

3D Computer Graphics and Animation

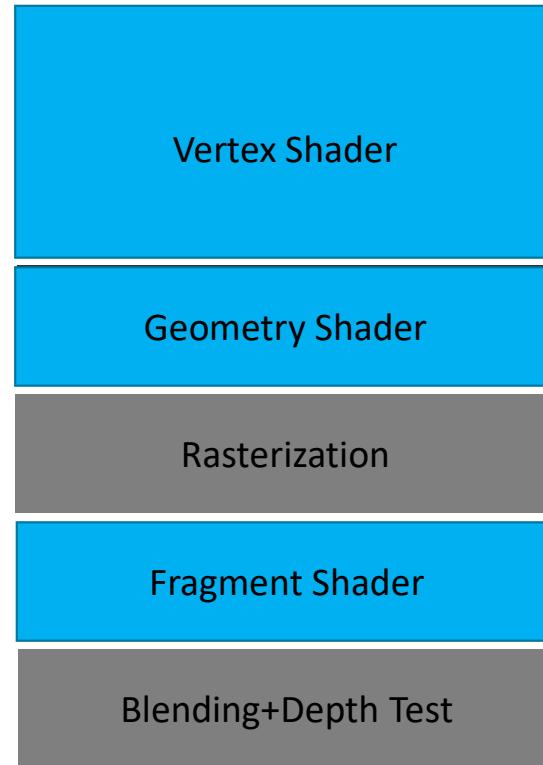
Advanced Texturing Working on your image

Elmar Eisemann

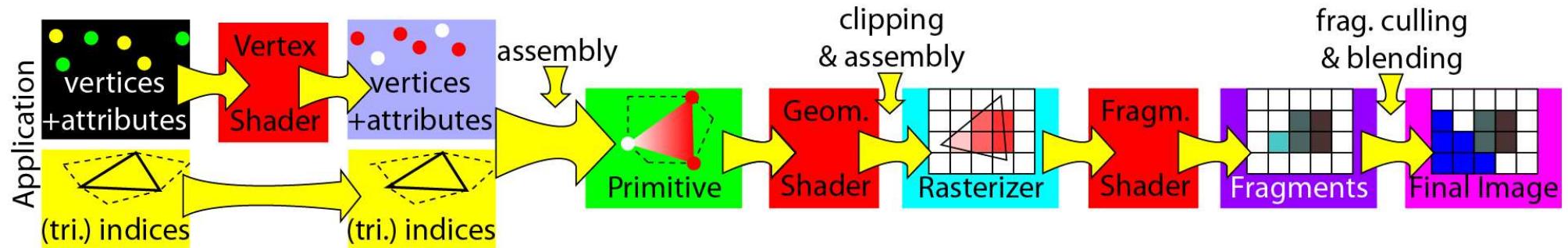
Delft University of Technology



Programmable Graphics Pipeline

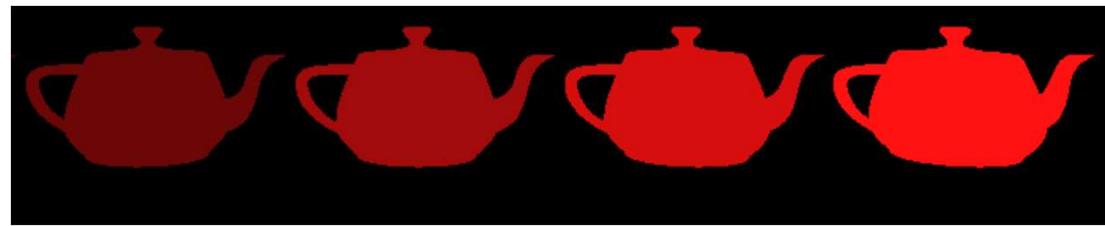


Programmable Graphics Pipeline



Shading

How to transform



in



Advanced Material Models



<https://blog.playcanvas.com/physically-based-rendering-comes-to-webgl/>

Something is still missing...

Misses quick material changes

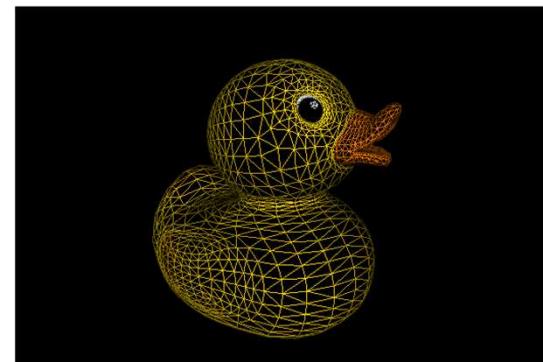
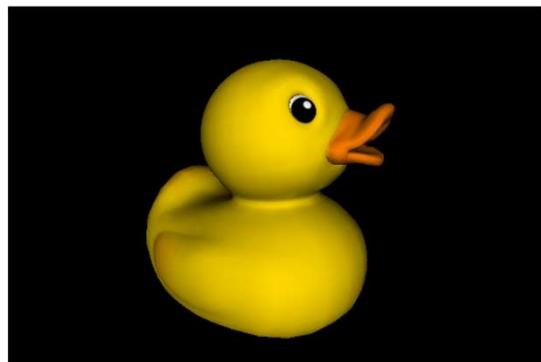


Today

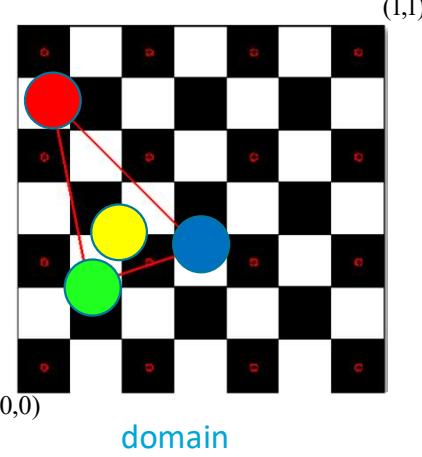


Textures

- Can be used to provide, e.g.,
 - parameters for ambient/diffuse material models



Textures

- Image mapped on the surface via texture coordinates
 - Specified at each vertex `glTexCoord{123}{fi}`
 - Interpolated over triangles
- 

(0,0) (1,1)

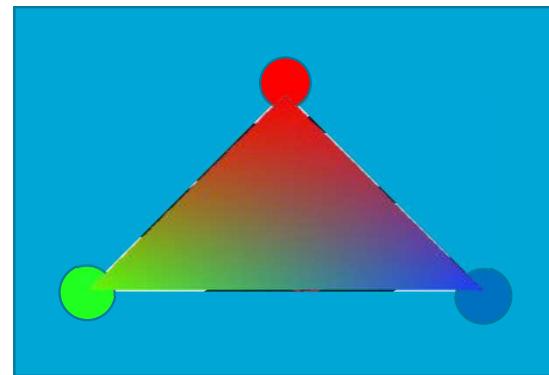
domain

A 2x2 grid of black and white squares representing a texture domain. Four vertices are highlighted with colored circles: top-left (red), bottom-left (green), bottom-right (blue), and top-right (yellow). Red lines connect these four points to their corresponding vertices on a triangle below.

```
TextureCoords (0.2f, 0.3f);
Vertex (-1.0f, 0.0f);

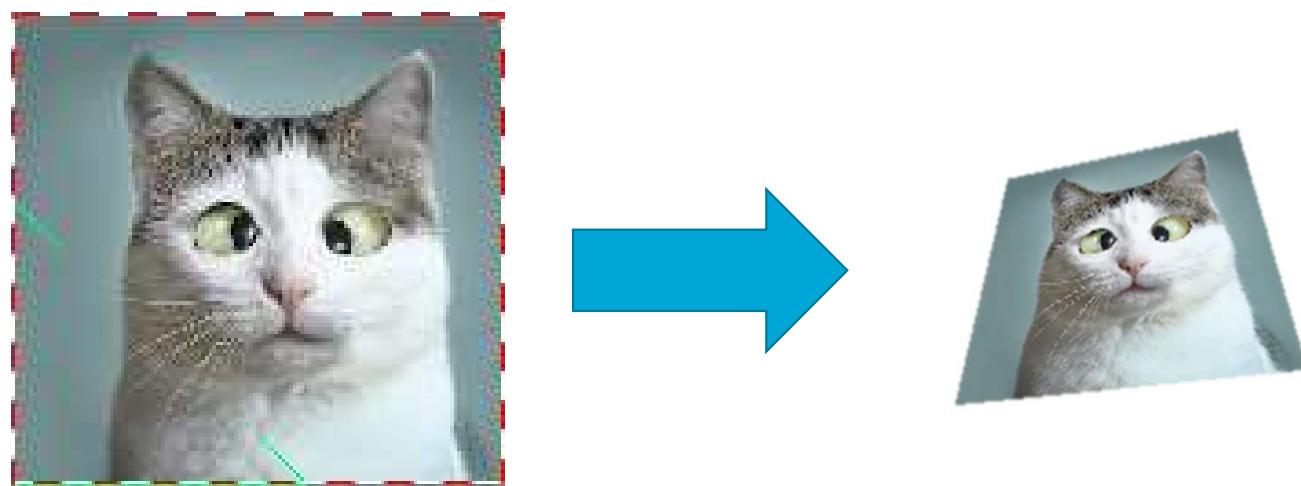
TextureCoords (0.5f, 0.4f);
Vertex (+1.0f, 0.0f);

TextureCoords (0.1f, 0.8f);
Vertex ( 0.0f, 1.0f);
```



3D View

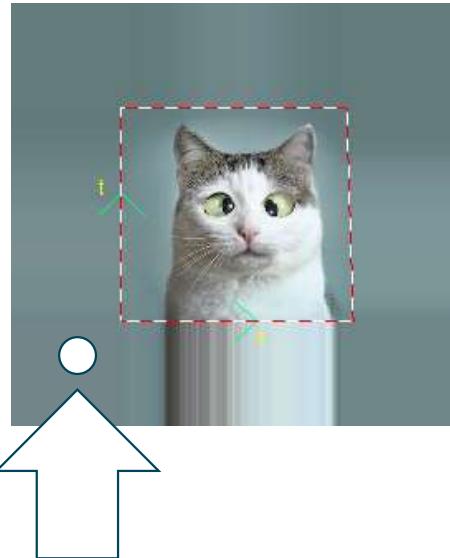
Example of a mapped texture



What happens outside the texture?

- Different modes can be defined **per axis**:

Border = constant color

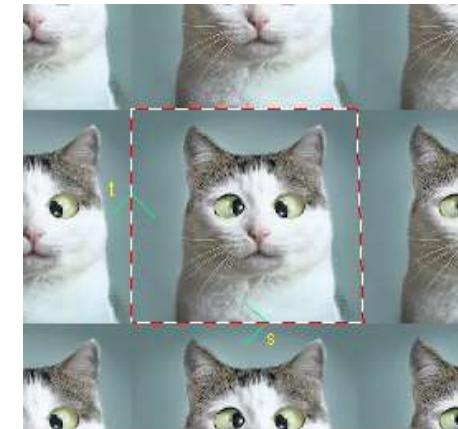


Texture coordinate?
(-0.25, -0.25)

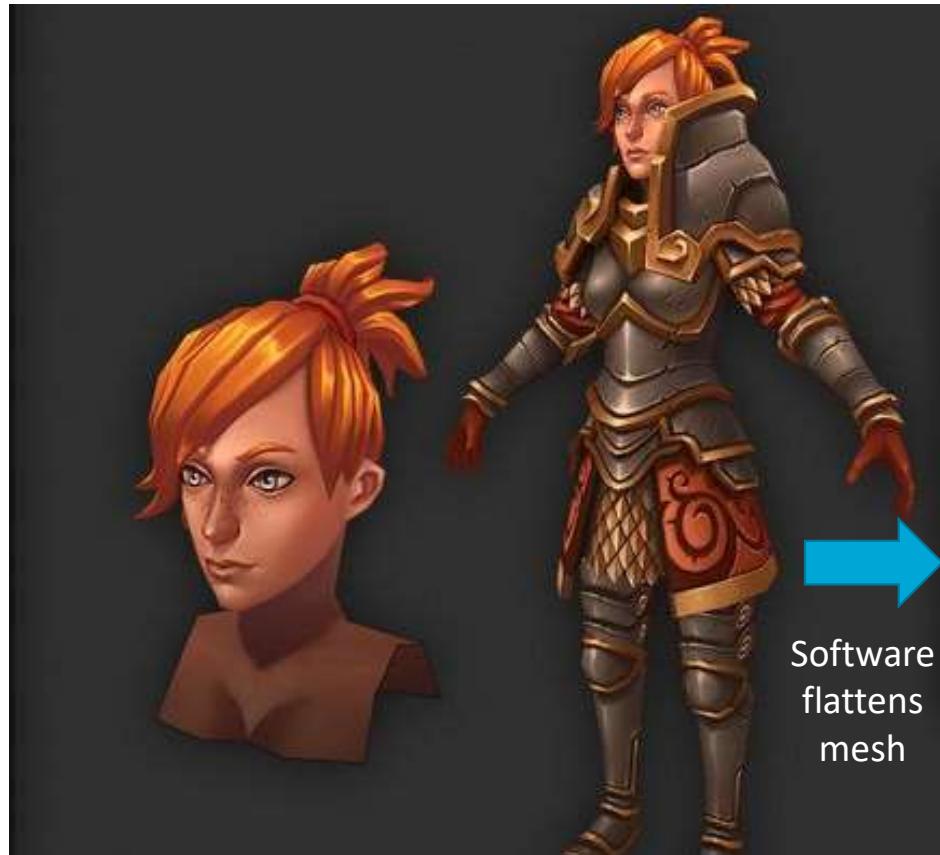


Clamp = keep texel value on the border

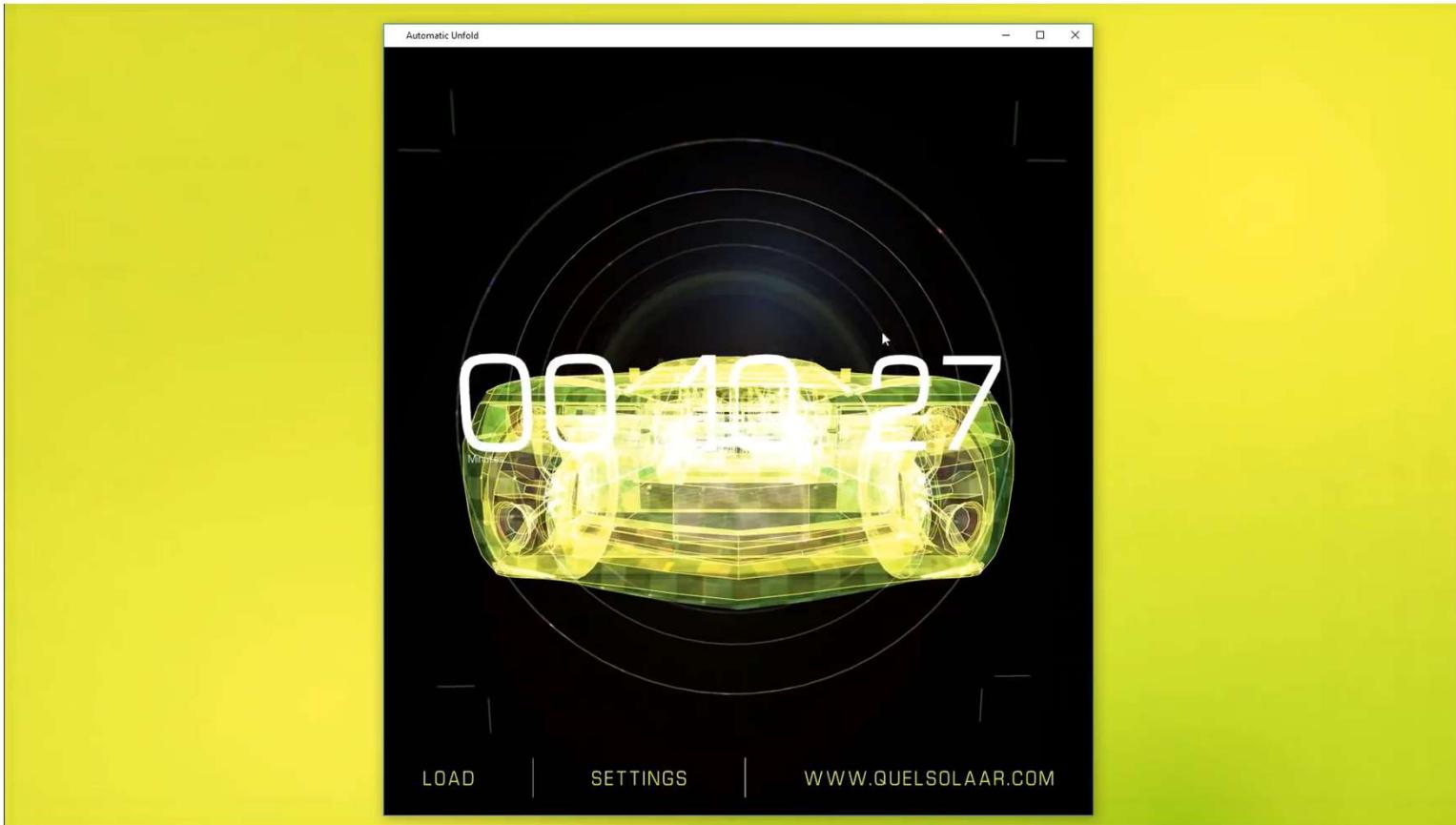
Repeat = repeat at borders



Texture Mapping: Special Software

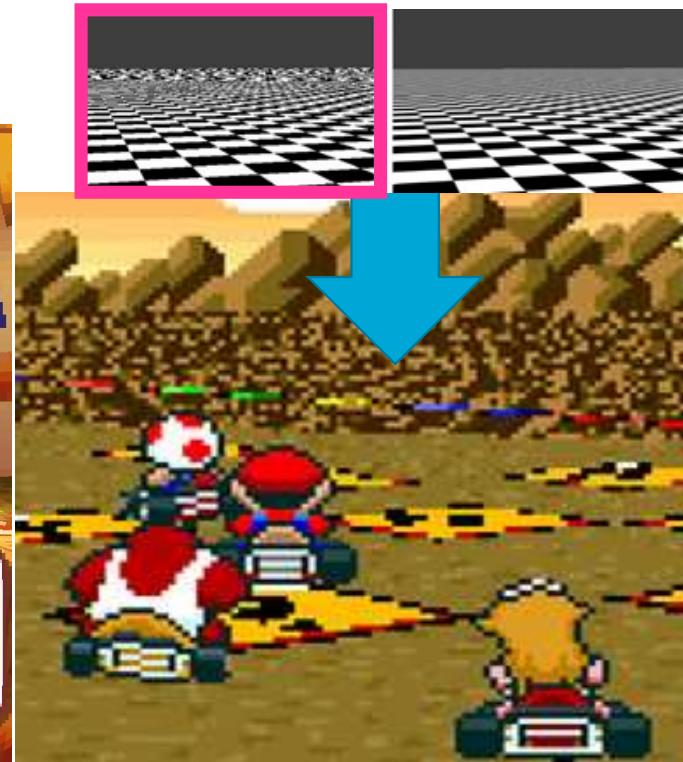


Unwrapping a Mesh



Texture issues: Aliasing

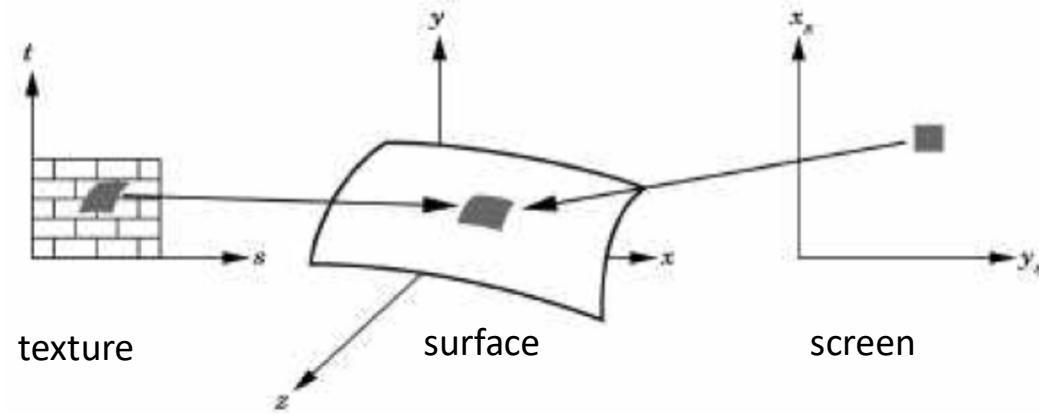
- Not always completely beautiful...



Aliasing

- From screen to texture:

Not a one-to-one pixel mapping!



1. Oversampling

- Due to limited texture resolution

Minecraft

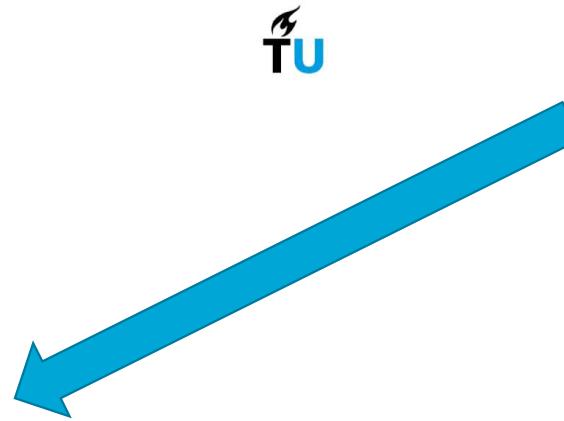


Resident Evil 4

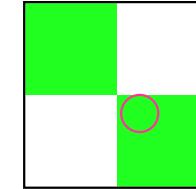


1. Oversampling

- Pixel smaller than texel



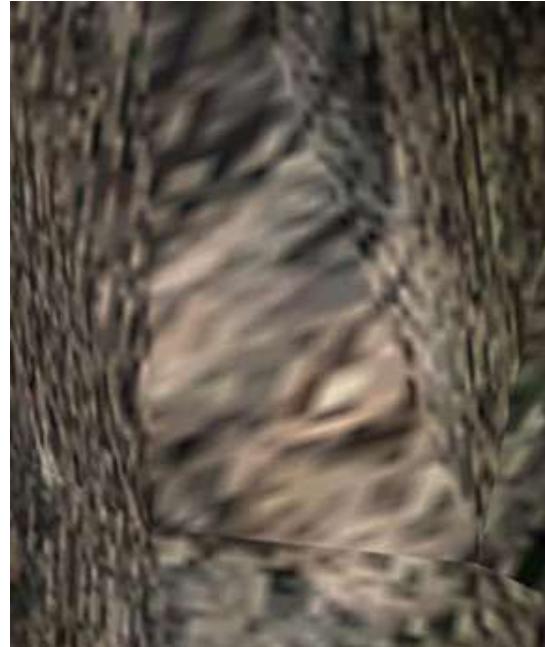
TU



1. Oversampling

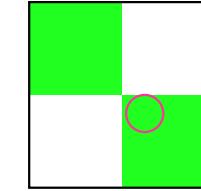
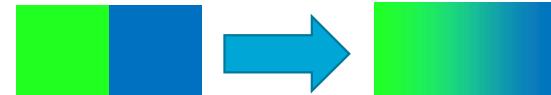
- In practice:

Often less blocky but washed out (most applications use texel interpolation)

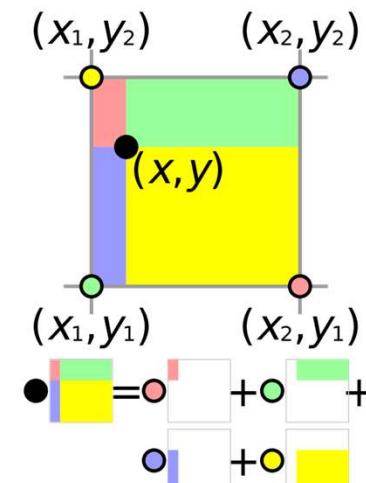
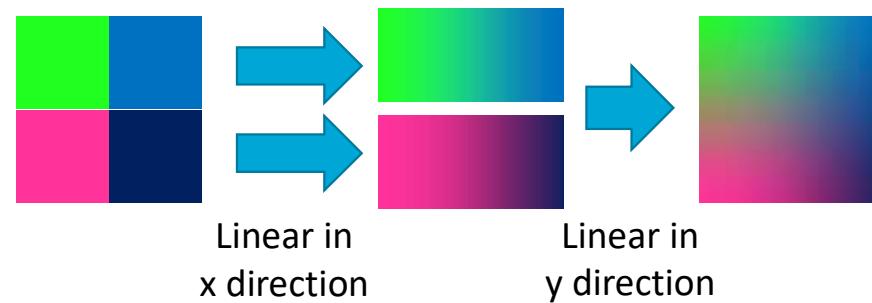


1. Oversampling

- Bilinear interpolation
 - Linear interpolation: $(1-\alpha) * \text{col1} + \alpha * \text{col2}$

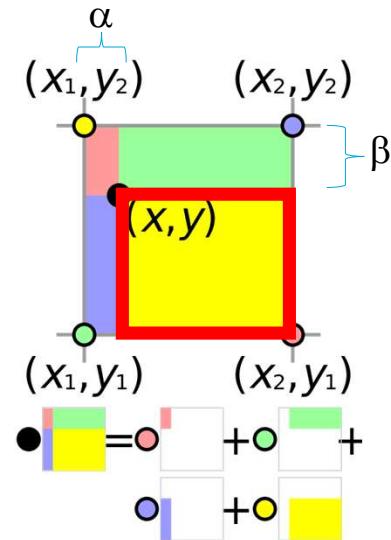


- Bilinear interpolation:



1. Oversampling

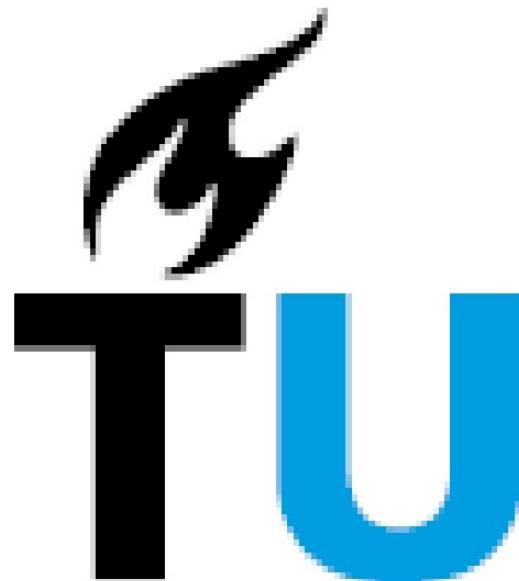
- Why does this work?



