

Statistical Analysis of Edmonds Karp, Ford Flukerson and Dinic Running Times

All these numbers were obtained running on an Intel i3-5005U CPU @ 2.0 GHz running on the same 100 test cases for each algorithm

```
In [1]: # read data
ford_flukerson = [] # data for ford flukerson
with open("FordFlukerson.txt") as text:
    ford_flukerson = [line.split(',') for line in text]
edmonds_karp = []
with open("EdmonsKarp.txt") as text:
    edmonds_karp = [line.split(',') for line in text]
Dinic = []
with open("Dinc.txt") as text:
    Dinic = [line.split(',') for line in text]
# make data integers
for i in range(len(ford_flukerson)):
    for j in range(len(ford_flukerson[i])):
        ford_flukerson[i][j] = ford_flukerson[i][j].rstrip('\n')
        ford_flukerson[i][j] = int(ford_flukerson[i][j])
        edmonds_karp[i][j] = edmonds_karp[i][j].rstrip('\n')
        edmonds_karp[i][j] = int(edmonds_karp[i][j])
        Dinic[i][j] = Dinic[i][j].rstrip('\n')
        Dinic[i][j] = int(Dinic[i][j])
```

Performance comparison

```
In [2]: total_ford = 0
for line in ford_flukerson:
    total_ford += line[3]
total_edmonds = 0
for line in edmonds_karp:
    total_edmonds += line[3]
total_dinic = 0
for line in Dinic:
    total_dinic += line[3]
print(
    "Total time for ford flukerson is " + str(total_ford) + " milliseconds, which is "
    + str(total_ford/(1000*60*60)) + " hours.")
print(
    "Total time for edmonds karp is " + str(total_edmonds) + " milliseconds, which is "
    + str(total_edmonds/(1000)) + " seconds.")
print(
    "Total time for dinic is " + str(total_dinic) + " milliseconds, which is "
    + str(total_dinic/(1000)) + " seconds.")
```

Total time for ford flukerson is 74524494 milliseconds, which is 20.701248333333332 hours.

Total time for edmonds karp is 56315 milliseconds, which is 56.315 seconds.

Total time for dinic is 56315 milliseconds, which is 1.971 seconds.

```
In [3]: total_ford/total_edmonds
```

```
Out[3]: 1323.3506880937584
```

```
In [4]: total_edmonds/total_dinic
```

```
Out[4]: 28.571790969051243
```

From the above we deduce that ford flukerson is more than 1300 times slower than edmonds karp and that dinic is 21 times faster than edmonds karp.

Performance difference on each test case

```
In [5]: ctr_edmonds = 0
ctr_ford = 0
ctr_same = 0
for i in range(len(ford_flukerson)):
    print("=====")
    print("Test#" + str(i + 1))
    print("Number of nodes: " + str(ford_flukerson[i][0]))
    print("Number of edges: " + str(ford_flukerson[i][1]))
    print("Max Flow: " + str(ford_flukerson[i][2]))
    print("Time took by ford flukerson: " + str(ford_flukerson[i][3]))
    print("Time took by edmonds karp: " + str(edmonds_karp[i][3]))
    print("Time took by Dinic: " + str(Dinic[i][3]))
    print("=====")
```

```
=====  
Test#1
```

```
Number of nodes: 292  
Number of edges: 42296  
Max Flow: 7551533  
Time took by ford flukerson: 2595346  
Time took by edmonds karp: 983  
Time took by Dinic: 23
```

```
=====  
Test#2
```

```
Number of nodes: 374  
Number of edges: 18946  
Max Flow: 1710813  
Time took by ford flukerson: 383112  
Time took by edmonds karp: 213  
Time took by Dinic: 31
```

```
=====  
Test#3
```

```
Number of nodes: 32  
Number of edges: 35775  
Max Flow: 53269950  
Time took by ford flukerson: 18821  
Time took by edmonds karp: 2600  
Time took by Dinic: 17
```

```
=====  
Test#4
```

```
Number of nodes: 319  
Number of edges: 14722  
Max Flow: 2496153  
Time took by ford flukerson: 350001  
Time took by edmonds karp: 96  
Time took by Dinic: 11
```

```
=====  
Test#5
```

```
Number of nodes: 351
```

