

Standard Code Library

Tempest

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Chapter 1

数论算法

1.1 $O(m^2 \log n)$ 求线性递推数列第 n 项

已知 a_0, a_1, \dots, a_{m-1}

$$a_n = c_0 * a_{n-m} + \dots + c_{m-1} * a_{n-1}$$

求 $a_n = v_0 * a_0 + v_1 * a_1 + \dots + v_{m-1} * a_{m-1}$

```
1 void linear_recurrence(long long n, int m, int a[], int c[], int p) {
2     long long v[M] = {1 % p}, u[M << 1], msk = !!n;
3     for(long long i(n); i > 1; i >>= 1) {
4         msk <<= 1;
5     }
6     for(long long x(0); msk; msk >>= 1, x <<= 1) {
7         fill_n(u, m << 1, 0);
8         int b(!!(n & msk));
9         x |= b;
10        if(x < m) {
11            u[x] = 1 % p;
12        } else {
13            for(int i(0); i < m; i++) {
14                for(int j(0), t(i + b); j < m; j++, t++) {
15                    u[t] = (u[t] + v[i] * v[j]) % p;
16                }
17            }
18            for(int i((m << 1) - 1); i >= m; i--) {
19                for(int j(0), t(i - m); j < m; j++, t++) {
20                    u[t] = (u[t] + c[j] * u[i]) % p;
21                }
22            }
23        }
24        copy(u, u + m, v);
25    }
26    //a[n] = v[0] * a[0] + v[1] * a[1] + ... + v[m - 1] * a[m - 1].
27    for(int i(m); i < 2 * m; i++) {
```

```

28     a[i] = 0;
29     for(int j(0); j < m; j++) {
30         a[i] = (a[i] + (long long)c[j] * a[i + j - m]) % p;
31     }
32 }
33 for(int j(0); j < m; j++) {
34     b[j] = 0;
35     for(int i(0); i < m; i++) {
36         b[j] = (b[j] + v[i] * a[i + j]) % p;
37     }
38 }
39 for(int j(0); j < m; j++) {
40     a[j] = b[j];
41 }
42 }

```

1.2 NTT

```

1  const int modulo(786433);
2  const int G(10); //原根
3  int pw[999999];
4  void FFT(int P[], int n, int oper) {
5      for(int i(1), j(0); i < n - 1; i++) {
6          for(int s(n); j ^= s >= 1, ~j & s;);
7          if (i < j)
8              swap(P[i], P[j]);
9      }
10     int unit_p0;
11     for(int d(0); (1 << d) < n; d++) {
12         int m(1 << d), m2(m * 2);
13         unit_p0 = oper == 1 ? pw[(modulo - 1) / m2] : pw[modulo - 1 - (modulo - 1) / m2];
14         for(int i = 0; i < n; i += m2) {
15             int unit(1);
16             for(int j(0); j < m; j++) {
17                 int &P1 = P[i + j + m], &P2 = P[i + j];
18                 int t = (long long)unit * P1 % modulo;
19                 P1 = (P2 - t + modulo) % modulo;
20                 P2 = (P2 + t) % modulo;
21                 unit = (long long)unit * unit_p0 % modulo;
22             }
23         }
24     }
25 }
26
27 int nn;
28 int A[N], B[N], C[N];
29 //A * B = C;
30 //len = nn

```



```

31 void multiply() {
32     FFT(A, nn, 1);
33     FFT(B, nn, 1);
34     for(int i(0); i < nn; i++) {
35         C[i] = (long long)A[i] * B[i] % modulo;
36     }
37     FFT(C, nn, -1);
38 }
39
40 int main() {
41     pw[0] = 1;
42     for(int i(1); i < modulo; i++) {
43         pw[i] = (long long)pw[i - 1] * G % modulo;
44     }
45 }

```

1.3 中国剩余定理

包括扩展欧几里得，求逆元，和保证除数互质条件下的 CRT

```

1  LL x, y;
2  void exGcd(LL a, LL b)
3  {
4      if (b == 0) {
5          x = 1;
6          y = 0;
7          return;
8      }
9      exGcd(b, a % b);
10     LL k = y;
11     y = x - a / b * y;
12     x = k;
13 }
14
15 LL inversion(LL a, LL b)
16 {
17     exGcd(a, b);
18     return (x % b + b) % b;
19 }
20
21 LL CRT(vector<LL> m, vector<LL> a)
22 {
23     int N = m.size();
24     LL M = 1, ret = 0;
25     for(int i = 0; i < N; ++ i)
26         M *= m[i];
27
28     for(int i = 0; i < N; ++ i) {
29         ret = (ret + (M / m[i]) * a[i] % M * inversion(M / m[i], m[i])) % M;

