), determinare:
i) i valori di V_A , V_B , V_{out} ; ii) l'espressione simbolica che lega V_{out} a V_{in} .

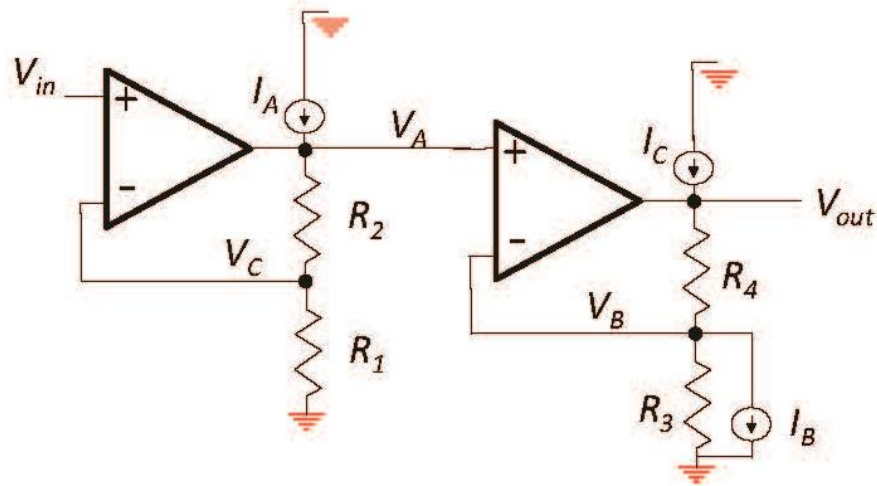
$$V_{out} = V_{in} \left(1 + \frac{R_2}{R_1} \right) \frac{R_4}{R_3} \frac{R_6}{R_5}$$



$$\begin{array}{lcl} V_A & = & + \begin{array}{|c|c|c|c|} \hline & & & 3 \\ \hline \end{array} \cdot \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & \\ \hline \end{array} \text{ V} \\ V_B & = & - \begin{array}{|c|c|c|c|} \hline & & & 6 \\ \hline \end{array} \cdot \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & \\ \hline \end{array} \text{ V} \\ V_{out} & = & + \begin{array}{|c|c|c|c|} \hline & & 1 & 2 \\ \hline \end{array} \cdot \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & \\ \hline \end{array} \text{ V} \end{array}$$

Dato il circuito in figura ($V_{in} = 1\text{ V}$, $I_A = I_B = I_C = 500\text{ }\mu\text{A}$, $R_1 = R_2 = R_3 = R_4 = 1\text{ k}\Omega$),
determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori di V_A , V_B , V_C , V_{out} .