Number of edges: 8508
Max Flow: 1343485
Time took by ford flukerson: 155305
Time took by edmonds karp: 43
Time took by Dinic: 8

Test#6

Number of nodes: 257
Number of edges: 32405
Max Flow: 6216967
Time took by ford flukerson: 1492679
Time took by edmonds karp: 468
Time took by Dinic: 38

Test#7

Number of nodes: 368
Number of edges: 29879
Max Flow: 4183913
Time took by ford flukerson: 1081498
Time took by edmonds karp: 496
Time took by Dinic: 17

Test#8

Number of nodes: 377
Number of edges: 42155
Max Flow: 5169099
Time took by ford flukerson: 2118126
Time took by edmonds karp: 623
Time took by Dinic: 32

Test#9

Number of nodes: 171
Number of edges: 12438
Max Flow: 4087840
Time took by ford flukerson: 123517
Time took by edmonds karp: 50
Time took by Dinic: 12

Test#10

Number of nodes: 106
Number of edges: 7791
Max Flow: 3621538
Time took by ford flukerson: 11048
Time took by edmonds karp: 30
Time took by Dinic: 36

Test#11

Number of nodes: 100
Number of edges: 30080
Max Flow: 14860593
Time took by ford flukerson: 186985
Time took by edmonds karp: 1473
Time took by Dinic: 25