```

```

30     }
31     return ret;
32 }

```

1.4 中国剩余定理 (可不互质)

```

1  namespace number_theory_basic {
2      inline void euclid(const long long &a, const long long &b, long long &x, long
        long &y) {
3          if (b == 0) {
4              x = 1;
5              y = 0;
6          } else {
7              euclid(b, a % b, x, y);
8              x -= a / b * y;
9              swap(x, y);
10         }
11     }
12 }
13 namespace chinese_remainder_theorem {
14     inline bool crt(int n, long long r[], long long m[], long long &remainder, long
        long &modular) {
15         remainder = modular = 1;
16         for (int i = 1; i <= n; ++i) {
17             long long x, y;
18             euclid(modular, m[i], x, y);
19             long long divisor = gcd(modular, m[i]);
20             if ((r[i] - remainder) % divisor) {
21                 return false;
22             }
23             x *= (r[i] - remainder) / divisor;
24             remainder += modular * x;
25             modular *= m[i] / divisor;
26             ((remainder %= modular) += modular) %= modular;
27         }
28         return true;
29     }
30 }

```

1.5 Miller Rabin

millier_rabin_32 是针对 32 位以下整数的; millier_rabin_64 是针对 64 位以下整数的. 直接调用 prime() 函数, 当返回值是 true 时表示是素数, 否则不是质数.

```

1  namespace millier_rabin_32 {
2      int const n = 3;
3      int const base[] = {2, 7, 61};

```

```

4
5     inline long long power(int x, int k, int p) {
6         long long ans = 1, num = x % p;
7         for (int i = k; i > 0; i >>= 1) {
8             if (i & 1) {
9                 (ans *= num) %= p;
10            }
11            (num *= num) %= p;
12        }
13        return ans;
14    }
15
16    inline bool check(int p, int base) {
17        int n = p - 1;
18        while (!(n & 1)) {
19            n >>= 1;
20        }
21        long long m = power(base, n, p);
22        while (n != p - 1 && m != 1 && m != p - 1) {
23            (m *= m) %= p;
24            n <<= 1;
25        }
26        return m == p - 1 || (n & 1) == 1;
27    }
28
29    inline bool prime(int p) {
30        for (int i = 0; i < n; ++i) {
31            if (base[i] == p) {
32                return true;
33            }
34        }
35        if (p == 1 || !(p & 1)) {
36            return false;
37        }
38        for (int i = 0; i < n; ++i) {
39            if (!check(p, base[i])) {
40                return false;
41            }
42        }
43        return true;
44    }
45 }
46
47 namespace miller_rabin_64 {
48     int const n = 9;
49     int const base[] = {2, 3, 5, 7, 11, 13, 17, 19, 23};
50
51     inline long long multiply(const long long &x, const long long &y, const long long
        &p) {

```

```

52     long long ans = 0, num = x % p;
53     for (long long i = y; i > 0; i >>= 1) {
54         if (i & 1) {
55             (ans += num) %= p;
56         }
57         (num += num) %= p;
58     }
59     return ans;
60 }
61
62 inline long long power(const long long &x, const long long &k, const long long &p
63 ) {
64     long long ans = 1, num = x % p;
65     for (long long i = k; i > 0; i >>= 1) {
66         if (i & 1) {
67             ans = multiply(ans, num, p);
68         }
69         num = multiply(num, num, p);
70     }
71     return ans;
72 }
73
74 inline bool check(const long long &p, const long long &base) {
75     long long n = p - 1;
76     while (!(n & 1)) {
77         n >>= 1;
78     }
79     long long m = power(base, n, p);
80     while (n != p - 1 && m != 1 && m != p - 1) {
81         m = multiply(m, m, p);
82         n <<= 1;
83     }
84     return m == p - 1 || (n & 1) == 1;
85 }
86
87 inline bool prime(const long long &p) {
88     for (int i = 0; i < n; ++i) {
89         if (base[i] == p) {
90             return true;
91         }
92     }
93     if (p == 1 || !(p & 1)) {
94         return false;
95     }
96     for (int i = 0; i < n; ++i) {
97         if (!check(p, base[i])) {
98             return false;
99         }
100     }