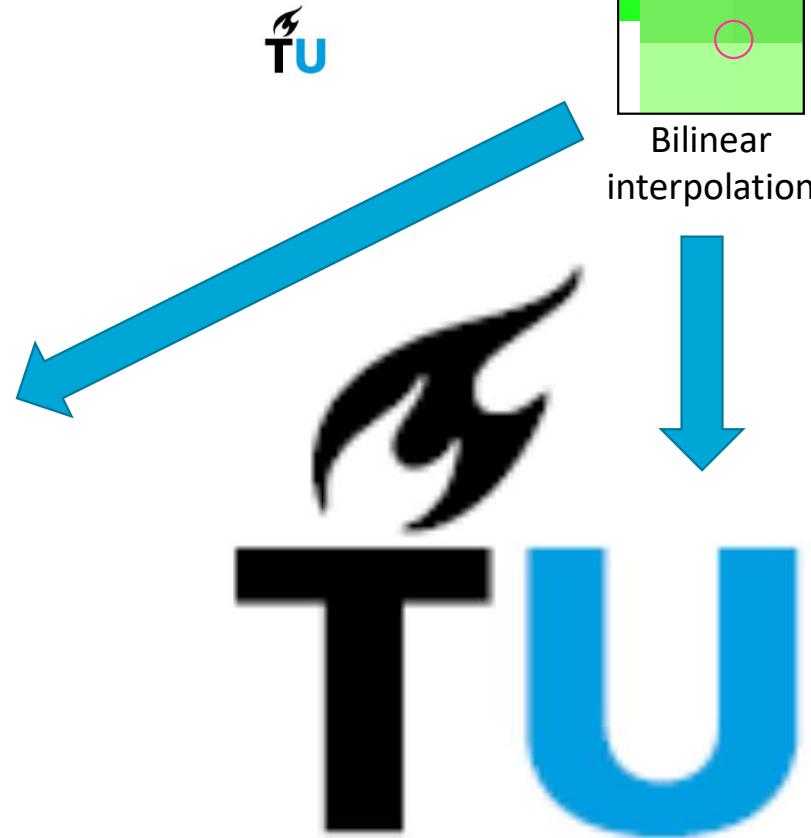
$$\begin{aligned}
 & ((1-\alpha) * \text{[Red]} + \alpha * \text{[Green]}) * (1-\beta) + \\
 & ((1-\alpha) * \text{[Blue]} + \alpha * \text{[Purple]}) * \beta
 \end{aligned}$$

1. Oversampling

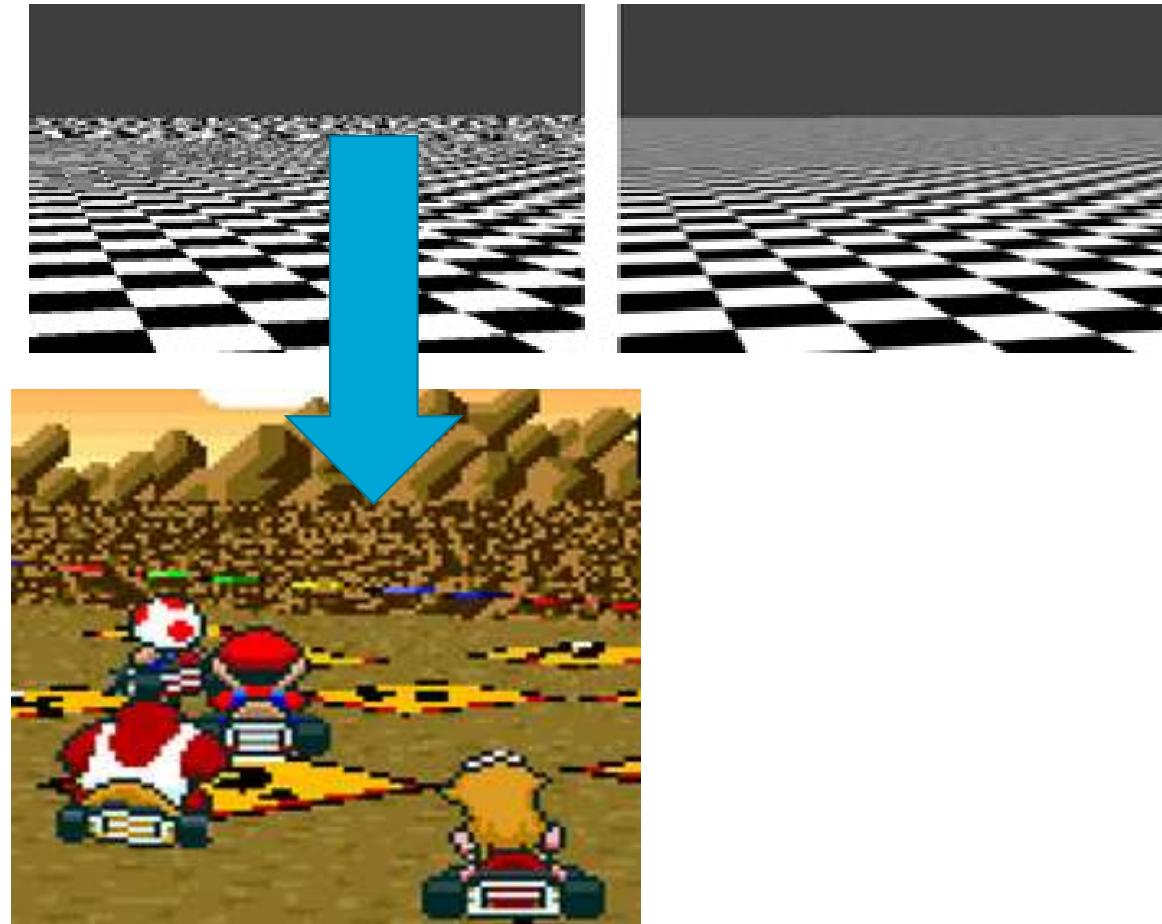
- Pixel smaller than texel



Nearest Neighbor

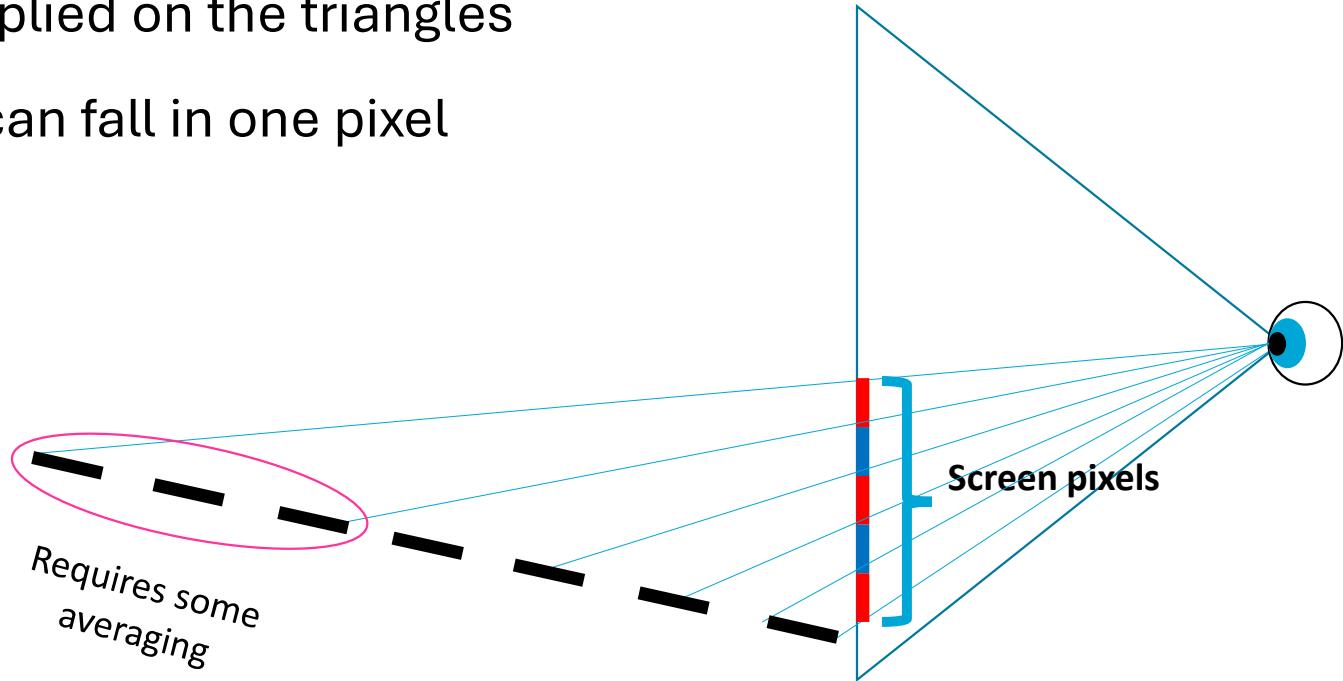


2. Undersampling



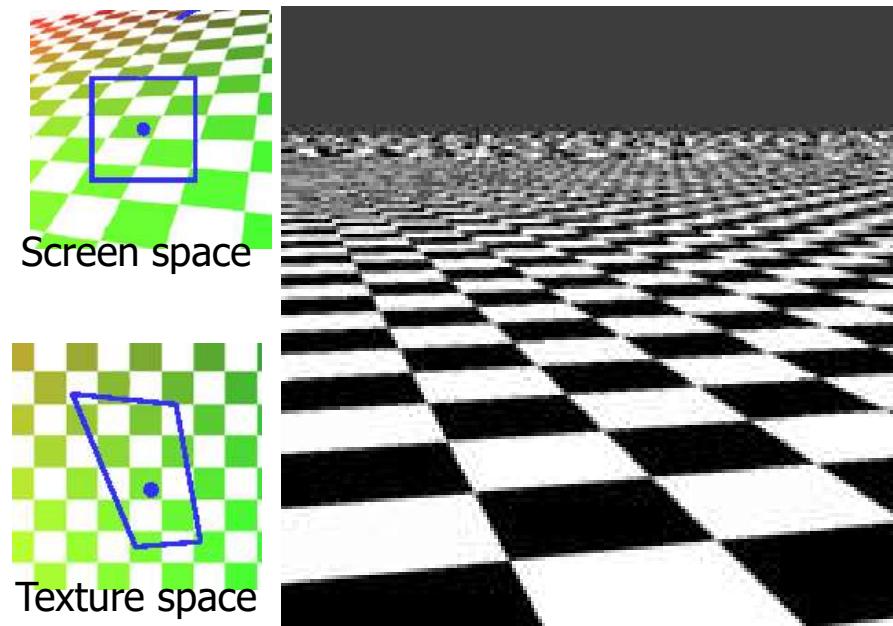
2. Undersampling

- Textures are applied on the triangles
- Several texels can fall in one pixel



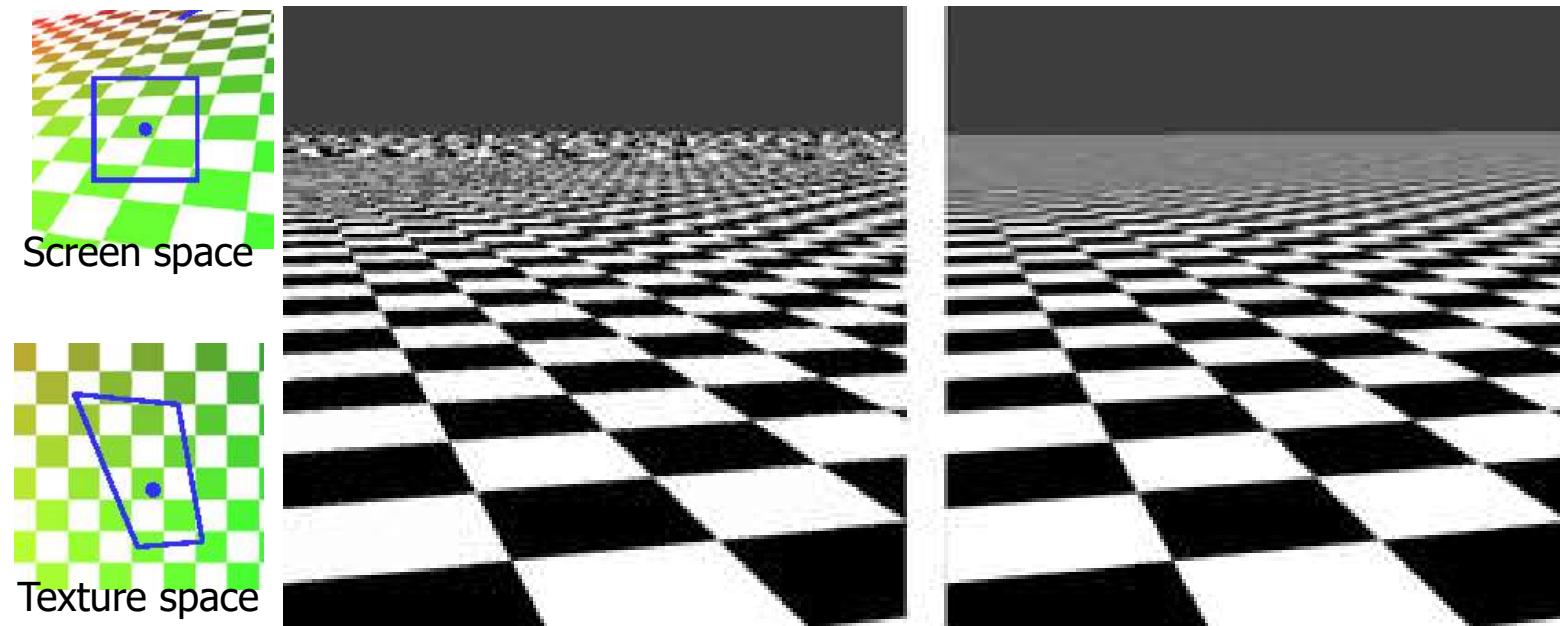
2. Undersampling

- One screen pixel does not necessarily correspond to one texel



2. Undersampling

- One screen pixel does not necessarily correspond to one texel



2. Undersampling

- Naïve solution:
Render at high resolution
then average the result



- Very costly....

MipMapping: Approximate Filtering

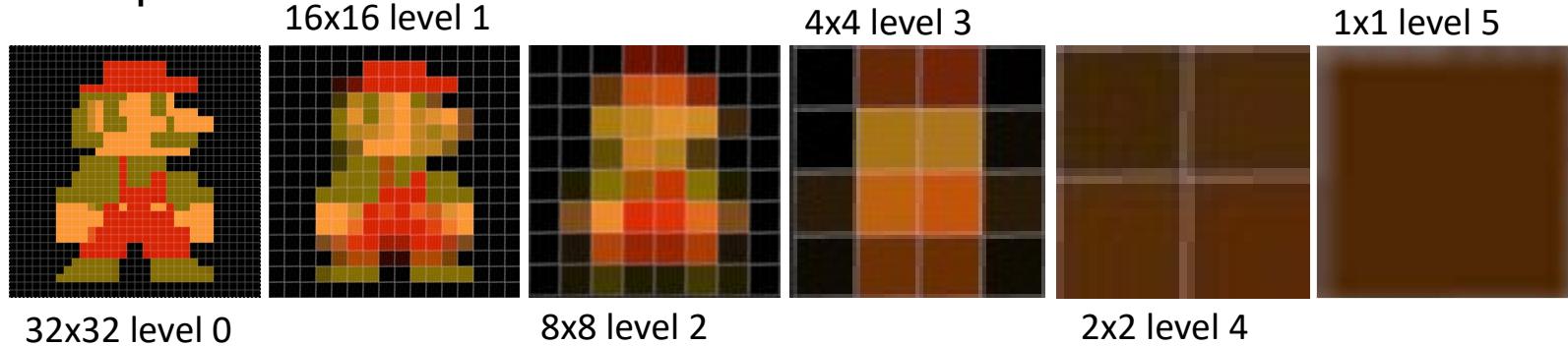
- **Mip** = *multum in parvo*



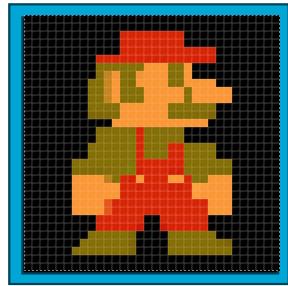
- meaning "much in little"

MipMapping: Approximate Filtering

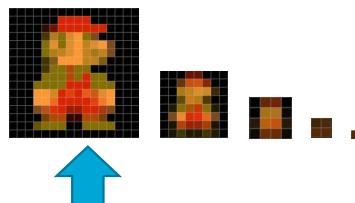
- Idea: Compute a filtered texture beforehand



Imagine
A 32x32
screen



Choose the correct level depending on pixel-to-texel matching



e.g., 4 texels per pixel

MipMapping: Approximate Filtering

- Precompute *Mipmap pyramid*:
 - *Hierarchical texture*
 - *Reduce resolution by 2x2 on each level*

For example:

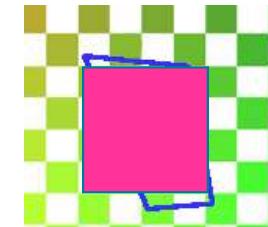
4x4 pixels covered



Then 16 lookups needed to average

Here: One pixel on LOD2 is a 4x4 pixel area in the original texture

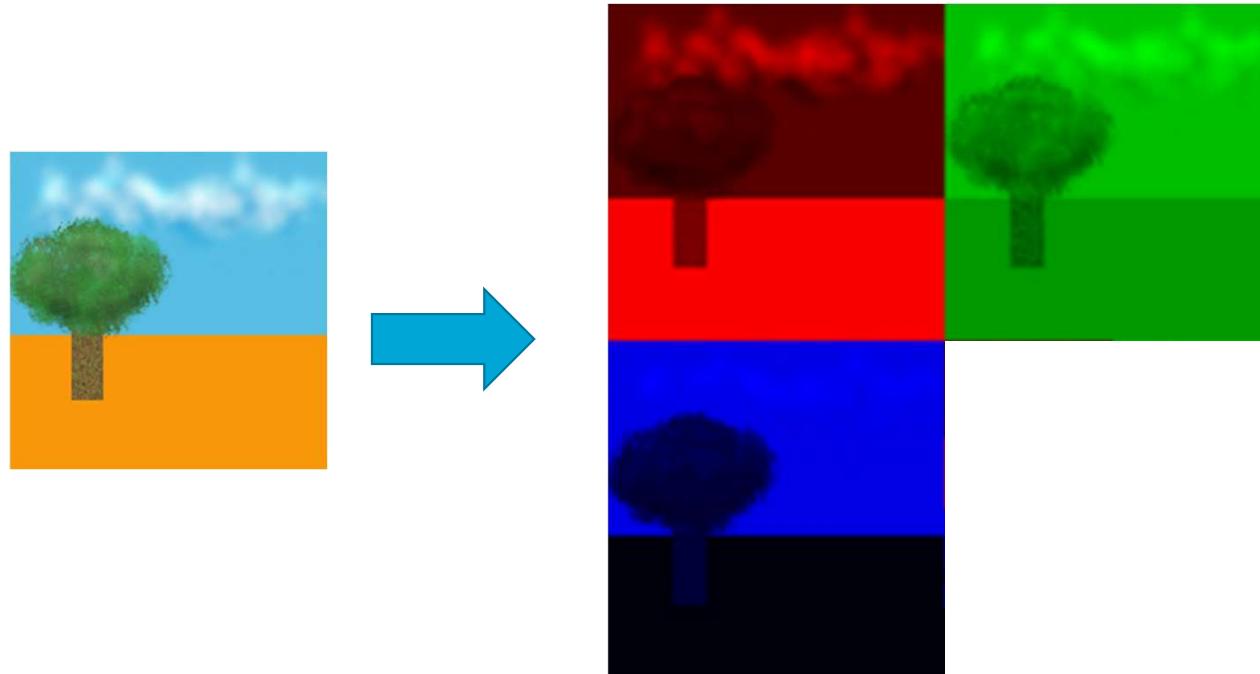
A single texture lookup is enough in LOD2.



Texture space
Per pixel,
approximate
region with a
square of size 2^k
 k is then the
mipmap level

MipMapping: Memory Requirements

- Visual Proof that it is $<1/3$ extra memory



MipMapping: Memory Requirements

- We assume memory of the original texture is 1
- Texture resolution $2^n \times 2^n$
- Then the memory cost for all mipmap levels is:

$$\begin{aligned} & \sum_{i=0}^n \left(\frac{1}{4}\right)^i \\ &= \frac{1 - 1/4^{n+1}}{1 - 1/4} \\ &= \frac{4}{3}(1 - 1/4^{n+1}) \end{aligned}$$

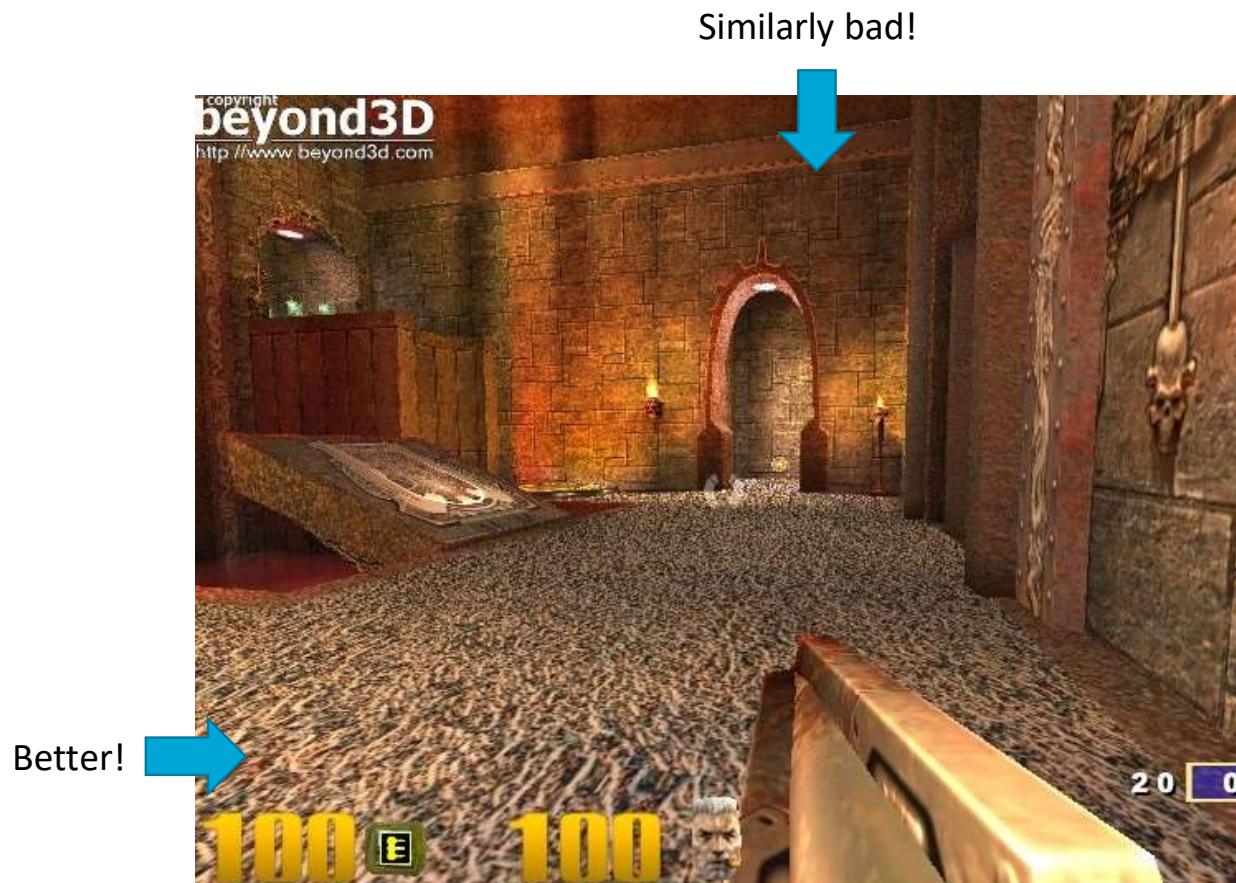
In the limit the cost is 1/3 higher.

MipMapping: OFF

- Just Nearest Neighbor looks noisy

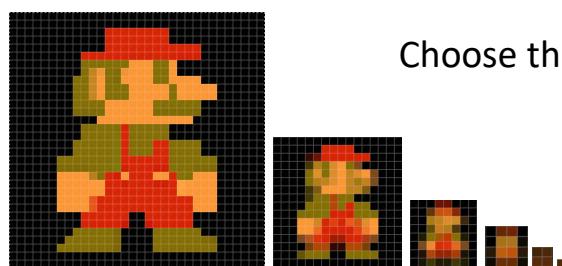
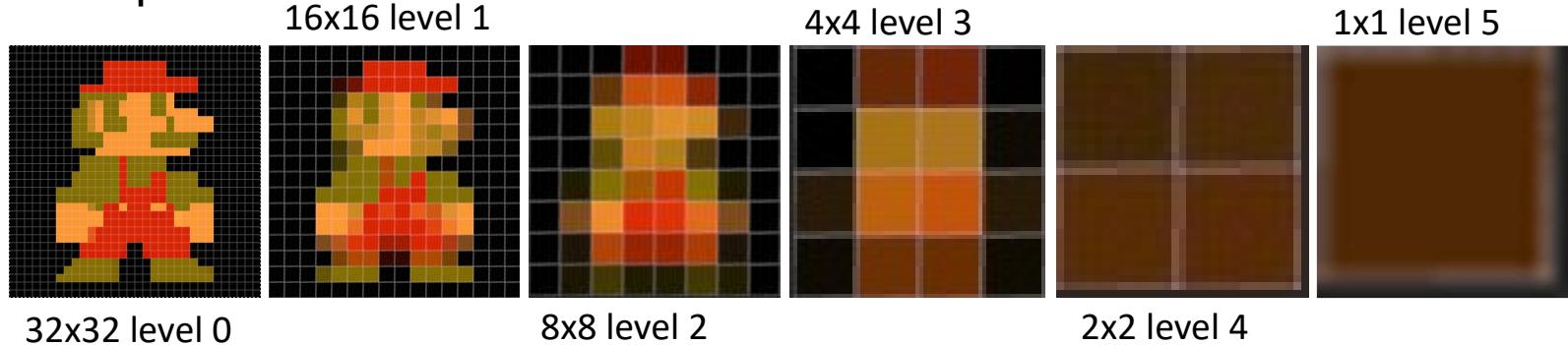


MipMapping: Off + Linear Filtering



MipMapping: Approximate Filtering

- Idea: Compute a filtered texture beforehand



Choose the correct level depending on pixel-to-texel matching

MipMapping On (use nearest level)

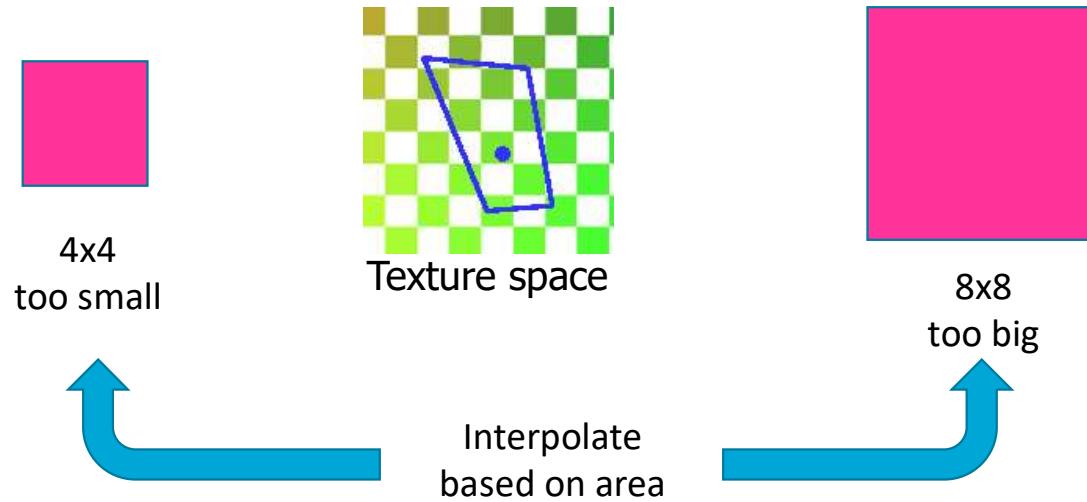
- Discontinuities at jumps from one level to next
Much nicer!

Bad: Different levels visible!



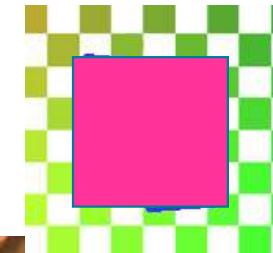
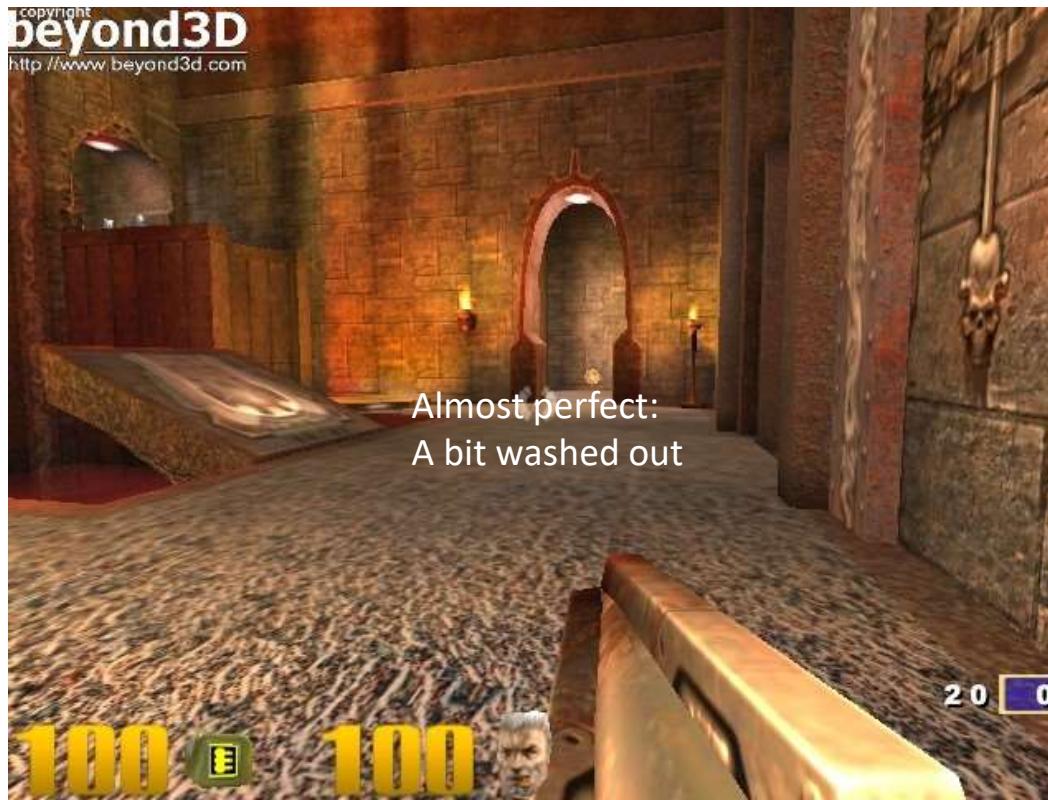
MipMapping

- Discontinuities come from changing region size



MipMapping: TriLinear Filtering

- Blend (mix) between different levels

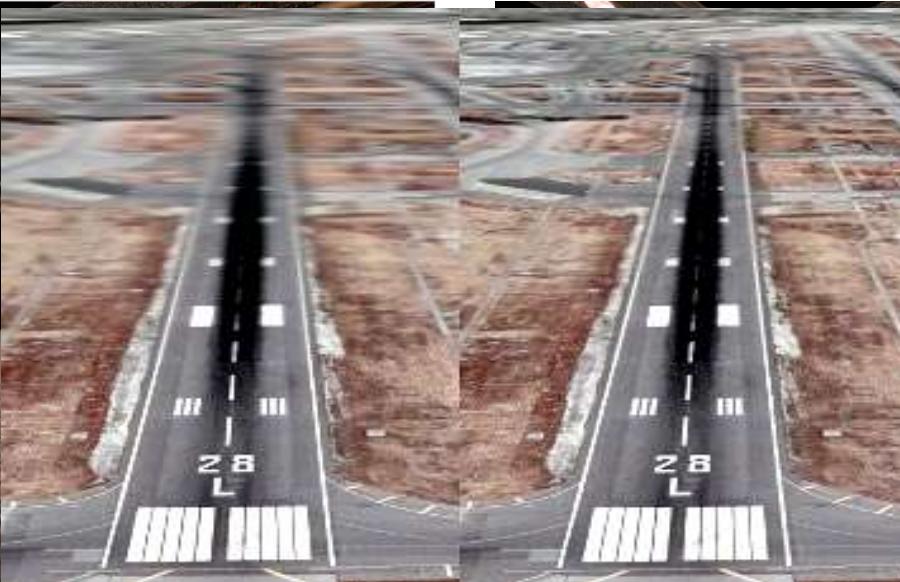


Anisotropic: Comparison

MipMapping



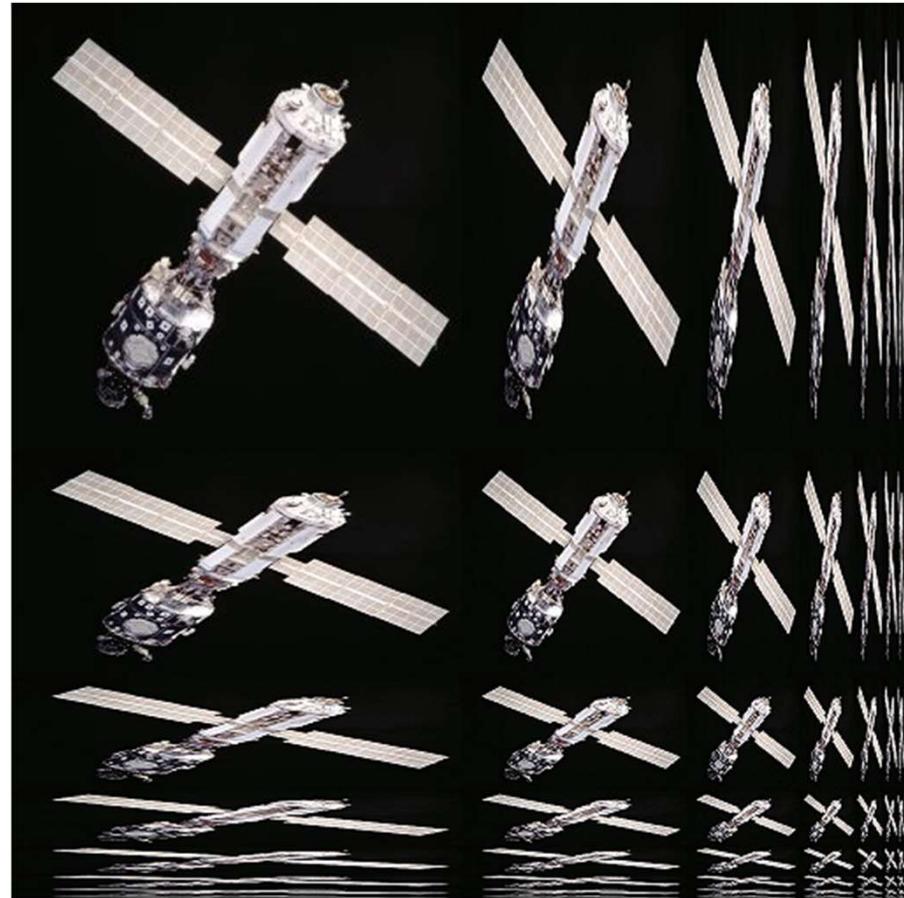
Anisotropic



- Better approximates
pixel projection in texture

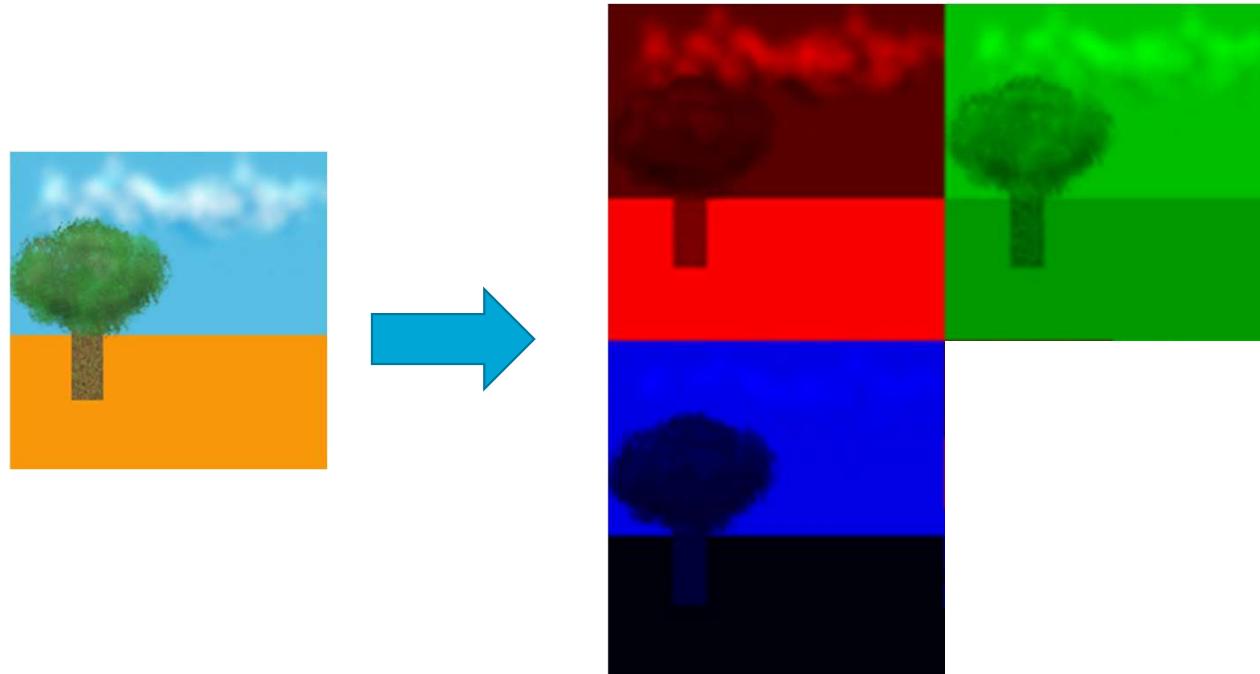
Anisotropic MipMaps

- Storage:
 - Power of two scaling on each axis
 - Fits into 4 times original memory