Test#12

Number of nodes: 72
Number of edges: 5676
Max Flow: 3853918

Time took by ford flukerson: 2128

Time took by edmonds karp: 51

Time took by Dinic: 3

Test#13

Number of nodes: 52

Number of edges: 11429

Max Flow: 10036046

Time took by ford flukerson: 3133

Time took by edmonds karp: 133

Time took by Dinic: 8

Test#14

Number of nodes: 243

Number of edges: 46011

Max Flow: 9468701

Time took by ford flukerson: 3681020

Time took by edmonds karp: 733

Time took by Dinic: 54

Test#15

Number of nodes: 472

Number of edges: 7545

Max Flow: 461142

Time took by ford flukerson: 79830

Time took by edmonds karp: 20

Time took by Dinic: 8

Test#16

Number of nodes: 411

Number of edges: 43024

Max Flow: 4810117

Time took by ford flukerson: 2962709

Time took by edmonds karp: 220

Time took by Dinic: 27

Test#17

Number of nodes: 294

Number of edges: 7852

Max Flow: 1254953

Time took by ford flukerson: 99732

Time took by edmonds karp: 29

Time took by Dinic: 7

Test#18

Number of nodes: 339

Number of edges: 12610

Max Flow: 1278247

Time took by ford flukerson: 150920

Time took by edmonds karp: 24

Time took by Dinic: 6

Test#19

Number of nodes: 250

Number of edges: 47844

Max Flow: 8289874

Time took by ford flukerson: 2858696

Time took by edmonds karp: 996

Time took by Dinic: 31

Test#20

Number of nodes: 415

Number of edges: 10063

Max Flow: 1377622

Time took by ford flukerson: 225128

Time took by edmonds karp: 56

Time took by Dinic: 7

Test#21

Number of nodes: 420

Number of edges: 1117

Max Flow: 3994

Time took by ford flukerson: 0

Time took by edmonds karp: 0

Time took by Dinic: 0

Test#22

Number of nodes: 110

Number of edges: 36677

Max Flow: 15375424

Time took by ford flukerson: 291145

Time took by edmonds karp: 1091

Time took by Dinic: 26

Test#23

Number of nodes: 258

Number of edges: 36062

Max Flow: 6466940

Time took by ford flukerson: 1542134

Time took by edmonds karp: 469

Time took by Dinic: 24

Test#24

Number of nodes: 141

Number of edges: 44417

Max Flow: 14682472

Time took by ford flukerson: 1342594

Time took by edmonds karp: 973

Time took by Dinic: 30

Test#25

Number of nodes: 346

Number of edges: 12602

Max Flow: 1793164

Time took by ford flukerson: 276340

Time took by edmonds karp: 48

Time took by Dinic: 9

Test#26

Number of nodes: 445

Number of edges: 8226

Max Flow: 833501

Time took by ford flukerson: 114100

Time took by edmonds karp: 13

Time took by Dinic: 6

```
=====
Test#27
Number of nodes: 84
Number of edges: 19531
Max Flow: 11318345
Time took by ford flukerson: 32084
Time took by edmonds karp: 299
Time took by Dinic: 12
=====
```

```
=====
Test#28
Number of nodes: 101
Number of edges: 47244
Max Flow: 22942730
Time took by ford flukerson: 768200
Time took by edmonds karp: 1809
Time took by Dinic: 36
=====
```

```
=====
Test#29
Number of nodes: 160
Number of edges: 29090
Max Flow: 9153164
Time took by ford flukerson: 444814
Time took by edmonds karp: 385
Time took by Dinic: 24
=====
```

```
=====
Test#30
Number of nodes: 92
Number of edges: 6839
Max Flow: 3443917
Time took by ford flukerson: 5730
Time took by edmonds karp: 48
Time took by Dinic: 4
=====
```

```
=====
Test#31
Number of nodes: 169
Number of edges: 25553
Max Flow: 7200214
Time took by ford flukerson: 458376
Time took by edmonds karp: 196
Time took by Dinic: 9
=====
```

```
=====
Test#32
Number of nodes: 219
Number of edges: 17907
Max Flow: 3561733
Time took by ford flukerson: 307818
Time took by edmonds karp: 56
Time took by Dinic: 11
=====
```

```
=====
Test#33
Number of nodes: 396
Number of edges: 12897
Max Flow: 1167579
Time took by ford flukerson: 150252
Time took by edmonds karp: 66
Time took by Dinic: 10
=====
```

```
=====
Test#34
```

Number of nodes: 98
Number of edges: 46311
Max Flow: 22415557
Time took by ford flukerson: 465946
Time took by edmonds karp: 3325
Time took by Dinic: 40

Test#35

Number of nodes: 137
Number of edges: 36107
Max Flow: 11900558
Time took by ford flukerson: 475420
Time took by edmonds karp: 410
Time took by Dinic: 29

Test#36

Number of nodes: 234
Number of edges: 45357
Max Flow: 9469420
Time took by ford flukerson: 2432396
Time took by edmonds karp: 846
Time took by Dinic: 35

Test#37

Number of nodes: 218
Number of edges: 38183
Max Flow: 8787699
Time took by ford flukerson: 1759380
Time took by edmonds karp: 798
Time took by Dinic: 19

Test#38

Number of nodes: 173
Number of edges: 39120
Max Flow: 10076362
Time took by ford flukerson: 983030
Time took by edmonds karp: 956
Time took by Dinic: 18

Test#39

Number of nodes: 206
Number of edges: 489
Max Flow: 70450
Time took by ford flukerson: 43
Time took by edmonds karp: 0
Time took by Dinic: 0

Test#40

Number of nodes: 257
Number of edges: 34255
Max Flow: 6239594
Time took by ford flukerson: 1384291
Time took by edmonds karp: 564
Time took by Dinic: 19

Test#41

Number of nodes: 471
Number of edges: 9586

Max Flow: 880325
Time took by ford flukerson: 146568
Time took by edmonds karp: 62
Time took by Dinic: 21

Test#42

Number of nodes: 161
Number of edges: 40025
Max Flow: 11593045
Time took by ford flukerson: 1004592
Time took by edmonds karp: 817
Time took by Dinic: 29

Test#43

Number of nodes: 143
Number of edges: 6487
Max Flow: 2045388
Time took by ford flukerson: 15870
Time took by edmonds karp: 43
Time took by Dinic: 4

Test#44

Number of nodes: 181
Number of edges: 32926
Max Flow: 8696594
Time took by ford flukerson: 979586
Time took by edmonds karp: 645
Time took by Dinic: 29

Test#45

Number of nodes: 12
Number of edges: 9287
Max Flow: 35255963
Time took by ford flukerson: 548
Time took by edmonds karp: 215
Time took by Dinic: 5

Test#46

Number of nodes: 326
Number of edges: 42415
Max Flow: 5806051
Time took by ford flukerson: 1799978
Time took by edmonds karp: 273
Time took by Dinic: 21