```

```

100         return true;
101     }
102 }

```

1.6 Pollard Rho

```

1  模板需要配合miller\_rabin一起使用。
2  调用factor()函数，会返回vector<long long>，表示分解结果。（例如分解12，会返回2，2和3）
3  namespace pollard_rho {
4      //可以改成LL*LL%LL的形式
5      inline long long multiply(const long long &x, const long long &y, const long long
        &p) {
6          long long ans = 0, num = x % p;
7          for (long long i = y; i > 0; i >>= 1) {
8              if (i & 1) {
9                  (ans += num) %= p;
10             }
11             (num += num) %= p;
12         }
13         return ans;
14     }
15
16     inline long long gcd(long long x, long long y) {
17         while (y > 0) {
18             x %= y;
19             swap(x, y);
20         }
21         return x;
22     }
23
24     inline long long pollard_rho(const long long &n, const long long &c) {
25         long long x = rand() % (n - 1) + 1, y = x;
26         int head = 1, tail = 2;
27         while (true) {
28             x = multiply(x, x, n);
29             if ((x += c) >= n) {
30                 x -= n;
31             }
32             if (x == y) {
33                 return n;
34             }
35             long long d = gcd(abs(x - y), n);
36             if (d > 1 && d < n) {
37                 return d;
38             }
39             if ((++head) == tail) {
40                 y = x;

```

```

41         tail <= 1;
42     }
43 }
44 }
45
46 inline vector<long long> mergy(const vector<long long> &a, const vector<long long>
    > &b) {
47     vector<long long> vec;
48     for (int i = 0; i < (int)a.size(); ++i) {
49         vec.push_back(a[i]);
50     }
51     for (int i = 0; i < (int)b.size(); ++i) {
52         vec.push_back(b[i]);
53     }
54     return vec;
55 }
56
57 inline vector<long long> factor(const long long &n) {
58     if (n <= 1) {
59         return vector<long long>();
60     }
61     if (miller_rabin::prime(n)) {
62         return vector<long long>(1, n);
63     }
64     long long p = n;
65     while (p >= n) {
66         p = pollard_rho(n, rand() % (n - 1) + 1);
67     }
68     return mergy(factor(n / p), factor(p));
69 }
70 }

```

1.7 离散对数

```

1 #include <iostream>
2 #include <cstdio>
3 #include <cstdlib>
4 #include <algorithm>
5 #include <cmath>
6 #include <map>
7 #include <cstring>
8
9 using namespace std;
10
11 typedef long long int64;
12
13 struct hash_table {
14     static const int MAXN = 100003;

```

```

15     int first[MAXN], key[MAXN], value[MAXN], next[MAXN], tot;
16     hash_table() : tot(0) {
17         memset(first, 255, sizeof first);
18     }
19     void clear() {
20         memset(first, 255, sizeof first);
21         tot = 0;
22     }
23     int &operator[] (const int &o) {
24         int pos = o % MAXN;
25         for (int i = first[pos]; i != -1; i = next[i])
26             if (key[i] == o)
27                 return value[i];
28         next[tot] = first[pos];
29         first[pos] = tot;
30         key[tot] = o;
31         return value[tot++];
32     }
33     bool has_key(const int &o) {
34         int pos = o % MAXN;
35         for (int i = first[pos]; i != -1; i = next[i])
36             if (key[i] == o)
37                 return true;
38         return false;
39     }
40 };
41
42 int discrete_log(int base, int n, int mod) {
43     int block = int(sqrt(mod)) + 1;
44     int val = 1;
45     hash_table dict;
46     for (int i = 0; i < block; ++i) {
47         if (dict.has_key(val) == 0)
48             dict[val] = i;
49         val = (int64)val * base % mod;
50     }
51     int inv = inverse(val, mod);
52     val = 1;
53     for (int i = 0; i < block; ++i) {
54         if (dict.has_key((int64)val * n % mod))
55             return dict[(int64)val * n % mod] + i * block;
56         val = (int64)val * inv % mod;
57     }
58     return -1;
59 }
60
61 int main() {
62     int base, n, p;
63     while (scanf("%d%d", &p, &base, &n) == 3) {

```

```

64     int ans = discrete_log(base, n, p);
65     if (ans == -1)
66         puts("no solution");
67     else
68         printf("%d\n", ans);
69 }
70 }

