**Exercise 2**

Ilana Pervoi 318271640, Omri Bar Oz 313325961

**Question 1:**

* 1. code
  2. code

|  |  |  |  |
| --- | --- | --- | --- |
| **Cluster number** | **Size** | **Common Label** | **Percentage** |
| 0 | 74 | 3 | 0.53 |
| 1 | 130 | 7 | 0.45 |
| 2 | 103 | 9 | 0.29 |
| 3 | 79 | 2 | 0.67 |
| 4 | 117 | 6 | 0.29 |
| 5 | 108 | 1 | 0.46 |
| 6 | 100 | 3 | 0.4 |
| 7 | 77 | 4 | 0.49 |
| 8 | 138 | 1 | 0.36 |
| 9 | 74 | 0 | 0.93 |

The algorithm classified correctly 460 out of 1000 samples classification error of 54% on the sample.

TODO explain calculations.



|  |  |  |  |
| --- | --- | --- | --- |
| **Cluster number** | **Size** | **Common Label** | **Percentage** |
| 0 | 291 | 1 | 0.1 |
| 1 | 1 | 0 | 1 |
| 2 | 1 | 2 | 1 |
| 3 | 1 | 0 | 1 |
| 4 | 1 | 4 | 1 |
| 5 | 1 | 5 | 1 |
| 6 | 1 | 5 | 1 |
| 7 | 1 | 5 | 1 |
| 8 | 1 | 6 | 1 |
| 9 | 1 | 6 | 1 |

The algorithm classified correctly 39 out of 1000 samples classification error of 87% on the sample.

The k-means clustering algorithm worked better for this problem than single linkage.

**K-means**:

|  |  |  |  |
| --- | --- | --- | --- |
| **Cluster number** | **Size** | **Common Label** | **Percentage** |
| 0 | 228 | 3 | 0.38 |
| 1 | 96 | 0 | 0.89 |
| 2 | 223 | 1 | 0.43 |
| 3 | 114 | 6 | 0.7 |
| 4 | 270 | 4 | 0.32 |
| 5 | 69 | 2 | 0.87 |

The algorithm classified correctly 493 out of 1000 samples classification error of 51% on the sample.

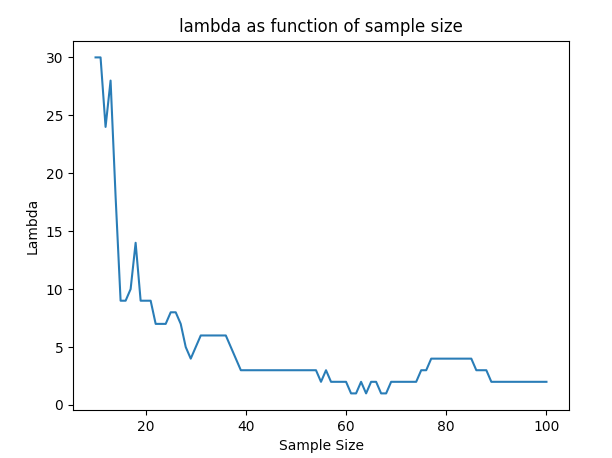
**Single Linkage**:

|  |  |  |  |
| --- | --- | --- | --- |
| **Cluster number** | **Size** | **Common Label** | **Percentage** |
| 0 | 295 | 0 | 0.1 |
| 1 | 1 | 2 | 1 |
| 2 | 1 | 2 | 1 |
| 3 | 1 | 2 | 1 |
| 4 | 1 | 3 | 1 |
| 5 | 1 | 4 | 1 |

The algorithm classified correctly 35 out of 1000 samples classification error of 88% on the sample.

TODO explain difference k=10 k=6.

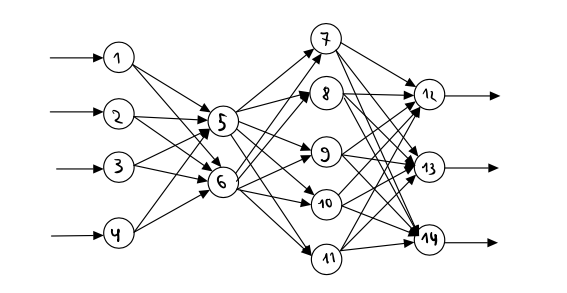
**Question 2:**



1. We expect to see the value of optimal decreases as the sample size increases. This is because when the sample size is low, the sample does not represent the distribution properly, hence we will obtain large hypothesis class which will result in overfitting. To handle that, a higher will be required as a penalty to reduce the hypothesis class size.   
   As the sample size increases, we expect to see a decrease in the optimal value of , until convergence. As the sample size increases, the hypothesis class size decreases. This results in less overfitting which means we don’t want to penalize the norm of w as much.
2. Yes, this is we got what we expected as explained 2.b, in the plot submitted in 2.a.
3. TODO

**Question 3:**

**Question 4:**

1. The graph that describes the neural network architecture:  
   

**Question 5:**

1. Let and . Let be the hypothesis class consisting of decision trees with depth at most n and binary attribute tests of the form for .

For each tree in it has at most nodes. This is because the longest path is n. Then the tree with the largest number of nodes is a perfect binary tree with height n. Then the number of nodes is: .  
For each node in the tree, we can select an attribute , and then choose one of the possible values of to check if it is larger then. Then there are such options. A node can also be a leaf with label or . Then every node has options. Then:

1. Danny is trying to use PAC boundaries equations we learned in class. The problem in this case is that ID3 is not an ERM algorithm.  
   This means that Danny is wrong using this equation.

**Question 6:**

1. No. We will show a contradiction to the Naïve-Bayes assumption:
2. TODO

**Question 7:**

1. Since we want to reduce the dimensionality from 4 to 2, the distortion would be the sum of the lowest 2 eigen-values of .  
   Notice that in the experiment the 3rd column is linearly dependent of the 1st and 2nd columns, and the 4th column linearly dependent of the 2nd and 3rd columns linearly dependent of the 1st and 2nd columns. Hence, the rank of would be 2 and would have 2 eigen-values that are 0, which are the 2 lowest, as is SPD matrix.

In conclusion, the distortion is 0.

1. TODO

**Question 8:**

1. TODO
2. TODO