3D Computer Graphics and Animation

Graphics PipelineTime to take some shade

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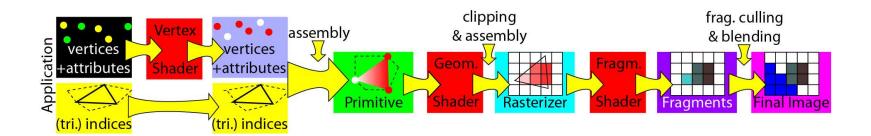






Rasterization

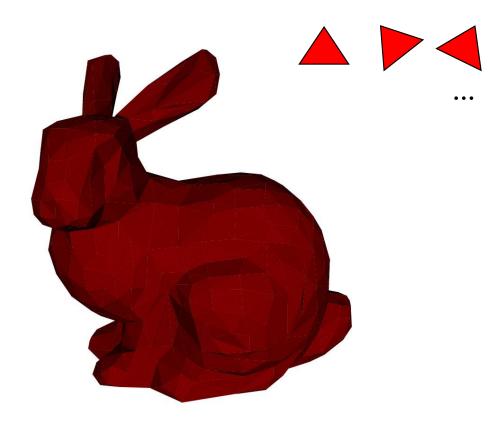
Rasterization via the Graphics Pipeline







Models are typically lists of triangles

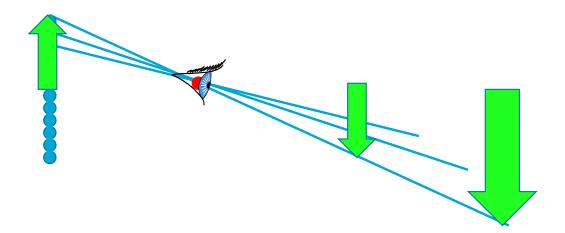






Virtual Camera

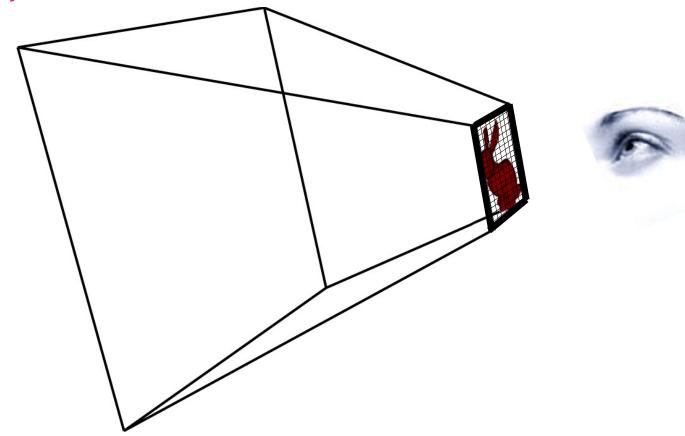
Camera Plane in front of the eye







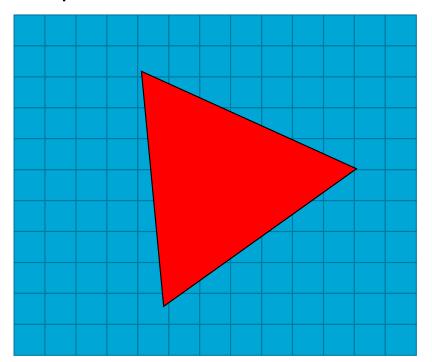
• Projection: Transform coordinates to screen







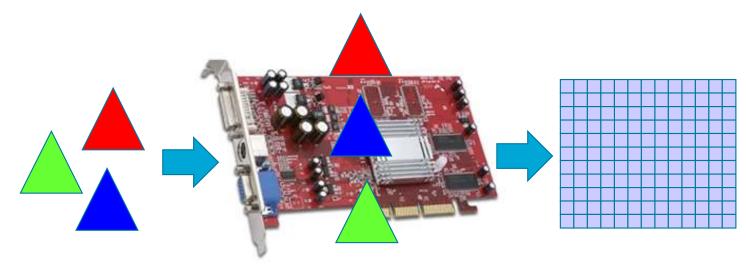
Rasterization: Fill screen pixels







Highly parallelizable GPUs

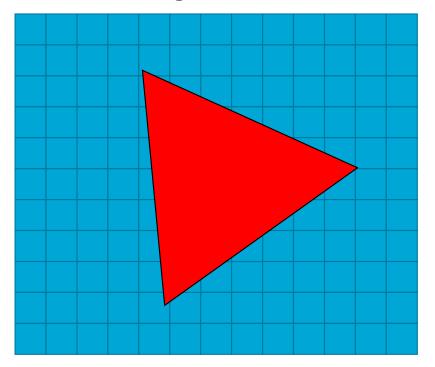


...NVIDIA RTX 3080 Ti has around 10240 cores...





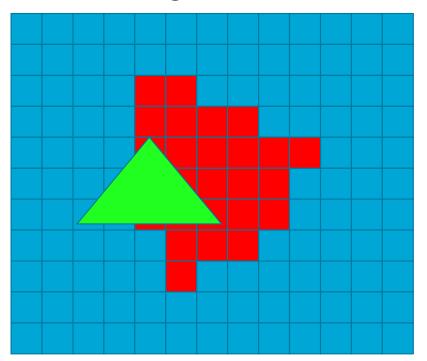
• Catch: Let's look at a second triangle...







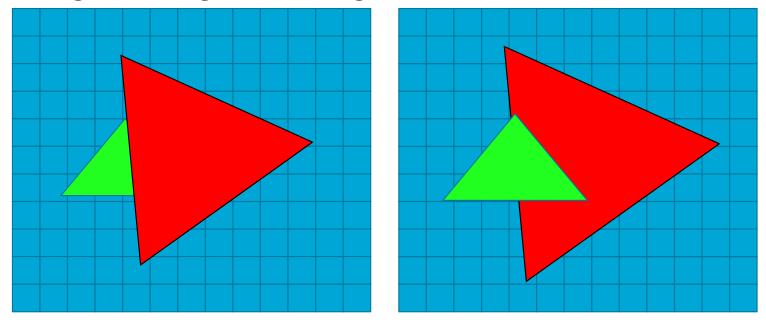
• Catch: Let's look at a second triangle...