```

1.8 原根

```

1  int primitive_root(int p) {
2      int n = p - 1;
3      while (true) {
4          int root = rand() % (p - 1) + 1, m = n;
5          bool found = true;
6          for (int i = 0; i < (int)prim.size(); ++i) {
7              int cur = prim[i];
8              if (m / cur < cur)
9                  break;
10             if (m % cur == 0) {
11                 if (pow_mod(root, n / cur, p) == 1) {
12                     found = false;
13                     break;
14                 }
15                 while (m % cur == 0)
16                     m /= cur;
17             }
18         }
19         if (m > 1)
20             if (pow_mod(root, n / m, p) == 1)
21                 found = false;
22         if (found)
23             return root;
24     }
25 }
26
27 vector<int> discrete_root(int expo, int n, int mod) {
28     if (n == 0)
29         return vector<int>(1, 0);
30     int g = primitive_root(mod);
31     int e = discrete_log(g, n, mod);
32     int64 u, v;
33     int d = extend_euclid(expo, mod - 1, u, v);
34     if (e % d != 0)
35         return vector<int>();
36     int64 delta = (mod - 1) / d;
37     u = u * e / d % delta;
38     if (u < 0)

```



```

39     u += delta;
40     vector<int> ret;
41     while (u < mod - 1) {
42         ret.push_back(pow_mod(g, u, mod));
43         u += delta;
44     }
45     return ret;
46 }

```

1.9 离散二次方根

```

1  inline bool quad_resi(int x, int p) {
2      return pow_mod(x, (p - 1) / 2, p) == 1;
3  }
4
5  struct quad_poly {
6      int zero, one, val, mod;
7
8      quad_poly(int zero, int one, int val, int mod) : zero(zero), one(one), val
9          (val), mod(mod) {}
10
11     quad_poly multiply(quad_poly o) {
12         int z0 = (zero * o.zero + one * o.one % mod * val % mod) % mod;
13         int z1 = (zero * o.one + one * o.zero) % mod;
14         return quad_poly(z0, z1, val, mod);
15     }
16
17     quad_poly pow(int x) {
18         if (x == 1)
19             return *this;
20         quad_poly ret = *this->pow(x / 2);
21         ret = ret.multiply(ret);
22         if (x & 1)
23             ret = ret.multiply(*this);
24         return ret;
25     }
26 };
27
28 inline int calc(int a, int p) {
29     a %= p;
30     if (a < 2)
31         return a;
32     if (!quad_resi(a, p))
33         return p;           // no solution
34     if (p % 4 == 3)
35         return pow_mod(a, (p + 1) / 4, p);
36     int b = 0;
37     while (quad_resi((my_sqr(b) - a + p) % p, p))

```

```

38     b = rand() % p;
39     quad_poly ret = quad_poly(b, 1, (my_sqr(b) - a + p) % p, p);
40     ret = ret.pow((p + 1) / 2);
41     return ret.zero;
42 }

```

1.10 牛顿迭代求平方根

```

1 //use newton-method to solve f(x) = 0
2 //init x0
3 //xi -> x(i + 1) = xi - f(xi) / f'(xi)
4 //O(N^2logN)
5 int64 square_root(int64 x) {
6     if (x <= 0)
7         return 0;
8     int64 last_root = -1, root = 1 << (bit_length(x) / 2);
9     while (true) {
10         int64 next_root = (root + x / root) >> 1;
11         if (next_root == last_root)
12             return min(next_root, root);
13         last_root = root;
14         root = next_root;
15     }
16 }

```

1.11 Pell 方程求根

$$x^2 - n * y^2 = 1$$

```

1 pair<int64, int64> solve_pell64(int64 n) {
2     const static int MAXC = 111;
3     int64 p[MAXC], q[MAXC], a[MAXC], g[MAXC], h[MAXC];
4     p[1] = 1; p[0] = 0;
5     q[1] = 0; q[0] = 1;
6     a[2] = square_root(n);
7     g[1] = 0; h[1] = 1;
8     for (int i = 2; ; ++i) {
9         g[i] = -g[i - 1] + a[i] * h[i - 1];
10        h[i] = (n - g[i] * g[i]) / h[i - 1];
11        a[i + 1] = (g[i] + a[2]) / h[i];
12        p[i] = a[i] * p[i - 1] + p[i - 2];
13        q[i] = a[i] * q[i - 1] + q[i - 2];
14        if (p[i] * p[i] - n * q[i] * q[i] == 1)
15            return make_pair(p[i], q[i]);
16    }
17 }

```

1.12 直线下整点个数

求 $\sum_{i=0}^{n-1} \lfloor \frac{a+bi}{m} \rfloor$.

```
1 typedef long long LL;
2
3 LL count(LL n, LL a, LL b, LL m) {
4     if (b == 0) {
5         return n * (a / m);
6     }
7     if (a >= m) {
8         return n * (a / m) + count(n, a % m, b, m);
9     }
10    if (b >= m) {
11        return (n - 1) * n / 2 * (b / m) + count(n, a, b % m, m);
12    }
13    return count((a + b * n) / m, (a + b * n) % m, m, b);
14 }
```