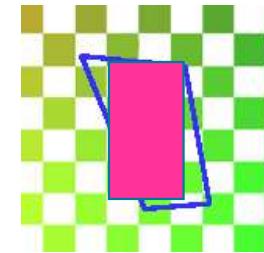


MipMapping: Memory Requirements

- Visual Proof that it is $<1/3$ extra memory

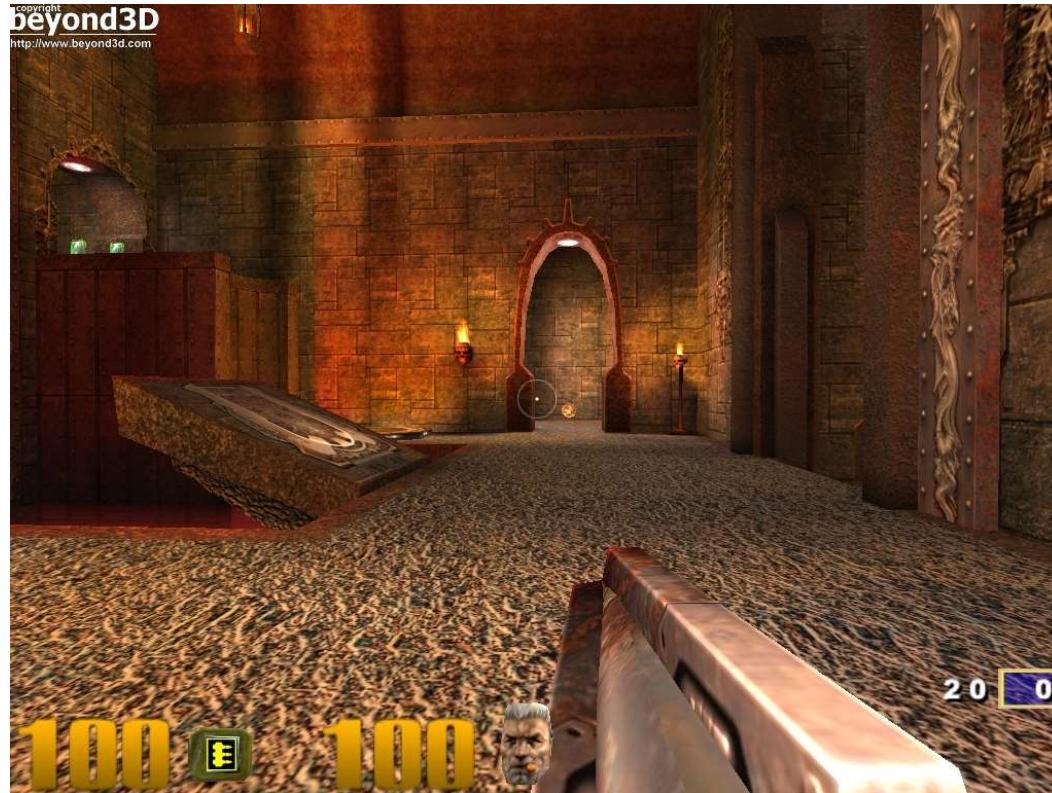


Anisotropic Filtering



- Better approximate real region

Beautiful!



Textures

- Image content mapped on surfaces
- Increase detail level without geometric cost
- Many applications for color textures



Questions?



Advanced Texture Representations

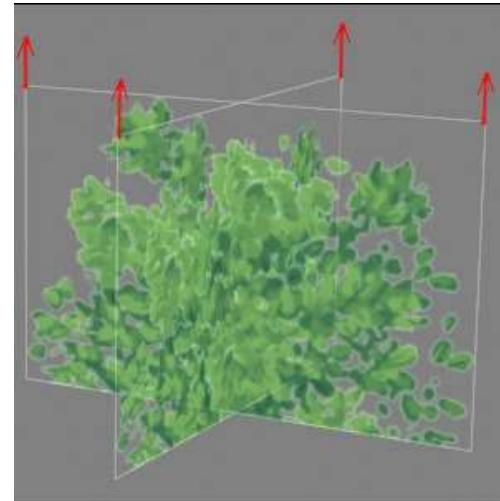
- Texture Data can represent more than just colors of an image
- Modern definition:
A texture stores values associated to a domain

Advanced Texture Representations

- Texture Data can represent more than just colors of an image
- Modern definition:
A texture stores **values** associated to a domain

Alpha Blending

- Used to create transparency effects
- Textures can have (R,G,B,A) values:
 - If $A=0$: texel is considered transparent – not drawn
 - If $A=1$: texel is drawn

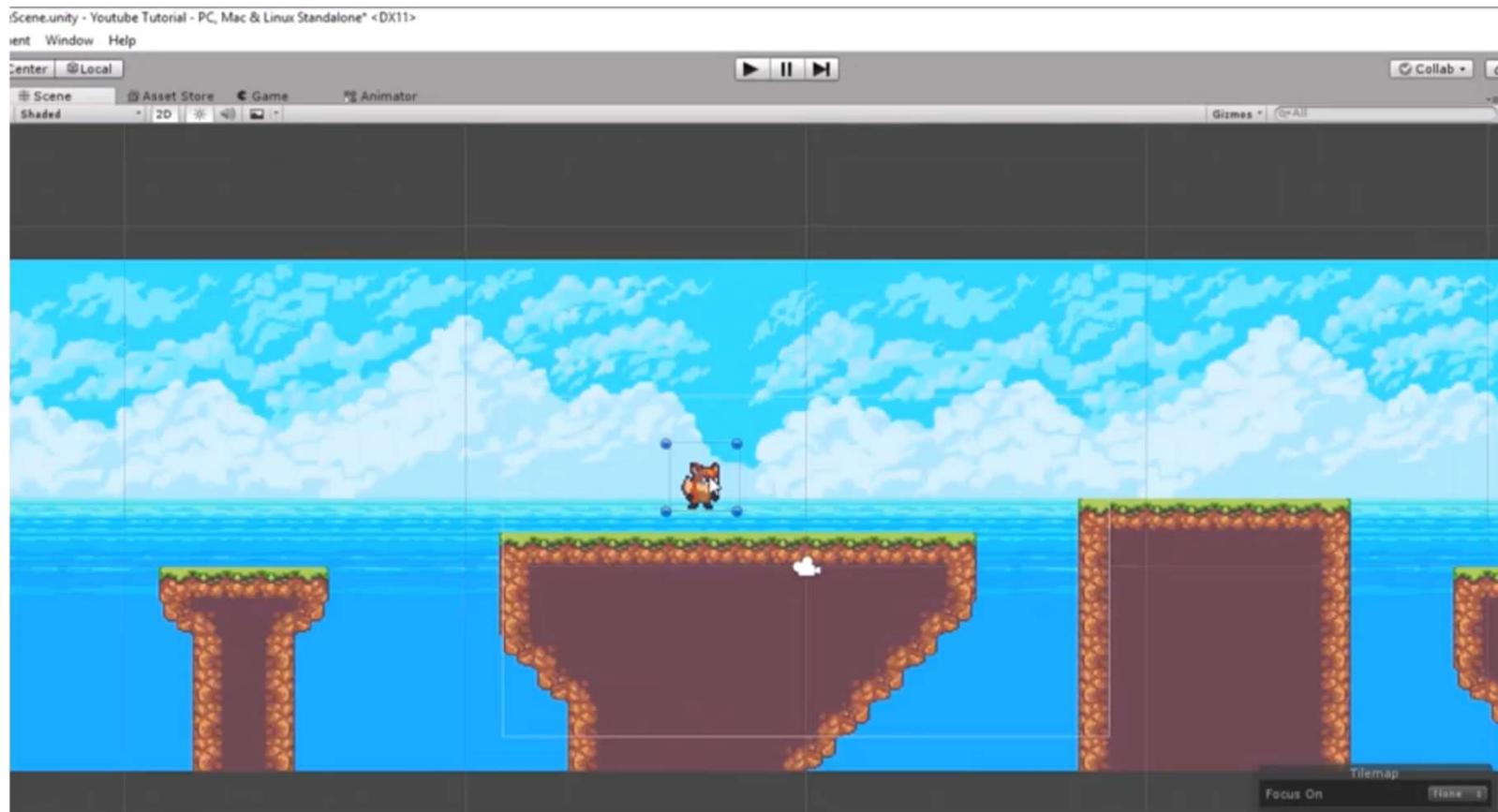


Alpha Blending - Stacked Polygons



- Source: irrlicht engine, artplants.blogspot.com

Alpha Blending - Sprites (here Unity)



Use pixel discard based on alpha to make the object background transparent

Alpha Blending - Water Particles

- Textured quads used as water particles



Advanced Texture Representations

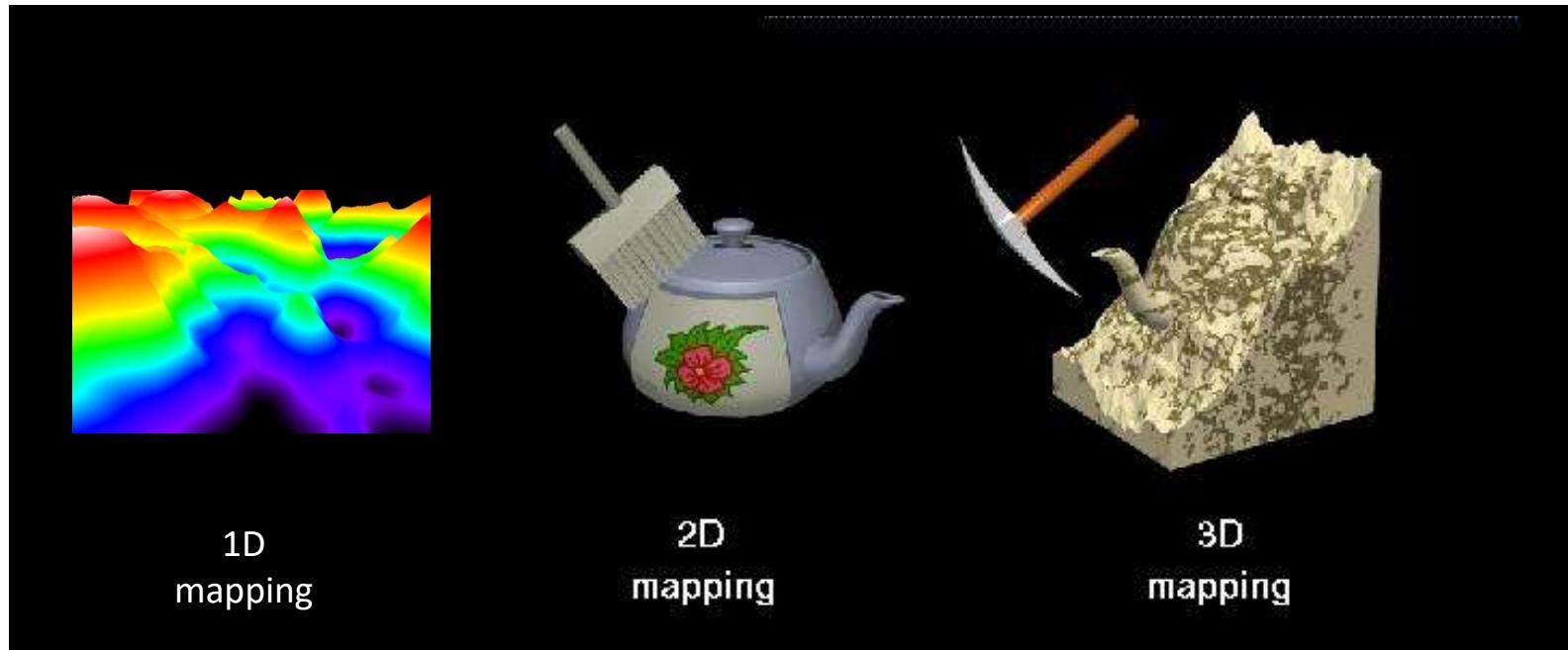
- Texture Data can represent more than just colors of an image

- Modern definition:
A texture stores values associated to a **domain**

domain is accessed via the texture coordinates

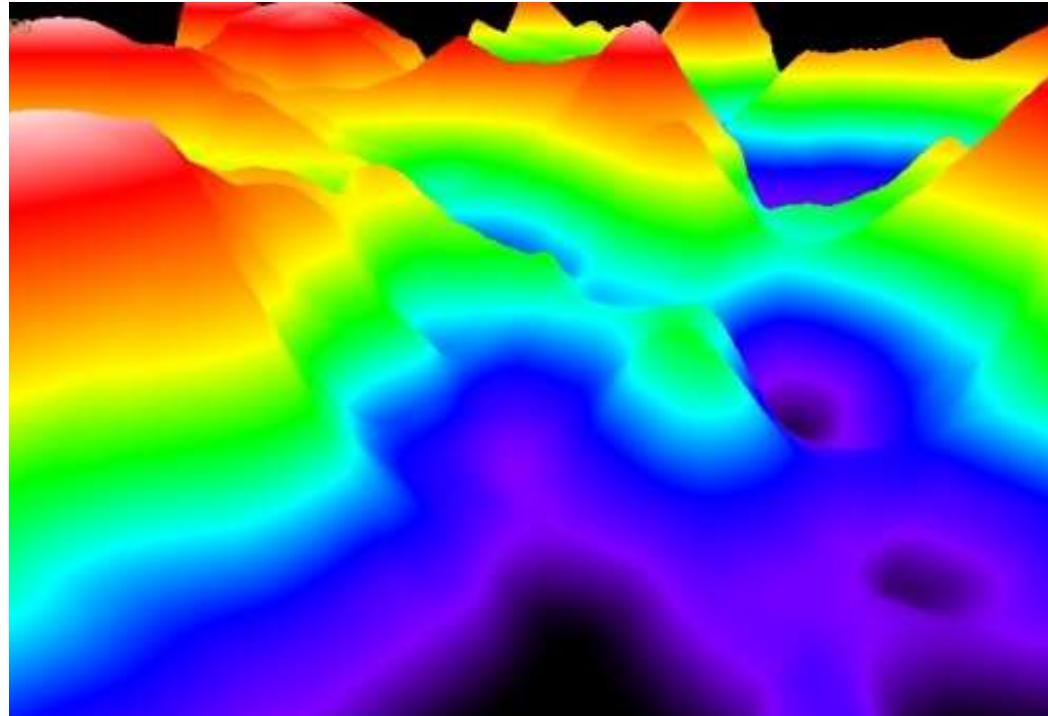
Advanced Texture Representations

- Different domain dimensions
- Texture coordinates can be 1D, 2D, 3D...
GPUs provide native support up to 3D



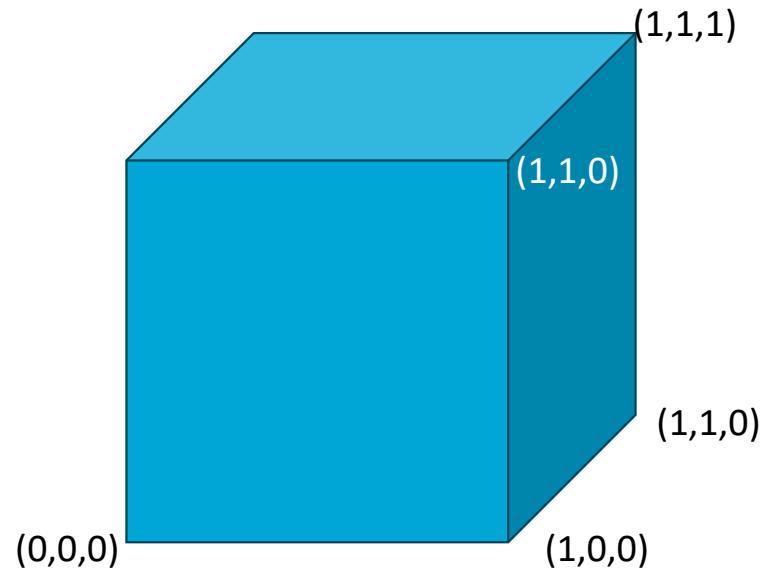
1D Textures

- We can theoretically use a 1-pixel wide 2D Texture via `glTexCoord2f(0,z)`.
- A 1D Texture always has 1-pixel width. Access with `glTexCoord1f(z)`.



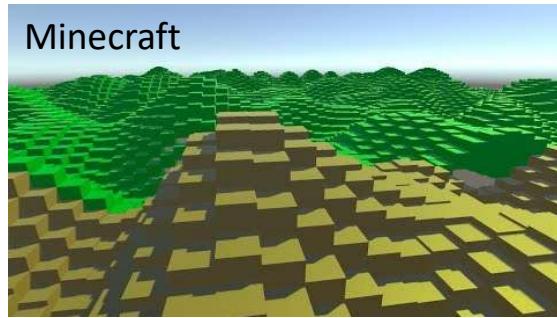
What are 3D Textures?

- They are accessed with 3 texture coordinates (u,v,w)
- Bilinear interpolation in 2D textures becomes trilinear with 3D textures



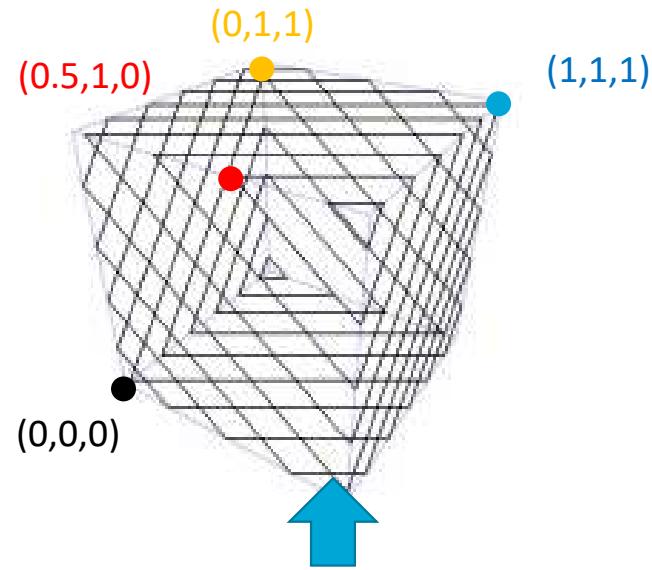
3D Textures are Volumes

- The equivalent of a texels is a small cubic volume (**volume element=voxel**)



Volume Rendering

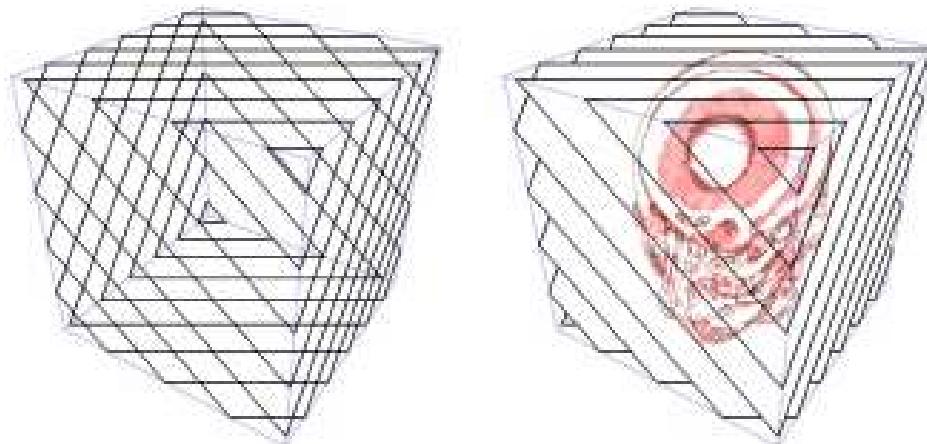
- How to render volumes?
 - One often-employed method is slicing



Draw slices with 3D texture coordinates
corresponding to the position of the
vertices in the volume

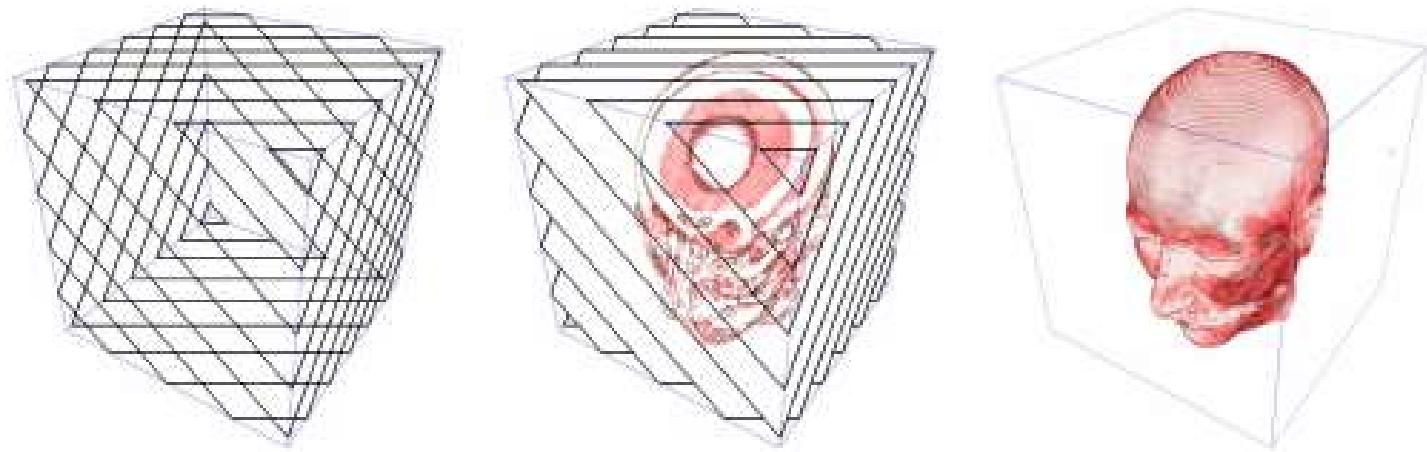
Volume Rendering

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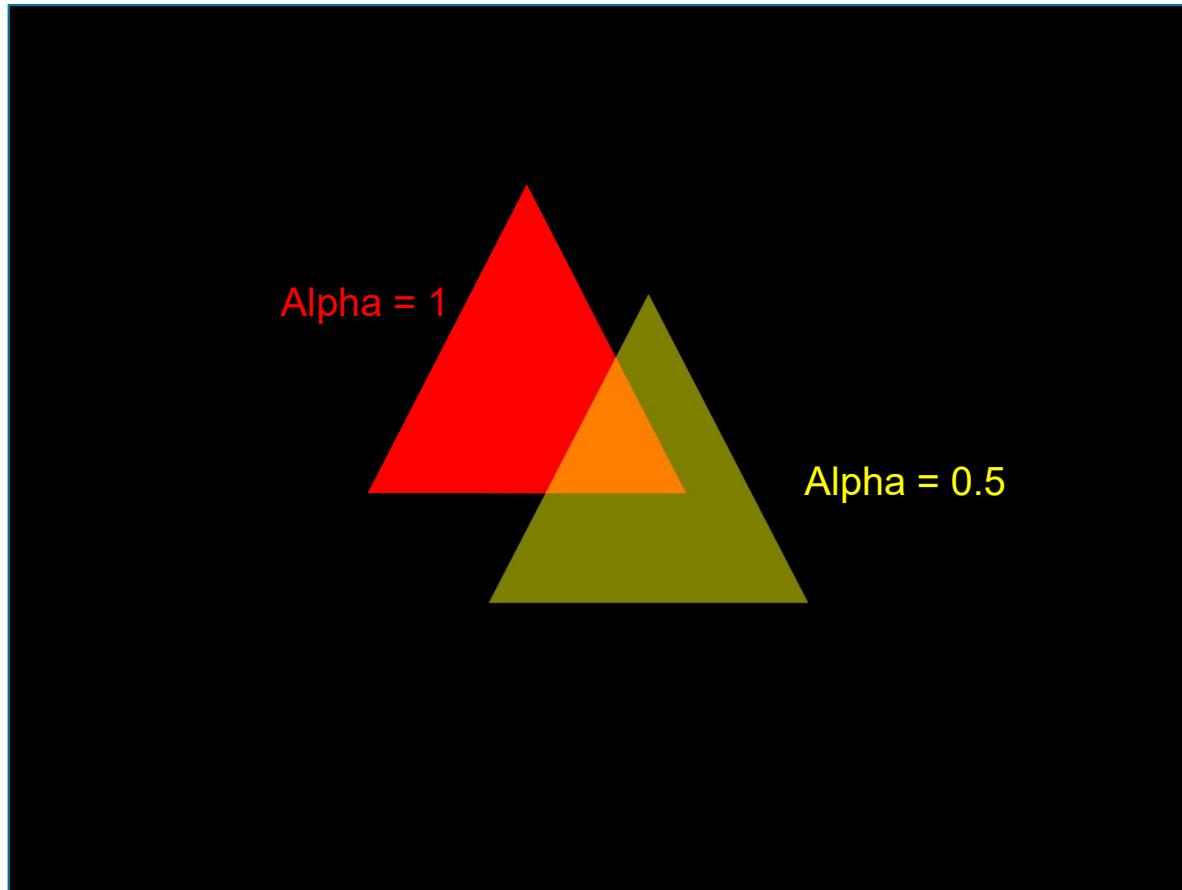
Volume Rendering

- How to render volumes?
 - One often-employed method is slicing



But wait? Why are there parts that are transparent?