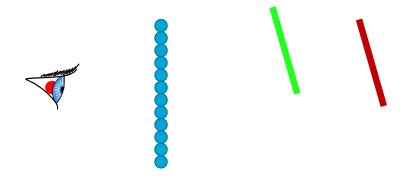
• Catch: Triangle drawing order changes result







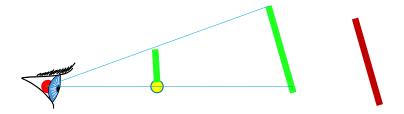
- Depth Test: Avoid sorting!
- Store a depth in each pixel







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- Store a depth in each pixel







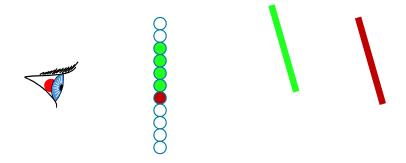
- Depth Test: Avoid sorting!
- Store a depth in each pixel

Compare new distance to stored distance
Update pixel only if new distance is nearer

Depth value



- Depth Test: Avoid sorting!
- Store a depth in each pixel







Creating a virtual camera model

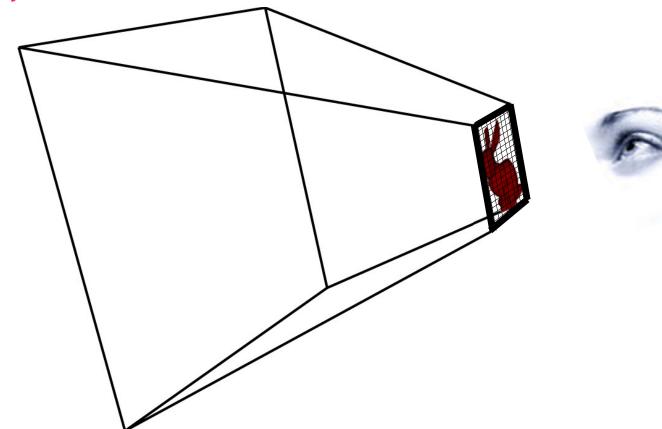
• Given a 3D point, we should find a function that results in the point's projection in the photo.







• Projection: Transform coordinates to screen







Virtual Camera Model

Projecting a scene point with the camera:

- Apply camera position (adding an offset)
- Apply rotation (matrix multiplication)
- Apply projection (non-linear scaling)

Our camera starts to become complicated and not well adapted to a hardware solution...

There has to be a better way...





Homogenous Coordinates - Definition

N-D projective space Pⁿ
is represented by N+1 coordinates, has no null vector,
but a special equivalence relation:

Two points p, q are equal

iff (if and only if)

exists a!=0 such that p*a = q

Examples in a 2D projective space P²:

$$(2,2,2) = (3,3,3) = (4,4,4) = (\pi, \pi, \pi)$$

$$(2,2,2) \neq (3,1,3)$$

$$(0,1,0) = (0,2,0)$$

(0,0,0) not part of the space





Homogeneous Coordinates

To embed a standard vector space Rⁿ in an n-D projective space Pⁿ, we can map:

$$(x_0,x_1,...x_{n-1})$$
 in R^n to $(x_0,x_1,...x_{n-1},1)$ in P^n

Typically, the last coordinate in a projective space is denoted with w.





Homogeneous Coordinates

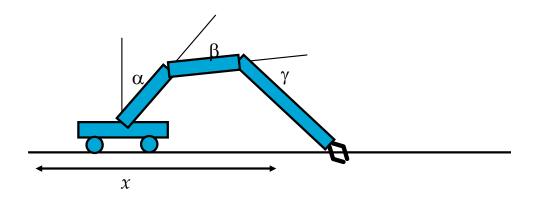
 We have seen that many operations in Rⁿ can be represented by matrices in Pⁿ

Transformations can be concatenated by multiplying the matrices together





- Objects are often defined via many components
 - E.g., wheels of cars, fingers on hands on arms ...
- Concatenate matrices to place objects relative to each other
 - Changing one matrix affects everything hereafter







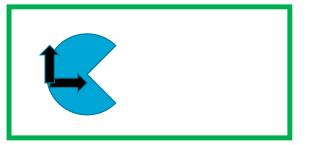
Example:

We make a "complex" robot arm consisting of two parts:

The arm itself and a hand

Both are designed independently and are at the origin (shown below)

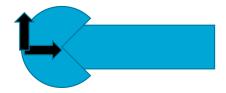








Using the coordinates as is, you get:



- That does not look right!
- Instead: Let's define a matrix to shift the objects to the wanted relative location





- Concatenate and apply matrices
 - S:=Translation matrix to position of arm (**S**houlder)







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- Concatenate and apply matrices
 - S:=Translation matrix to position of arm (Shoulder)
 - Apply S to all vertices of arm

Resulting positions
After applying the object
vertices to matrix S







- Concatenate and apply matrices
 - S:=Translation matrix to position of arm (Shoulder)
 - Apply S to all vertices of arm
 - T:=translation along arm (to the Joint of the hand)
 - J=S T







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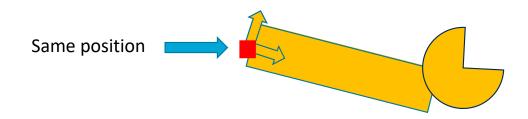
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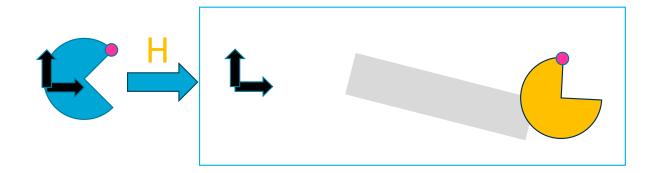






Complex Objects

We found a matrix H to transform the vertices from the original hand definition into the wanted position relative to the arm!

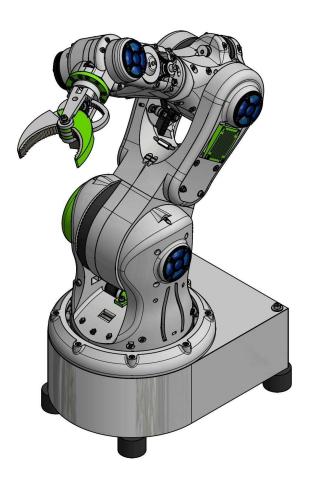






Let's try it out!

Professional Robot Arm:







Let's try it out!

Professional Robot Arm:

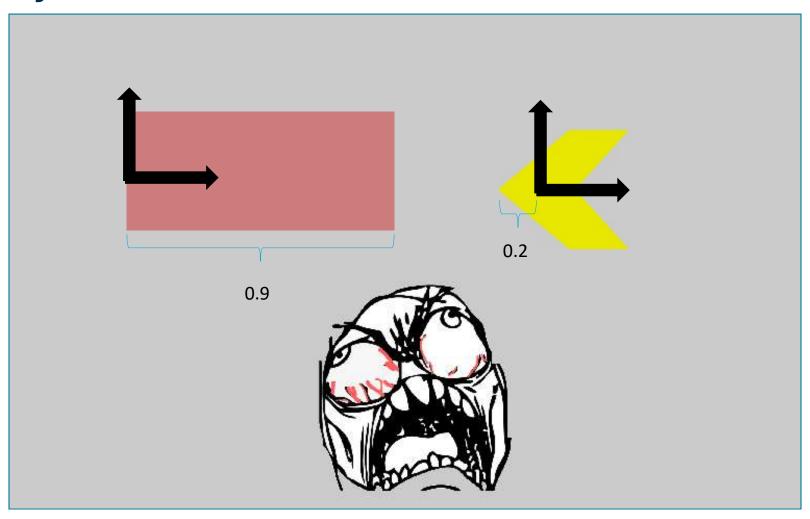








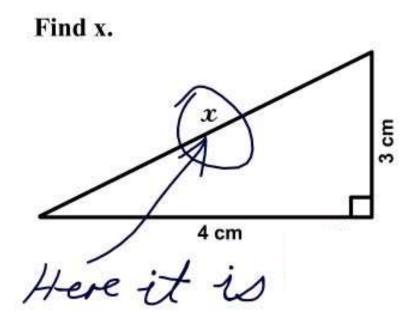
Let's try it out!