Chapter 2

数值算法

2.1 FFT

```
1 void FFT(Complex P[], int n, int oper) {
2     for (int i(1), j(0); i < n - 1; i++) {
3         for (int s(n); j ^= s >>= 1, ~j & s;);
4         if (i < j)
5             swap(P[i], P[j]);
6     }
7     Complex unit_p0;
8     for (int d(0); (1 << d) < n; d++) {
9         int m(1 << d), m2(m * 2);
10        double p0(pi / m * oper);
11        unit_p0.imag(sin(p0));
12        unit_p0.real(cos(p0));
13        for (int i(0); i < n; i += m2) {
14            Complex unit = 1;
15            for (int j = 0; j < m; j++) {
16                Complex &P1 = P[i + j + m], &P2 = P[i + j];
17                Complex t = unit * P1;
18                P1 = P2 - t;
19                P2 = P2 + t;
20                unit = unit * unit_p0;
21            }
22        }
23    }
24 }
25 void multiply() {
26     FFT(a, n, 1);
27     FFT(b, n, 1);
28     for(int i(0); i < n; i++) {
29         c[i] = a[i] * b[i];
30     }
31     FFT(c, n, -1);
```

```

32     for(int i(0); i < n; i++) {
33         ans[i] += (int)(c[i].real() / n + 0.5);
34     }
35 }

```

2.2 解一元三次方程 + 求三阶二次型的标准型

```

1  double sqr(const double & x) {
2      return x * x;
3  }
4  double eps(1e-8);
5  int main() {
6      double A, B, C, D, E, F;
7      for(; 6 == scanf("%lf%lf%lf%lf%lf%lf", &A, &B, &C, &D, &E, &F);) {
8          D /= 2; E /= 2; F /= 2;
9          complex<double> a(1), b(-A - B - C), c(A * B + B * C + C * A - sqr(D) - sqr(E)
          ) - sqr(F)), d(-A * B * C - 2 * D * E * F + A * sqr(D) + B * sqr(E) + C *
          sqr(F));
10         complex<double> delta(pow(pow(b * c / 6. / a / a - b * b * b / 27. / a / a /
          a - d / 2. / a, 2) + pow(c / 3. / a - b * b / 9. / a / a, 3), 0.5));
11         complex<double> p(pow(b * c / 6. / a / a - b * b * b / 27. / a / a / a - d /
          2. / a + delta, 1. / 3));
12         complex<double> q(pow(b * c / 6. / a / a - b * b * b / 27. / a / a / a - d /
          2. / a - delta, 1. / 3));
13         complex<double> omega1(-0.5, 0.5 * sqrt(3.)), omega2(-0.5, -0.5 * sqrt(3.));
14         complex<double> x1(-b / 3. / a + p + q), x2(-b / 3. / a + omega1 * p + omega2
          * q), x3(-b / 3. / a + omega2 * p + omega1 * q);
15         printf("%.10f\n", min(min(sqrt(1 / x1.real()), sqrt(1 / x2.real())), sqrt(1 /
          x3.real())));
16     }
17 }

```

2.3 高斯消元

```

1  vector<double> operator* (const vector<double> &a, double b) {
2      vector<double> ret;
3      for (int i = 0; i < (int)a.size(); ++i)
4          ret.push_back(a[i] * b);
5      return ret;
6  }
7
8  vector<double> operator+ (const vector<double> &a, const vector<double> &b) {
9      vector<double> ret;
10     for (int i = 0; i < (int)a.size(); ++i)
11         ret.push_back(a[i] + b[i]);
12     return ret;

