A Gas-Efficient Superlight Bitcoin Client in Solidity

ABSTRACT

Superlight clients enable the verification of proof-of-workbased blockchains by checking only a small representative number of block headers instead of all the block headers as done in SPV. Such clients can be embedded within other blockchains by implementing them as smart contracts, allowing for cross-chain verification. One such interesting instance is the consumption of Bitcoin data within Ethereum by implementing a Bitcoin superlight client in Solidity. While such theoretical constructions have demonstrated security and efficiency, no practical implementation exists. In this work, we put forth the first practical Solidity implementation of a superlight client which implements the NIPoPoW superblocks protocol. Contrary to previous work, our Solidity smart contract achieves sufficient gas-efficiency to allow a proof and counter-proof to fit within the gas limit of a block, making it practical. We provide extensive experimental measurements for gas. The optimizations that enable gas-efficiency heavily leverage a novel technique which we term hash-and-resubmit, which almost completely eliminates persistent storage requirements, the most expensive operation of smart contracts in terms of gas. Instead, the contract asks contesters to resubmit data and checks their veracity by hashing it. We show that such techniques can be used to bring down gas costs significantly and may have applications to other contracts. We also identify and rectify multiple implementation security issues of previous work such as premining vulnerabilities. Lastly, our implementation allows us to calculate concrete cryptoeconomic parameters for the superblocks NIPoPoWs protocol and in particular to make recommendations about the monetary value of the collateral parameters. We provide such parameter recommendations over a variety of liveness and adversarial bound settings.

CCS CONCEPTS

• Security and privacy → Use https://dl.acm.org/ccs.cfm to generate actual concepts section for your paper;

KEYWORDS

Blockchain; Superlight clients; NIPoPoWs, Solidity

1 INTRODUCTION

Blockchain interoperability [18] is the ability of distinct blockchains to communicate. This cross-chain [7, 9, 10, 13, 17] communication can enable useful features across blockchains such as the transfer of asset from one chain to another (one-way peg) and back (one-way peg) [13]. To date, there is no commonly accepted decentralized protocol that enables cross-chain transactions. Currently, crosschain operations are only

available to the users via third-party applications, such as multi-currency wallets. However, this treatment is opposing to the nature of decentralized currencies.

In general, crosschain-enabled blockchains A, B would support the following operations:

- Crosschain trading: A user with deposits in blockchain A, can make a payment to a user in blockchain B.
- Crosschain fund transfer: A user can transfers her funds from blockchain A to blockchain B. After this operation, the funds no longer exist in blockchain A. The user can later decide to transfer any portion of the original amount to the blockchain of origin.

In order to perform crosschain operations, there must be a mechanism to allow for users of blockchain A to discover events that occur in chain B, such that a transaction occurred. A trivial manner to perform such an audit is to participate as a full node in both chains. This approach, however, is impractical because a sizeable amount of storage is needed to host entire chains as they grow with time. As of May 2020, Bitcoin [15] chain spans roughly 245 GB, and Ethereum [2, 16] has exceeded 350 GB¹. Naturally, not all users are able to accommodate this size of data, especially if portable media are used, such as mobile phones.

An early solution to compress the extensive space of blockchain was given by Nakamoto with the Simplified Payment Verification (SPV) protocol [15]. In SPV, only the headers of blocks are stored, saving a considerable amount of storage. However, even with this protocol, the process of downloading and validating all block headers can lead to unpleasant user experience. In Ethereum, for instance, headers sum up to approximately $5.1~{\rm GB^2}$ of data. A mobile client needs several minutes, even hours, to fetch all information needed in order to function as an SPV client.

In order to deliver more practical solutions for blockchain transaction verification, a new generation of superlight clients [1, 8, 11, 12] emerged. In these protocols, cryptographic proofs are generated, which prove the occurrence of events inside a blockchain. Better performance is achieved due to considerably smaller size of proofs compared to the data needed in SPV. By utilizing superlight client protocols, a compressed proof for an event in chain A is constructed, and, if chain B supports smart contracts, the proof can then be verified automatically and transparently on-chain. Note that, this communication is realized without the intervention of third-party

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The size of the Bitcoin chain was derived from https://www.statista.com/statistics/647523/worldwide-bitcoin-blockchain-size/, and the size of the Ethereum chain by https://etherscan.io/chartsync/chaindefaults

²Calculated as the number of blocks (10,050,219) times the size of header (508 bytes). Statistics by https://etherscan.io/

applications. An interesting application of such a protocol is the communication between Bitcoin and Ethereum.