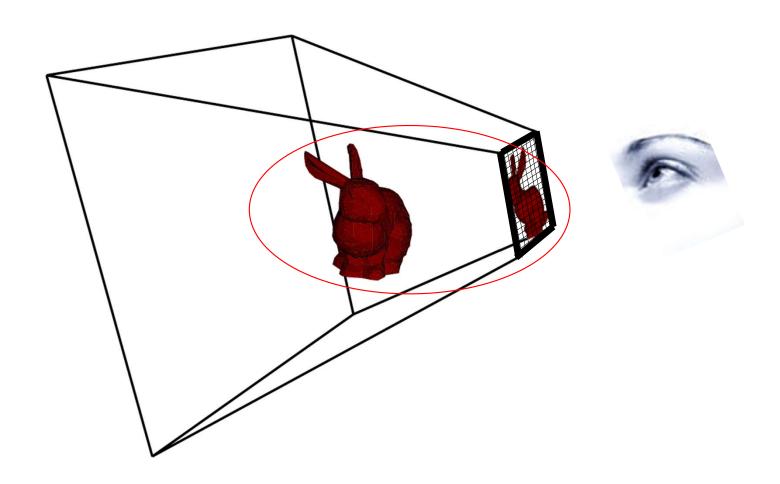
Questions?







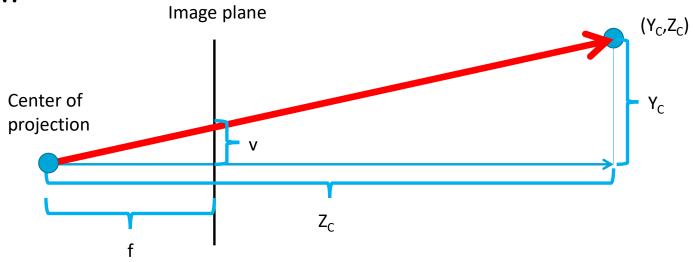
One pipeline step is still missing...







• sideview:

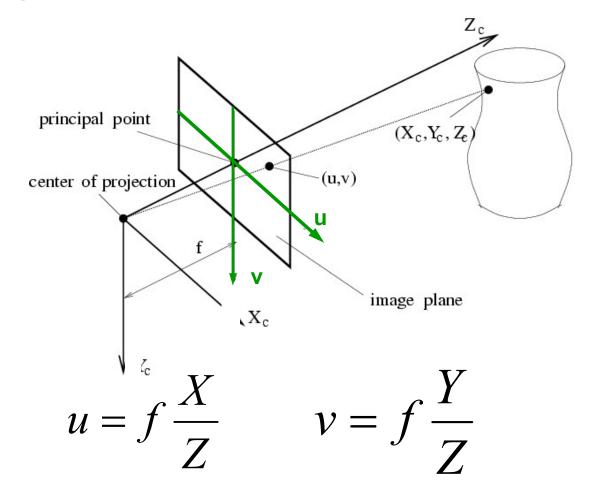


Similar triangles:
$$v / f = Y_C / Z_C$$



9

Perspective Projection





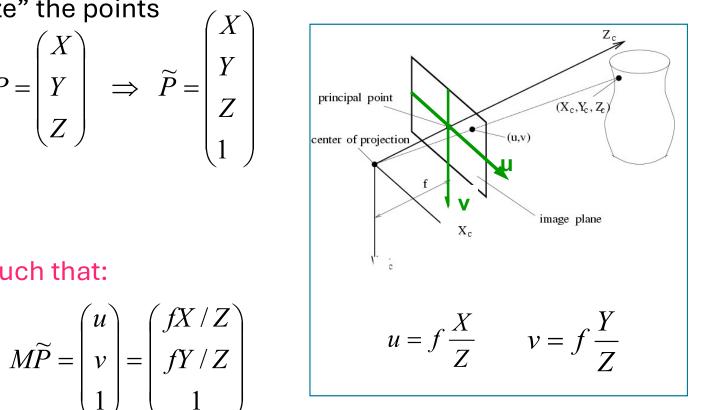


"Homogenize" the points

$$P = \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} \implies \widetilde{P} = \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$

Look for M such that:

$$M\widetilde{P} = \begin{pmatrix} u \\ v \\ 1 \end{pmatrix} = \begin{pmatrix} fX/Z \\ fY/Z \\ 1 \end{pmatrix}$$







Hint: Think projective!

$$M\widetilde{P} = \begin{pmatrix} fX/Z \\ fY/Z \\ 1 \end{pmatrix} \Rightarrow M\widetilde{P} = \begin{pmatrix} fX \\ fY \\ Z \end{pmatrix}$$



• Solution:

$$M = \begin{pmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$



• Solution:

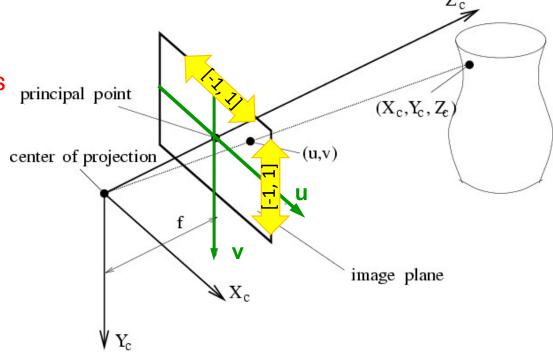
$$M = \begin{pmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$



9

Adding Image Space to Camera Model

 Transform u, v into pixel positions



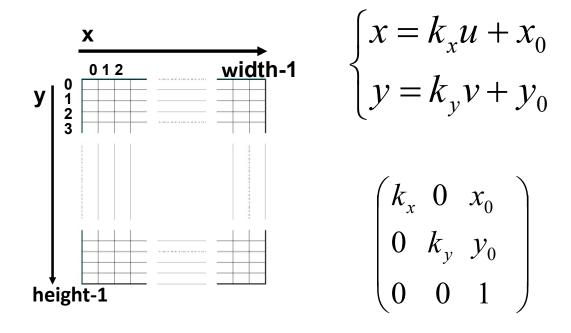
$$u = f \frac{X}{Z} \qquad v = f \frac{Y}{Z}$$