```

```

13 }
14
15 vector<double> operator- (const vector<double> &a, const vector<double> &b) {
16     vector<double> ret;
17     for (int i = 0; i < (int)a.size(); ++i)
18         ret.push_back(a[i] - b[i]);
19     return ret;
20 }
21
22 struct solution {
23     int size, dimension;
24     vector<vector<double> > null_space;
25     vector<double> special;
26     solution(int size = 0, int dimension = 0) : size(size), dimension(dimension)
27     {
28         special = vector<double>(size, 0);
29         null_space = vector<vector<double> >(size, vector<double>(dimension,
30             0));
31     }
32 };
33
34 solution gauss_elimination(vector<vector<double> > a, vector<double> b) {
35     int n = (int)a.size(), m = (int)a[0].size();
36     static const int MAX_SIZE = 211;
37     int index[MAX_SIZE], row = 0;
38     bool pivot[MAX_SIZE];
39     fill(index, index + n, -1);
40     fill(pivot, pivot + m, false);
41
42     for (int col = 0; row < n && col < m; ++col) {
43         int best = row;
44         for (int i = row + 1; i < n; ++i)
45             if (fabs(a[i][col]) > fabs(a[best][col]))
46                 best = i;
47         swap(a[best], a[row]);
48         swap(b[best], b[row]);
49         if (fabs(a[row][col]) < EPS)
50             continue;
51         pivot[col] = true;
52         index[row] = col;
53         double coef = a[row][col];
54         a[row] = a[row] * (1. / coef);
55         b[row] = b[row] * (1. / coef);
56         for (int i = 0; i < n; ++i)
57             if (i != row && fabs(a[i][col]) > EPS) {
58                 double coef = a[i][col];
59                 a[i] = a[i] - a[row] * coef;
60                 b[i] = b[i] - b[row] * coef;
61             }

```

```

62     ++row;
63 }
64
65 for (int i = row; i < n; ++i)
66     if (fabs(b[i]) > EPS)
67         return solution(0, 0);           //no solution
68
69 solution ret(m, m - row);
70 for (int i = 0; i < row; ++i)
71     ret.special[index[i]] = b[i];
72
73 int cnt = 0;
74 for (int i = 0; i < m; ++i)
75     if (!pivot[i]) {
76         for (int j = 0; j < row; ++j)
77             ret.null_space[index[j]][cnt] = a[j][i];
78         ret.null_space[i][cnt++] = -1;
79     }
80 return ret;
81 }

```

2.4 最小二乘法

```

1 // calculate argmin ||AX - B||
2 solution least_squares(vector<vector<double> > a, vector<double> b) {
3     int n = (int)a.size(), m = (int)a[0].size();
4     vector<vector<double> > p(m, vector<double>(m, 0));
5     vector<double> q(m, 0);
6     for (int i = 0; i < m; ++i)
7         for (int j = 0; j < m; ++j)
8             for (int k = 0; k < n; ++k)
9                 p[i][j] += a[k][i] * a[k][j];
10    for (int i = 0; i < m; ++i)
11        for (int j = 0; j < n; ++j)
12            q[i] += a[j][i] * b[j];
13    return gauss_elimination(p, q);
14 }

```

2.5 多项式求根

```

1 const double eps=1e-12;
2 double a[10][10];
3 typedef vector<double> vd;
4 int sgn(double x) { return x < -eps ? -1 : x > eps; }
5 double mypow(double x,int num){
6     double ans=1.0;

```



```

7     for(int i=1;i<=num;++i)ans*=x;
8     return ans;
9 }
10 double f(int n,double x){
11     double ans=0;
12     for(int i=n;i>=0;--i)ans+=a[n][i]*mypow(x,i);
13     return ans;
14 }
15 double getRoot(int n,double l,double r){
16     if(sgn(f(n,l))==0)return l;
17     if(sgn(f(n,r))==0)return r;
18     double temp;
19     if(sgn(f(n,l))>0)temp=-1;else temp=1;
20     double m;
21     for(int i=1;i<=10000;++i){
22         m=(l+r)/2;
23         double mid=f(n,m);
24         if(sgn(mid)==0){
25             return m;
26         }
27         if(mid*temp<0)l=m;else r=m;
28     }
29     return (l+r)/2;
30 }
31 vd did(int n){
32     vd ret;
33     if(n==1){
34         ret.push_back(-1e10);
35         ret.push_back(-a[n][0]/a[n][1]);
36         ret.push_back(1e10);
37         return ret;
38     }
39     vd mid=did(n-1);
40     ret.push_back(-1e10);
41     for(int i=0;i+1<mid.size();++i){
42         int t1=sgn(f(n,mid[i])),t2=sgn(f(n,mid[i+1]));
43         if(t1*t2>0)continue;
44         ret.push_back(getRoot(n,mid[i],mid[i+1]));
45     }
46     ret.push_back(1e10);
47     return ret;
48 }
49 int main(){
50     int n; scanf("%d",&n);
51     for(int i=n;i>=0;--i){
52         scanf("%lf",&a[n][i]);
53     }
54     for(int i=n-1;i>=0;--i)
55         for(int j=0;j<=i;++j)a[i][j]=a[i+1][j+1]*(j+1);

```

```
56     vd ans=did(n);
57     sort(ans.begin(),ans.end());
58     for(int i=1;i+1<ans.size();++i)printf("%.10f\n",ans[i]);
59     return 0;
60 }
```