Test#47

Number of nodes: 34
Number of edges: 17443
Max Flow: 21817709
Time took by ford flukerson: 5403
Time took by edmonds karp: 446
Time took by Dinic: 12

Test#48

Number of nodes: 355
Number of edges: 23773
Max Flow: 2661820
Time took by ford flukerson: 427738

Time took by edmonds karp: 84

Time took by Dinic: 14

Test#49

Number of nodes: 321

Number of edges: 29221

Max Flow: 3975644

Time took by ford flukerson: 944826

Time took by edmonds karp: 277

Time took by Dinic: 27

Test#50

Number of nodes: 159

Number of edges: 43340

Max Flow: 14165346

Time took by ford flukerson: 1537592

Time took by edmonds karp: 1327

Time took by Dinic: 25

Test#51

Number of nodes: 226

Number of edges: 34477

Max Flow: 7362445

Time took by ford flukerson: 1369338

Time took by edmonds karp: 390

Time took by Dinic: 22

Test#52

Number of nodes: 464

Number of edges: 39721

Max Flow: 4124478

Time took by ford flukerson: 1874327

Time took by edmonds karp: 404

Time took by Dinic: 36

Test#53

Number of nodes: 350

Number of edges: 30586

Max Flow: 3838285

Time took by ford flukerson: 1066497

Time took by edmonds karp: 328

Time took by Dinic: 17

Test#54

Number of nodes: 62

Number of edges: 14438

Max Flow: 12284011

Time took by ford flukerson: 10013

Time took by edmonds karp: 180

Time took by Dinic: 10

Test#55

Number of nodes: 260

Number of edges: 33251

Max Flow: 6312124

Time took by ford flukerson: 1132808

Time took by edmonds karp: 299

Time took by Dinic: 27

Test#56

Number of nodes: 31
Number of edges: 18473
Max Flow: 28356847
Time took by ford flukerson: 5760
Time took by edmonds karp: 457
Time took by Dinic: 12

Test#57

Number of nodes: 72
Number of edges: 43328
Max Flow: 30238887
Time took by ford flukerson: 151733
Time took by edmonds karp: 1568
Time took by Dinic: 27

Test#58

Number of nodes: 402
Number of edges: 20477
Max Flow: 2807420
Time took by ford flukerson: 651805
Time took by edmonds karp: 136
Time took by Dinic: 19

Test#59

Number of nodes: 463
Number of edges: 23736
Max Flow: 2073432
Time took by ford flukerson: 572731
Time took by edmonds karp: 357
Time took by Dinic: 24

Test#60

Number of nodes: 378
Number of edges: 41991
Max Flow: 4534610
Time took by ford flukerson: 1466819
Time took by edmonds karp: 218
Time took by Dinic: 35

Test#61

Number of nodes: 304
Number of edges: 49741
Max Flow: 7287019
Time took by ford flukerson: 3282942
Time took by edmonds karp: 814
Time took by Dinic: 30

Test#62

Number of nodes: 140
Number of edges: 9925
Max Flow: 2761396
Time took by ford flukerson: 32369
Time took by edmonds karp: 25
Time took by Dinic: 4

Test#63

Number of nodes: 312

Number of edges: 30871

Max Flow: 5477114

Time took by ford flukerson: 1276601

Time took by edmonds karp: 178

Time took by Dinic: 19

Test#64

Number of nodes: 330

Number of edges: 35839

Max Flow: 5036102

Time took by ford flukerson: 1718302

Time took by edmonds karp: 300

Time took by Dinic: 40

Test#65

Number of nodes: 440

Number of edges: 30334

Max Flow: 3421107

Time took by ford flukerson: 1045253

Time took by edmonds karp: 304

Time took by Dinic: 24

Test#66

Number of nodes: 90

Number of edges: 16717

Max Flow: 8875038

Time took by ford flukerson: 28177

Time took by edmonds karp: 316

Time took by Dinic: 7

Test#67

Number of nodes: 221

Number of edges: 34811

Max Flow: 8418148

Time took by ford flukerson: 1517187

Time took by edmonds karp: 390

Time took by Dinic: 16

Test#68

Number of nodes: 345

Number of edges: 2675

Max Flow: 225792

Time took by ford flukerson: 17435

Time took by edmonds karp: 3

Time took by Dinic: 2

Test#69

Number of nodes: 93

Number of edges: 18000

Max Flow: 9892693

Time took by ford flukerson: 45933

Time took by edmonds karp: 219

Time took by Dinic: 11

Test#70

Number of nodes: 470

Number of edges: 8713
Max Flow: 736191
Time took by ford flukerson: 119336
Time took by edmonds karp: 9
Time took by Dinic: 5