Alpha Blending

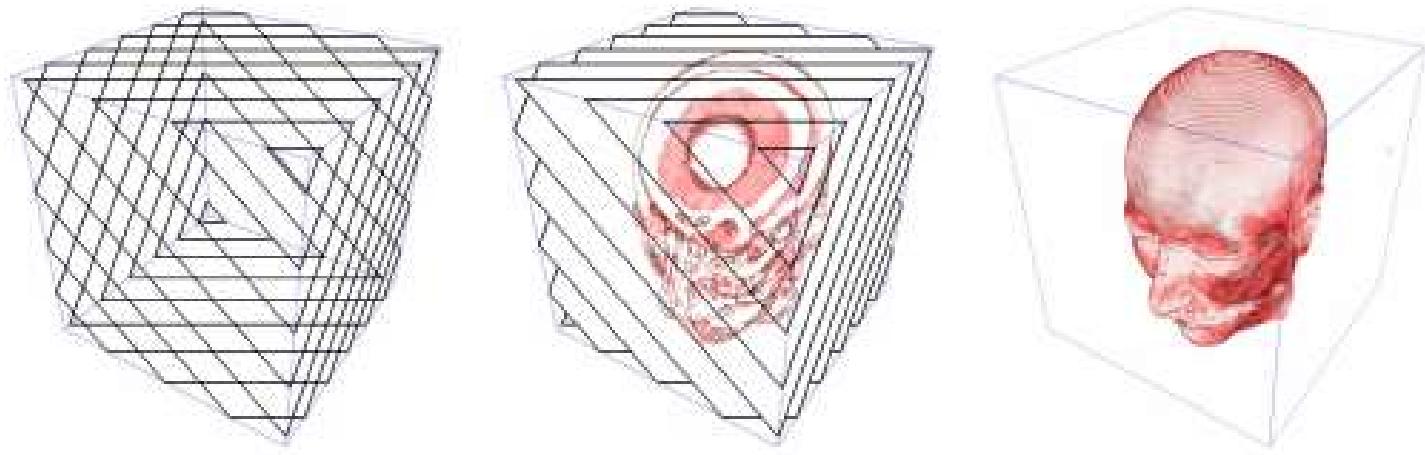


Standard Alpha Blending

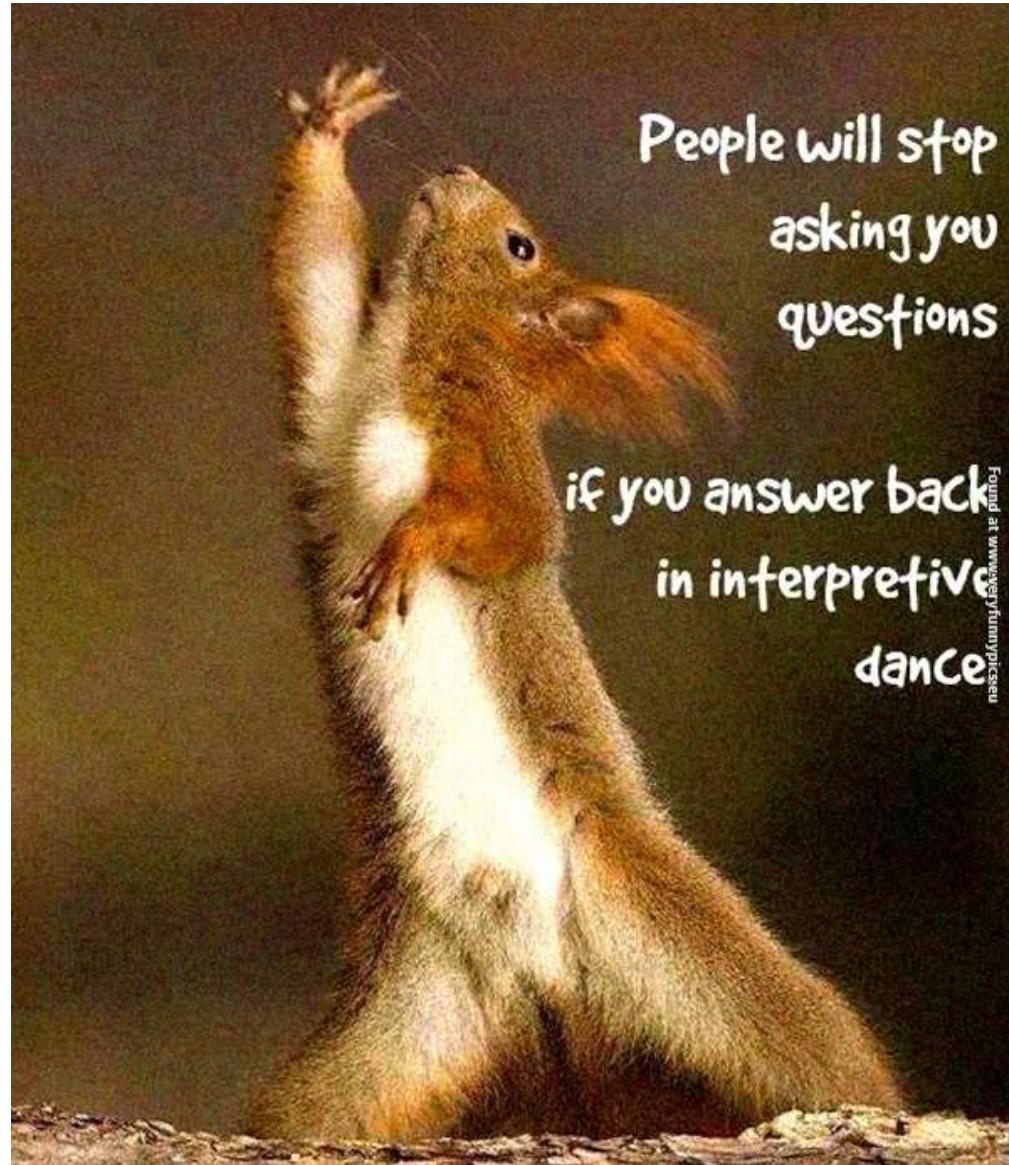
- Color with four components: RGB and an alpha value
- Alpha describes the “opacity”
 - 0 : object is completely transparent
 - 1 : object is completely opaque
 - 0.5: 50% of the stored color and 50% background
- In general, drawn (R, G, B, A) and in a pixel with color (R_B, G_B, B_B) results in:
$$A * RGB + (1 - A) * R_B G_B B_B$$

Volume Rendering

- One often-employed method is slicing



Questions?



Advanced Texture Use-Cases

- Encode material properties
- Approximate the environment
- Represent Geometry
- Encode complex functions

Last of Us on PS1



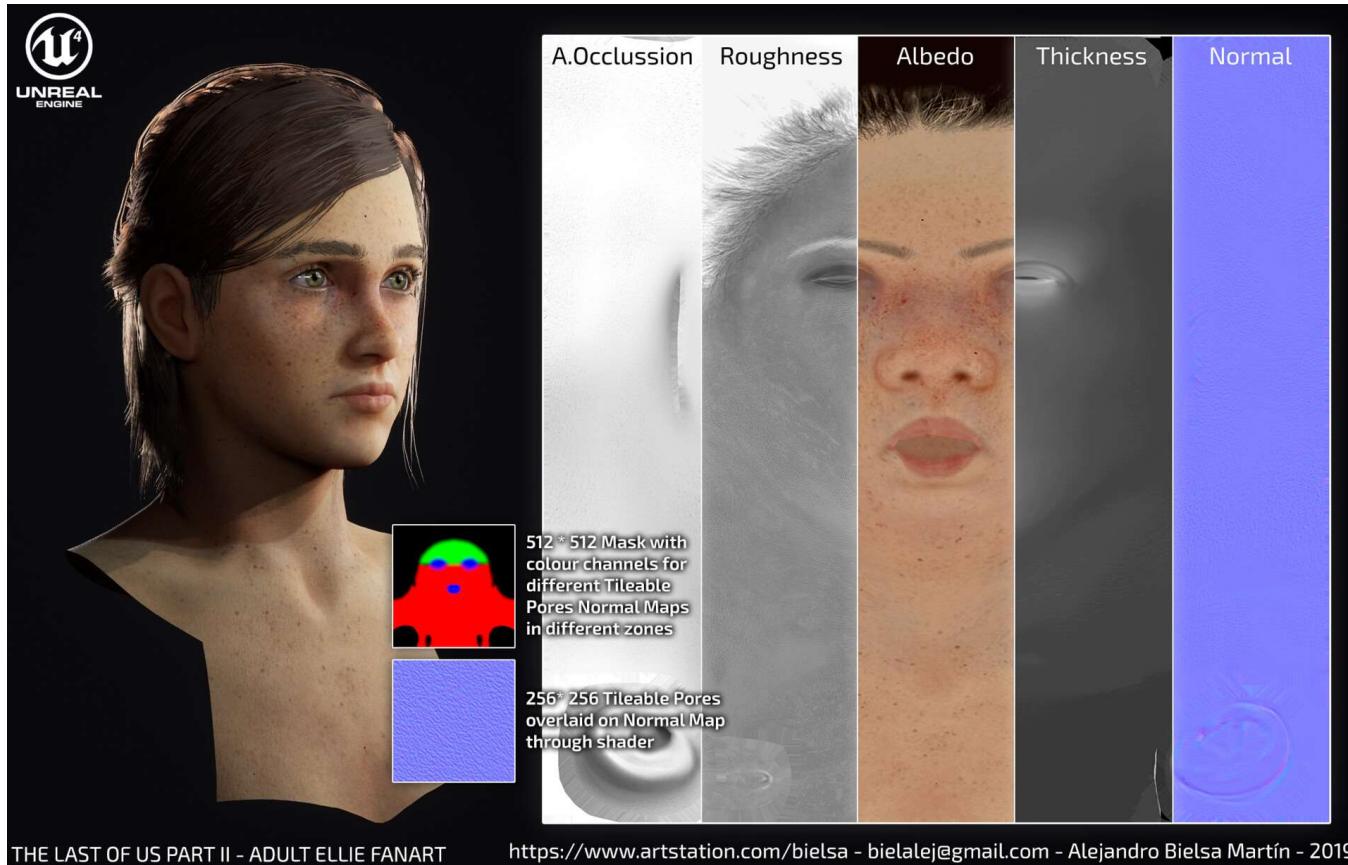
Last of Us on PS1



Last of Us 2

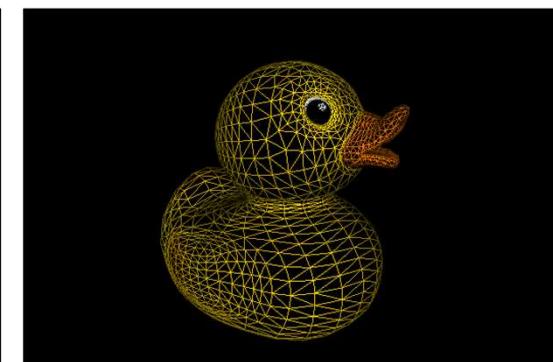
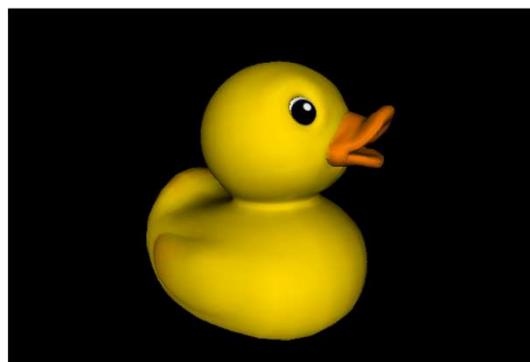
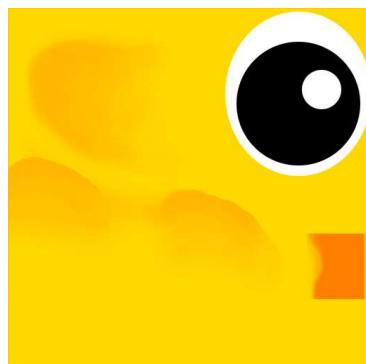
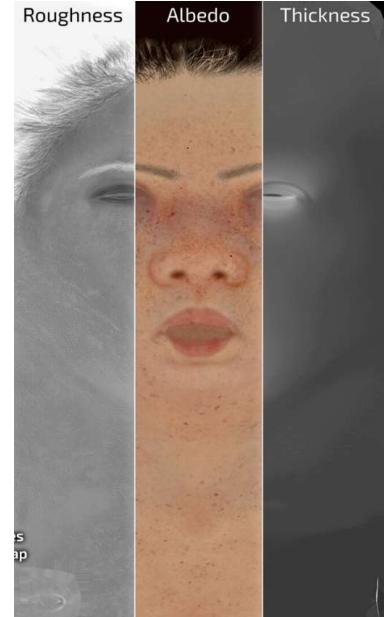


Professional Example

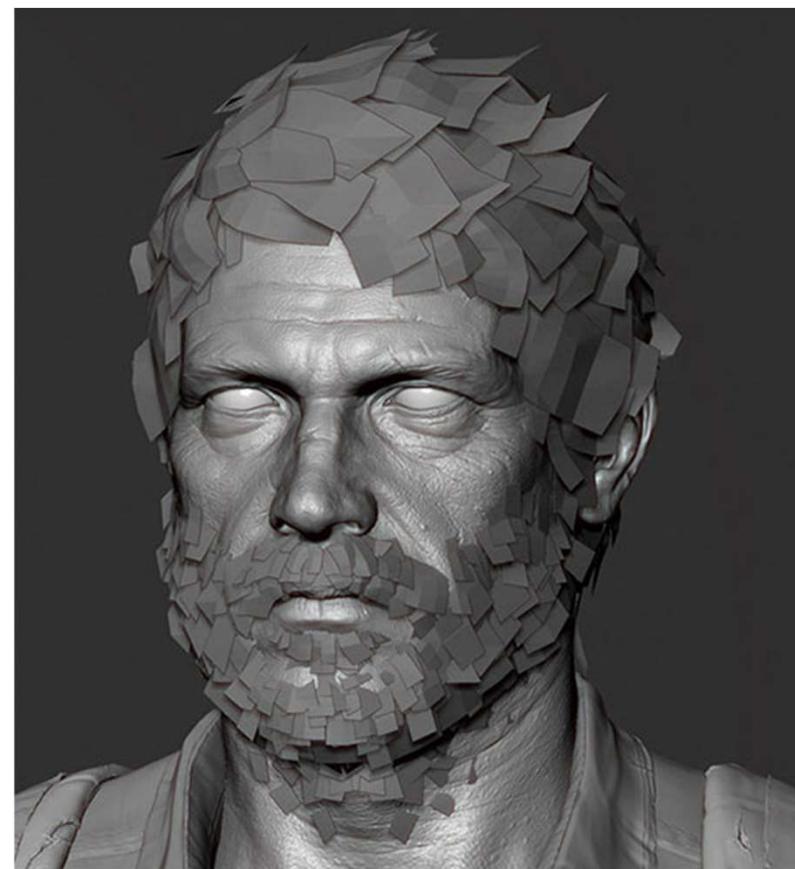


Textures: Materials

- Can be used to provide, e.g.,
 - parameters for material models
(ambient, diffuse...)



Alpha Blending - Hair

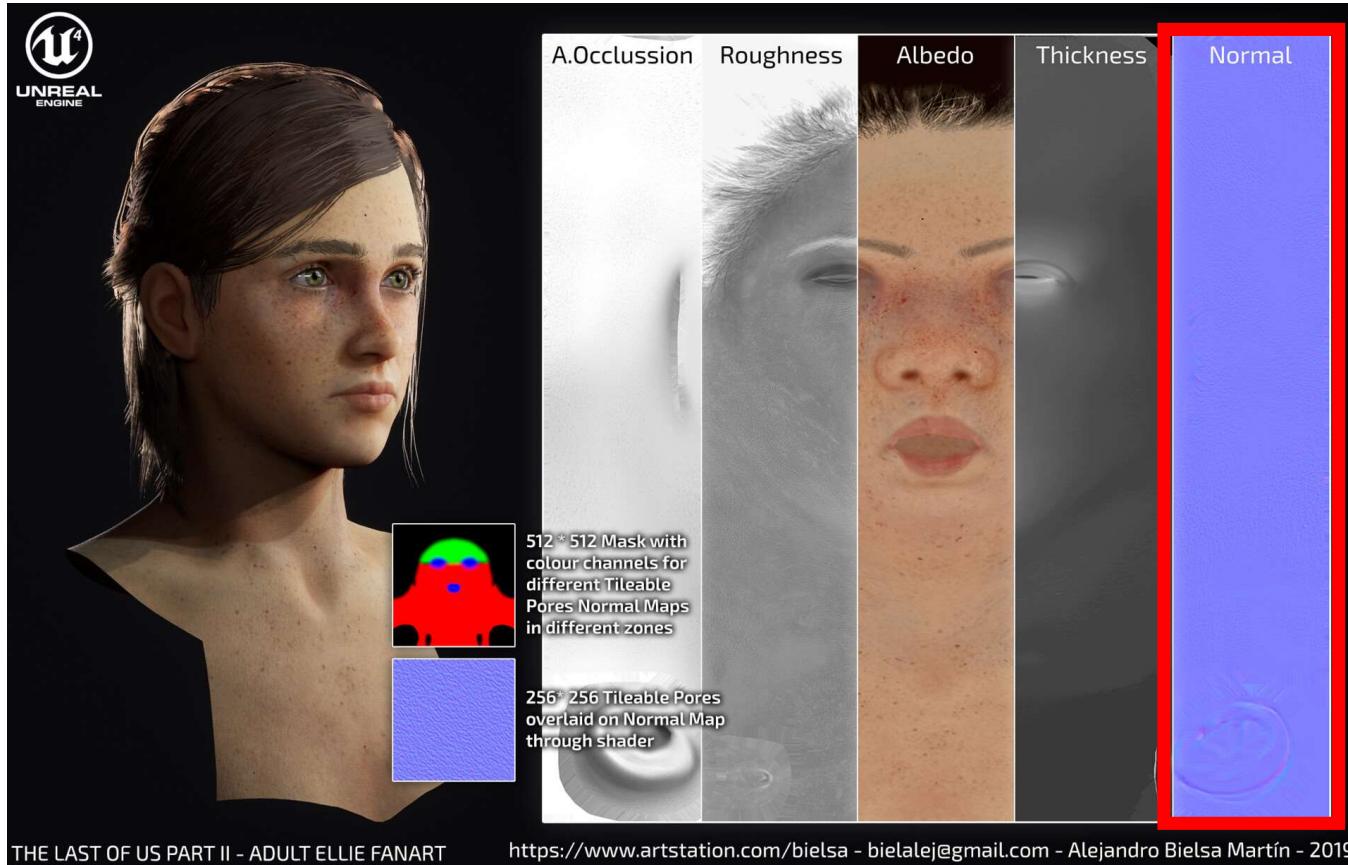


Alpha Blending - Hair



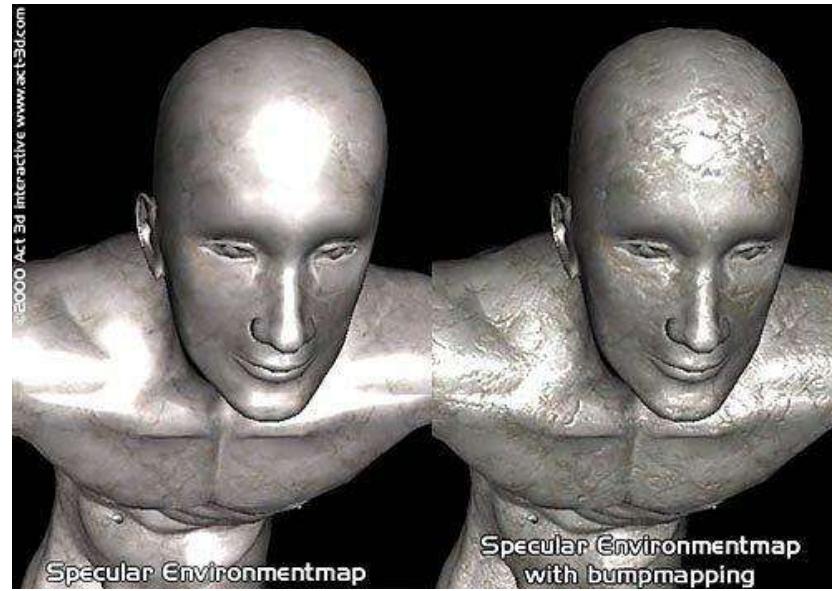
Last of us

Professional Example



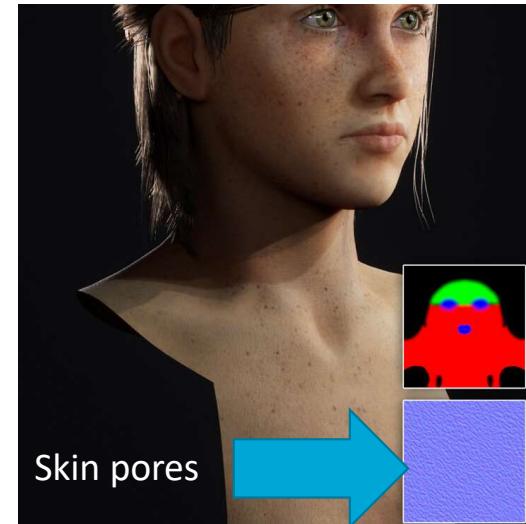
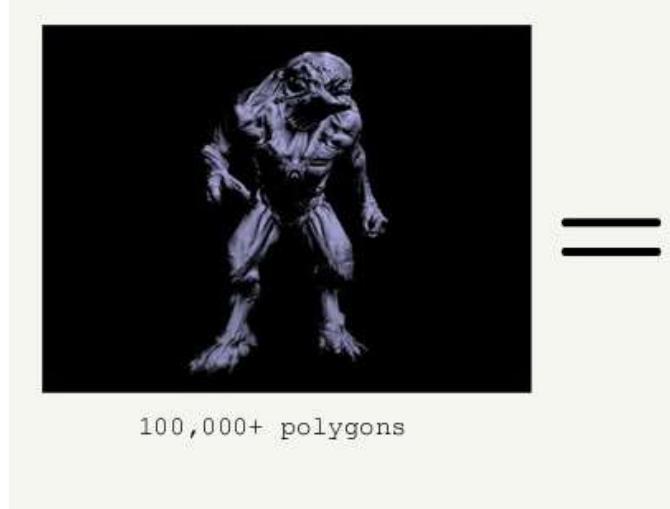
Textures

- Can be used to provide, e.g.,
 - Colors for ambient/diffuse
 - Normals (*bump mapping*)

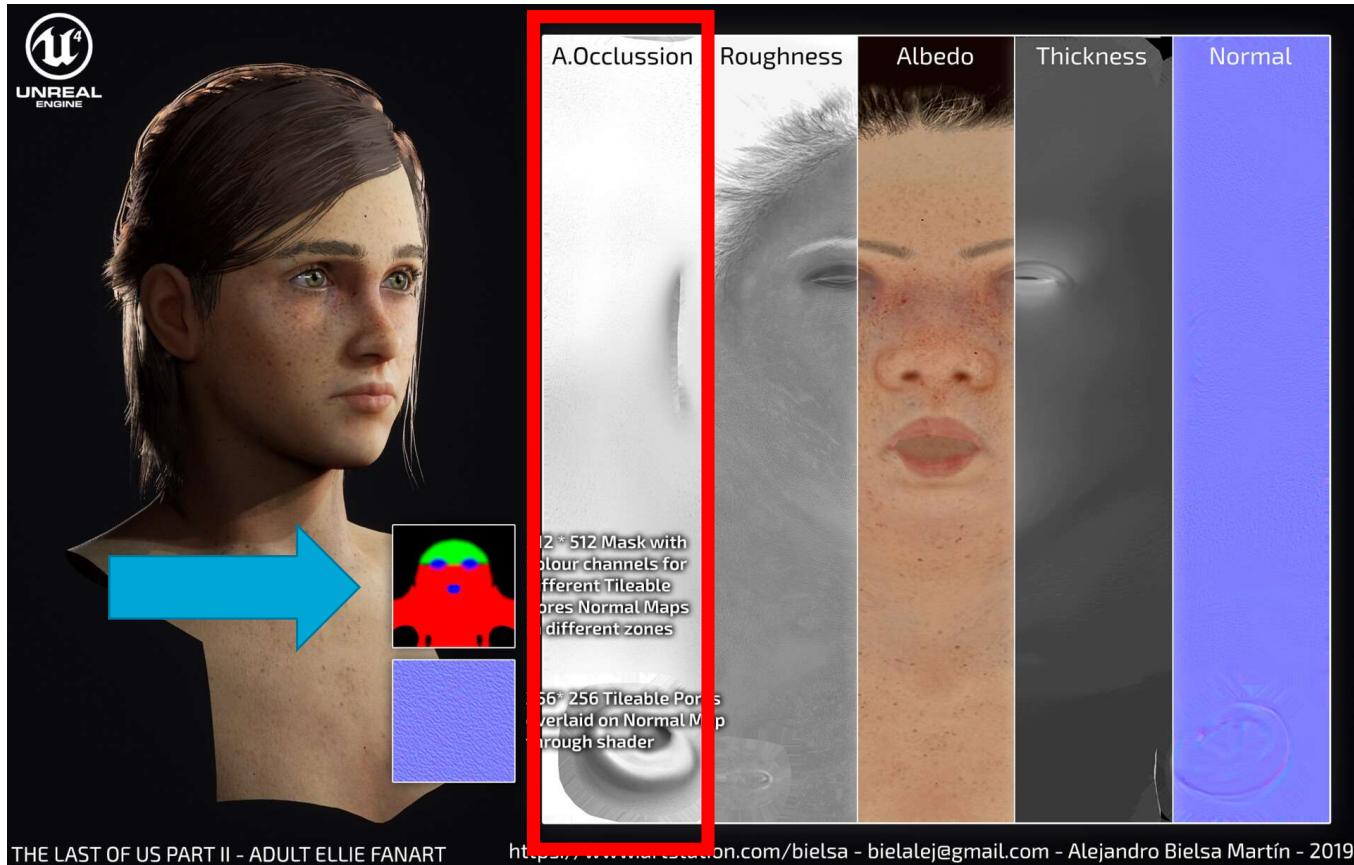


Textures

- Normal Mapping



Professional Example

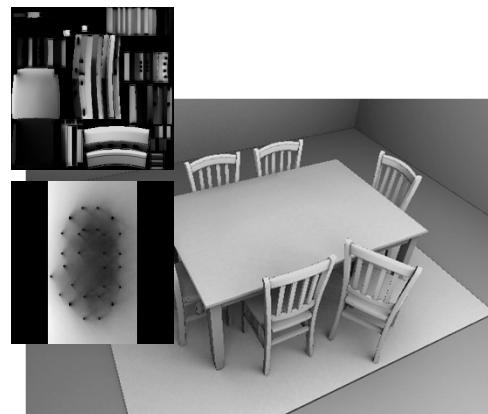


Textures

- Can be used to provide, e.g.,
 - Colors for ambient/diffuse
 - Normals (*bump mapping*)
 - Precomputed illumination (*light map*)



Diffuse mapped on scene



Lightmap mapped on scene



Combined

Textures

- Can be used to provide, e.g.,
 - Colors for ambient/diffuse
 - Normals (*bump mapping*)
 - Precomputed illumination (*light map*)

Quake – id Software



Materials

*



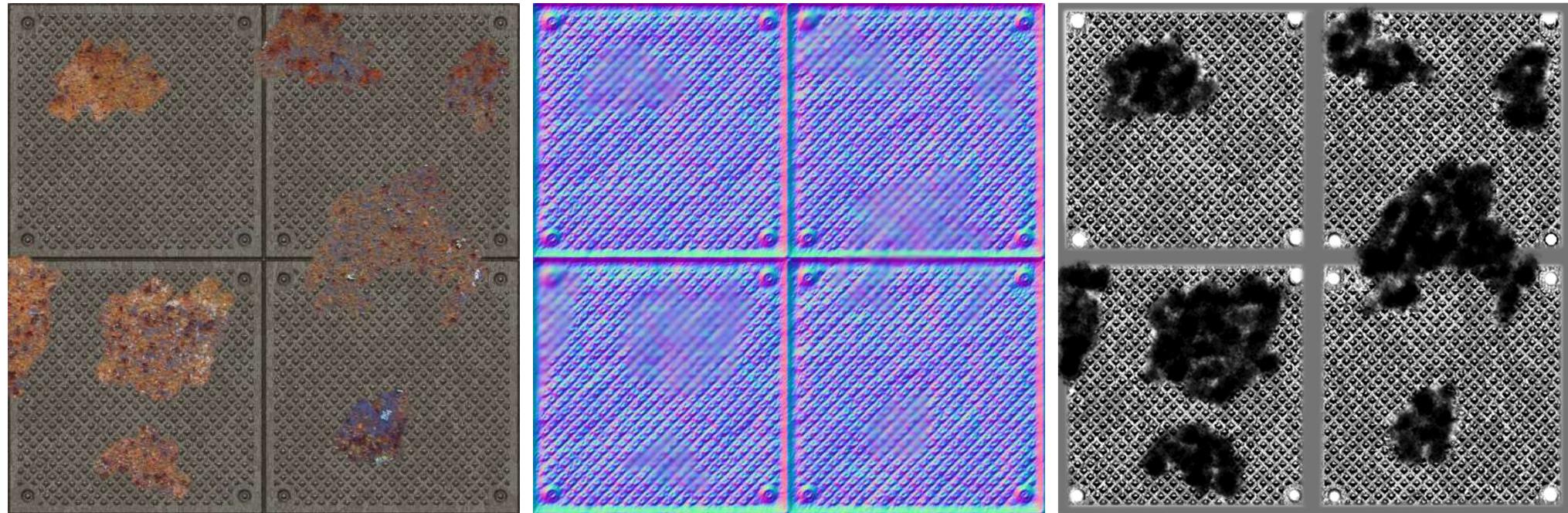
=

Light Map



Final result

Demo - Building a Corroded Metal Sheet



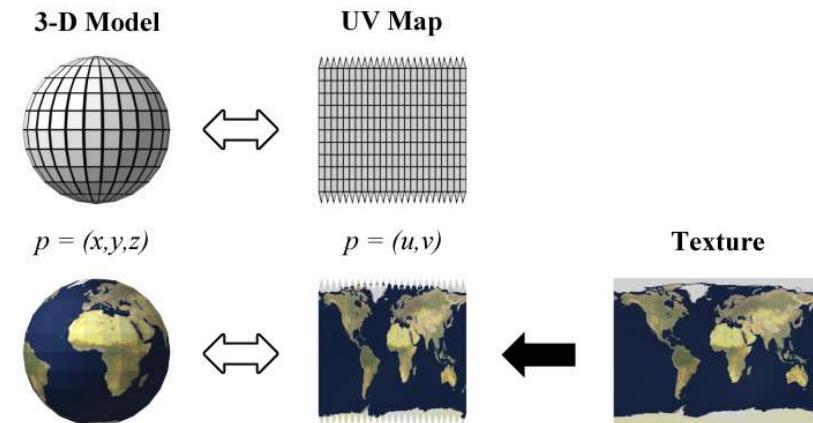
Advanced Texture Use-Cases

- Encode material properties
- **Approximate the environment**
- Represent Geometry
- Encode complex functions

Environment Mapping

- Textures can encode an environment
An environment map (approximation of scene)

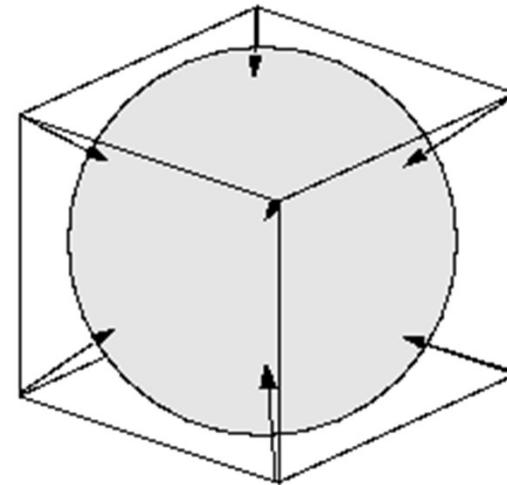
Spherical mapping



Environment Mapping

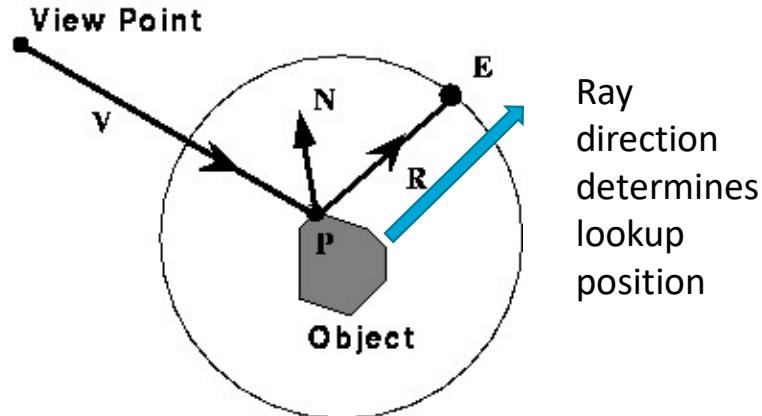
- Textures can encode an environment
An environment map (approximation of scene)

Cube mapping



Environment Mapping

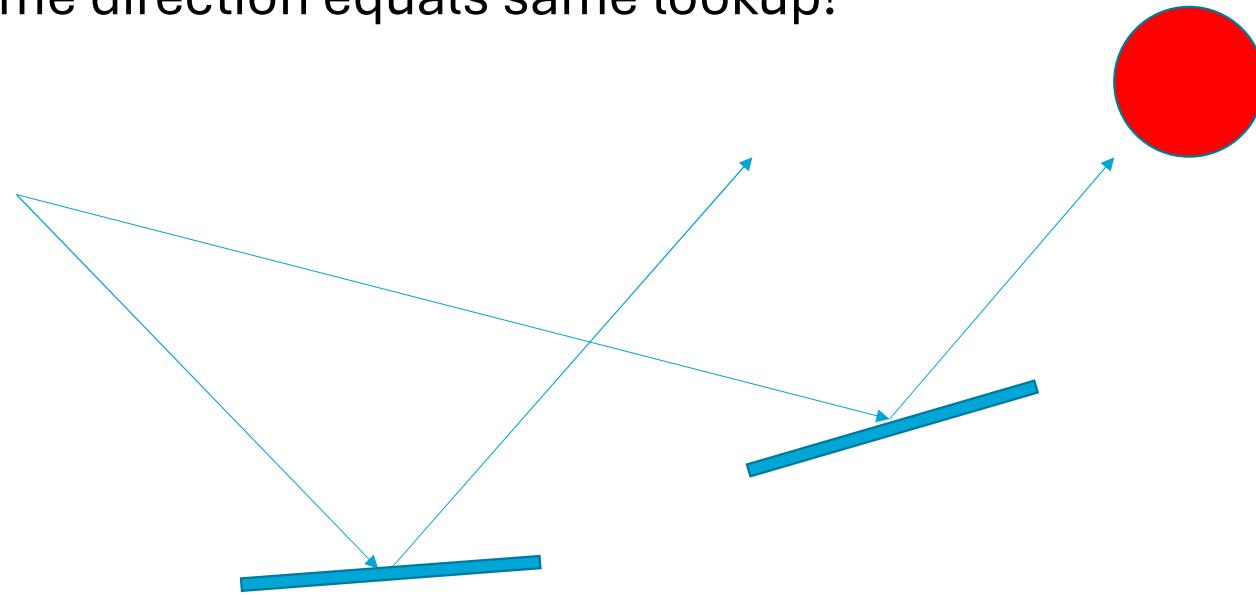
- Textures can encode an environment
An environment map (approximation of scene)
is useful for, e.g., reflections (texcoords = ray)



- This *environment mapping* is an approximation!