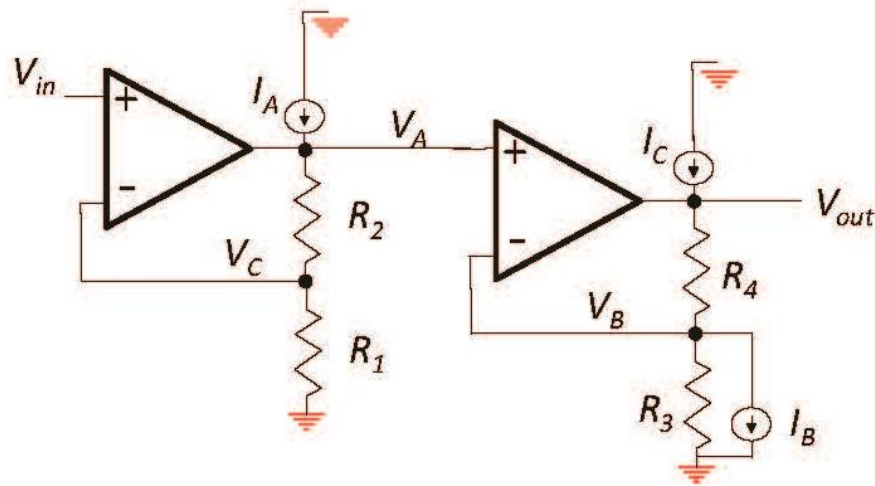
$$V_{out} =$$



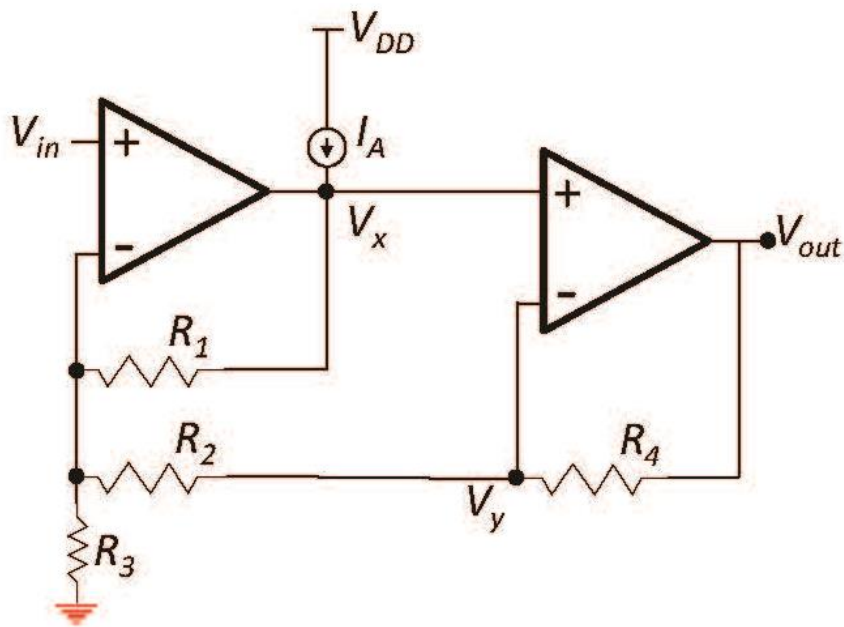
$$\begin{array}{lcl} V_A & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \\ V_B & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \\ V_C & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \\ V_{out} & = & \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} . \boxed{} \boxed{} \boxed{} \boxed{} \boxed{} \text{ V} \end{array}$$

Dato il circuito in figura ($V_{in} = 1\text{ V}$, $I_A = I_B = I_C = 500\text{ }\mu\text{A}$, $R_1 = R_2 = R_3 = R_4 = 1\text{ k}\Omega$),
determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori di V_A , V_B , V_C , V_{out} .

$$V_{out} = V_{in} \left(1 + \frac{R_2}{R_1} \right) \left(1 + \frac{R_4}{R_3} \right) + R_4 I_B$$



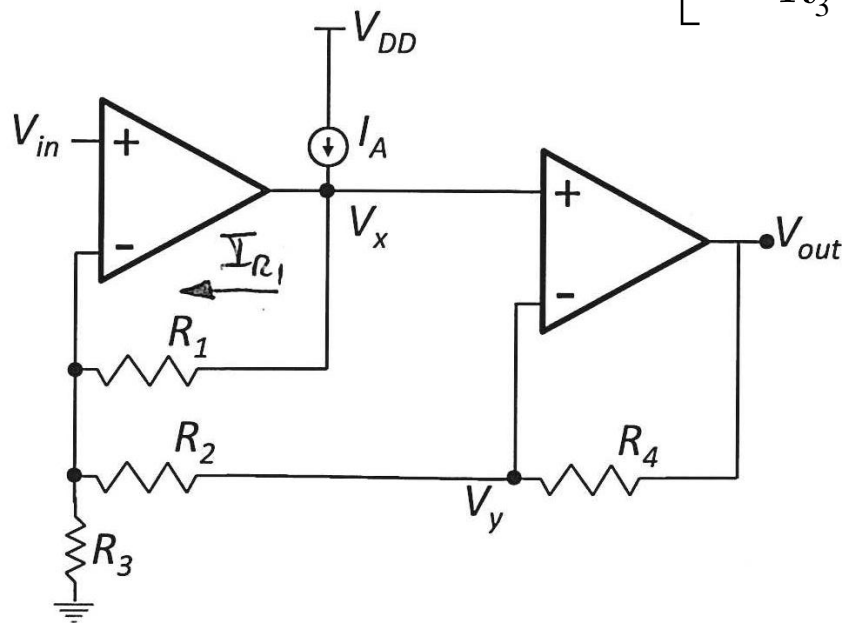
V_A	=	+				2	.	0	0	0	V
V_B	=	+				2	.	0	0	0	V
V_C	=	+				1	.	0	0	0	V
V_{out}	=	+				4	.	5	0	0	V

$$V_{\text{out}} =$$


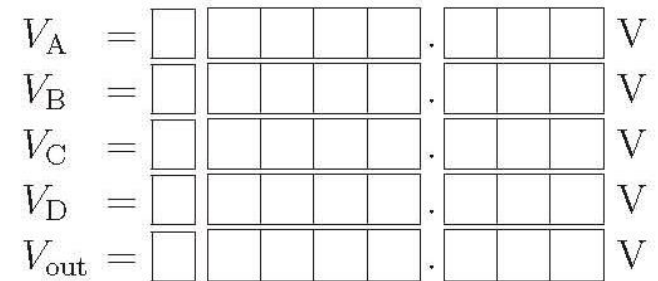
I_{R1}	=	<div style="border: 1px solid black; width: 30px; height: 30px; display: inline-block;"></div>	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	.	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	μA
V_x	=	<div style="border: 1px solid black; width: 30px; height: 30px; display: inline-block;"></div>	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	.	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	V
V_y	=	<div style="border: 1px solid black; width: 30px; height: 30px; display: inline-block;"></div>	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	.	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	V
V_{out}	=	<div style="border: 1px solid black; width: 30px; height: 30px; display: inline-block;"></div>	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	.	<div style="border: 1px solid black; width: 60px; height: 30px; display: inline-block;"></div>	V

