

Data Structures & Algorithms

Quick Sort Algorithm

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Theme 1: The Problem

۷ - بر روی داده های زیر دو مرحله مرتب سازی سریع را اجرا کنید (pivot اولین عنصر). مرتب سازی به صورت نزولی انجام شود. (۱.۵ نمره)

33, 40, 2, 19, 71, 55, 29, 60, 22, 26

Theme 2: Solution

Reasoning

The goal of the partitioning stage is to place the pivot in its final sorted position such that:

- ✓ All elements to its left are $\geq pivot$ (since we are sorting in descending order, these are the smaller elements).
- ✓ All elements to its right are $\leq pivot$ (these are the larger elements).

First Pass:

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.

$A[i] > \text{pivot}$	pivot	i								j
$A[j] < \text{pivot}$	↓	↓								↓
$i < j$	33,	40,	2,	19,	71,	55,	29,	60,	22,	26

$A[i] < \text{pivot}$	pivot	i							j	
$A[j] < \text{pivot}$	↓	↓							↓	
$i < j$	33,	40,	2,	19,	71,	55,	29,	60,	22,	26

$A[i] < \text{pivot}$	pivot	i						j		
$A[j] > \text{pivot}$	↓	↓						↓		
$i < j$	33,	40,	2,	19,	71,	55,	29,	60,	22,	26

First Pass (Cont.):

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.

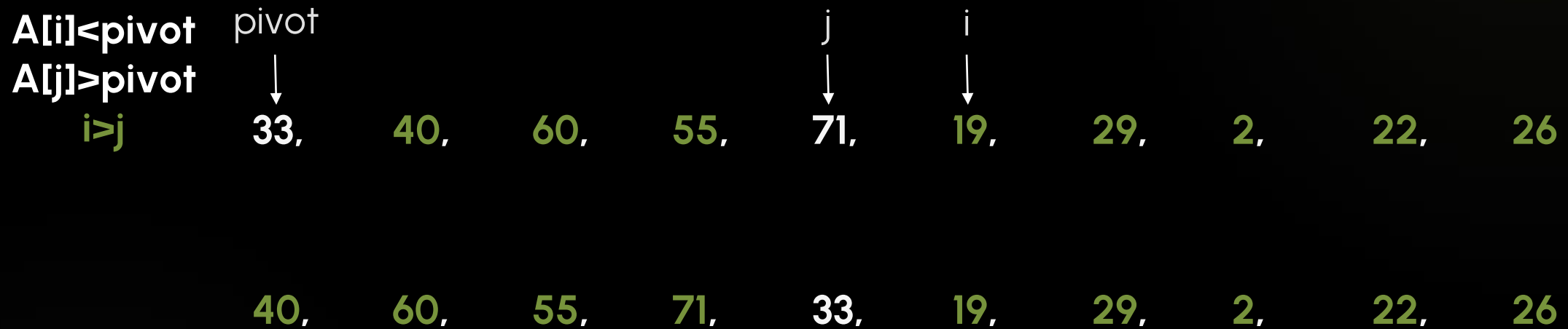
$A[i] < \text{pivot}$	pivot			i			j			
$A[j] < \text{pivot}$	↓			↓			↓			
$i < j$	33,	40,	60,	19,	71,	55,	29,	2,	22,	26

$A[i] < \text{pivot}$	pivot			i		j				
$A[j] > \text{pivot}$	↓			↓		↓				
$i < j$	33,	40,	60,	19,	71,	55,	29,	2,	22,	26

$A[i] > \text{pivot}$	pivot			i, j						
$A[j] > \text{pivot}$	↓			↓						
$i = j$	33,	40,	60,	55,	71,	19,	29,	2,	22,	26

First Pass (Cont.):

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.



Second Pass – First Part:

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.

$A[i] > \text{pivot}$
 $A[j] > \text{pivot}$
 $i < j$

pivot	i		j
↓	↓		↓
40,	60,	55,	71

$A[i] < \text{pivot}$
 $A[j] < \text{pivot}$
 $i < j$

pivot		i	j
↓		↓	↓
40,	60,	55,	71

$A[i] < \text{pivot}$
 $A[j] < \text{pivot}$
 $i = j$

pivot			i, j
↓			↓
40,	60,	55,	71

Second Pass – First Part:

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.

60, 55, 71, 40

Second Pass – Second Part:

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.

$A[i] > \text{pivot}$
 $A[j] > \text{pivot}$
 $i < j$

pivot	i			j
↓	↓			↓
19,	29,	2,	22,	26

$A[i] < \text{pivot}$
 $A[j] > \text{pivot}$
 $i < j$

pivot		i		j
↓		↓		↓
19,	29,	2,	22,	26

$A[i] > \text{pivot}$
 $A[j] > \text{pivot}$
 $i = j$

pivot			i, j	
↓			↓	
19,	29,	26,	22,	2

Second Pass – Second Part:

Move i right while $A[i] > \text{pivot}$ and move j left while $A[j] < \text{pivot}$.
When both stop, swap $A[i]$ and $A[j]$ — but only while $i < j$.

$A[i] < \text{pivot}$
 $A[j] > \text{pivot}$
 $i > j$

	pivot			j	i
	↓			↓	↓
	19,	29,	26,	22,	2
		29,	26,	22,	19,
					2

Assembling:

60, 55, 71, 40, 33, 29, 26, 22, 19, 2

Questions?

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