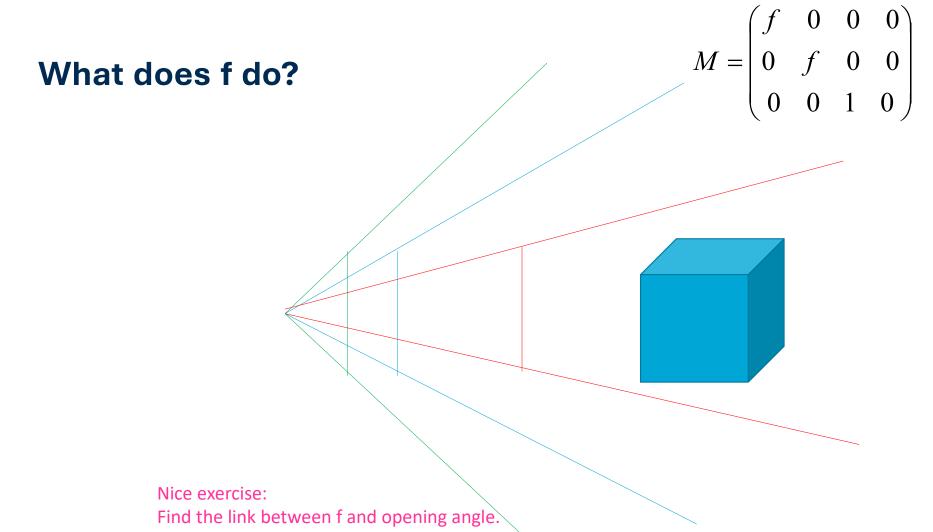


Internal Camera Parameters

- $(-1,1)^2$ (0, width-1)x(0,height-1)
- Homework: Find a matrix to do this mapping











6

It could have been so simple...

• What is the problem of this matrix for the Graphics Pipeline?

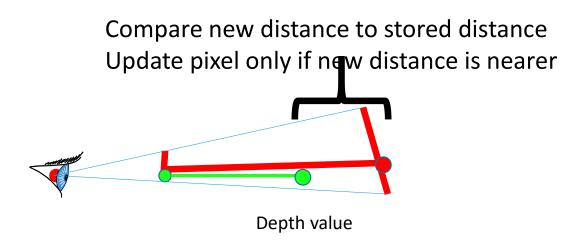
$$M = \begin{pmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$





We need a depth value!

We need to keep a Z coordinate!

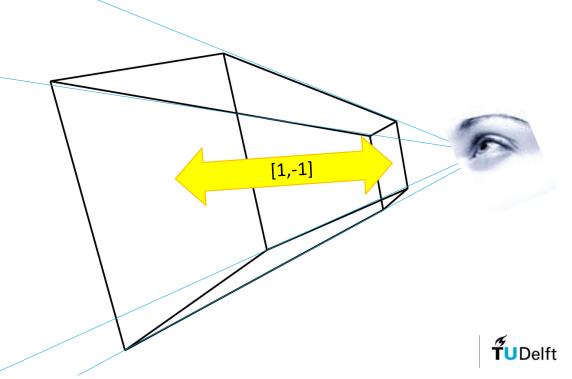




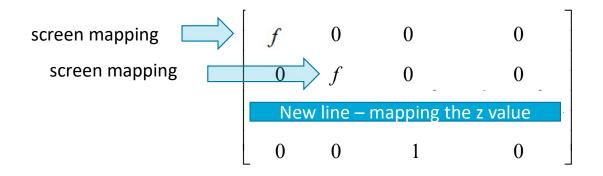


Problem:

- A 3D scene is infinite...
- How do we represent Z?
- Solution: Add a near and far clipping plane!

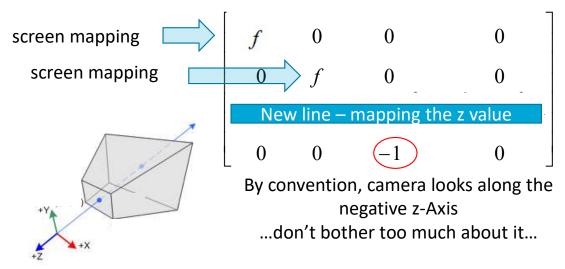






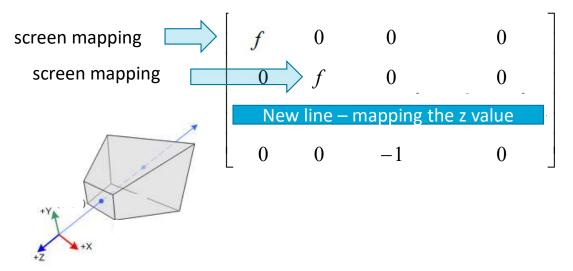






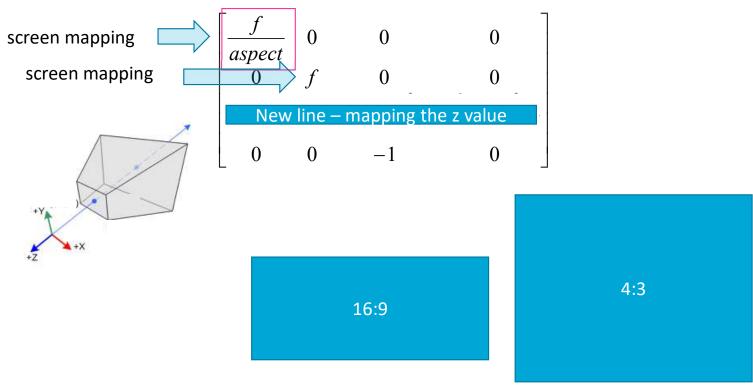






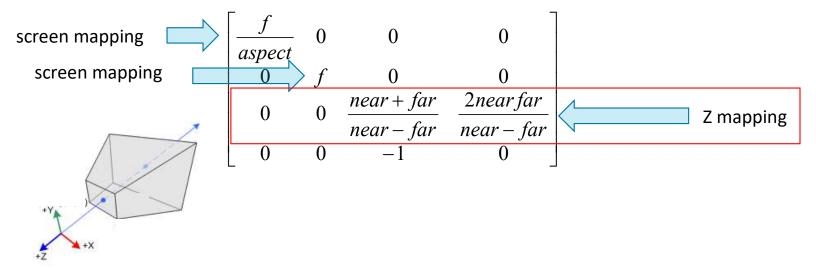






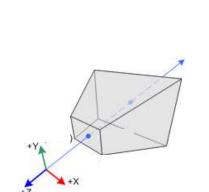












$$\begin{bmatrix} \frac{f}{aspect} & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & \frac{near + far}{near - far} & \frac{2near far}{near - far} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

- Verify: (0,0,-near,1) maps to depth -1, and (0,0,-far,1) to 1
- What depth does (0,0,-(far+near)/2,1) map to?
 Z-Buffer is not linear!