Dato il circuito in figura ($V_{DD} = 5\text{ V}$, $V_{in} = 1\text{ V}$, $I_A = 100\text{ }\mu\text{A}$, $R_1 = 10\text{ k}\Omega$, $R_2 = 4\text{ k}\Omega$, $R_3 = 4\text{ k}\Omega$, $R_4 = 2\text{ k}\Omega$), determinare: i) l'espressione simbolica che lega V_{out} a V_{in} ; ii) i valori numerici indicati.

$$V_{out} = \left[1 + \frac{R_1 (R_2 + R_4)}{R_3 (R_1 + R_2)} \right] V_{in}$$

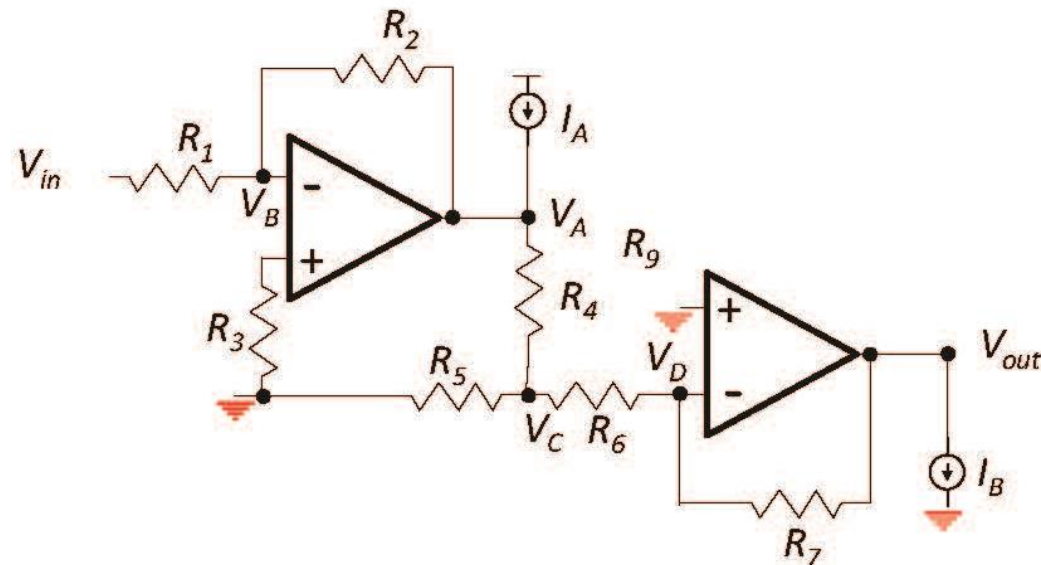


I_{R1}	=	+				71	.	4			μA
V_x	=	+				1	.	714			V
V_y	=	+				1	.	714			V
V_{out}	=	+				2	.	071			V

$$V_{\text{out}} =$$


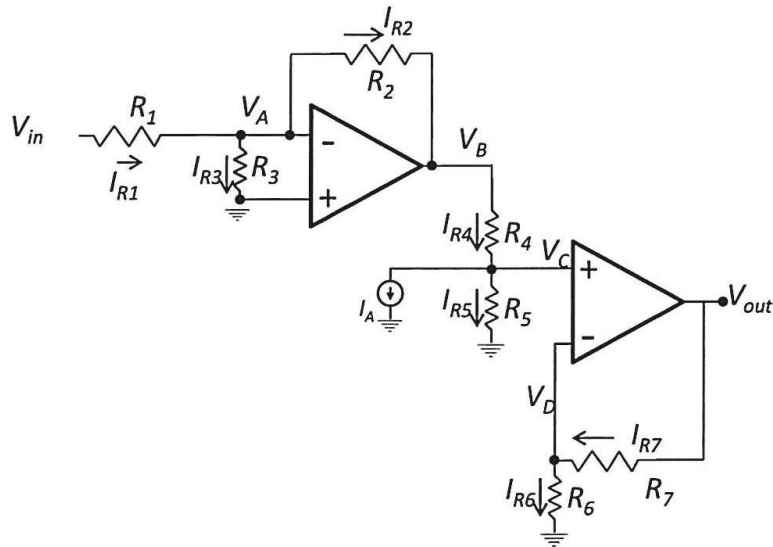
Dato il circuito in figura ($V_{in} = 2\text{ V}$, $I_A = I_B = 500\text{ }\mu\text{A}$, $R_1 = 1\text{ k}\Omega$, $R_2 = R_3 = 2\text{ k}\Omega$, $R_4 = R_5 = R_6 = 1\text{ k}\Omega$, $R_7 = 2\text{ k}\Omega$), determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori numerici indicati.