Related Work. We use the Non-Interactive Proofs of Proof of Work (NIPoPoWs) [12, 13] as the fundamental building block of our solution. This cryptographic primitive is *provably secure* and provides *succinct proofs* regarding the existence of an arbitrary event in a chain. Contrary to the linear growth rate of the underlying blockchain, NIPoPoWs span polylogarithmic size of blocks.

Christoglou [5], has provided a Solidity smart contract which is the first ever implementation of crosschain events verification based on NIPoPoWs, where proofs are submitted and checked for their validity. This solution, however, is impossible to apply to the real blockchain due to extensive usage of resources.

Our contributions. We put forth the following contributions:

- (1) We developed the first ever decentralized client that securely verifies crosschain events and is applicable to the real blockchain. Our client establishes a safe, cheap and trust-less solution to the interoperability problem. We implemented our client in Solidity, and we verify Bitcoin events to the Ethereum blockchain.
- (2) We present a novel pattern which we term hash-and-resubmit. This pattern improves the performance of Ethereum smart contracts [2, 16] in terms of gas consumption by utilizing calldata space to eliminate high-cost storage operations.
- (3) We design an *optimistic* schema for our client which can be used in the design of smart contracts replacing *non-optimistic* architectures. This design achieves the improvement of smart contracts' performance enabling multiple phases of interactions.
- (4) We prove via application that NIPoPoWs can be utilized in the real blockchain, making the cryptographic primitive the first ever provably secure construction of succinct proofs which is applied in a real setting.

Our implementation meets the following requirements:

- Secure: The client is invulnerable against all adversarial attacks.
- (2) Trustless: The client is not dependent on third-party applications and operates in a transparent, decentralized manner.
- (3) Practical: The client can be utilized in the real blockchain and comply with all environmental constraints, i.e. block gas limit and calldata size of Ethereum blockchain.
- (4) Cheap: The application is cheaper to use than the current state of the art technologies.

We selected Bitcoin as source blockchain as it the most used cryptocurrency and enabling crosschain transactions in Bitcoin is beneficial to the vast majority of blockchain community. We selected Ethereum as the target blockchain because it is also very popular and it supports smart contracts, which is a requirement in order to perform on-chain verification.

Structure. In Section 2 describe all blockchain technologies which are relevant to our work. In Section 3 we put forth In Section 4 we show ... and, finally, in Section 5, we discuss ...

2 THE HASH-AND-RESUBMIT PATTERN

We now introduce a novel design pattern for Solidity smart contracts which results into massive gas optimization due to the elimination of expensive storage operations.

Motivation. It is essential for smart contracts to store data in the blockchain. However, interacting with the storage of a contract is among the most expensive operations of the EVM. Therefore, only necessary data should be stored and redundancy should be avoided when possible. This is contrary to conventional software architecture, where storage is considered cheap. Usually, the performance of data access in traditional systems is related with time. However, in Ethereum performance is related to gas consumption. Access to persistent data costs a substantial amount of gas, which has a direct monetary value. One way to mitigate gas cost of reading variables from the blockchain is to declare them public. This leads to the creation of a getter function in the background, allowing free access to the value of the variable. But this treatment does not prevent the initial population of storage data, which is significantly costly, especially for large size of data. Towards the goal of implementing gas-efficient smart contracts, several patterns have been proposed [3, 4, 6].

By using the hash-and-resubmit pattern, large storage variables are omitted entirety, and structures are contained in memory which results to vastly improved performance. When a function call is performed, the arguments and signature of the function is included in the transactions field of the body of a block. The contents of blocks are public to the network, therefore this information is available to nodes. By simply observing blocks, a node retrieves data sent by other users, which be processed off-chain. To advertise the process of data to the public network, the node re-sends the retrieved data accompanied with complementary data depending on the context of the application. While the concept of resending data would be inefficient in conventional systems

...

