

**Collaborators:**

**Colley 5.4 #4** Find the value of

$$\iiint_W z \, dV,$$

where  $W = [-1, 2] \times [2, 5] \times [-3, 3]$ , without resorting to explicit calculation.

■

**Colley 5.4 #5** Evaluate

$$\int_{-1}^2 \int_1^{z^2} \int_0^{y+z} 3yz^2 \, dx \, dy \, dz.$$

■

**Colley 5.4 #18** Integrate

$$f(x, y, z) = z$$

over  $W$ , where  $W$  is the region bounded by  $z = 0$ ,  $x^2 + 4y^2 = 4$ , and  $z = x + 2$ .

■

**Colley 5.4 #29(a),(b)** Consider the iterated integral

$$\int_{-2}^2 \int_0^{\frac{1}{2}\sqrt{4-x^2}} \int_{x^2+3y^2}^{4-y^2} (x^3 + y^3) \, dz \, dy \, dx.$$

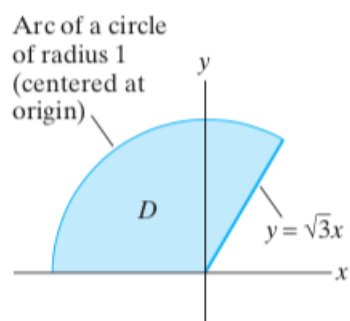
- (a) This integral is equal to a triple integral over a solid region  $W$  in  $\mathbb{R}^3$ . Describe  $W$ .
- (b) Set up an equivalent iterated integral by integrating first with respect to  $z$ , then with respect to  $x$ , then with respect to  $y$ . Do not evaluate your answer.

■

**Colley 5.5 #25** Evaluate

$$\iint_D \cos(x^2 + y^2) dA,$$

where  $D$  is the shaded region in the following figure.



■

**Colley 5.5 #31** Determine

$$\int \int \int_W (x^2 + y^2 + 2z^2) dV,$$

where  $W$  is the solid cylinder defined by the inequalities  $x^2 + y^2 \leq 4$ ,  $-1 \leq z \leq 2$ .

■

**Colley 5.5 #34** Determine the value of

$$\iiint_W \frac{dV}{\sqrt{x^2 + y^2 + z^2}},$$

where  $W$  is the region bounded by the two spheres  $x^2 + y^2 + z^2 = a^2$  and  $x^2 + y^2 + z^2 = b^2$ , for  $0 < a < b$ .

■

**Colley 5.5 #38** Determine

$$\int \int \int_W (2 + \sqrt{x^2 + y^2}) \, dV,$$

where  $W = \{(x, y, z) \mid \sqrt{x^2 + y^2} \leq z/2 \leq 3\}$ .

■