$$V_{out} = V_{in} \frac{R_2 R_7}{R_1 R_4 R_6} \left(\frac{1}{R_4} + \frac{1}{R_5} + \frac{1}{R_6} \right)^{-1} = V_{in} \frac{R_2 R_5 R_7}{R_1 (R_4 R_5 + R_4 R_6 + R_5 R_6)}$$



V_A	=	-				4	.	0	0	0	V
V_B	=					0	.	0	0	0	V
V_C	=	-				1	.	3	3	3	V
V_D	=					0	.	0	0	0	V
V_{out}	=	+				2	.	6	6	6	V

4. Dato il circuito in figura ($V_{in} = 1\text{ V}$, $R_1 = 1\text{ k}\Omega$, $R_2 = 2\text{ k}\Omega$, $R_3 = 1\text{ k}\Omega$, $R_4 = 2\text{ k}\Omega$, $R_5 = 2\text{ k}\Omega$, $R_6 = 1\text{ k}\Omega$, $R_7 = 4\text{ k}\Omega$, $I_A = 600\text{ }\mu\text{A}$), determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori numerici indicati.



$$I_{R1} =$$

$$I_{R2} =$$

$$I_{R4} =$$

$$I_{R5} =$$

$$I_{R7} =$$

$$V_A =$$

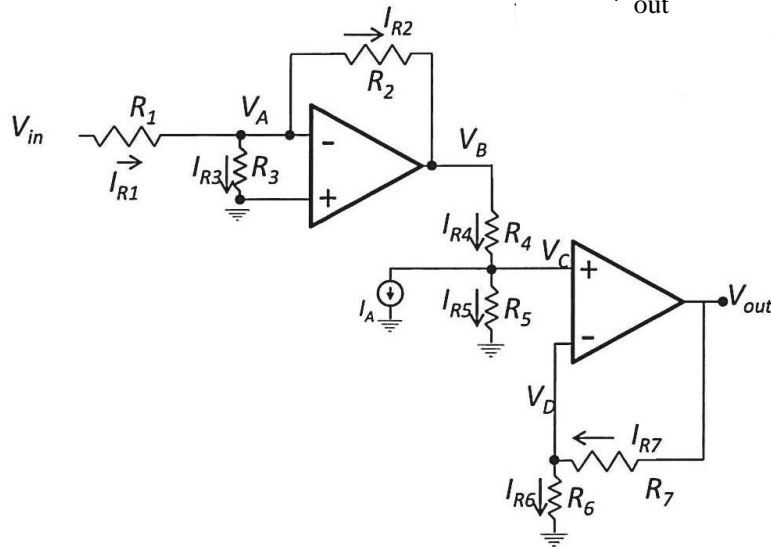
$$V_B =$$

$$V_C =$$

$$V_{out} =$$

4. Dato il circuito in figura ($V_{in} = 1\text{ V}$, $R_1 = 1\text{ k}\Omega$, $R_2 = 2\text{ k}\Omega$, $R_3 = 1\text{ k}\Omega$, $R_4 = 2\text{ k}\Omega$, $R_5 = 2\text{ k}\Omega$, $R_6 = 1\text{ k}\Omega$, $R_7 = 4\text{ k}\Omega$, $I_A = 600\text{ }\mu\text{A}$), determinare: *i)* l'espressione simbolica che lega V_{out} a V_{in} ; *ii)* i valori numerici indicati.

$$V_{out} = -\frac{R_2}{R_1} \frac{R_5}{R_4 + R_5} \left(1 + \frac{R_7}{R_6} \right) V_{in} - \frac{R_4 R_5}{R_4 + R_5} \left(1 + \frac{R_7}{R_6} \right) I_A$$



I_{R1}	=	+	1	0	0	0	.	0	0	0	μA
I_{R2}	=	+	1	0	0	0	.	0	0	0	μA
I_{R4}	=	-		2	0	0	.	0	0	0	μA
I_{R5}	=	-		8	0	0	.	0	0	0	μA
I_{R7}	=	-	1	6	0	0	.	0	0	0	μA
V_A	=					0	.	0	0	0	V
V_B	=	-				2	.	0	0	0	V
V_C	=	-				1	.	6	0	0	V
V_{out}	=	-				8	.	0	0	0	V