Environment Mapping

- Typical approximation:
Assume environment is infinitely far away.
Same direction equals same lookup!



- Red ball reflection seen by both or none.

Environment Mapping



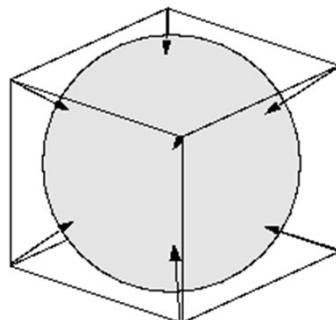
Not blown away yet?

- It is getting better!
- Textures can be dynamically created!



Dynamic Textures

Dynamic Cube map



[Hollaender et al. EGSR 2011]

Dynamic Textures

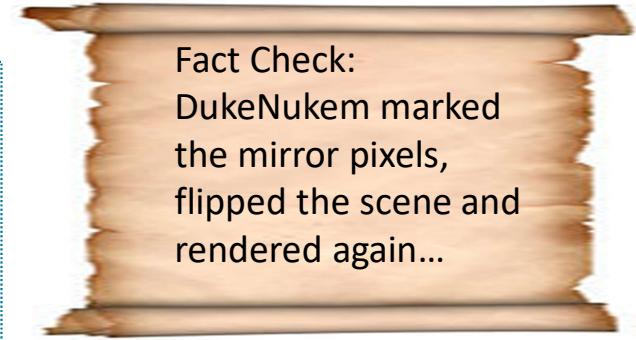
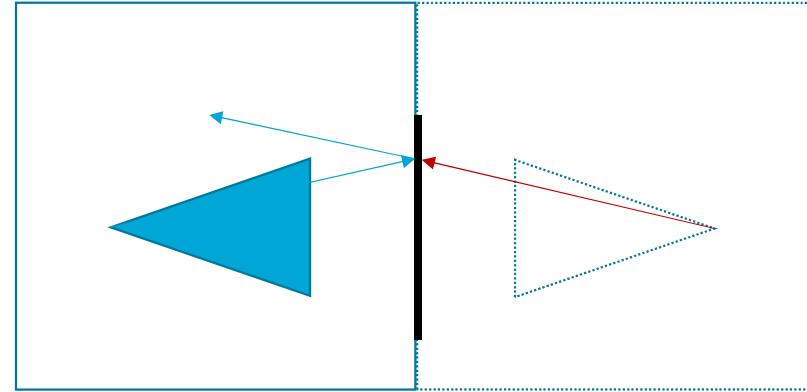
- Flat mirrors can be well simulated with textures



- Duke Nukem3D

Environment Mapping

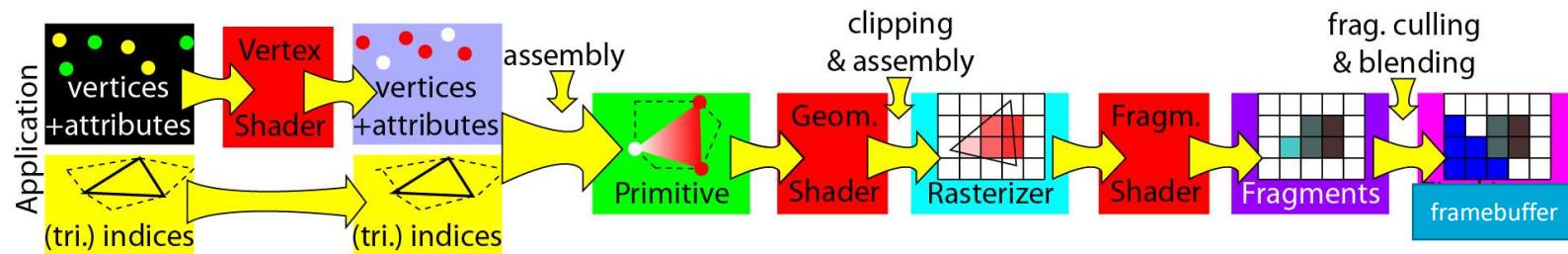
- Flat mirrors can be well simulated with textures



- Virtually flip camera center along mirror.
- Take an image from this virtual camera
- Apply image as a texture onto the mirror.

Render to a texture?

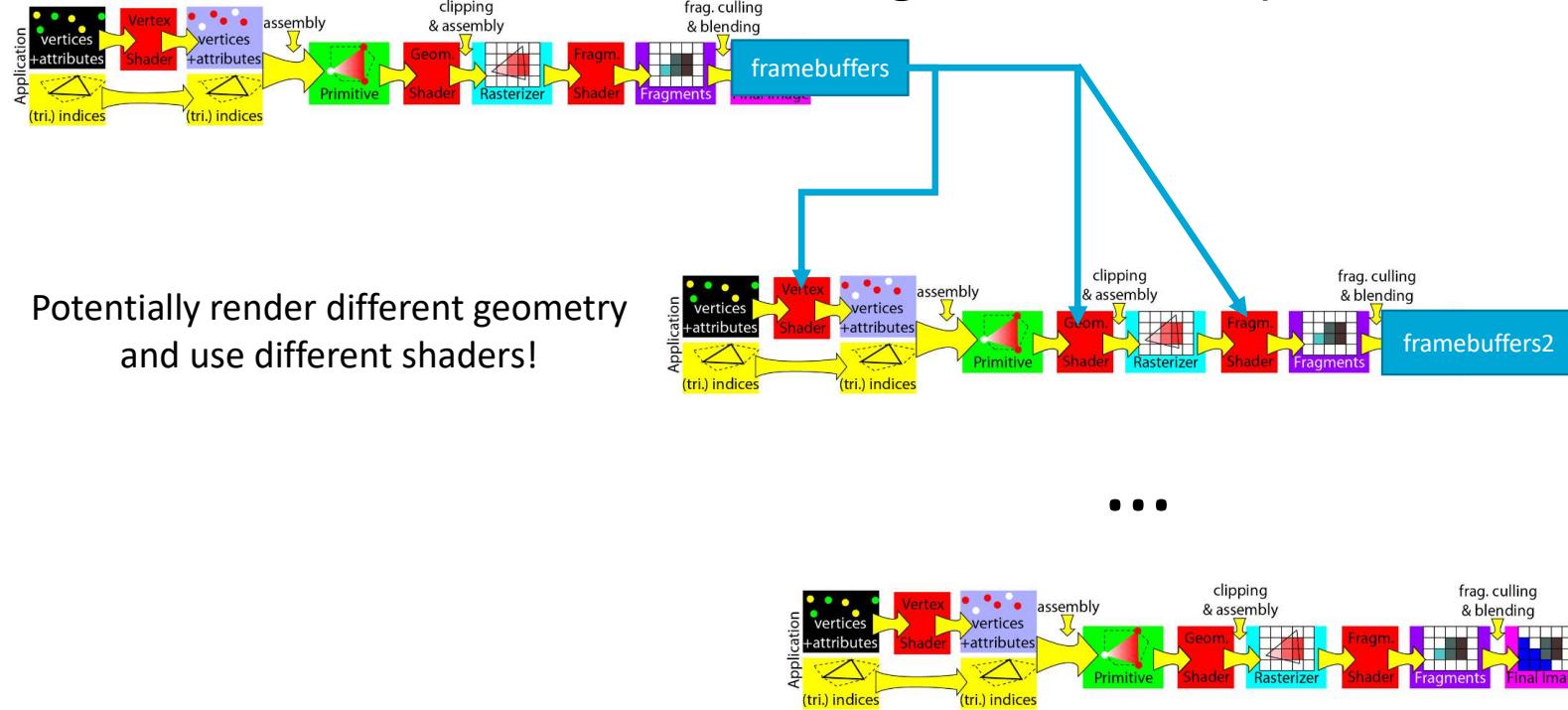
- Rendering to texture is done by attaching a “framebuffer object” to your pipeline.
- Output is written to this framebuffer



- You can attach several buffers/textures and write to the **same** pixel location (MRT – multiple render targets) – i.e., one fragment is drawn into several images!

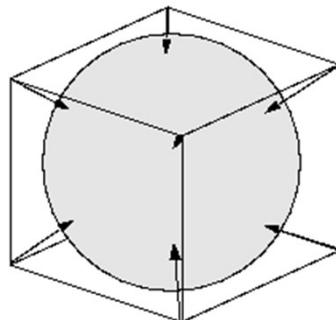
Iterative Rendering

- Take texture output as input texture during a new render pass



Dynamic Textures

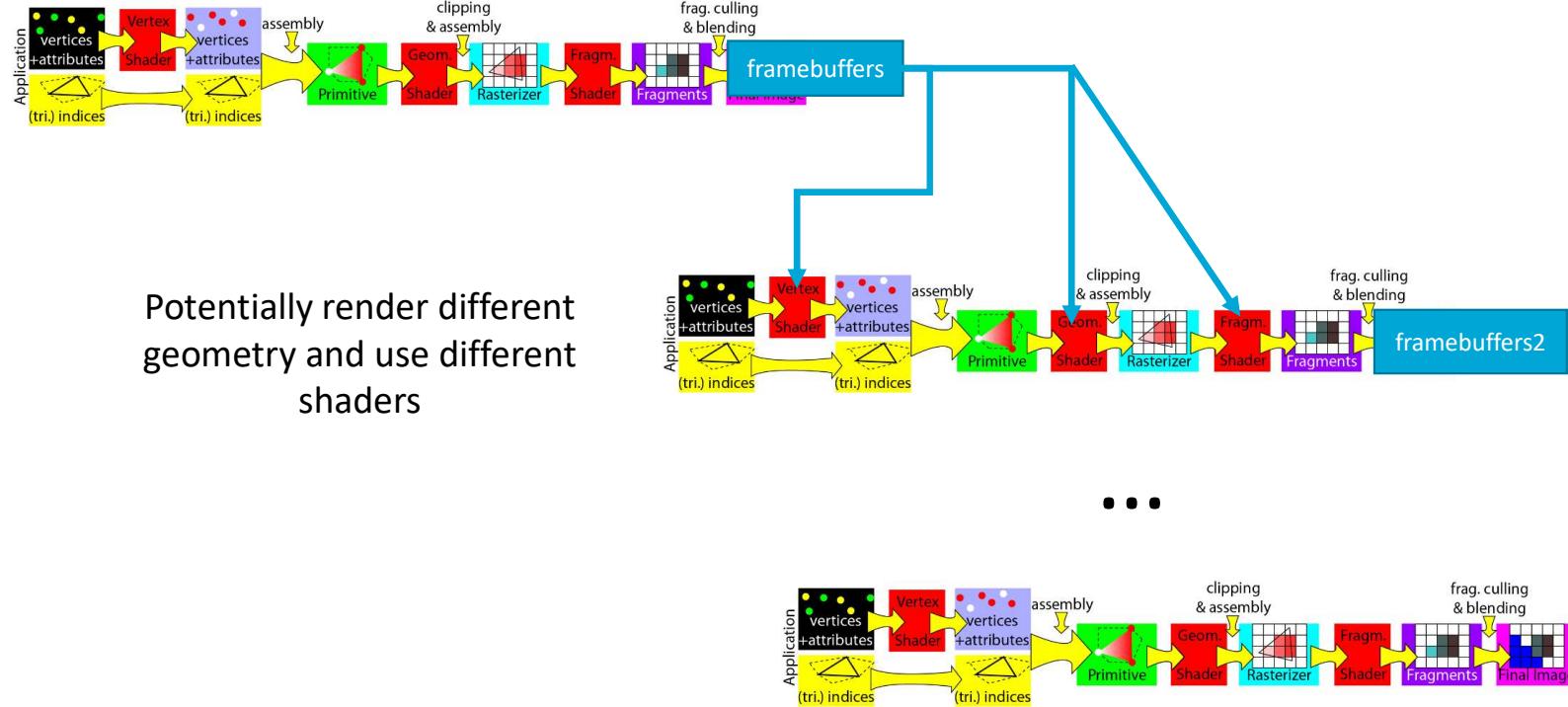
Dynamic Cube map



[Hollaender et al. EGSR 2011]

Iterative Rendering

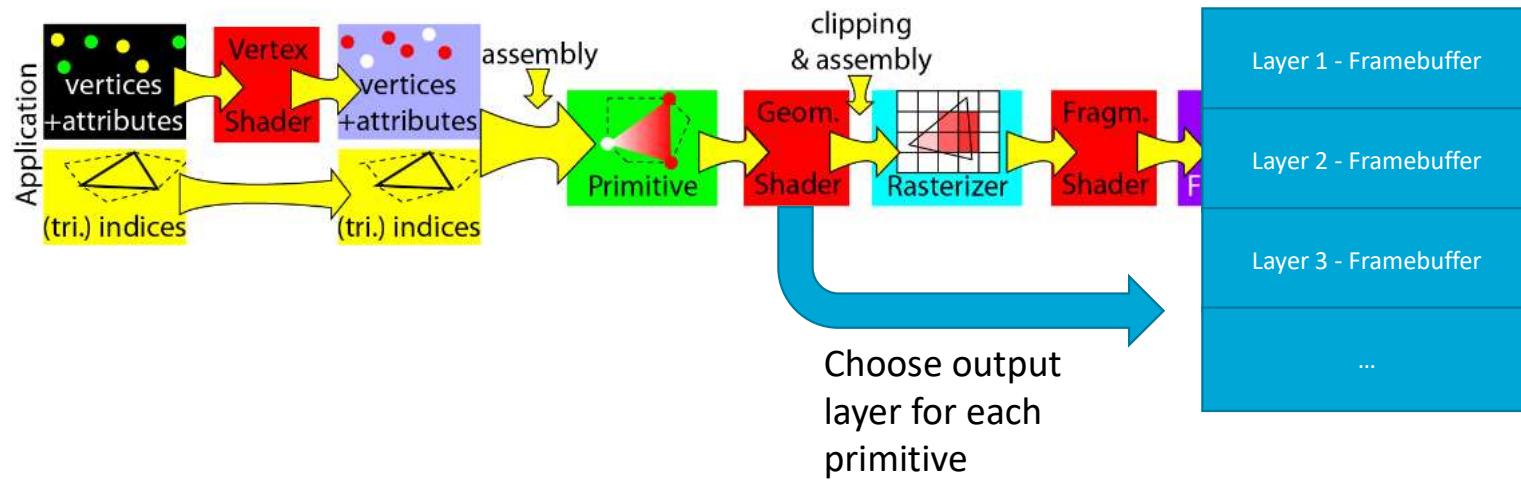
- Take texture output as input to a new render



You can attach several buffers/textures and write to the **same** pixel location
 (MRT – multiple render targets)

Multi-Output Rendering

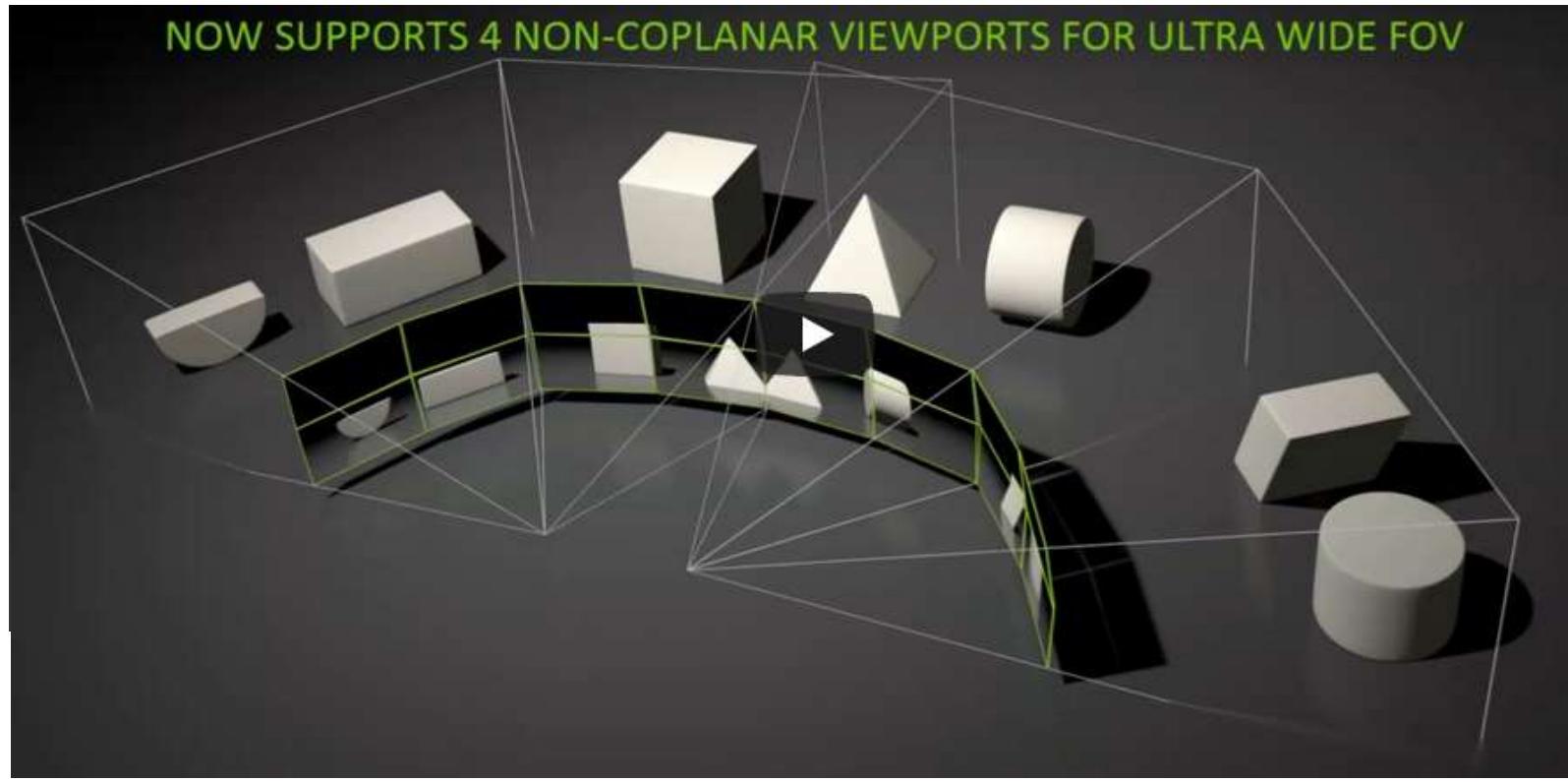
- Output into a specific texture: Layered Rendering



- The operation redirects geometry to only ONE layer of a layered buffer (contrary to using MRT, where it appears in all buffers)

Multi-Output Rendering

- Simultaneous Multi-Projection (SMP)



Later today:

- We will use such iterative rendering solutions to address shadows



<https://www.pinterest.com/pin/482307441323449946/>

Advanced Texture Use-Cases

- Encode material properties
- Approximate the environment
- **Represent Geometry**
- Encode complex functions

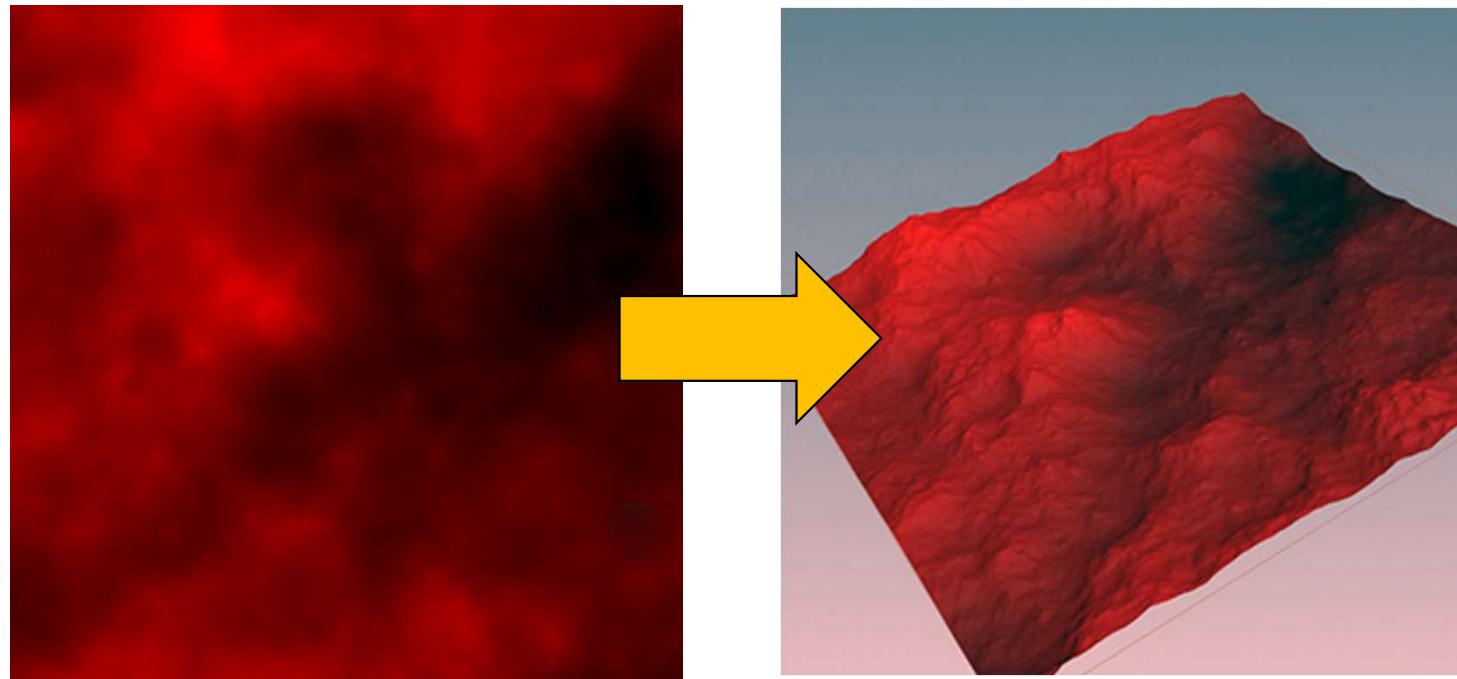
Terrain definition

- Source: DocMojo



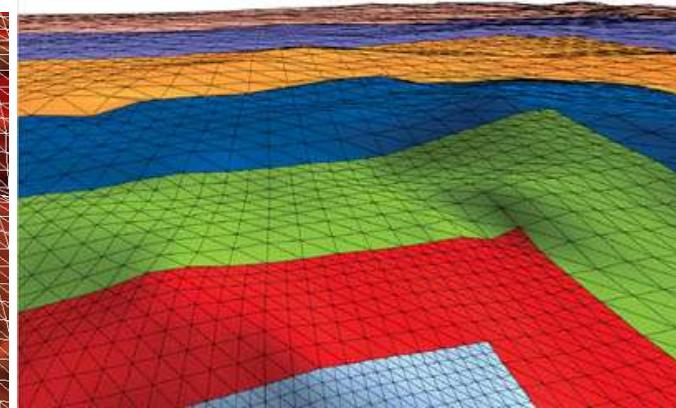
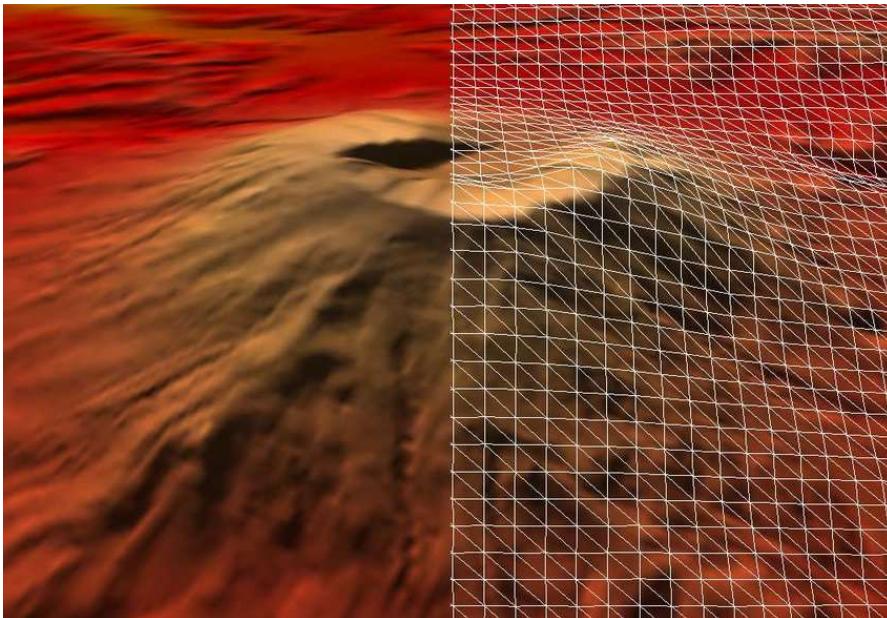
Terrain definition

- Source: <https://bubblepins.com/blog/output-terrain-texture-maps-houdini-height-fields>



Height Map Representations

- Use triangle grid and move vertices according to texture data



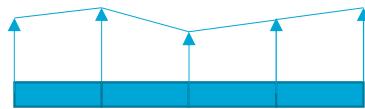
Possible to make grid subdivision adaptive,
based on distance to the observer
e.g., Clipmaps [GPU Gems 2]

Alternatively, move a pre-subdivided grid
along with the observer that has higher
resolution nearby

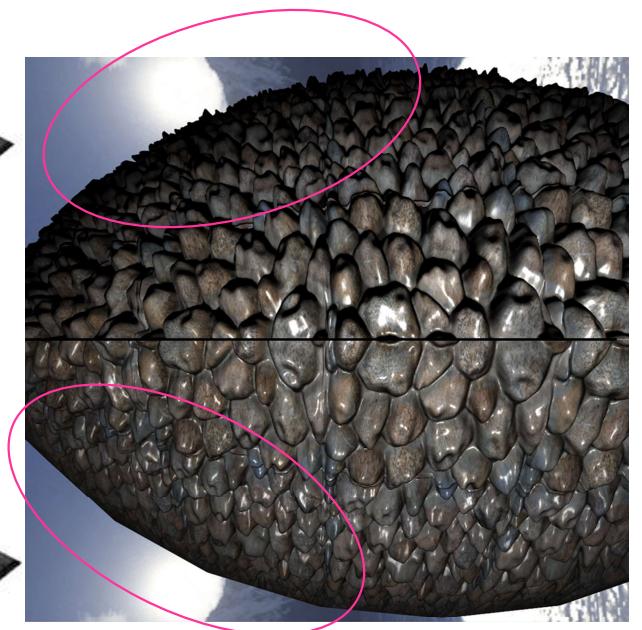
Displacement Mapping

- Store not only normals, but also an offset

Displacement mapping

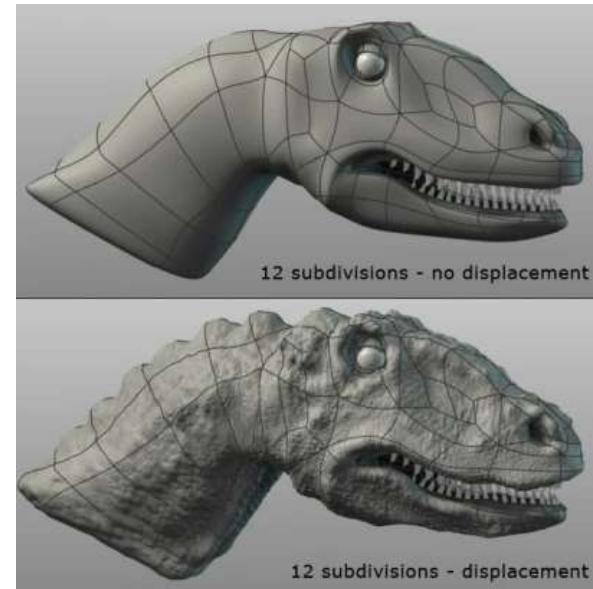
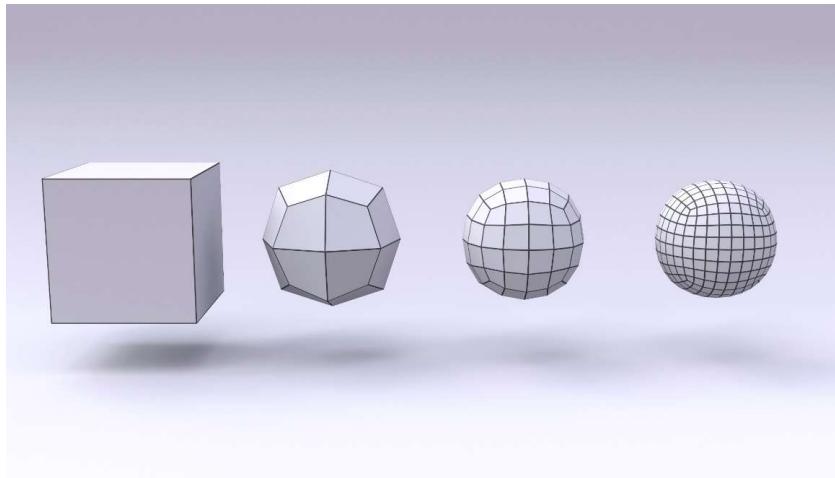