Applicability. We now list the cases in which the *hash-and-resubmit* pattern is efficient to use:

- Avoid high gas cost due to extensive storage read/write and make smart contracts that exceed block gas limit practical.
- (2) Interact with smart contract depending of previous actions of other users
- (3) Process data off-chain

Participants and collaborators. The participants are the smart contract S which accepts function calls, the client E_1 ,

who dispatches arbitrary data d to contract $\mathtt{send}(d)$, and the observer E_2 , who is a node that observes transactions towards S in the blockchain. After observation, E_2 retrieves data d. Finally, E_2 acts as a client, making an interaction with S , $\mathtt{send}(d)$. However, we need to consider that since the retrieval was realized off-chain, a malicious E_2 may alter d before interacting with S . We will denote the potentially modified data as d^* . The verification that $d = d^*$ consists a part of the pattern and is performed during $\mathtt{send}(d^*)$.

Implementation. The implementation of this pattern is divided into two parts. The first part covers the way d^* is retrieved by E_2 , whereas the second part explains how the we verify that $d=d^*$. The challenge here is twofold:

- (1) Availability: E_2 must be able to retrieve d without the need of accessing on-chain data.
- (2) Consistency: E_2 must be prevented from dispatching d^* that differs from the originally submitted d.

Hash-and-resubmit technique is performed in two stages to face these challenges: (a) the hash phase, which addresses reliability, and (b) the resubmit phase which addresses availability.

Addressing availability: During hash phase, E_1 makes the function call $\mathtt{send}(d)$. This transaction, which includes a function signature (\mathtt{send}) and the corresponding data (d), is added in a block by a miner. Due to blockchain's transparency, the observer of \mathtt{send} , E_2 , retrieves a copy of d, without the need of accessing contract data.

Addressing reliability: We prevent an adversary E_2 from altering d^* by storing the *hash* of d in contract's state during the execution of $\mathsf{send}(\mathsf{d})$ by E_1 . Although we can make use of any cryptographic hash function it is convenient to use the pre-compiled $\mathsf{sha256}$ hash function of Solidity:

$$hash = sha256(d)$$

Then, during contest phase, a verification is performed by comparing the stored hash of d with the hash of d^* .

```
require(hash = sha256(datao))
```

In solidity, the size of the hash is 32 bytes. To persist such a small value in contract's memory only adds a constant, negligible cost overhead.

Sample. We will now demonstrate the usage of the hash-and-resubmit pattern with a practical example. We create a smart contract that orchestrates a game between two players, P1 and P2. The winner is the player with the most valuable array. The interaction between the players and the smart contract is realized in two phases: (a) Submit phase and (b) Contest phase.

Submit phase: P1 submits an N-sized array, $array_1$ and becomes the holder of the contract.

Contest phase: P2 submits $array_2$. If $array_2 > array_1$, then the *holder* of the contract is changed. The comparison between the two arrays can be implemented arbitrarily.

We make use of the hash-and-resubmit pattern by demanding from P2 to provide two arrays to the contract during contest phase: (a) $array_1^*$, which is a copy of the originally

submitted array by P1, and (b) $array_2$, which is the contesting array.

We show the storage implementation of the above game in Algorithm ?? and the hash-and-resubmit version in Algorithm ??.

Algorithm 1 Compare N-sized arrays using storage

```
1: function Submit(array)
      best\_array \leftarrow array
                                    ▷ array saved in storage
3:
      holder \leftarrow msg.sender
4:
      return true
5: end function
1: function Contest(new_array)
      if !compare(new_array) then
3:
         return false
4:
      end if
5:
      holder \leftarrow msg.sender
      return true
6:
7: end function
1: function compare(new_array)
      for i in best\_array.length do
         if new\_array[i] < best\_array[i] then
3:
             return false
4:
         end if
5:
      end for
      return true
8: end function
```

Gas analysis. The gas consumption of the two algorithms is displayed in Figure 1.