2.6 自适应辛普森

```
1 namespace adaptive_simpson {
2     template<typename function>
3     inline double area(function f, const double &left, const double &right) {
4         double mid = (left + right) / 2;
5         return (right - left) * (f(left) + 4 * f(mid) + f(right)) / 6;
6     }
7
8     template<typename function>
9     inline double simpson(function f, const double &left, const double &right, const
10        double &eps, const double &area_sum) {
11         double mid = (left + right) / 2;
12         double area_left = area(f, left, mid);
13         double area_right = area(f, mid, right);
14         double area_total = area_left + area_right;
15         if (fabs(area_total - area_sum) <= 15 * eps) {
16             return area_total + (area_total - area_sum) / 15;
17         }
18         return simpson(f, left, right, eps / 2, area_left) + simpson(f, mid, right,
19            eps / 2, area_right);
20     }
21
22     template<typename function>
23     inline double simpson(function f, const double &left, const double &right, const
24        double &eps) {
25         return simpson(f, left, right, eps, area(f, left, right));
26     }
27 }
```

Chapter 3

计算几何

3.1 圆与多边形交

```
1  #include <cstdio>
2  #include <cstdlib>
3  #include <algorithm>
4  #include <cmath>
5  #include <vector>
6  using namespace std;
7
8  const double eps = 5e-7;
9  const int N = 2222;
10 const double pi = acos(-1.0);
11
12 int sign(double x) {
13     return x < -eps ? -1 : x > eps;
14 }
15
16 double sqr(double x) {
17     return x * x;
18 }
19
20 struct Point {
21     double x, y;
22     Point (double x = 0, double y = 0) : x(x), y(y) {}
23     friend inline Point operator +(const Point &a, const Point &b) {
24         return Point(a.x + b.x, a.y + b.y);
25     }
26     friend inline Point operator -(const Point &a, const Point &b) {
27         return Point(a.x - b.x, a.y - b.y);
28     }
29     friend inline Point operator *(const Point &a, double k) {
30         return Point(a.x * k, a.y * k);
31     }
```

```

32     friend inline Point operator / (const Point &a, double k) {
33         return Point(a.x / k, a.y / k);
34     }
35     double dist() const {
36         return hypot(x, y);
37         return sqrt(x * x + y * y);
38     }
39     double dist2() const {
40         return x * x + y * y;
41     }
42     double ang() const {
43         return atan2(y, x);
44     }
45 };
46
47 vector<Point> convex;
48
49 int n;
50 double radius;
51 Point points[N][2];
52 Point target;
53
54 double det(Point a, Point b, Point c) {
55     return (b.x - a.x) * (c.y - a.y) - (c.x - a.x) * (b.y - a.y);
56 }
57
58 double dot(Point a, Point b, Point c) {
59     return (b.x - a.x) * (c.x - a.x) + (b.y - a.y) * (c.y - a.y);
60 }
61
62 double det(Point a, Point b) {
63     return a.x * b.y - b.x * a.y;
64 }
65
66 double dot(Point a, Point b) {
67     return a.x * b.x + a.y * b.y;
68 }
69
70 inline bool point_on_line(const Point &a, const Point &b, const Point &c) {
71     return sign(det(Point(0, 0), a - b, c - b)) == 0 && dot(Point(0, 0), b - a, c - a)
72         < eps;
73 }
74
75 double point_to_line(const Point &a, const Point &b, const Point &c) {
76     return fabs(det(Point(0, 0), c - b, a - b)) / (b - c).dist();
77 }
78
79 Point project_to_line(const Point &p, const Point &a, const Point &b) {
80     return a + (b - a) * dot(Point(0, 0), p - a, b - a) / sqr((b - a).dist());