Normal mapping



Displacement Mapping

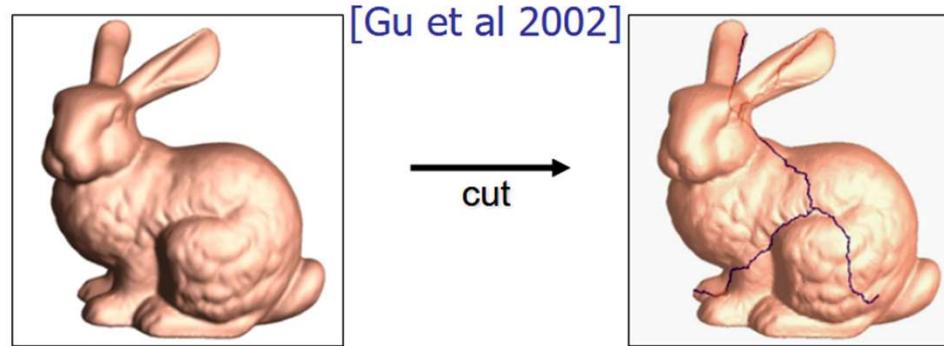
- Store not only normals, but also an offset
- Often used together with subdivision surfaces



- Leads to a large amount of geometry - mostly used in offline rendering

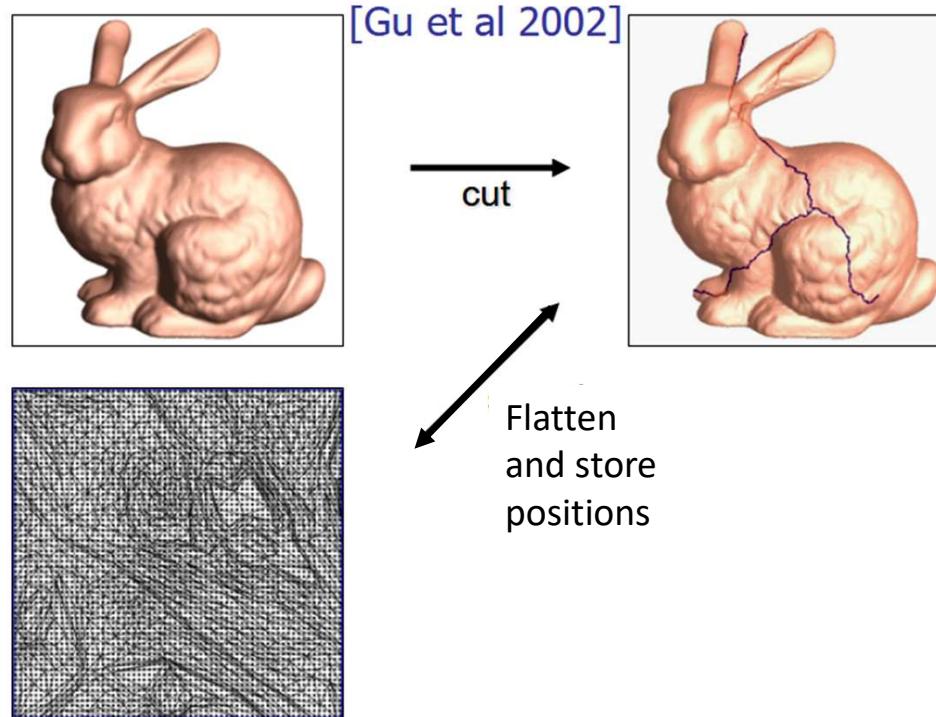
Geometry Images

- Textures can encode a general object



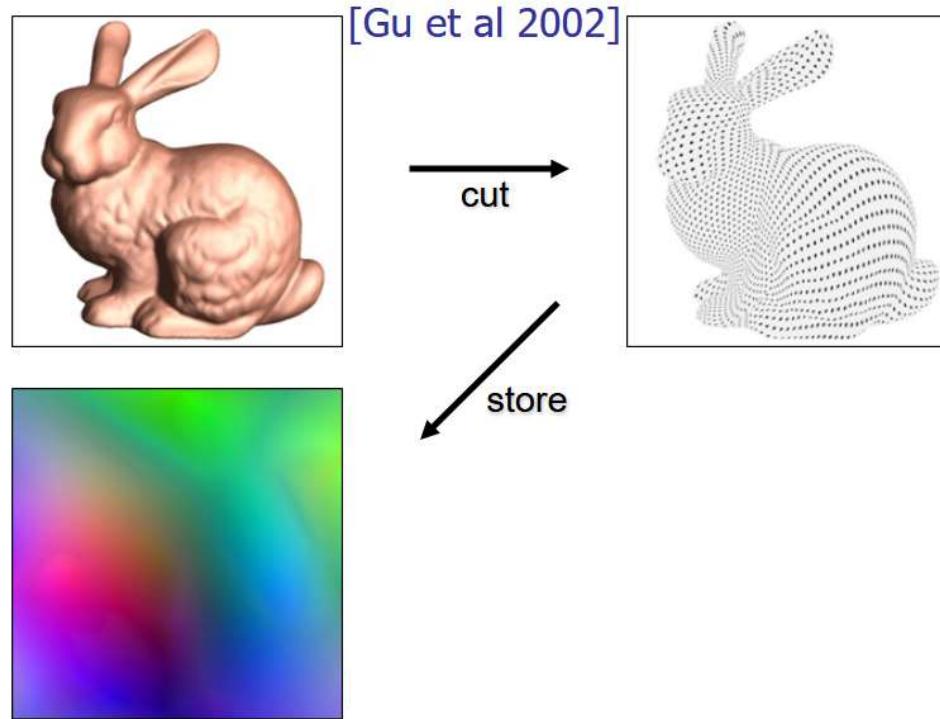
Geometry Images

- Textures can encode a general object



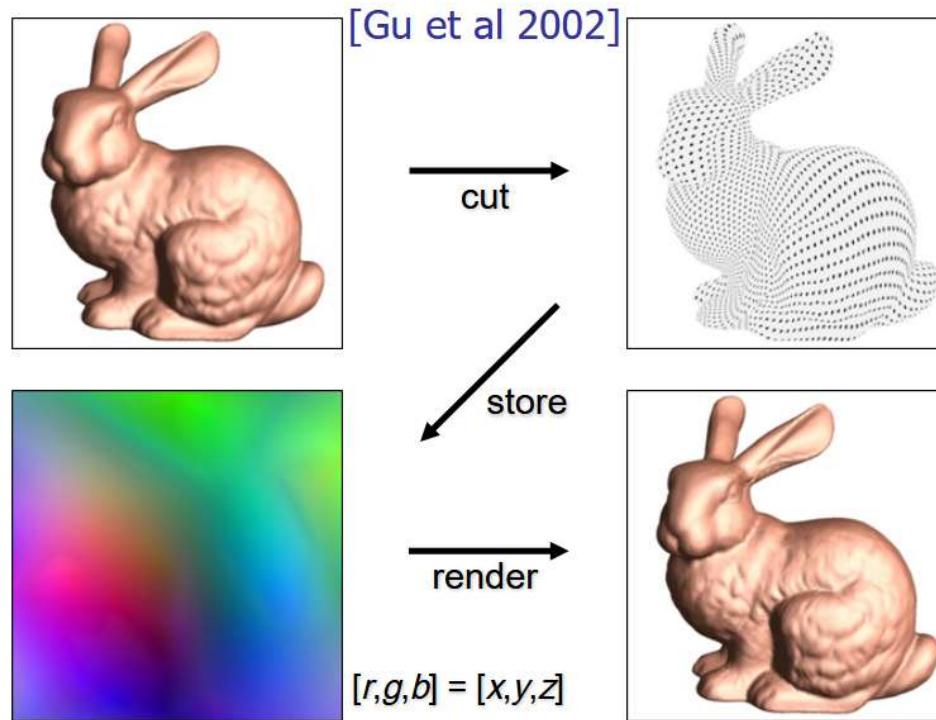
Geometry Images

- Textures can encode a general object



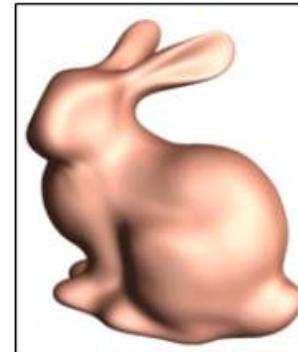
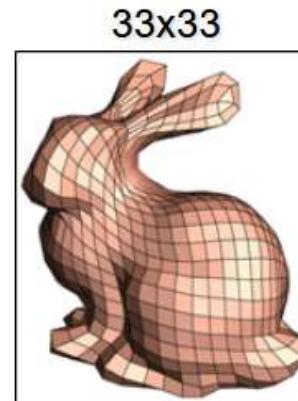
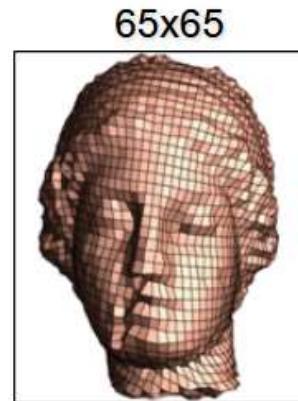
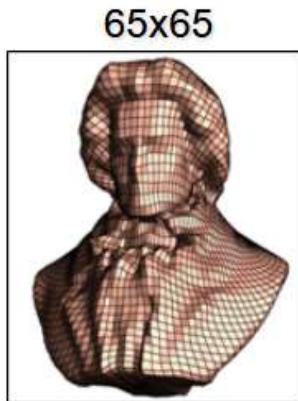
Geometry Images

- Textures can encode a general object



Geometry Images

- Low-Resolution Examples

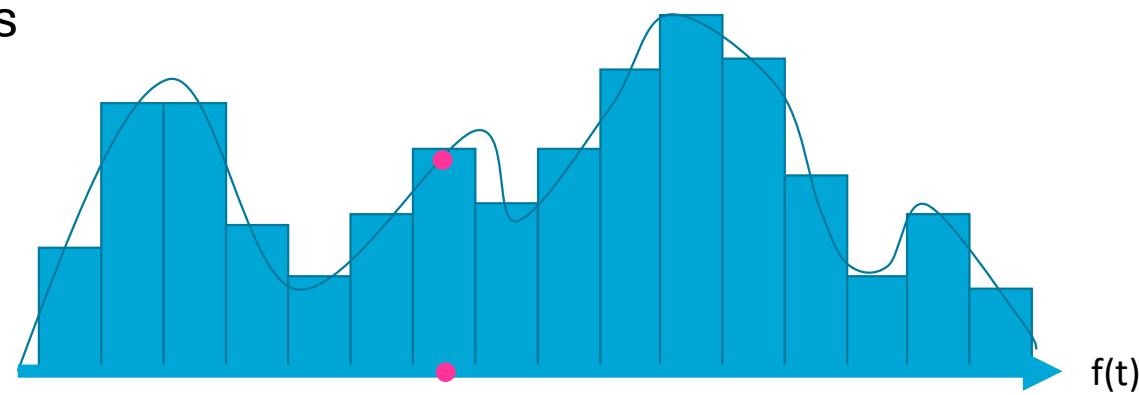


Advanced Texture Use-Cases

- Encode material properties
- Approximate the environment
- Represent Geometry
- **Encode complex functions**

Textures as Lookup Table

- Approximate complex computations via texture lookups



Replace
computation
by a lookup
in a texture



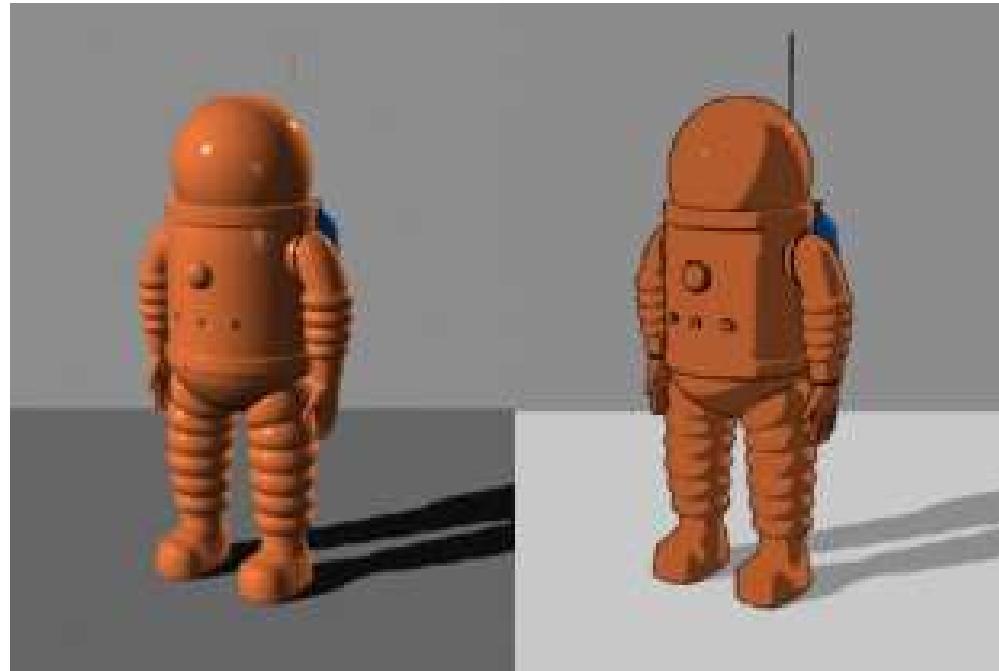
Textures as Lookup Table

- Activating linear texture interpolation leads to a piecewise linear approximation



Simple Example: Lookup Table Use

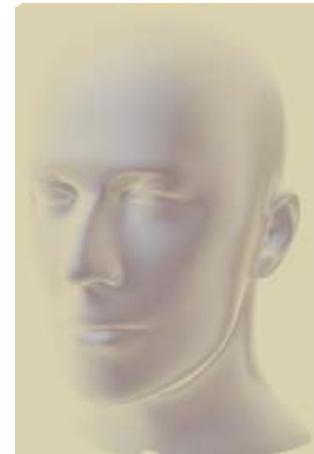
- Non-photorealistic materials



- Cel-shading: threshold the diffuse shading

X-Toon (Barla et al. 06) – see Exercises

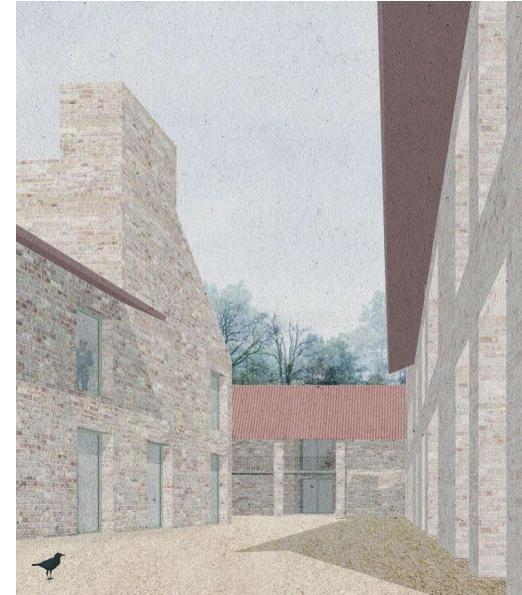
- Instead of calculating, implement it via a 1D texture lookup



Second parameter can be distance to camera, or curvature, or material coefficient, or...

Playing with Tex Coords: Creating Paper Structure

- Example application:
Add paper grain over your rendered image



How would you define the texture mapping T to obtain screen-space texture coordinates?
Hint: Use the projected vertex position!

Advanced Texture Use-Cases

- Encode material properties
- Approximate the environment
- Represent Geometry
- Encode complex functions

Advanced Texture Use-Cases

- Encode material properties
- Approximate the environment
- Represent Geometry
- **Encode complex functions**



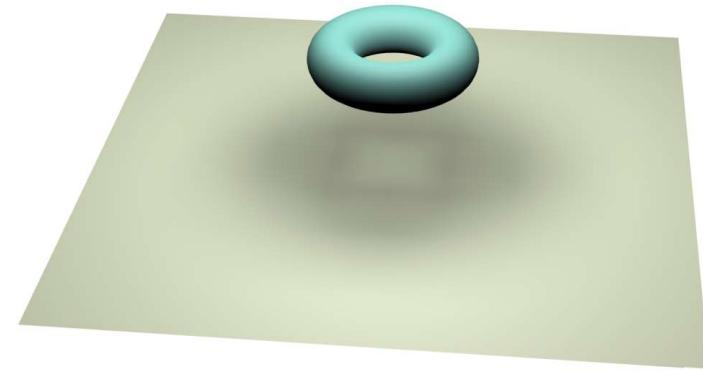
What is a Shadow?

- WordNet:

Shade within clear boundaries

or

An unilluminated area.

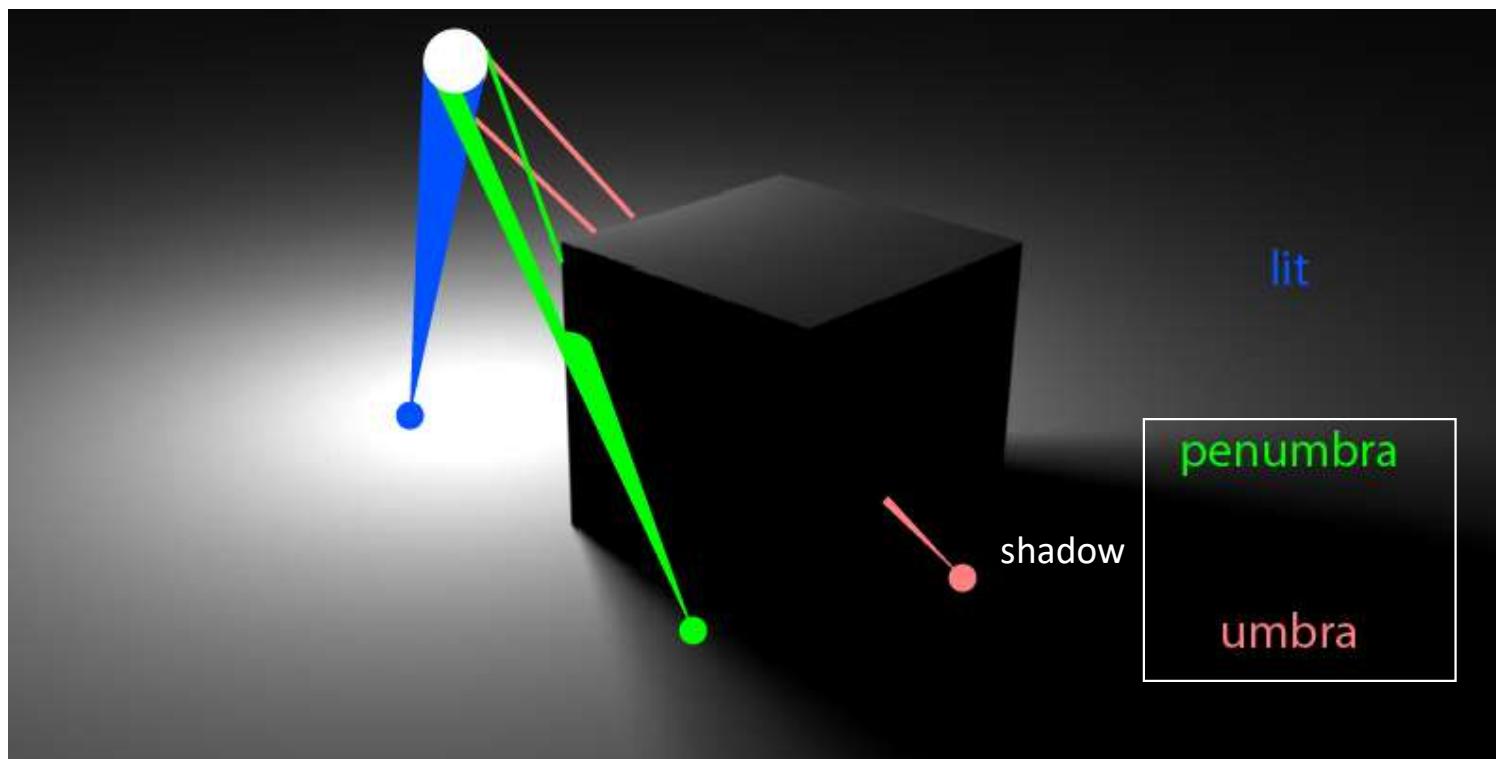


What is a Shadow?

- Hasenfratz et al. [2003]:

*Shadow [is] the region of space
for which at least one point of the light source is occluded.*

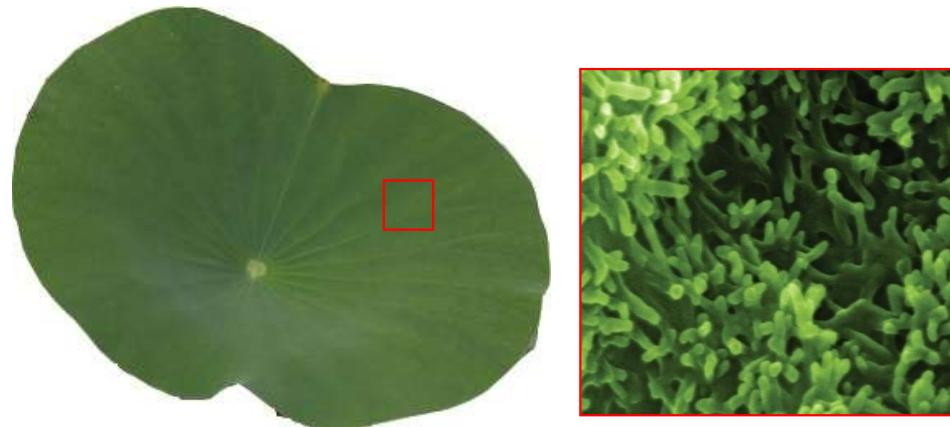
What is a Shadow?



What is a Shadow?

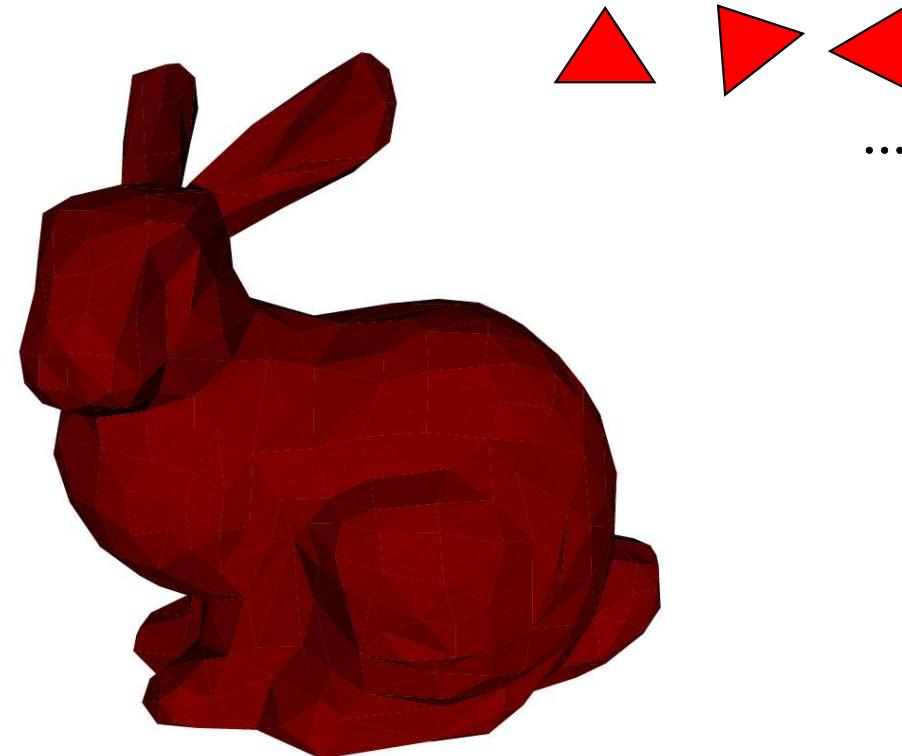
- Hasenfratz et al. [2003]:

*Shadow [is] the region of space
for which at least one point of the light source is occluded.*



Our models are simple...

- Typically a list of triangles



What is a Shadow?

- Hasenfratz et al. [2003]:

*Shadow [is] the region of space
for which at least one point of the light source is occluded.*

How to draw shadows?

- Artists know how to draw shadows!

Or not?



Fra Carnevale
(1467)

122

How to draw shadows?

- Artists know how to draw shadows!

Or not?



Signorelli
(1488)

123

How to draw shadows?

- Artists know how to draw shadows!

Or not?



Moore
(1893)

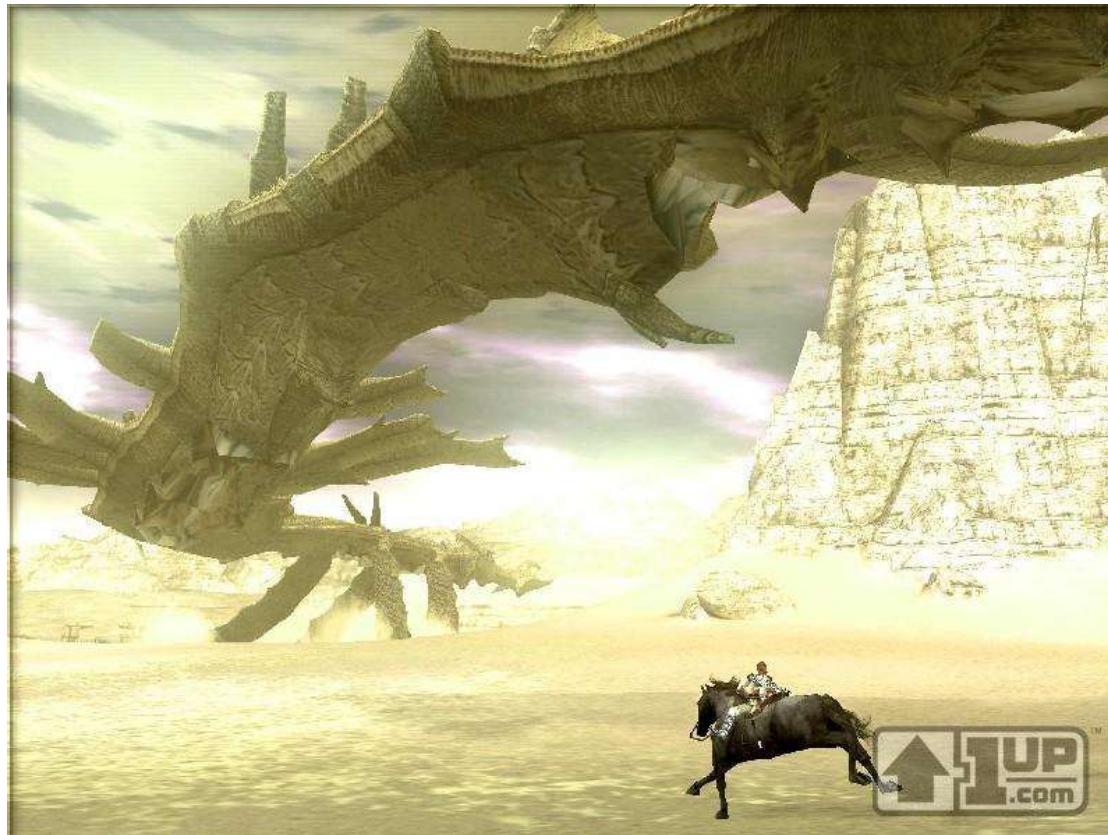
124

How to draw shadows?

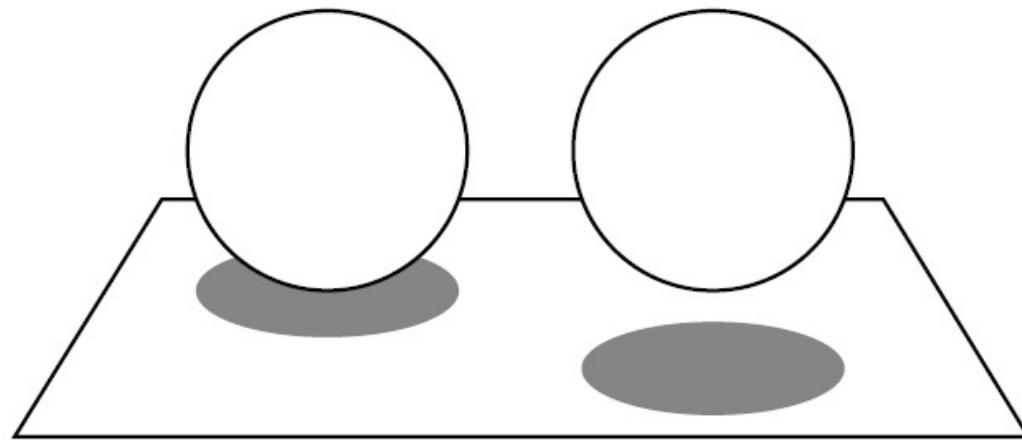
- Drawing shadows is apparently difficult...

So why not just ignore shadows?

- Shadow of the Colossus, Sony



So why not just ignore shadows?



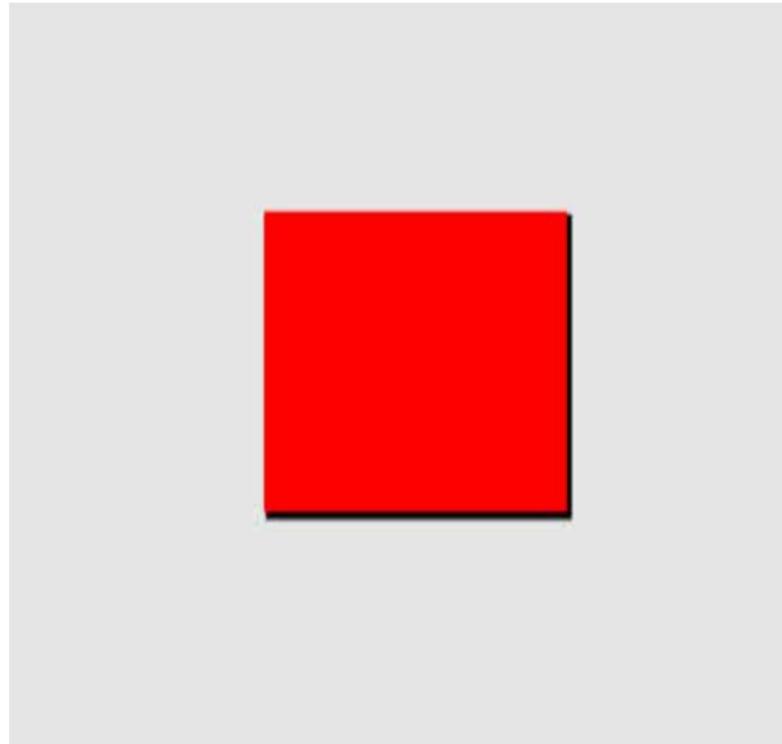
So why not just ignore shadows?

