CS3230 Tutorial 6

AY 25/26 Sem 1—github/omgeta

Q1). (a)
$$TRI(x, y) = 0 \text{ if } y - x \le 1$$

(b)
$$TRI(x,y) = \min_{i \in [x+1,y-1]\{TRI(x,i)+W(x,i,y)+TRI(i,y)\}}$$

Q2).
$$T(n) = n + (T(1) + T(n-1)) + (T(2) + T(n-2)) + \dots + (T(n-1) + T(1))$$

= $n + 2T(1) + 2T(2)) + \dots + 2T(n-1) = n + 2\sum_{i=1}^{n-1} T(i)$
So, $T(n-1) = (n-1) + 2\sum_{i=1}^{n-2} T(i)$

Then,
$$T(n) - T(n-1) = 1 + 2T(n-1) \implies T(n) = 1 + 3T(n-1) \implies T(n) = \Theta(3^n)$$

- Q3). (c) There are n^2 subproblems with many overlaps
- Q4).