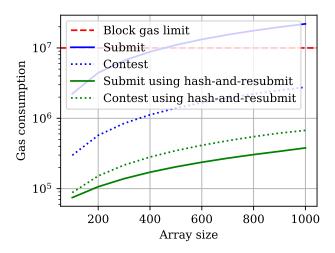


Figure 1: Gas-cost reduction using the *hash-and-resubmit* pattern. By avoiding gas-heavy storage operations, the cost of function invocations is decreased significantly by 93-95%.

Algorithm 2 Compare N-sized arrays using hash-and-resubmit pattern

```
1: function Submit(array[N])
2:
       hash \leftarrow sha256(array)
                                      ⊳ hash saved in storage
3:
       holder \leftarrow msg.sender
       return true
4:
5: end function
1:
   function Contest(existing\_array, new\_array)
2:
       if hash256(existing\_array) \neq hash then
          return false
                                    ▷ Invalid original_array
3:
4:
       if !compare(original_array, new_array) then
5:
          return false
6:
       end if
7:
       holder \leftarrow msq.sender
8:
       return true
9:
10: end function
1: function compare (array_1, array_2)
       for i in array_1.length do
2.
          if array_1[i] \leq array_2[i] then
3:
              return false
4:
           end if
5:
       end for
6:
       return true
7.
8: end function
```

By using the hash-and-resubmit pattern, the gas consumption decreased by 93-95%. This significantly affects the applicability of the contract. Note that, the storage implementation exceeds the Ethereum block gas limit for arrays of size 500 and above, contrary to the hash-and-resubmit-optimized version, which consumes approximately 1/10th of the block gas limit for arrays of 1000 elements.

Consequences

Known uses. To our knowledge, we are the first to combine the notion of the transparency of the blockchain with signatures of data structures to eliminate storage variables from Solidity smart contracts by resubmitting data.

Hash-and-Resubmit. We introduce a novel design pattern for Solidity smart contracts that results into massive gas optimization. This technique, which we term <code>hash-and-resubmit</code>, is based on observing public data of the blockchain in order to leverage <code>off-chain</code> operations. By utilizing <code>hash-and-resubmit</code>, the performance of the smart contract is improved considerably since computations are performed locally by the user, and gas-heavy storage variables are discarded.

The critical observation we make is that persistent data structures, i.e. arrays, can be migrated from storage to memory space. Such an adjustment results to substantial increase of smart contracts' performance due to the sizable discrepancy between persistent and temporary memory operations. This is due to the fact that in the body of the Ethereum block, information regarding transactions is stored. Nodes have access to this information which includes signatures and input arguments of function invocations, as shown in Figure 2. This type of *off-chain* access can be applied by any node.

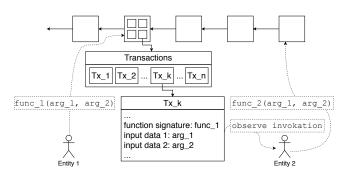


Figure 2: Entity 1 makes a function call with arguments arg1 and arg2. Entity 2 reads the content of transactions in the block and retrieves the input data. Entity 2 can use this data to make a different invocation.

Enabling NIPoPoWs. We now present how the hash-and-resubmit pattern can used in the context of the NIPoPoW superlight client. Similar to the aforementioned example, the NIPoPoW verifier adheres to a submit-and-contest-phase schema, and the inputs of the functions are arrays that are processed on-chain.

In submit-phase, a proof is submitted, which can be contested by another user in contest-phase. The user that initiates the contest, needs to monitor the traffic of the smart contract. This is a logical assumption as mentioned in the NIPoPoW paper. The input of submit function includes the submit proof, π_{subm} , that indicates the occurrence of an event, e, in the source chain, and the input of contest function includes the contesting proof, π_{cont} . A successful contest of the π_{subm} is realized when π_{cont} a better score. The process of score evaluation, which is described in [12] is irrelevant to the pattern, and remains unchained.

In previous work [5], NIPoPoW arrays are stored on-chain during submit-phase, and are processed during contest-phase. This operation is performed by utilizing storage, which limits the applicability of the contract considerably. In Algorithm ?? we show how hash-and-resubmit pattern is embedded into the NIPoPoW client. In Figure 3 we display how the gas consumption differentiates from previous work for the aggregated cost of submit and contest phase.