Is z-Buffer non-linearity a problem?

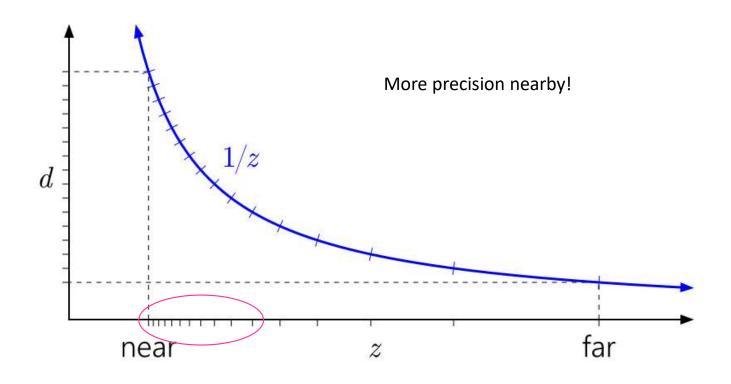
Compare new distance to stored distance Update pixel only if new distance is nearer

Depth value





Z-Buffer Visualization

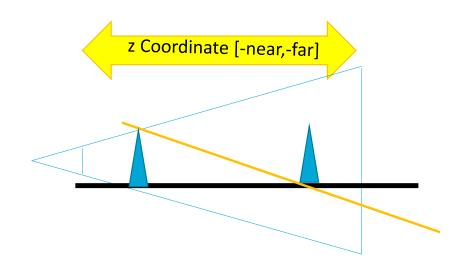


https://developer.nvidia.com/content/depth-precision-visualized





Illustration of the Camera Mapping



$$\begin{bmatrix} \frac{f}{aspect} & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & \frac{near + far}{near - far} & \frac{2nearfar}{near - far} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

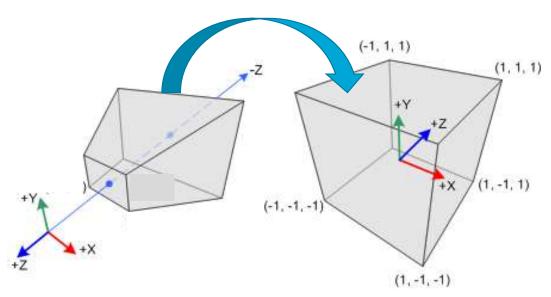
After normalization (division by w)





Camera Space

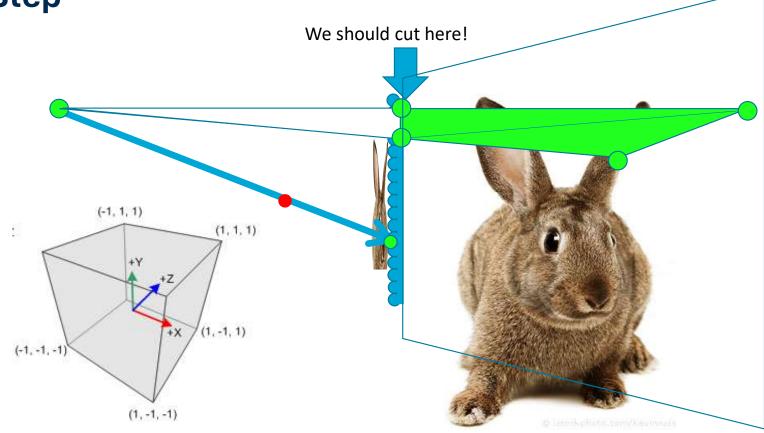
• Perspective Frustum is mapped on a cube







Final Step



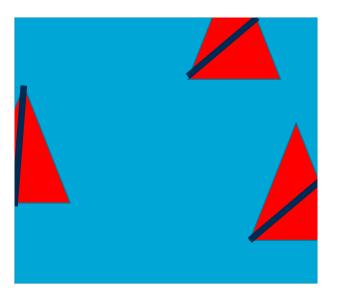
• Test if triangle lies in the cube!





Clip Space

Create clipped triangles

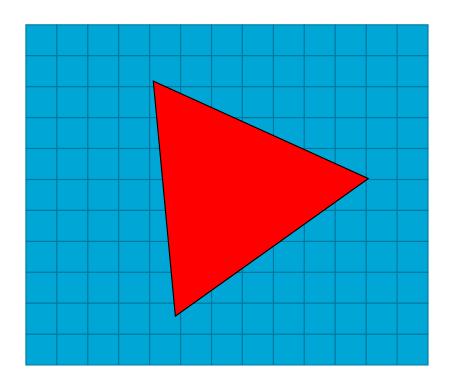






Last pipeline step: Rasterization

- Now, all primitives are clipped and projected on the screen.
- Pixel filling +
- Depth Buffer







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• Pixel filling +

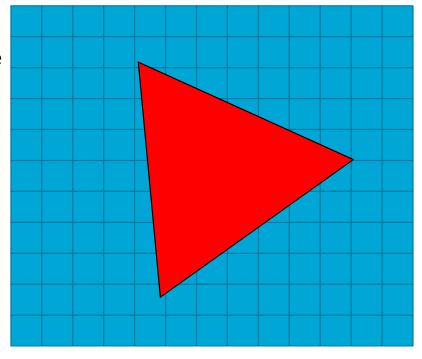
Rema to avo

Depth Buffer



Remark2: The projection delivers depth d in [-1,1], d is stored using (d+1)/2, thus in [0,1]

Remark 1: Complex rules to avoid ambiguities, but if pixel center is inside the triangle, the pixel is filled







Object Transformation

Viewing Transformation (Perspective / Orthographic)

Clipping

Scan Conversion (Rasterization)



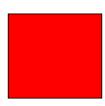


Object Transformation

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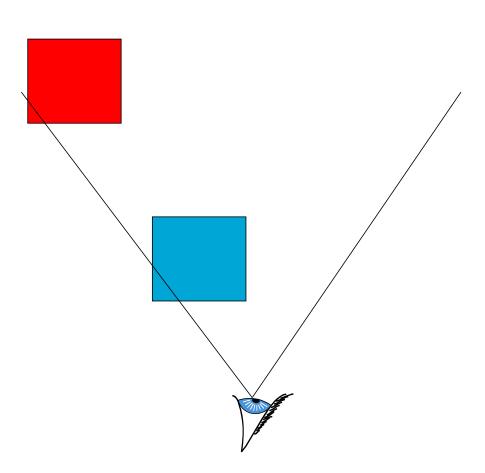


