

fun total[] = 0.0

| total h::t = amount(h) + total(t): h::t

total[(coins 37), (notes 6), cheque("cibc", 107.36)]

$\Rightarrow 0.37 + 6.0 + 107.36$

[1, 2.0, 3.5, 4]

datatype number = i of int

| r of real;

sum[r(1.0), i(7), r(3.4), i(5)]: number list $\Rightarrow 1.0 + 7.0 + 3.4 + 5.0$

sum: number list \rightarrow real

fun sum[] = 0.0

| sum (r(x) :: Tail) = x + sum(tail)

| sum (i(N) :: Tail) = real(N) + sum(Tail)

sum[i(1), r(7.3), i(2)]

i(1) :: [r(7.5), i(2)]

$\begin{matrix} 1 \\ n \end{matrix}$ tail

\Rightarrow real + sum[r(7.3), i(2)]

\vdots

$\Rightarrow 1.0 + 7.3 + 2.0 + \text{sum}[] \Rightarrow 1.0 + 7.3 + 2.0 + 0.0 \Rightarrow 10.3$

Recursive Datatypes



datatype tree = leaf of int

| node of tree * tree

node(leaf(3), node(leaf(2), leaf(5)))

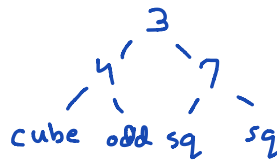


fun sum leaf(N) = N

| sum node(T1, T2) = sum(T1) + sum(T2)

sum: tree → int

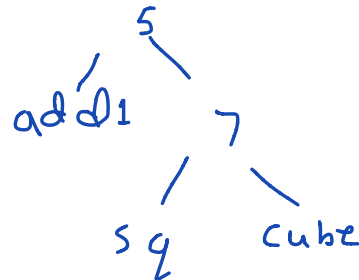
higher-order recursive type



datatype tree = leaf of (int → int)

| node of int * tree * tree

node(5, leaf(add1), node(7, leaf(sq), leaf(cube)))



gather: tree → (int → int) list

fun gather leaf(F) = [F]

| gather node(N, T1, T2)

= append(gather(T1), gather(T2));

sum: tree · int → int

fun sum (leaf (f), N) = F(N)

| sum (node (M, T1, T2), N) =

M + sum (T1, N) + sum (T2, N);

sum: tree · int → int

Polymorphic recursive datatypes

node (leaf (1), node (leaf (2), leaf (3)): int + tree

node (leaf (2), leaf ("abc")): error

datatype 'a tree = leaf of 'a

| node of ('a tree) * ('a tree)

| datatype intstrtree

= leaf1 of int

| leaf2 of string

| node of (intstrtree) * (intstrtree)

fun count leaf (x) = 1

| count node (T1, T2) = count (T1) + count (T2);

count: 'a tree → int