3 REMOVING MUTABLE STORAGE

Now that we can freely retrieve immutable structures, we can focus on other storage variables. A challenge we faced is that the protocol of NIPoPoWs dependents on DAG structure which is a mutable hashmap. This logic is intuitive and efficient to implement in most traditional programming

 $^{^3\}mathrm{As}$ of July 2020, the Ethereum block gas limit approximates $10{,}000{,}000$ gas units

Algorithm 3 The NIPoPoW client using hash-and-resubmit pattern

```
1: function Constructor(genesis)
        Gen \leftarrow genesis
3: end function
 1: function Submit(\pi, e)
        require(\pi[0] = Gen)
2:
        require(events[e].pred = false)
3:
 4:
        require(validInterlink(\pi))
        DAG_s \leftarrow DAG_s \cup \pi
 5:
        events[e].hash \leftarrow sha256(\pi)
                                                     ⊳ enable pattern
6:
        ancestors_s \leftarrow findAncestors(DAG_s)
 7:
        events[e].pred \leftarrow evaluatePredicate(ancestors_s, e)
 8:
        delete ancestors
9:
10: end function
 1: function Contest(\pi, \tilde{\pi}, e) \triangleright dispatch \pi^*_{sumb} and \pi_{cont}
        require(events[e].hash = sha256(\pi)) \triangleright verify \pi^*_{subm}
2:
3:
        require(\tilde{\pi}[0] = Gen)
        require(events[e].pred = true)
 4.
        require(validInterlink(\tilde{\pi}))
 5:
6:
        lca = findLca(\pi, \tilde{\pi})
        require(score(\tilde{\pi}[:lca]) > score(\pi[:lca]))
 7:
        DAG \leftarrow DAG \cup \tilde{\pi}
8:
        ancestors_s \leftarrow findAncestors(DAG_s)
9:
        events[e].pred \leftarrow evaluatePredicate(ancestors_s, e)
10:
        delete ancestors
11:
12: end function
```

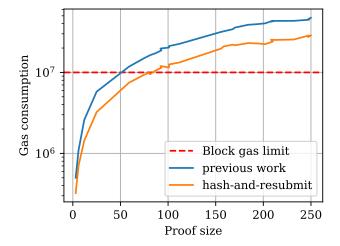


Figure 3: Performance improvement using hash-and-resubmit pattern in NIPoPoWs related to previous work. The gas consumption decreased by approximately 50%

languages such as C++, JAVA, Python, JavaScript, etc. However, as our analysis demonstrates, such an algorithm cannot

be efficiently implemented in Solidity. This is not due to the lack of support of look-up structures, but because Solidity hashmaps can only be contained in storage. Other mutable structures, such as *ancestors* that are stored in the persistent memory also affect performance, especially for large proofs.

We make a keen observation regarding the possible position of the *block of interest* in the proof which lead us the constriction of an architecture that does not require DAG, ancestors or any other complementary structures. We will use the notation from [12] to present our claim.

Position of block of interest. NIPoPoWs are sets of sampled interlinked blocks, which means that they can be perceived as chains. If π_1 differs from π_2 , then a fork is created at the index of the last common ancestor (lca). The block of interest, b, lies at a certain index within π_{subm} and indicates a stable predicate [12, 14] that is true for π_{subm} . The case in which b is absent from π_{subm} is aimless, because the submission automatically fails since the predicated is evaluated against π_{subm} . We will refer to such aimless actions as irrational and components that are included in such actions irrational components, i.e. irrational proof, blocks etc. We will use the term rational to describe non-irrational actions and components.

The entity that initiates the contest of π_{subm} , tries to prove the falseness of the underlying predicate against π_{cont} . This means that, if the block of interest is included in π_{cont} , then the contest is irrational.