- Shadow of the Colossus, Sony



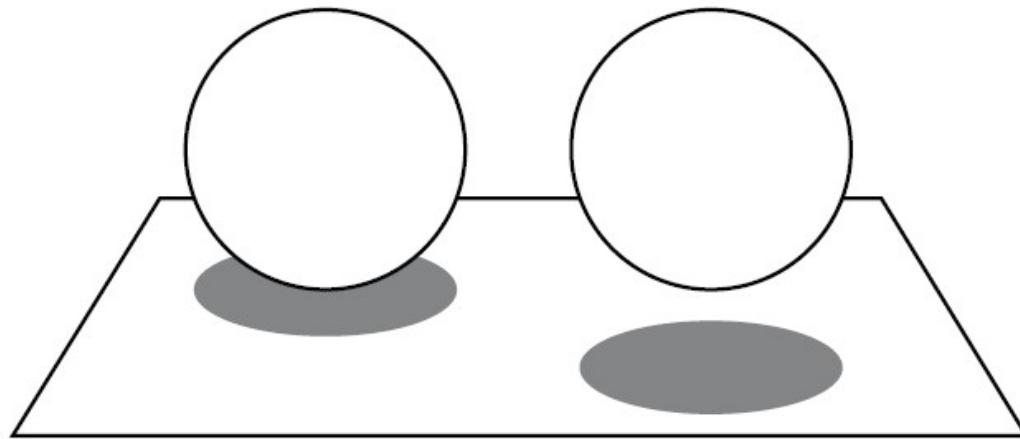
Psychophysical-Experiments

[Kersten et al. 96]

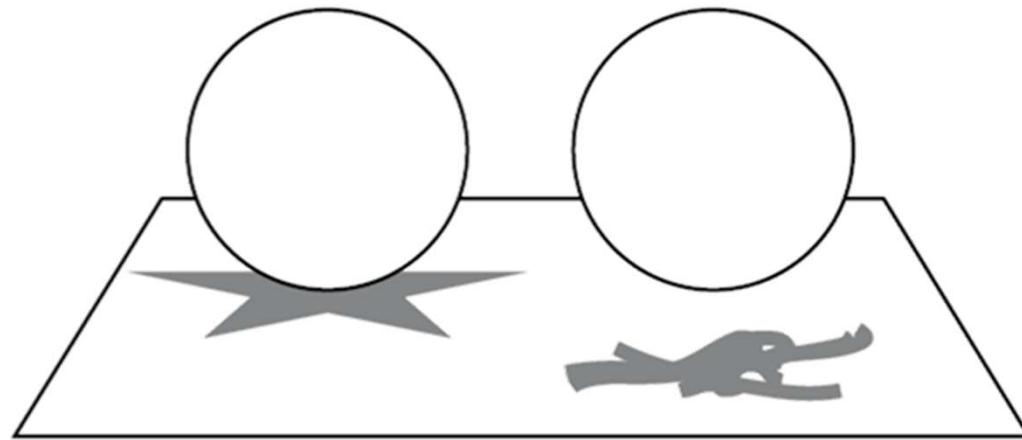


So why not just ignore shadows?

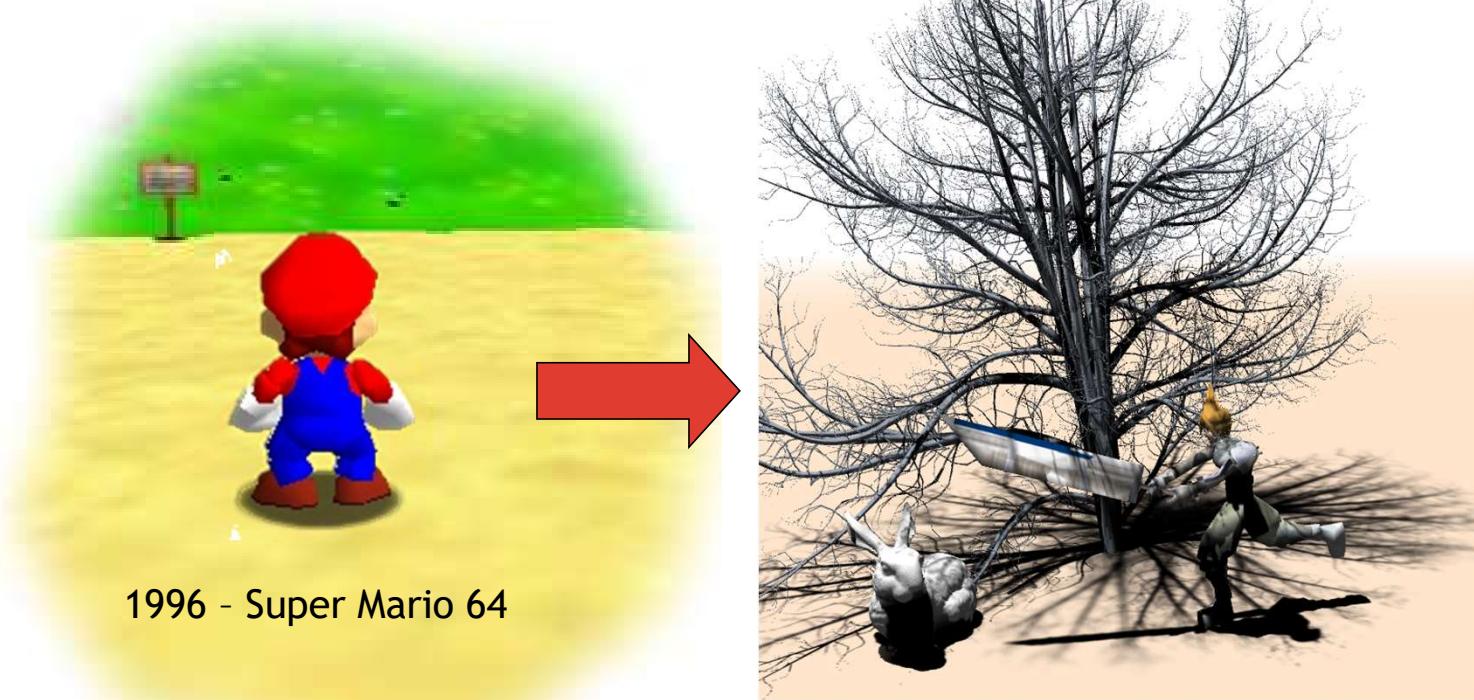
- But this is not a good argument for realistic shadows...



So why not just ignore shadows?

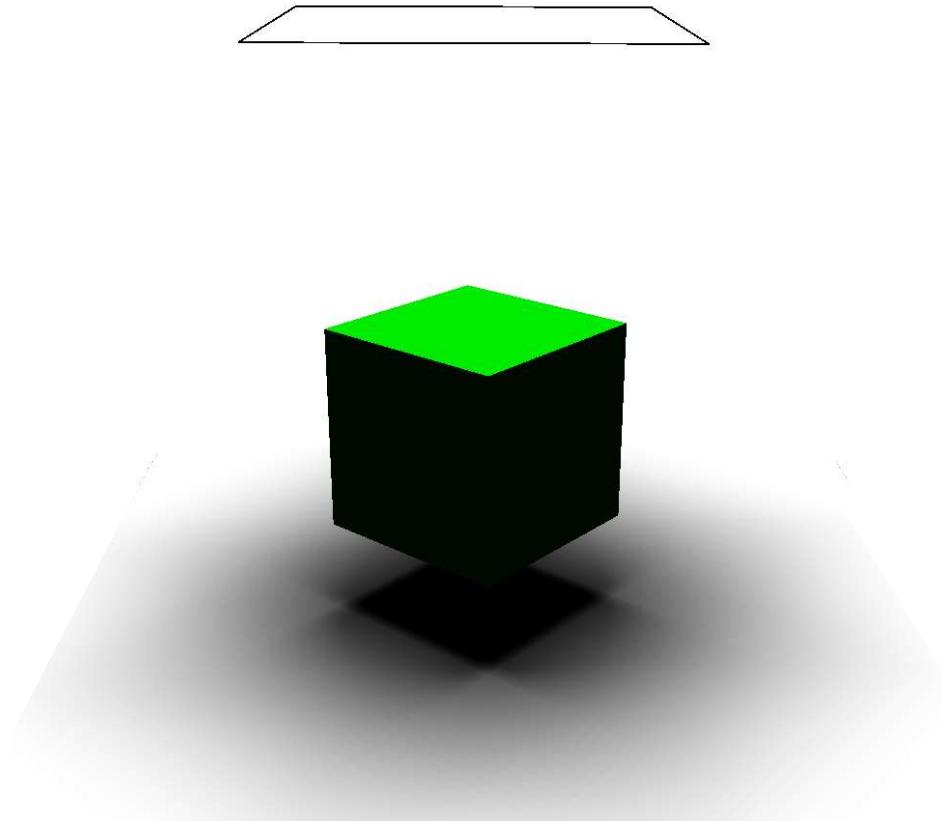


Simple shadows can be sufficient



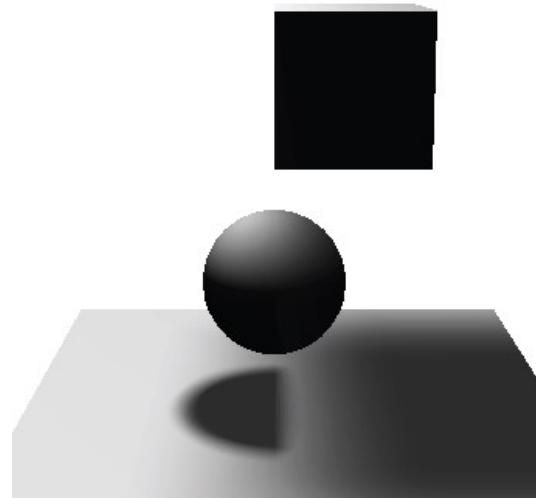
1996 - Super Mario 64

Plausible shadows



Plausible shadows

- Attention: “plausible” can often fail



Realistic shadows are important



Realistic shadows are important

- Many contexts in which accuracy is needed:
 - Architecture
 - Simulation
 - Movies
- ...



Chicago



Boston

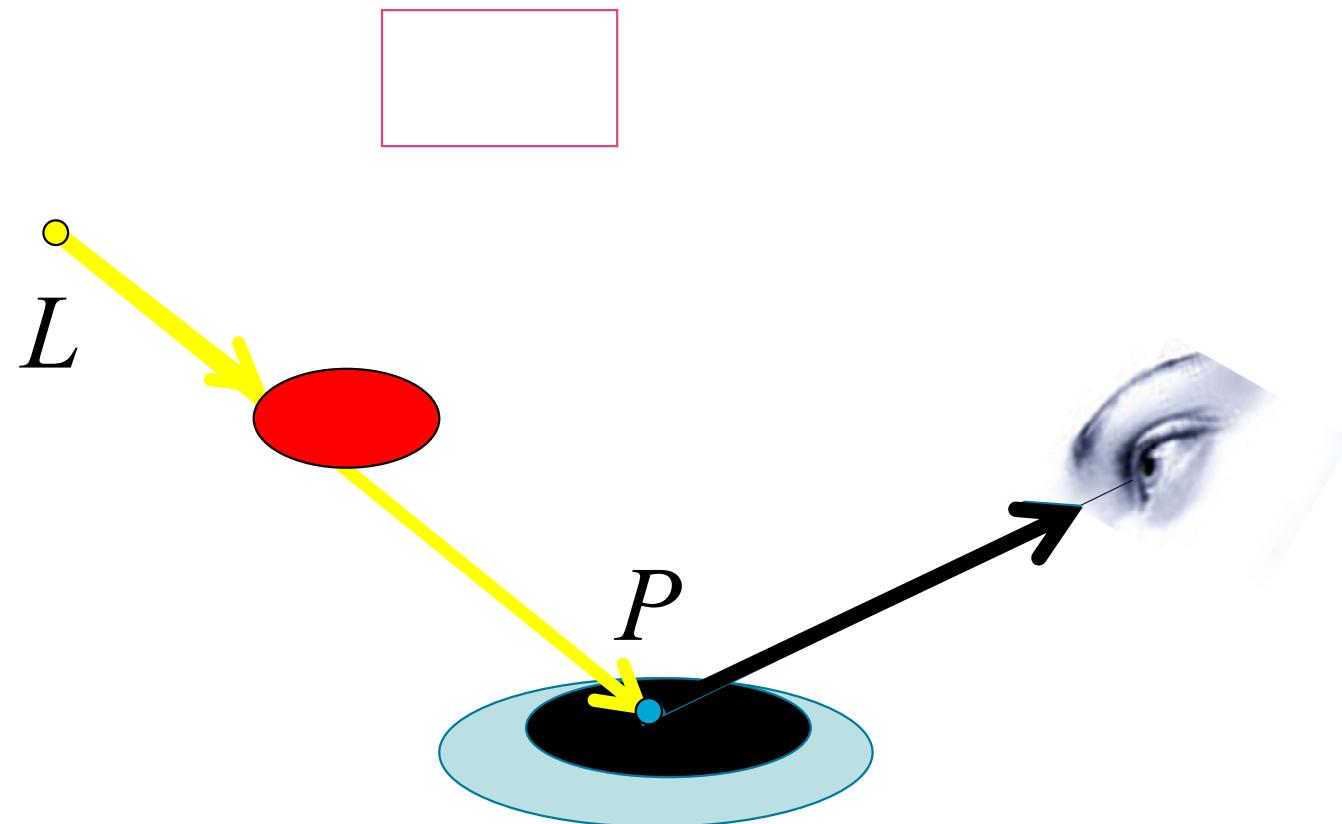


NYC

Desert villa by Studio Aiko

Miranda et al. TVCG2019

How to compute shadows?



Hard Shadows



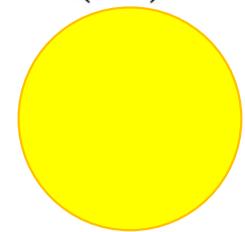
Point lights do not create penumbrae

Soft Shadows

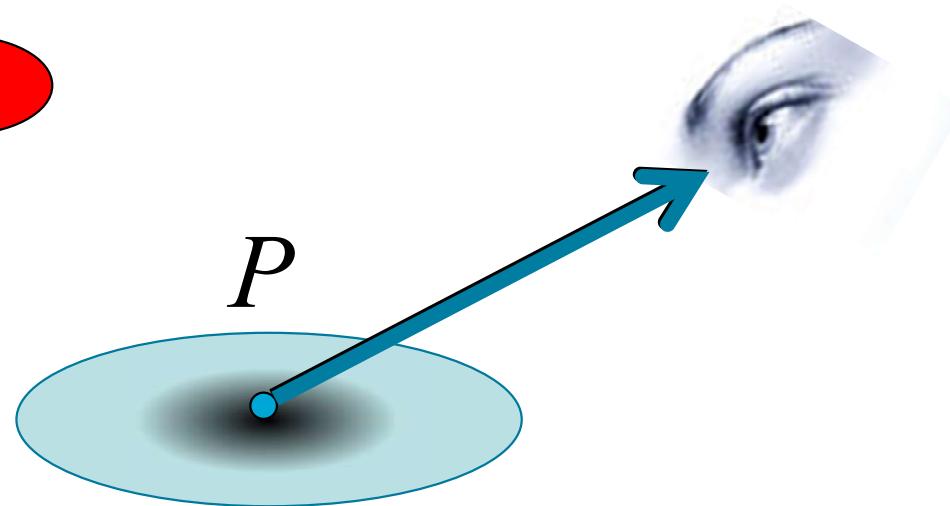
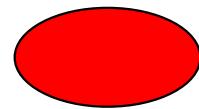


What is a Shadow ? – Part II

$$B(P) = E(L) \ v(P,L) \ Transfer(P,L)$$

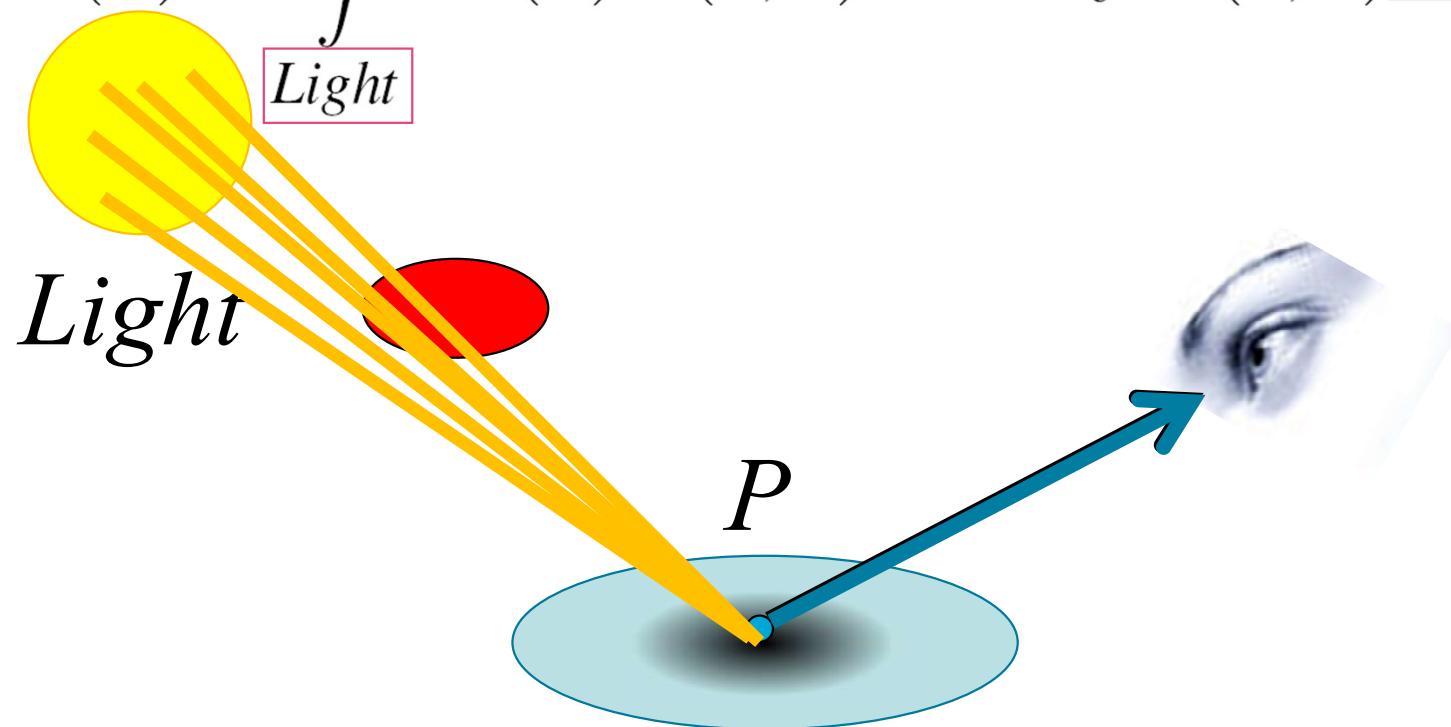


Light



What is a Shadow ? – Part II

$$B(P) = \int E(L) v(P,L) Transfer(P,L) dL$$



Bad news

- Prior to 2008:

All real-time shadow algorithms

attempted to only approximate :

$$\int_{Light} v(P, L) \, dL$$

and all failed...

Today: Hard Shadows within the Rendering Pipeline

- Meaning: light source L is a point



•
 L

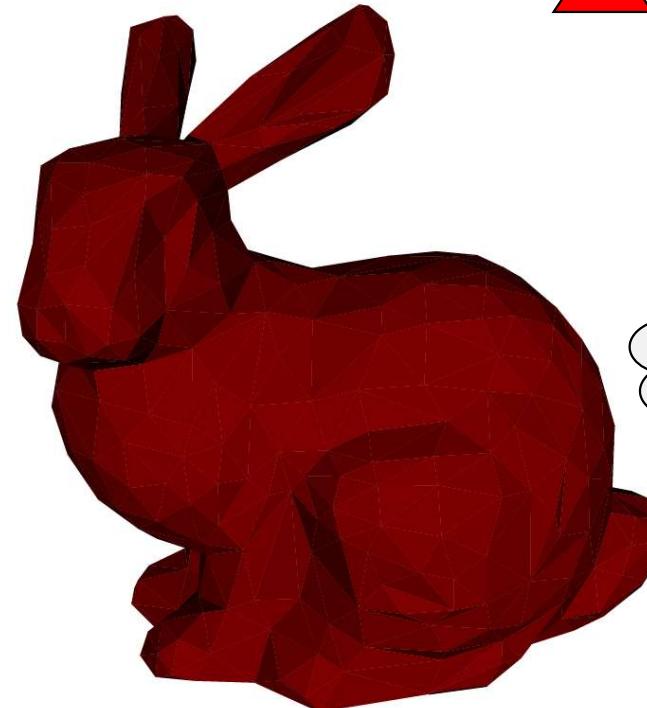
How to accelerate the process?

Use GeForce,
Luke!



Simplified Graphics Pipeline

- Models are typically lists of triangles

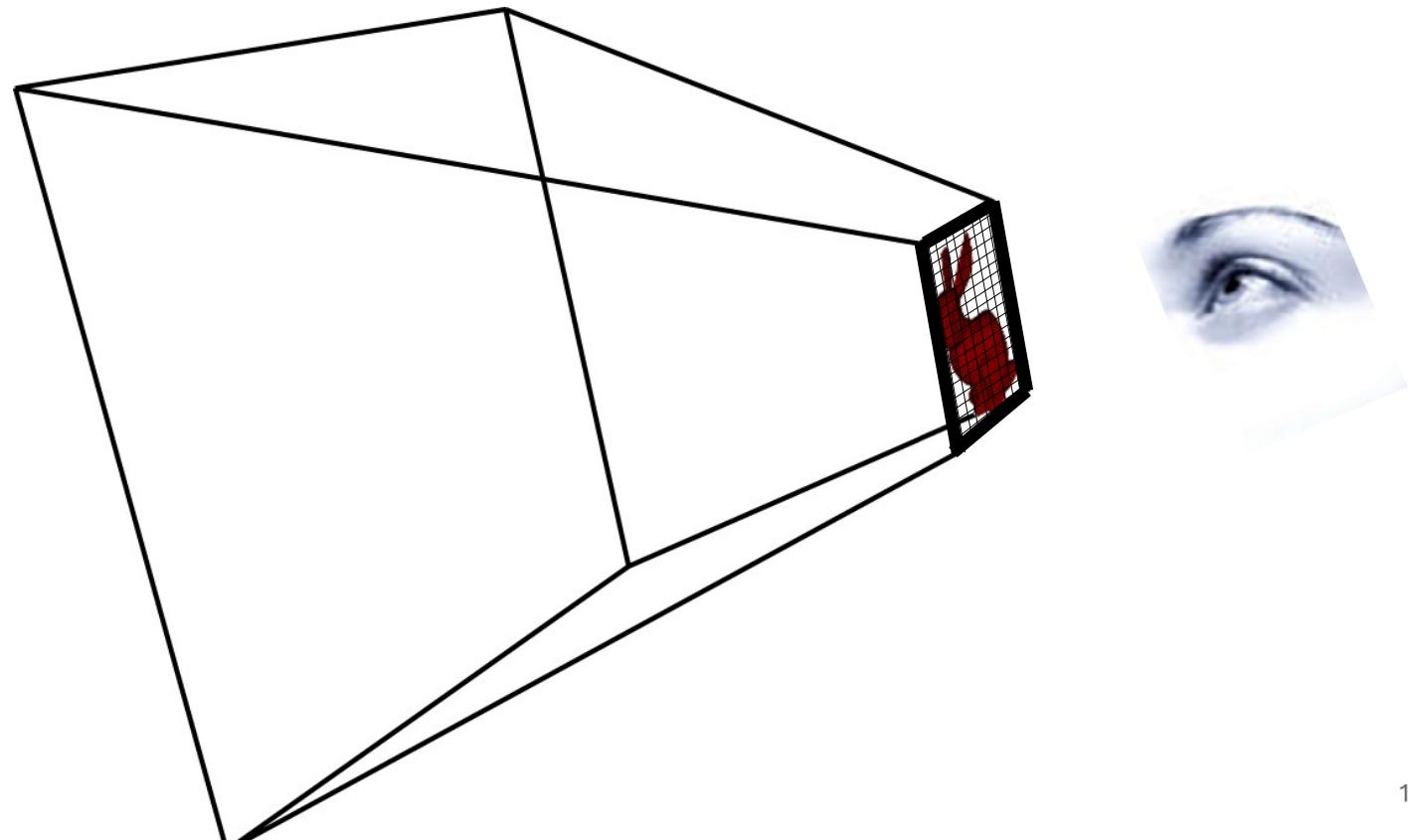


All this slide
recycling...



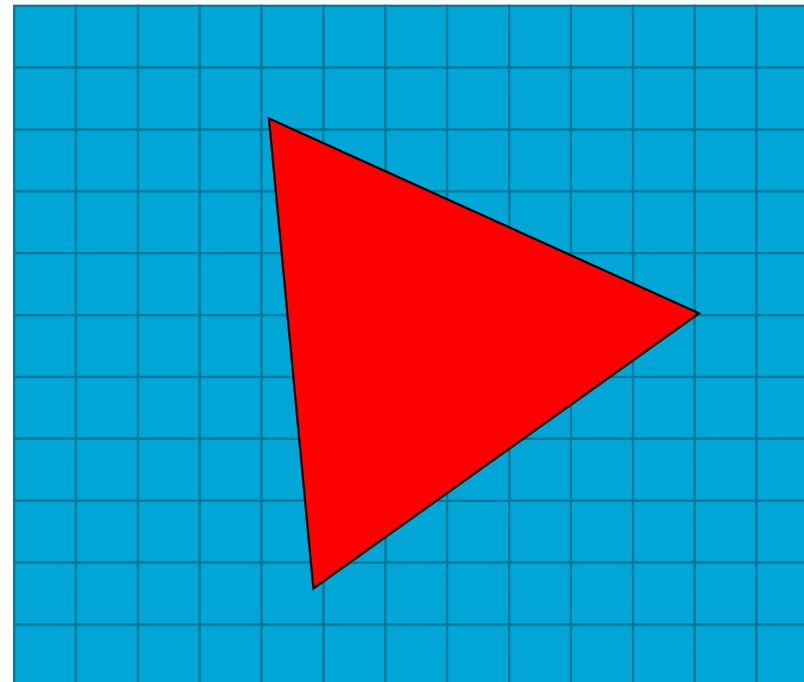
Simplified Graphics Pipeline

- **Projection:** Transform coordinates to screen



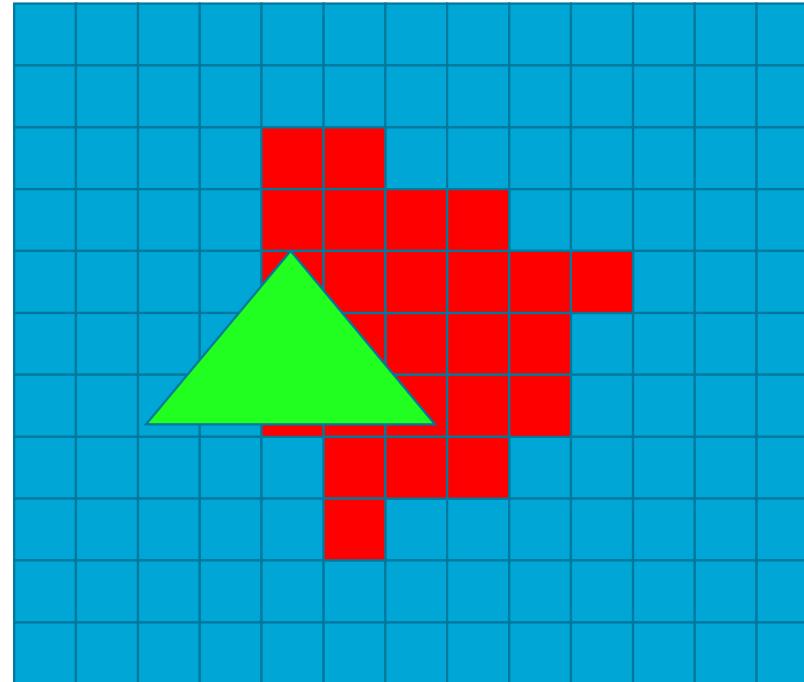
Simplified Graphics Pipeline

- **Rasterization:** Fill screen pixels



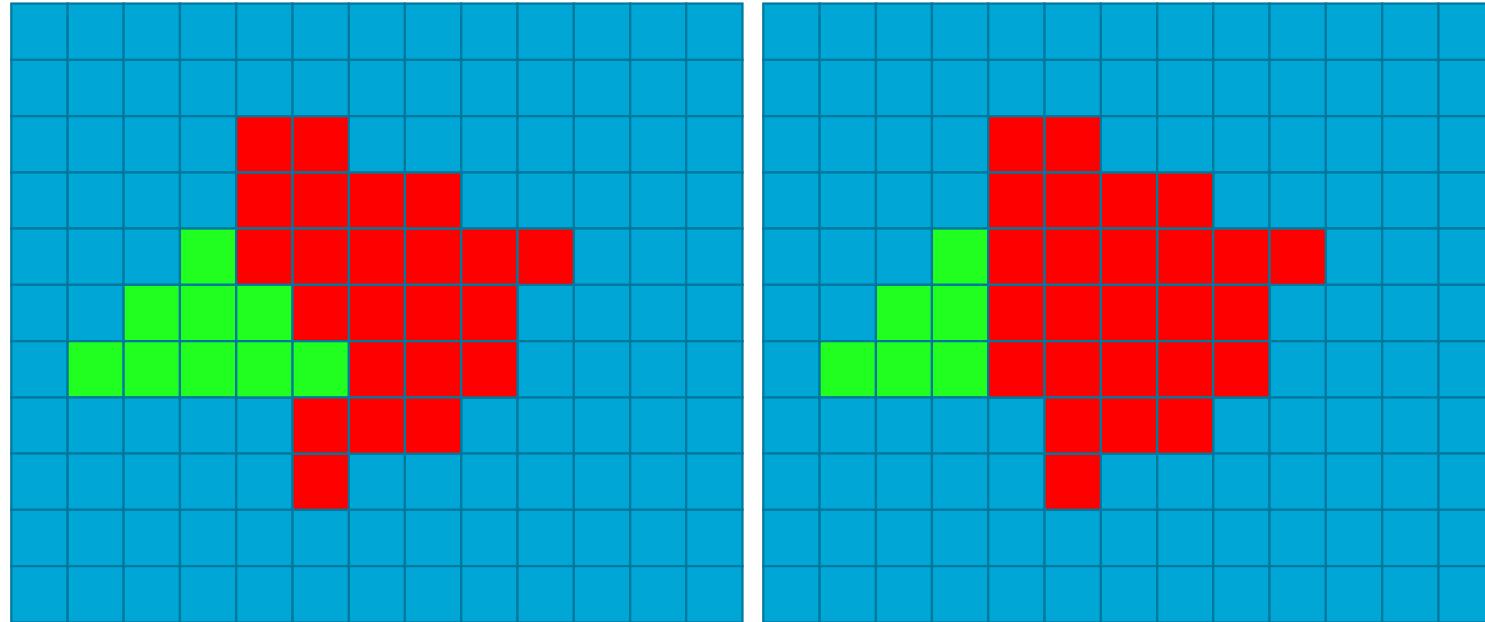
Simplified Graphics Pipeline

- **Catch:** Let's look at a second triangle...