Test#71

Number of nodes: 148
Number of edges: 32111
Max Flow: 9716799
Time took by ford flukerson: 553088
Time took by edmonds karp: 307
Time took by Dinic: 23

Test#72

Number of nodes: 466
Number of edges: 1760
Max Flow: 384752
Time took by ford flukerson: 29649
Time took by edmonds karp: 2
Time took by Dinic: 1

Test#73

Number of nodes: 23
Number of edges: 34793
Max Flow: 71859298
Time took by ford flukerson: 12442
Time took by edmonds karp: 2108
Time took by Dinic: 27

Test#74

Number of nodes: 485
Number of edges: 17392
Max Flow: 1206775
Time took by ford flukerson: 301455
Time took by edmonds karp: 73
Time took by Dinic: 10

Test#75

Number of nodes: 133
Number of edges: 45465
Max Flow: 17191918
Time took by ford flukerson: 1004602
Time took by edmonds karp: 3004
Time took by Dinic: 38

Test#76

Number of nodes: 350
Number of edges: 1820
Max Flow: 337436
Time took by ford flukerson: 13742
Time took by edmonds karp: 3
Time took by Dinic: 1

Test#77

Number of nodes: 414
Number of edges: 7476
Max Flow: 897963

Time took by ford flukerson: 115653

Time took by edmonds karp: 21

Time took by Dinic: 4

Test#78

Number of nodes: 47

Number of edges: 23039

Max Flow: 22932228

Time took by ford flukerson: 16584

Time took by edmonds karp: 877

Time took by Dinic: 14

Test#79

Number of nodes: 43

Number of edges: 43235

Max Flow: 46906083

Time took by ford flukerson: 43872

Time took by edmonds karp: 3235

Time took by Dinic: 33

Test#80

Number of nodes: 175

Number of edges: 2090

Max Flow: 562423

Time took by ford flukerson: 5600

Time took by edmonds karp: 3

Time took by Dinic: 2

Test#81

Number of nodes: 308

Number of edges: 26710

Max Flow: 4069987

Time took by ford flukerson: 913478

Time took by edmonds karp: 249

Time took by Dinic: 24

Test#82

Number of nodes: 455

Number of edges: 2412

Max Flow: 305958

Time took by ford flukerson: 24229

Time took by edmonds karp: 3

Time took by Dinic: 1

Test#83

Number of nodes: 104

Number of edges: 9972

Max Flow: 3824197

Time took by ford flukerson: 11027

Time took by edmonds karp: 139

Time took by Dinic: 6

Test#84

Number of nodes: 86

Number of edges: 26824

Max Flow: 15617901

Time took by ford flukerson: 87856

Time took by edmonds karp: 802

Time took by Dinic: 18

=====

Test#85

Number of nodes: 485

Number of edges: 19804

Max Flow: 1663186

Time took by ford flukerson: 473005

Time took by edmonds karp: 109

Time took by Dinic: 16

=====

Test#86

Number of nodes: 422

Number of edges: 9659

Max Flow: 607093

Time took by ford flukerson: 97395

Time took by edmonds karp: 30

Time took by Dinic: 7

=====

Test#87

Number of nodes: 481

Number of edges: 48894

Max Flow: 4909696

Time took by ford flukerson: 3037768

Time took by edmonds karp: 429

Time took by Dinic: 32

=====

Test#88

Number of nodes: 31

Number of edges: 49926

Max Flow: 77292152

Time took by ford flukerson: 42678

Time took by edmonds karp: 3607

Time took by Dinic: 34

=====

Test#89

Number of nodes: 327

Number of edges: 17140

Max Flow: 2486568

Time took by ford flukerson: 362296

Time took by edmonds karp: 95

Time took by Dinic: 14

=====

Test#90

Number of nodes: 149

Number of edges: 44473

Max Flow: 13383762

Time took by ford flukerson: 1124583

Time took by edmonds karp: 1340

Time took by Dinic: 38

=====

Test#91

Number of nodes: 246

Number of edges: 43861