In the NIPoPoW protocol, proofs' segments $\pi_{subm}\{: lca\}$ and $\pi_{cont}\{: lca\}$ are merged to prevent adversaries from skipping or adding blocks, and the predicate is evaluated against $\pi_{subm}\{: lca\} \cup \pi_{cont}\{: lca\}$. We observe that $\pi_{submit}\{: lca\}$ can be omitted because there is no block $\{B: B \notin \pi_{subm}\{: lca\} \land B \in \pi_{cont}\{: lca\}\}$ that results to positive evaluation of the predicate. This is due to the fact that b is not included in $\pi_{cont}\{: lca\}$, and, presumably there is no B such that b = B.

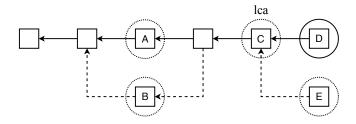


Figure 4: Fork of two chains. Solid lines connection blocks of π_{subm} and dashed lines connect blocks of π_{cont} . Given the configuration, blocks in dashed circles are irrational blocks of interest, and the block i in the solid circle is a rational block of interest.

In Figure 4 we display a fork of two proofs. Solid lines connect blocks of π_{subm} and dashed lines connect blocks of π_{cont} . Examining which scenarios are rational depending on different positions of the block of interest, we observe

that blocks B, C and E do not qualify, because they are included only in π_{cont} . Block A is included in $\pi_{subm}\{:lca\}$, which means that π_{cont} is an irrational contest. Given this configuration, the only rational block of interest is D.

Minimal forks. By combining the above observations, we derive that, π_{cont} can be truncated into $\pi_{cont}\{:lca\}$ without affecting the correctness of the protocol. We will term this truncated proof π_{cont}^{tr} . Security is preserved if we require π_{cont}^{tr} to be a minimal fork of π_{subm} . A minimal fork is a fork chain that shares exactly one common block with the main chain. Proof $\tilde{\pi}$, which is a minimal fork of proof π , has the following attributes:

- $\begin{array}{ll} (1) & \pi\{lca\} = \tilde{\pi}[0] \\ (2) & \pi\{lca:\} \cap \tilde{\pi}[1:] = \varnothing \end{array}$
- By requiring that π_{cont}^{tr} is a minimal fork of π_{subm} , we prevent an adversary from dispatching an augmented π_{cont}^{tr} to claim better score against π_{subm} . Such an attempt is displayed in Figure 5.

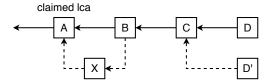


Figure 5: An adversary tries to send a malformed proof consisting of blocks {A, X, B, C, D'} that achieves better score against {A, B, C, D}. This attempt is rejected due to the minimal-fork requirement.

In Algorithm $\ref{thm:eq:condition}$, we show how minimal fork technique is incorporated in our client, replacing DAG and ancestors. In Figure 6 we show how the performance of the client has improved.

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Algorithm 4 The NIPoPoW client using the minimal fork technique

```
1: function Submit(\pi, e)
       require(\pi[0] = Gen)
       require(events[e] = false)
       require(validInterlink(\pi))
       events[e].pred \leftarrow evaluatePredicate(\pi, e)
       events[e].hash \leftarrow sha256(\pi)
7: end function
1: function Contest(\pi, \tilde{\pi}, e, f)
                                                \triangleright f: fork index in \pi
       require(\tilde{\pi}[0] = \pi[f])
                                            ▷ check min. fork head
       require(events[e].hash = sha256(\pi))
3:
       require(events[e].pred = true)
4:
       require(validInterlink(\tilde{\pi}))
5:
       require(disjoint(\pi[f+1:], \tilde{\pi}[1:])) \triangleright check min. fork
6:
7:
       require(score(\tilde{\pi}) > score(\pi[f:]))
       events[e].pred \leftarrow evaluatePredicate(\tilde{\pi}, e)
9: end function
```

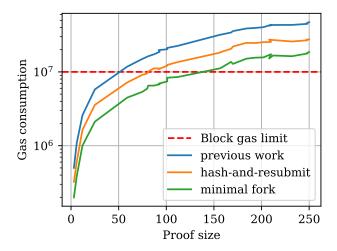


Figure 6

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 $[\]overline{^4\text{We cannot}}$ proceed to further truncation of $\pi^{tr}_{cont},$ because in the NIPoPoW protocol blocks within segment $\pi\{:lca\}$ of each proof are required for the score calculation.

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