Object Transformation

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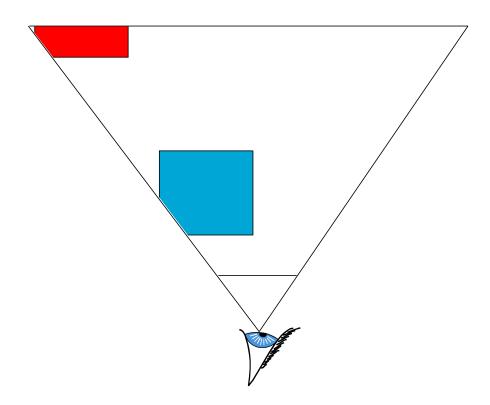


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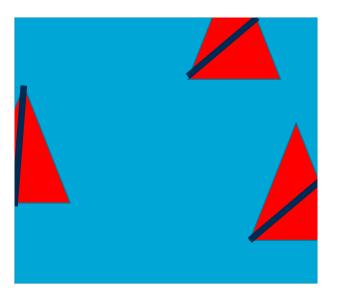






Clip Space

Create clipped triangles







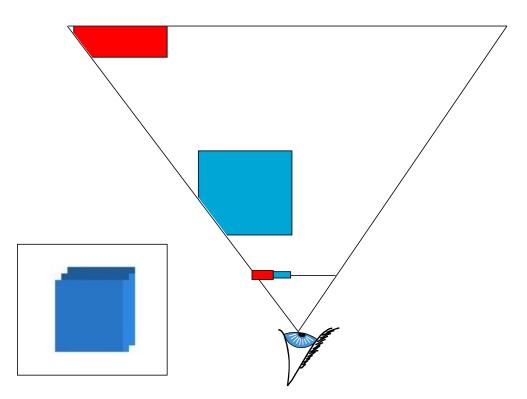
Graphics Pipeline

Object Transformation

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Clipping

Scan Conversion (Rasterization)







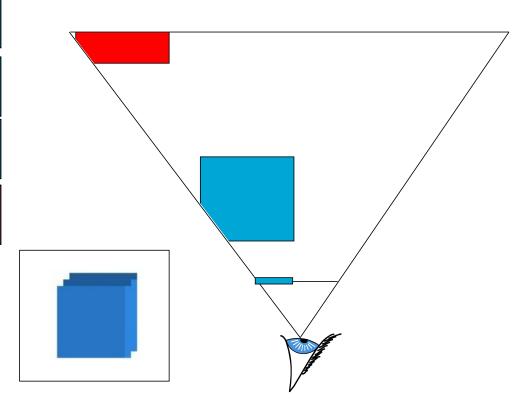
Graphics Pipeline

Object Transformation

Viewing Transformation (Perspective / Orthographic)

Clipping

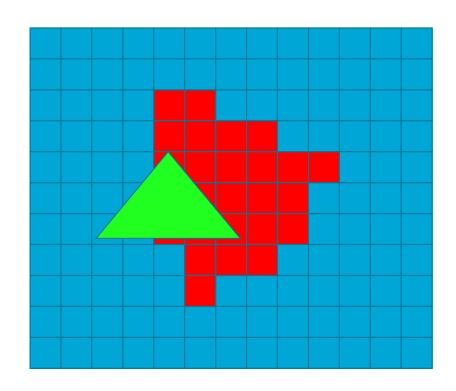
Scan Conversion (Rasterization)







Blending and Depth Test







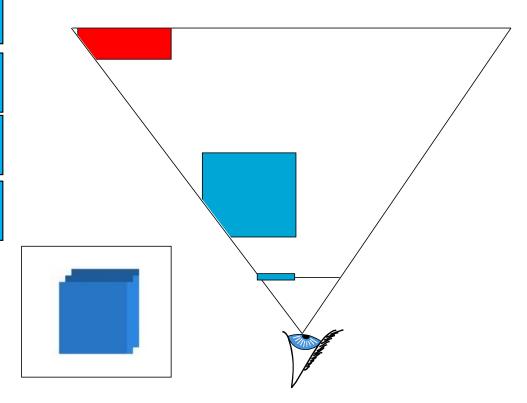
Graphics Pipeline

Object Transformation

Viewing Transformation (Perspective / Orthographic)

Clipping

Scan Conversion (Rasterization)







Questions?







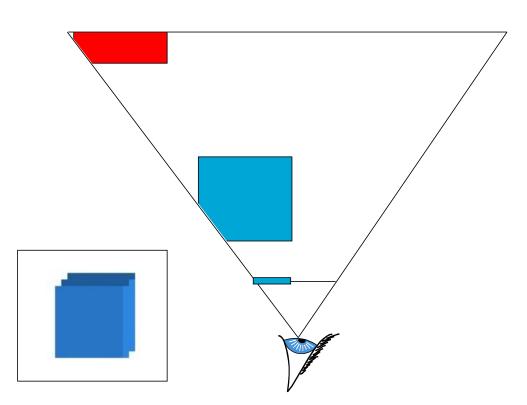
Standard Graphics Pipeline

Object Transformation

Viewing Transformation (Perspective / Orthographic)

Clipping

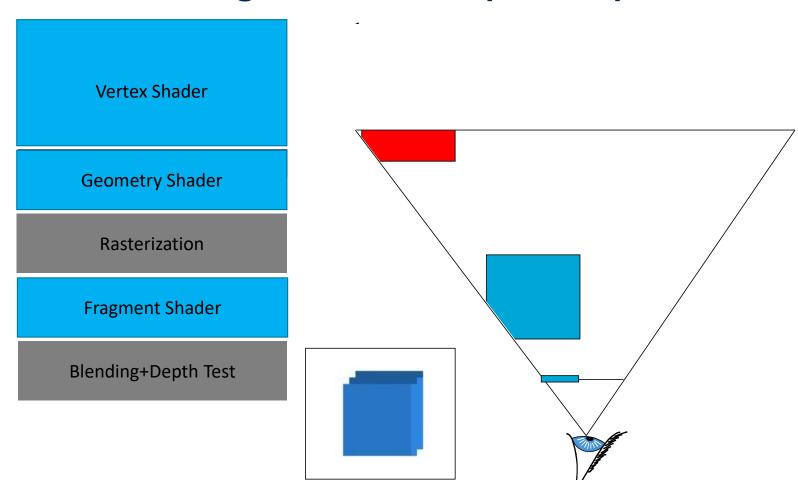
Scan Conversion (Rasterization)







Today's Modern/Programmable Graphics Pipeline







Programmable Graphics Pipeline

On today's GPUs stages are customizable (programmable)

Vertex shader: Computations on vertices

Geometry shader: Computations on primitives
 (primitives = triangles, quads...)

 Fragment shader: Computations on pixels (Fragment=pixel+attributes)





Graphics API

- To communicate and control the graphics card, we can make use of special APIs.
- The most famous APIs are
 - Direct X
 - OpenGL
 - Vulkan

- In this course, we will focus on OpenGL
- To program the shaders, we will use GLSL (OpenGL shading language)





What makes a GPU fast?