Max Flow: 8397805

Time took by ford flukerson: 2305761

Time took by edmonds karp: 509

Time took by Dinic: 40

=====

```
=====
Test#92
Number of nodes: 176
Number of edges: 41512
Max Flow: 10485570
Time took by ford flukerson: 1122195
Time took by edmonds karp: 711
Time took by Dinic: 42
=====
=====
Test#93
Number of nodes: 426
Number of edges: 12165
Max Flow: 1125359
Time took by ford flukerson: 215421
Time took by edmonds karp: 74
Time took by Dinic: 9
=====
=====
Test#94
Number of nodes: 52
Number of edges: 47148
Max Flow: 42140834
Time took by ford flukerson: 84923
Time took by edmonds karp: 1926
Time took by Dinic: 32
=====
=====
Test#95
Number of nodes: 93
Number of edges: 29234
Max Flow: 13871779
Time took by ford flukerson: 101323
Time took by edmonds karp: 731
Time took by Dinic: 20
=====
=====
Test#96
Number of nodes: 254
Number of edges: 34385
Max Flow: 7077528
Time took by ford flukerson: 1586589
Time took by edmonds karp: 285
Time took by Dinic: 21
=====
=====
Test#97
Number of nodes: 166
Number of edges: 41016
Max Flow: 12648466
Time took by ford flukerson: 1822960
Time took by edmonds karp: 667
Time took by Dinic: 29
=====
=====
Test#98
Number of nodes: 59
Number of edges: 45772
Max Flow: 37011565
Time took by ford flukerson: 130019
Time took by edmonds karp: 1760
Time took by Dinic: 32
=====
=====
Test#99
```

```

Number of nodes: 343
Number of edges: 16972
Max Flow: 2182652
Time took by ford flukerson: 482920
Time took by edmonds karp: 51
Time took by Dinic: 10

```

```

=====
=====

```

```

Test#100
Number of nodes: 414
Number of edges: 44505
Max Flow: 4537663
Time took by ford flukerson: 2339487
Time took by edmonds karp: 392
Time took by Dinic: 57

```

```

=====

```

The fastest time that ford flukerson performed was on test 21 where all of them finished the algorithm nearly instantaneously. If we take a closer look at that test case below

Test 21

Number of nodes: 420

Number of edges: 1117

Max Flow: 3994

Time took by ford flukerson: 0

Time took by edmonds karp: 0

Time took by Dinic: 0

we see that despite having a large number of nodes which is near the max number of nodes (500) It has a small max flow (less than 10^5)

Spearman Rank Correlation Coefficient between Big O Notation and real running time

First we need to get the data ready to calculate the correlation

```
In [6]: from scipy.stats import pearsonr
```

```
In [7]: time = []
        bigo = []
        # Ford Flukerson runs in O(E * MAX_FLOW)
        for line in ford_flukerson:
            bigo.append(line[1] * line[2])
            time.append(line[3])
        _, corr = pearsonr(time, bigo)
        print("%.10f" % corr)
```

```
0.5621336621
```

```
In [8]: time = []
        bigo = []
        # Edmonds Karp runs in O(V * E**2)
```



```
for line in edmonds_karp:
    bigo.append(line[0] * (line[1]**2))
    time.append(line[3]/1000)
_, corr = pearsonr(time, bigo)
print("%.10f" % corr)
```

0.3736263093

```
In [9]: time = []
        bigo = []
        # Dinic runs in  $O(V^2 * E)$ 
        for line in Dinic:
            bigo.append((line[0]**2) * line[1])
            time.append(line[3]/1000)
        _, corr = pearsonr(time, bigo)
        print("%.10f" % corr)
```

0.0000483895

From the above we see that both of them exhibit a positive correlation which enforces the mathematical analysis of the running times.