The logic of dimension reduction