- Very high parallel throughput
- The data typically resides on the GPU and is streamed through specialized programs
- To illustrate parallel processing:
 imagine a stream of vertices,
 groups of vertices are processed in parallel
 (e.g., each vertex is multiplied by a matrix)
 result is put back into a stream





Flat Mesh Representation

Simply store vertices in order

What about attributes like color?

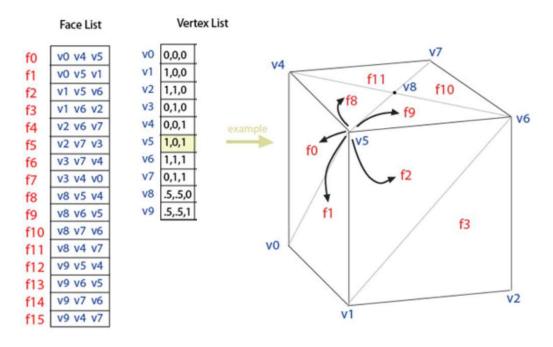
What is suboptimal about this?





Optimized Mesh Representation

Indexed Face Set





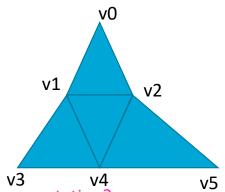


Mesh with attributes GPU-ready

- Data stored in arrays containing all vertices and attributes
- Triangles are defined by an index array:
 consecutive indices in this array define faces
- Advantage: Shared vertices only stored once

Vertex Positions: [x0,y0,z0, x1, y1, z1, ...x5, y5, z5] Attributes (can be several): [r0,g0,b0, r1, g1, b1, ... r5, g5, b5] IndexBuffer: [0,2,1,1,3,4,1,4,2,2,4,5]

e.g., T0 uses indices 0, 2, 1 meaning it uses vertices v0, v2, and v1. Given an index, we can retrieve the data of the vertex from the other arrays. For v0: x0, y0, z0 and r0, g0, b0



How often would all attributes of v1 be stored if not using this representation?





Today's Standard Graphics Pipeline

Vertex Shader

Geometry Shader

Rasterization

Fragment Shader





Today's Standard Graphics Pipeline

Vertex Shader

Geometry Shader

Rasterization

Fragment Shader

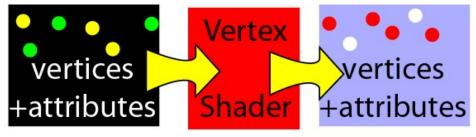




Vertex Shader

Input: Vertex with attributes

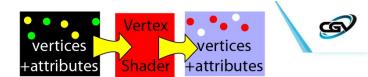
Output: Vertex with attributes



What operation is done in standard pipeline?

Usually camera projection / object placement!





Vertex Shader Example (GLSL 4.3)

```
Constant for all vertices
#version 430
layout(location=0) uniform mat4 ModelViewMatrixValue;
layout(location=0) in vec4 pos; //world-space position
layout(location=1) in vec3 normal; //world-space normal
//Data to be passed to geometry shader
out vec3 gColor;
void main(){
  gl Position = ModelViewMatrixValue * pos;
  gColor = vec3(normal.x,0,0); //normal.x used as color
                                             Example applications?
```





Today's Standard Graphics Pipeline

Vertex Shader

Geometry Shader

Rasterization

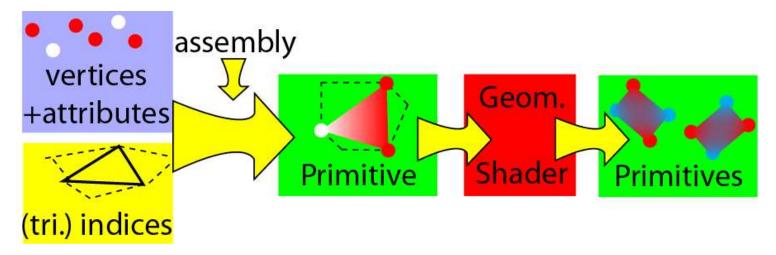
Fragment Shader





Geometry Shader

- Input: Vertex/Attribute **array** of current primitive (e.g., triangle or its immediate neighborhood)
- Output: Several primitives (vertices + attributes)

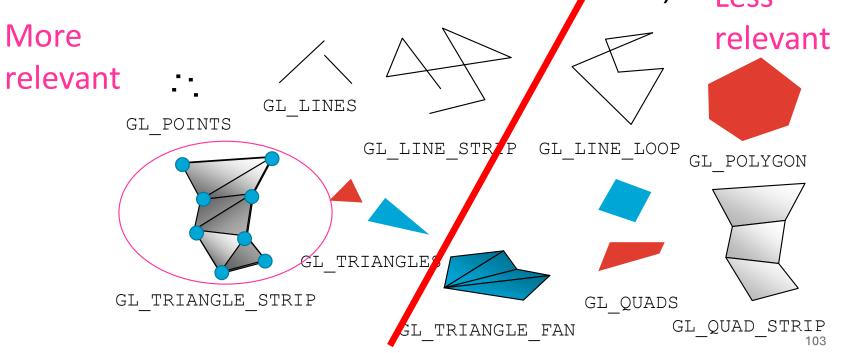






Primitives?

Primitives are specified by vertices
 (These are the traditional OpenGL primitives – some can be considered outdated)
 Less







Geometry Shader: Input

- Geometry shader interprets input as:
 Points, lines, lines with adjacency, triangles or triangles with adjacency
- Default usage: current triangle's vertices are accessible
 - Works like for the indexed face set, with indices 0,1,2



Per extension: triangles/lines + neighbors (tri.) indices
 (this requires special data formatting, just using strips does not work)





Geometry Shader: Output

Geometry shader supports points, line_strip and triangle_strip as output









Geometry Shader Example

```
#version 430
layout (triangles) in;
layout (triangle strips, max vertices=3) out;
in vec3 gColor[3];
out vec3 fColor;
void main(void) {
      for (int i=0;i<3;++i) {
            gl_Position=gl_in[i].gl_position;
            fColor=gColor[i];
            EmitVertex();
      EndPrimitive();
```







Geometry Shader Example

```
#version 430
layout (triangles) in;
layout (triangle strips, max vertices=3) out;
in vec3 gColor[3];
                      Arrays coming from vertex shader
                         containing the data of the current triangle
out vec3 fColor;
void main(void) {
      for (int i=0;i<3;++i) {
             gl Position=gl in[i].gl position;
             fColor=gColor[i];
             EmitVertex();
      EndPrimitive();
```







Geometry Shader Example

```
#version 430
layout (triangles) in;
layout (triangle_strips, max vertices=3) out;
in vec3 gColor[3];
                       Arrays coming from vertex shader
                           containing the data of the current triangle
out vec3 fColor;
void main(void) {
       for (int i=0;i<3;++i) {
              gl_Position=gl_in[i].gl_position;
                                                              Use current primitive's data
                                                              (position and color)
                                                              and store them
               fColor=gColor[i];
              EmitVertex();
Create a vertex
                                  Build a primitive (here a triangle) out
       EndPrimitive();
                                  of the created vertices
```