Simplified Graphics Pipeline

- **Catch:** Drawing order changes result



Need to **keep nearest** pixels

Simplified Graphics Pipeline

[Catmull74] , [Strasser74]

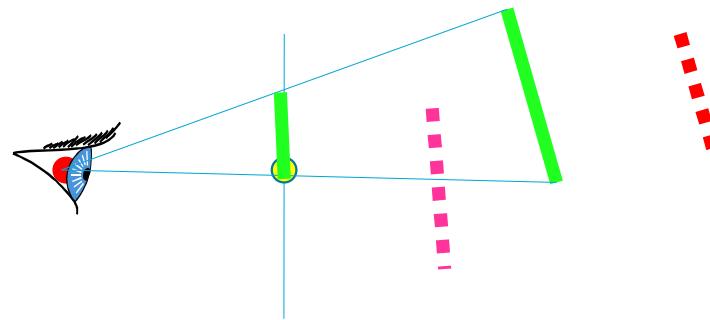
- Depth Buffer: Avoid sorting triangles!
- Store a color and depth in each pixel



Simplified Graphics Pipeline

[Catmull74] , [Strasser74]

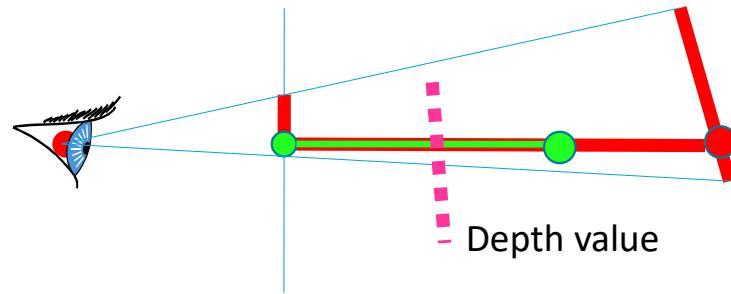
- Depth Buffer: Avoid sorting triangles!
- Store a color and depth in each pixel



Simplified Graphics Pipeline

[Catmull74] , [Strasser74]

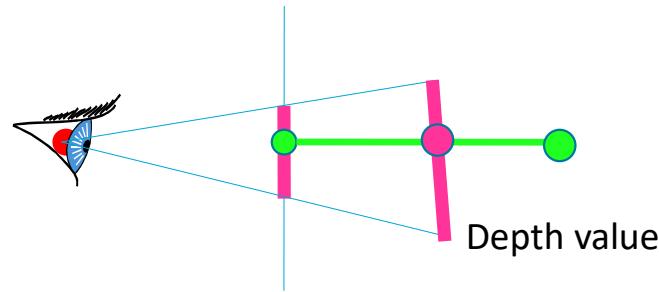
- Depth Buffer: Avoid sorting triangles!
- Store a color and depth in each pixel



Simplified Graphics Pipeline

[Catmull74] , [Strasser74]

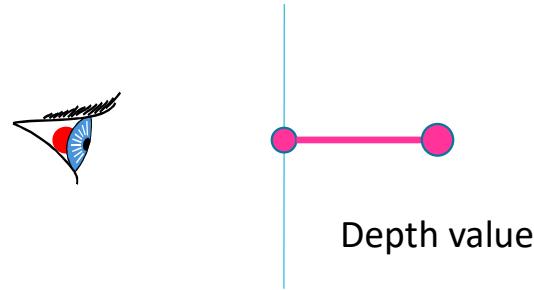
- Depth Buffer: Avoid sorting triangles!
- Store a color and depth in each pixel



Simplified Graphics Pipeline

[Catmull74] , [Strasser74]

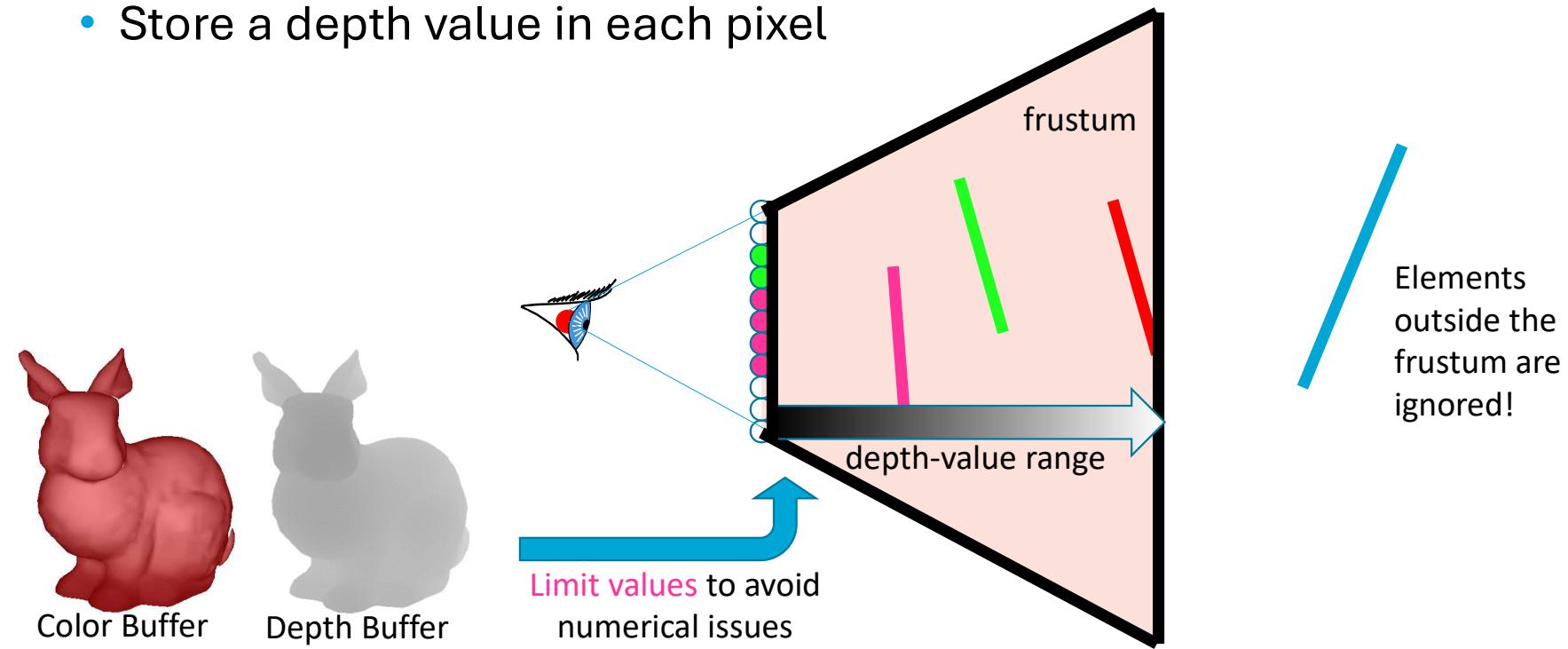
- Depth Buffer: Avoid sorting triangles!
- Store a color and depth in each pixel



Simplified Graphics Pipeline

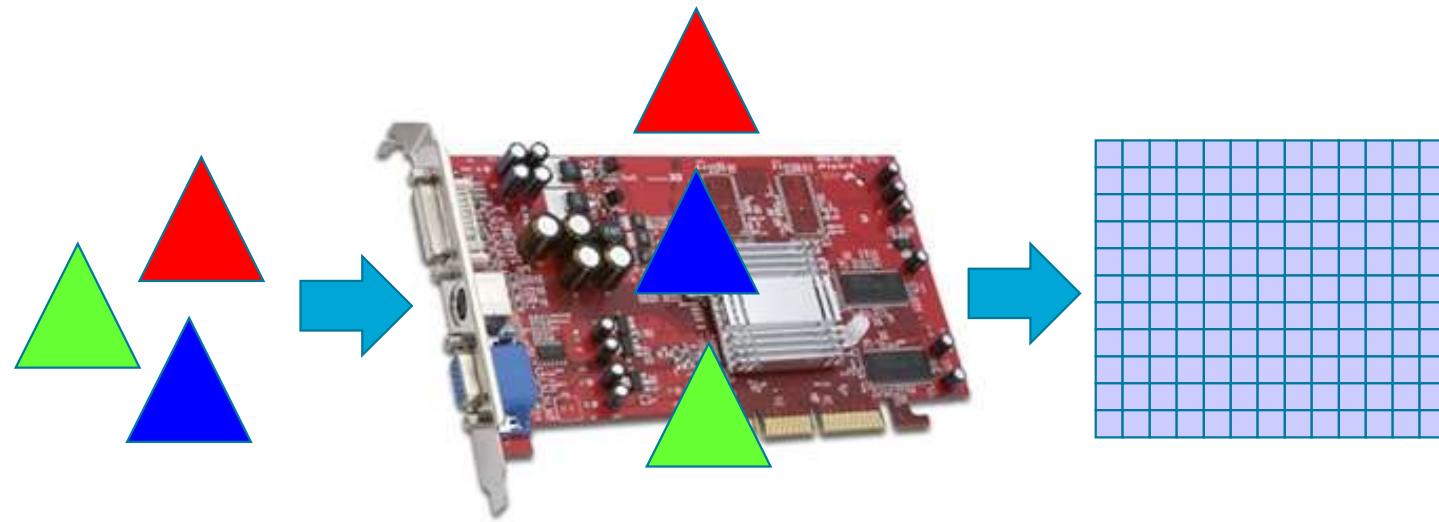
[Catmull74] , [Strasser74]

- **Depth Buffer:** Avoid sorting triangles!
- Store a depth value in each pixel



Simplified Graphics Pipeline

- Highly parallelizable
→ Graphics Processing Units (GPUs)

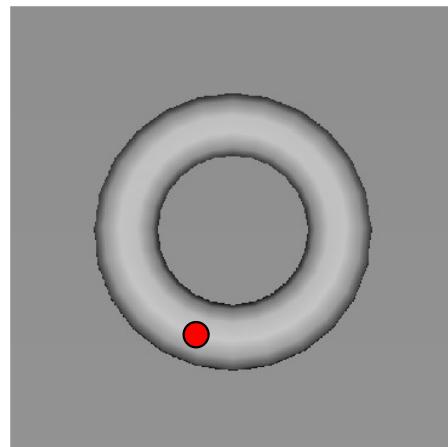
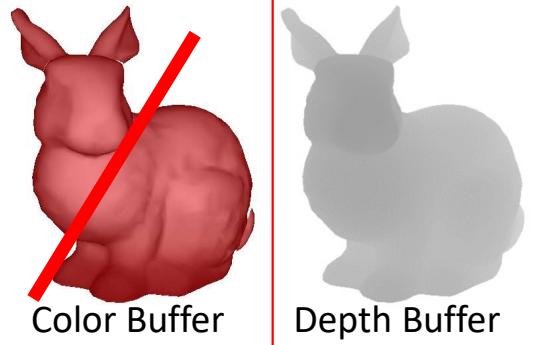


Simplified Graphics Pipeline

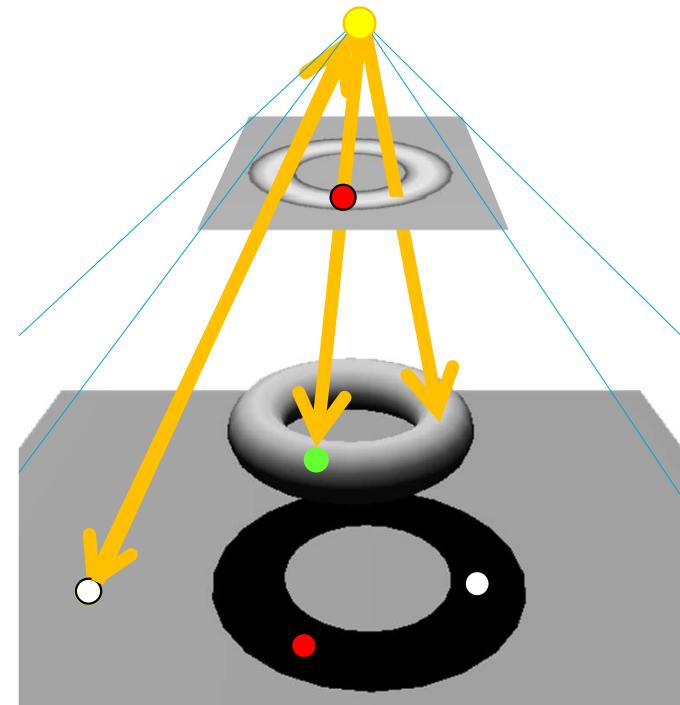


- Local computations:
- Processor only knows its current triangle
this is NOT enough for shadows

Shadow Mapping [Williams78]



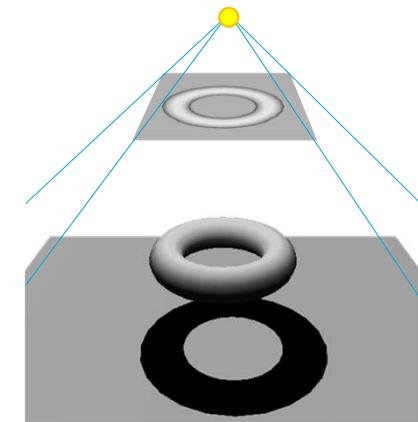
1. render view from light
use **depth buffer**



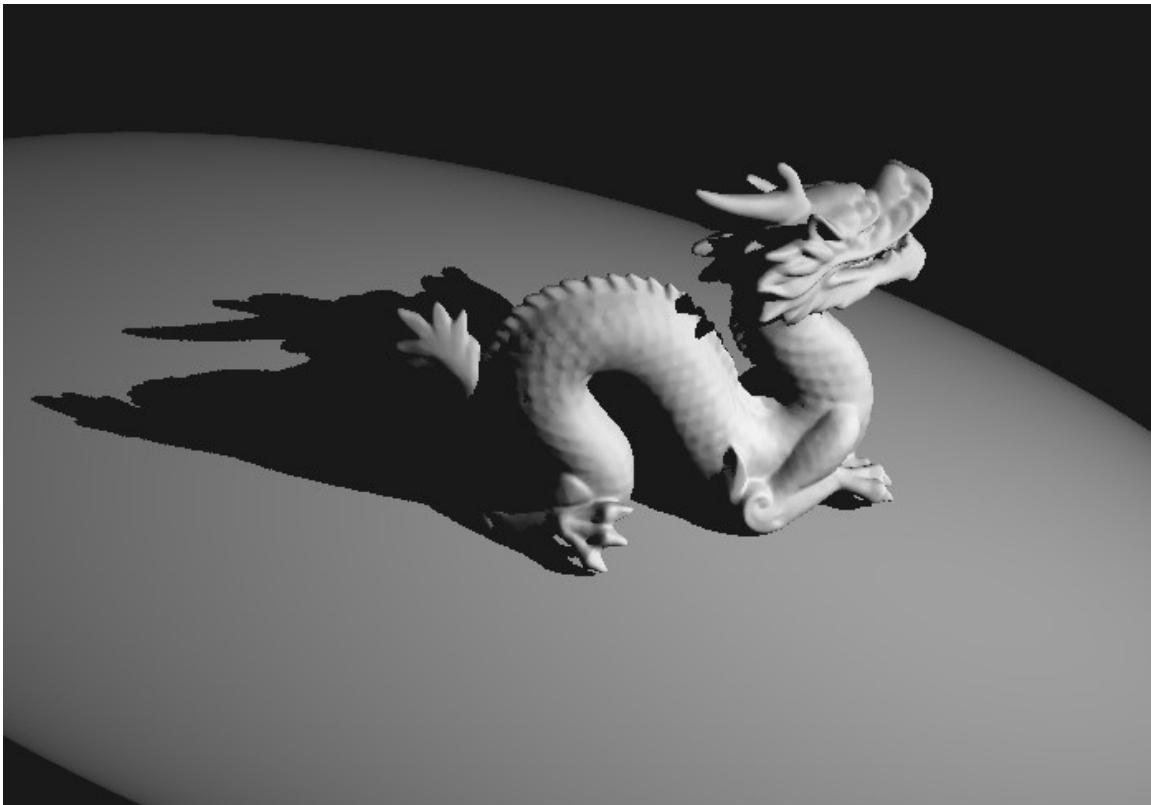
Shadow Mapping [Williams78]

1. Render depth buffer from light (**Shadow Map**)
 - Store result in a texture

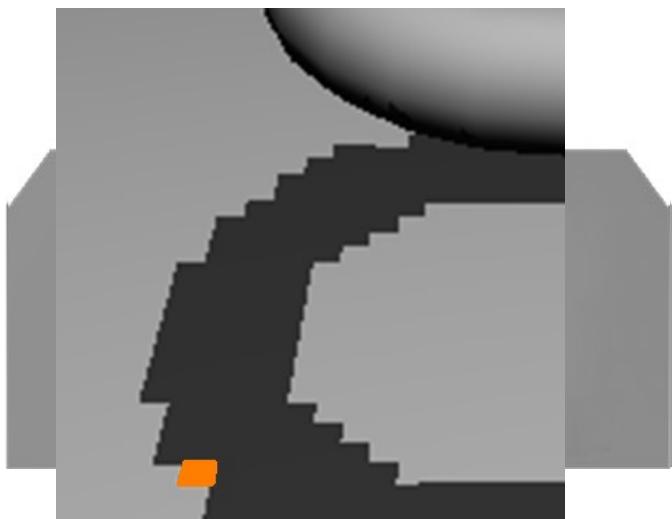
2. Render from viewpoint
 - For each drawn pixel:
Compare its depth in the light's view
to the stored depth at this texel location
in the Shadow Map
 - Equal: pixel is lit
 - Farther: pixel is in shadow



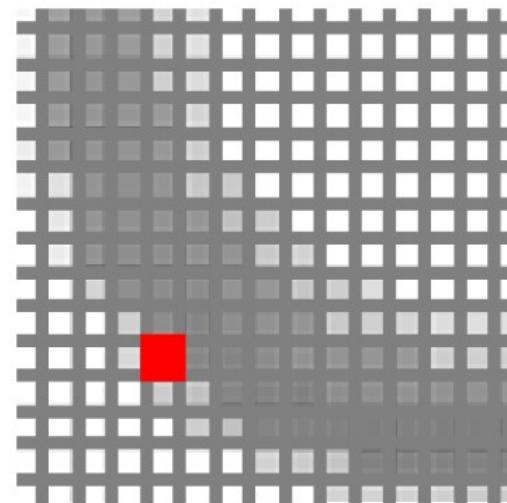
Demo



Problem 1: Discretization



from viewpoint



from light

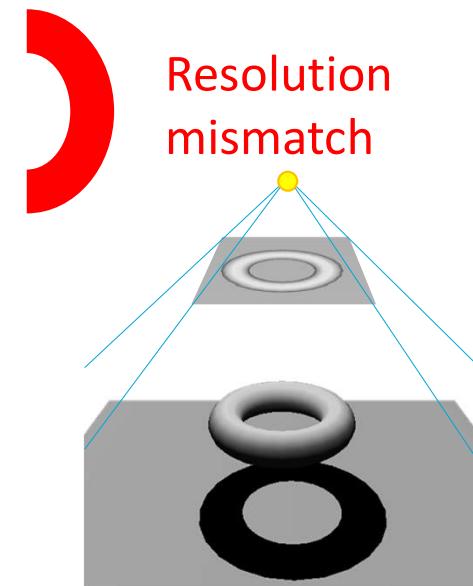
Shadow Mapping [Williams78]

1. Render depth buffer from light (Shadow Map)

- Store result in a texture

2. Render from **viewpoint**

- For each drawn pixel:
Compare its depth in the **light view**
to the stored depth at the texel location
in the Shadow Map
 - Equal: pixel is lit
 - Farther: pixel is in shadow



Example: Hellsweeper (2023)



Shadow Mapping [Williams78]

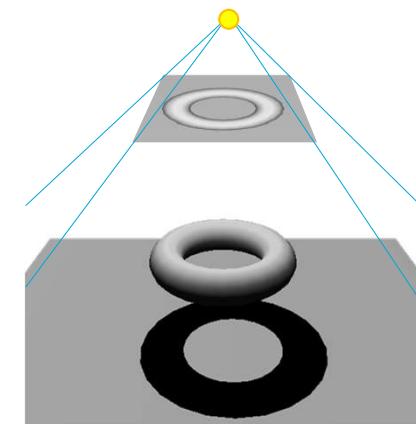
1. Render depth buffer from light (Shadow Map)

- Store result in a texture

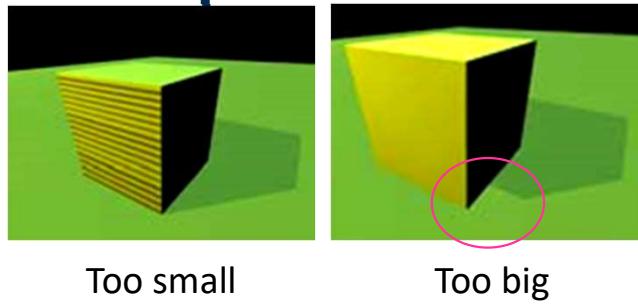
2. Render from viewpoint

- For each drawn pixel:
Compare its depth in the light view
to the stored depth at the texel location
in the Shadow Map

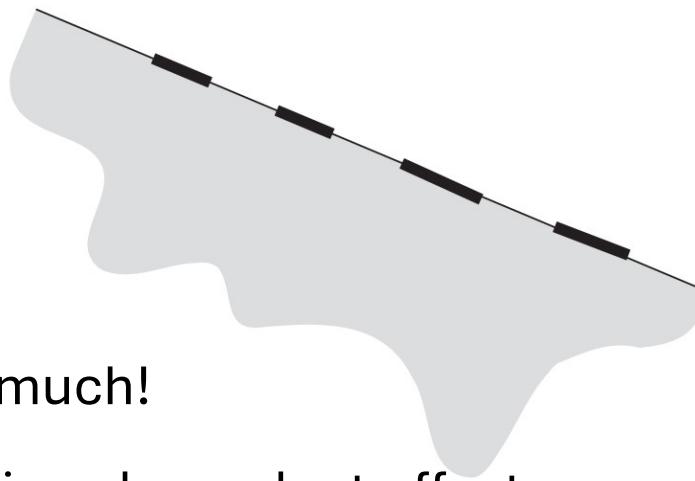
- Equal: pixel is lit
- Farther: pixel is in shadow



Problem 2: Depth Bias



- Self-shadowing
 - Discretisation
 - Limited precision
- Solution:
add an offset, but not too much!
- OpenGL supports orientation-dependent offsets



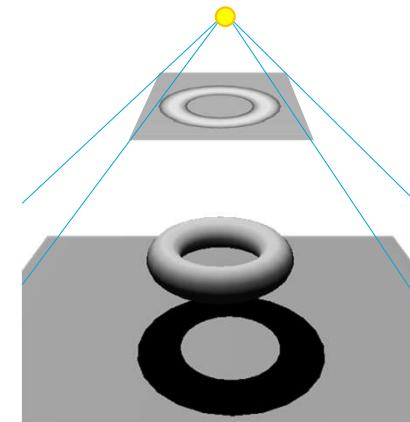
Problem 2: Depth Bias

- “Real-world” example in Crysis by Crytek



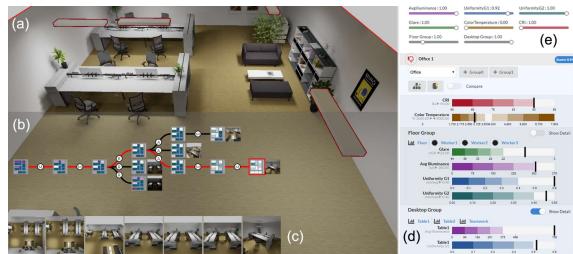
Conclusion: Shadow Mapping [Williams78]

- Simple, efficient, and easy to implement
- Compatible to most object representations
- Additional hardware support
- Variants are common
 - (games, movies...)



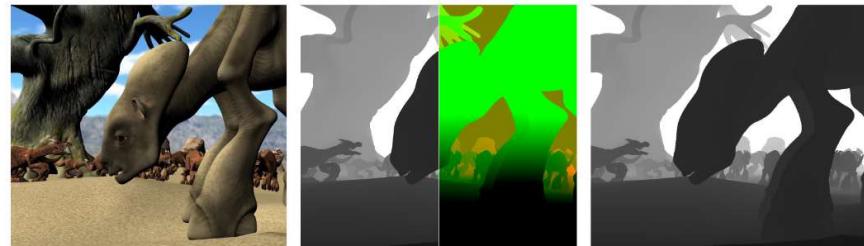
Shadow Maps have a widespread use!

Light Design



Schwaerzler et al. VIS2020

Real-time Visibility Testing of Objects



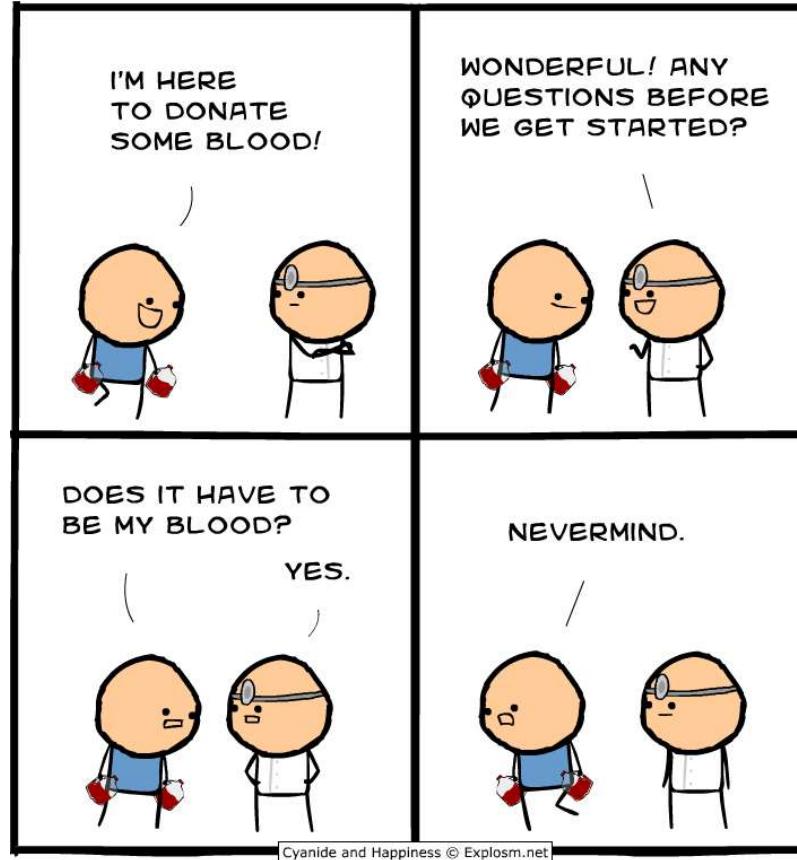
Lee et al. ToG2019

Urban Design

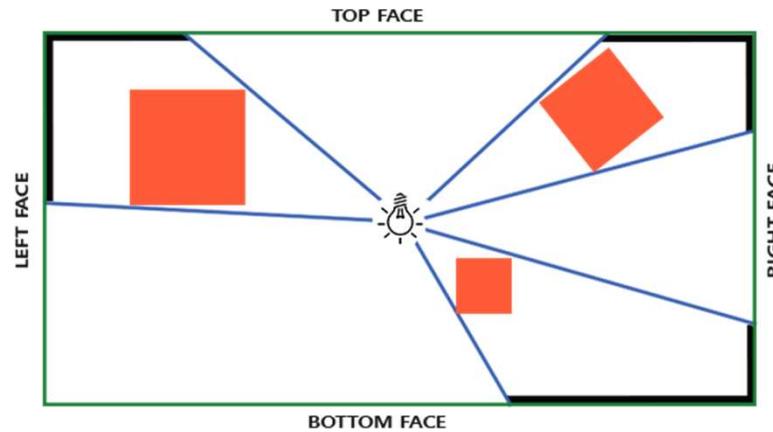


many many more...

Questions?

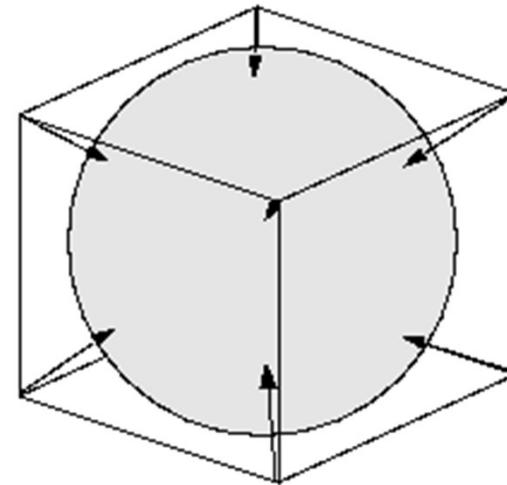
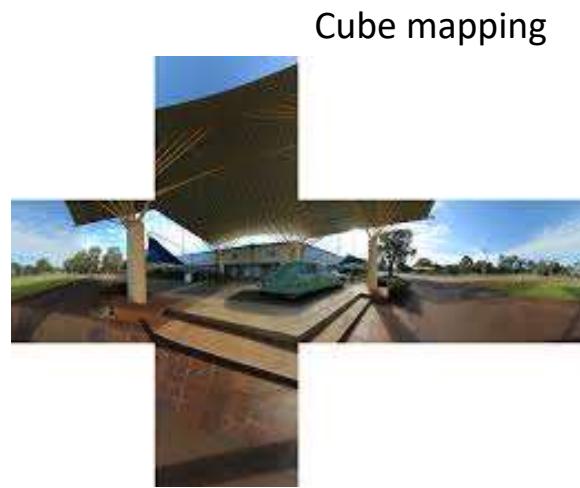


Omnidirectional Shadow Mapping?



Environment Mapping

- Render a shadow map for each view.
- Could use Geometry Shader to avoid 6 loops



Thank you very much
for your attention!

