

**IE 203****HW1**

Process and Due times:

Jobs	1	2	3	4	5
Process Time	2	2	2	3	1
Due Time	3	3	2	6	4

Sets:

J: Jobs ( $j = 1, 2, 3, 4, 5$ )

T: Intervals ( $t = 1, 2, \dots, 10$ )

Parameters:

$P_{tj}$ : process time of job  $j$

$D_{tj}$ : due time of job  $j$

Decision Variables:

$X_{jt}$ : 1 if job  $j$  begins at time  $t$   
0 o/w

$Tardy_j$ : 1 if job  $j$  could not be completed in time  
0 o/w

The Objective Function:  $\min z = \sum Tardy_j$

Subject to:

$$\sum_{t=1}^{T-P_{tj}+1} X_{jt} = 1$$

$$X_{jt+1} - X_{jt} \leq 1 \quad \text{first approach constraint } O(J^2 \cdot T^2)$$

$$\sum_{j=1}^J \sum_{s=\max\{0, t-P_{tj}+1\}}^t X_{jt} \leq 1 \quad \text{second approach constraint } O(T)$$

$$j' \in J \setminus \{j\}$$

$$X_{(j,t)} = \{1, 0\}$$

$$Tardy_{(j,t)} = \{1, 0\}$$