Today's Standard Graphics Pipeline

Vertex Shader

Geometry Shader

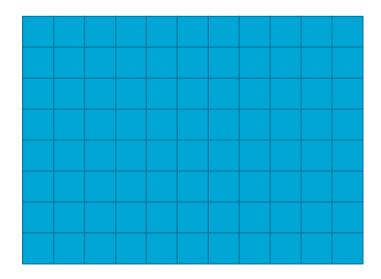
Rasterization

Fragment Shader





Triangles into fragments (pixels+attributes)

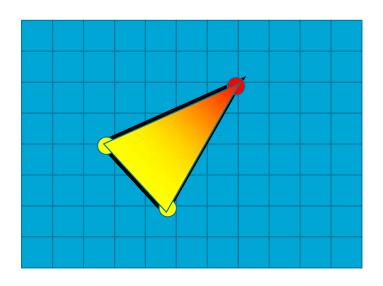


- Fragment data determined by interpolation
- Values are extracted at pixel centers





Triangles into fragments (pixels+attributes)



Two yellow, one red vertex

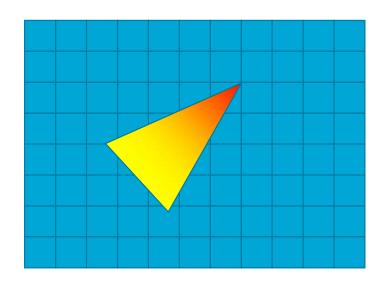
Colors are interpolated over triangle

- Fragment data determined by interpolation
- Values are extracted at pixel centers





Triangles into fragments (pixels+attributes)



Two yellow, one red vertex

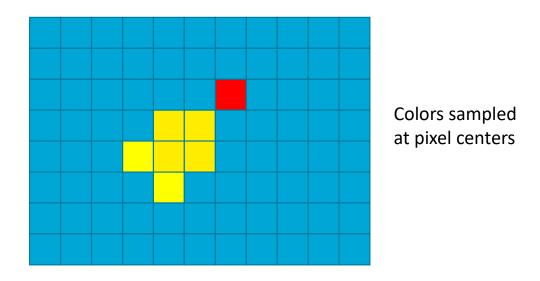
Colors are interpolated over triangle

- Fragment data determined by interpolation
- Values are extracted at pixel centers





Triangles into fragments (pixels+attributes)



- Fragment data determined by interpolation
- Values are extracted at pixel centers





Triangles into fragments (pixels+attributes)



- Fragment data determined by interpolation
- Values are extracted at pixel centers

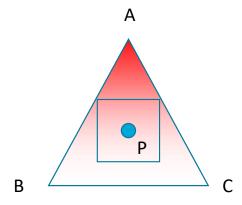




Example: Interpolation

What are "interpolated" vertex attributes in each Fragment?

- Imagine P=1/3 A + 1/3 B + 1/3 C
- If the colors at A, B, C are red (1,0,0),
 white (1,1,1), white (1,1,1) respectively
- The interpolated color at P would be:
 (1, 2/3, 2/3), which is pink







Today's Standard Graphics Pipeline

Vertex Shader

Geometry Shader

Rasterization

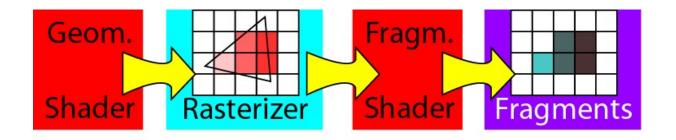
Fragment Shader





Fragment Shader

- Input: "Pixel" with interpolated vertex/attributes
- Output: New fragment for this position
 - Typically a new pixel color is computed







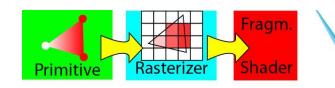
Fragment Shader

Fragment = colors + depth at a pixel location

 Two fragments can fall in the same pixel (e.g., two overlapping triangles)

 Fragments cannot be moved in the Fragment shader, their location on the screen is fixed





Fragment Shader Example

outColor = vec4(fColor,1.0);

Vertex values are interpolated!!!





Today's Standard Graphics Pipeline

Vertex Shader

Geometry Shader

Rasterization

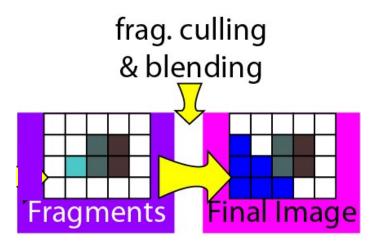
Fragment Shader





Blending Stage

- Blending stage cannot be programmed.
- It takes the produced fragment and combines it with the current image.







Blending Stage

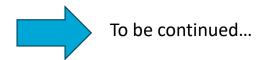
Typically two choices exist:

Culling:

Do not produce an output e.g., depth test failed or fragment is discarded in the code

Blending:

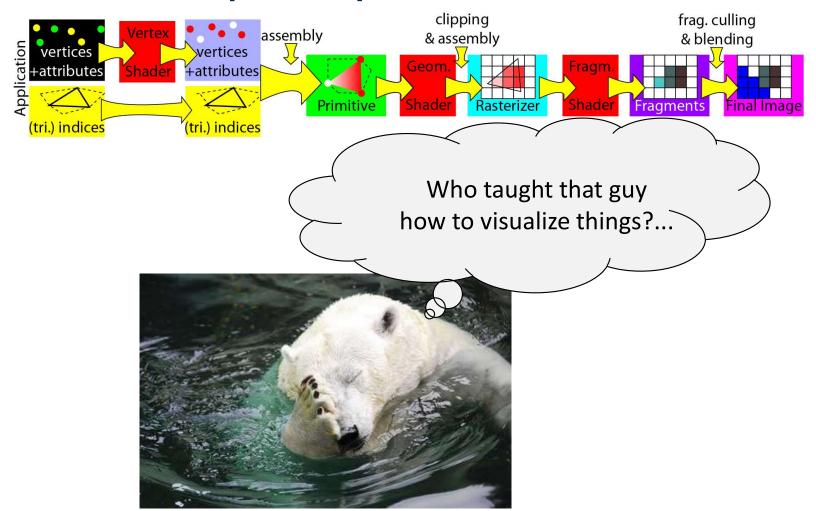
Combine background and new fragment
e.g., sum current and incoming value
(there are a few operations to choose from)







Programmable Graphics Pipeline







Cool stuff in the fragment shader!

- Similar means as in my demo:
- https://www.shadertoy.com/view/3lyBDw

- Using textures (a little outlook):
- https://www.shadertoy.com/view/XcXXzS
- https://www.shadertoy.com/view/XltGRX





Questions?







Thank you very much for your attention!