```

```

80 }
81
82 Point intersect(Point a, Point b, Point c, Point d) {
83     double s1 = det(a, b, c);
84     double s2 = det(a, b, d);
85     return (c * s2 - d * s1) / (s2 - s1);
86 }
87
88 inline Point line_to_circle(const Point &a, const Point &b) {
89     double x = sqrt(sqr(radius) - sqr(point_to_line(Point(0, 0), a, b)));
90     return project_to_line(Point(0, 0), a, b) - (b - a) / (b - a).dist() * x;
91 }
92
93 inline double area_tri(Point a, Point b) {
94     return det(Point(0, 0), a, b) / 2;
95 }
96
97 inline double area_cir(Point a, Point b, double radius) {
98     if (sign(det(Point(0, 0), a, b)) == 0)
99         return 0;
100     a = a / a.dist() * radius;
101     b = b / b.dist() * radius;
102     double d = atan2(det(Point(0, 0), a, b), dot(Point(0, 0), a, b));
103     //printf("%f\n", sqr(radius) * d / 2);
104     return sqr(radius) * d / 2;
105 }
106
107 int intersect(const Point &a, const Point &b, Point &u, Point &v, double radius) {
108     if (point_to_line(Point(0, 0), a, b) + eps > radius)
109         return 0;
110     u = line_to_circle(a, b);
111     v = line_to_circle(b, a);
112     return point_on_line(u, a, b) + point_on_line(v, a, b);
113 }
114
115 vector<Point> calc(vector<Point> vec, Point a, Point b) {
116     vector<Point> result;
117     for(int i = 0; i < (int)vec.size(); i++) {
118         Point c = vec[i], d = vec[(i + 1) % (int)vec.size()];
119         if (det(a, b, c) > -eps) {
120             result.push_back(c);
121         }
122         if (sign(det(a, b, c)) * sign(det(a, b, d)) == -1) {
123             result.push_back(intersect(a, b, c, d));
124         }
125     }
126     return result;
127 }
128 double areaCT(double R, Point pa, Point pb)

```

```

129 {
130     if (pa.dist() < pb.dist()) swap(pa, pb);
131     if (pb.dist() < eps) return 0;
132     Point pc = pb - pa;
133     double a = pb.dist(), b = pa.dist(), c = pc.dist();
134     double cosB = dot(pb, pc) / a / c, B = acos(cosB);
135     double cosC = dot(pa, pb) / a / b, C = acos(cosC);
136     double S, h, theta;
137     if (a > R) {
138         S = C * 0.5 * R * R;
139         h = a * b * sin(C) / c;
140         if (h < R && B < pi * 0.5)
141             S -= acos(h / R) * R * R - h * sqrt(max(0.0, R * R - h * h));
142     } else if (b > R) {
143         theta = pi - B - asin(sin(B) / R * a);
144         S = 0.5 * a * R * sin(theta) + (C - theta) * 0.5 * R * R;
145     } else {
146         S = 0.5 * sin(C) * a * b;
147     }
148     return S;
149 }
150
151 void solve() {
152     scanf("%lf%d", &radius, &n);
153     convex.clear();
154     convex.push_back(Point(-radius, -radius));
155     convex.push_back(Point(radius, -radius));
156     convex.push_back(Point(radius, radius));
157     convex.push_back(Point(-radius, radius));
158     for(int i = 1; i <= n; i++) {
159         scanf("%lf%lf%lf%lf", &points[i][0].x, &points[i][0].y, &points[i][1].x, &
160             points[i][1].y);
161     }
162     scanf("%lf%lf", &target.x, &target.y);
163     for(int i = 1; i <= n; i++) {
164         if (det(points[i][0], points[i][1], target) < -eps) {
165             swap(points[i][0], points[i][1]);
166         }
167         convex = calc(convex, points[i][0], points[i][1]);
168     }
169     double ans = 0;
170     for(int i = 0; i < (int)convex.size(); i++) {
171         ans += areaCT(radius, convex[i], convex[(i + 1) % (int)convex.size()]) * sign
172             (det(convex[i], convex[(i + 1) % (int)convex.size()]]);
173     }
174     printf("%.5f", max(0., fabs(ans) / (pi * radius * radius) * 100));
175     puts("%");
176 }

```

```

176 int main() {
177     int test;
178     scanf("%d", &test);
179     while(test--) {
180         static int testCount = 0;
181         printf("Case_%d:", ++testCount);
182         solve();
183     }
184 }

```

3.2 动态凸包

```

1  #define x first
2  #define y second
3  typedef map<int, int> mii;
4  typedef map<int, int>::iterator mit;
5  struct point { // something omitted
6      point(const mit &p): x(p->first), y(p->second) {}
7  };
8  inline bool checkInside(mii &a, const point &p) { // `border inclusive`
9      int x = p.x, y = p.y;
10     mit p1 = a.lower_bound(x);
11     if (p1 == a.end()) return false;
12     if (p1->x == x) return y <= p1->y;
13     if (p1 == a.begin()) return false;
14     mit p2(p1--);
15     return sign(det(p - point(p1), point(p2) - p)) >= 0;
16 }
17 inline void addPoint(mii &a, const point &p) { // `no collinear points`
18     int x = p.x, y = p.y;
19     mit pnt = a.insert(make_pair(x, y)).first, p1, p2;
20     for (pnt->y = y; ; a.erase(p2)) {
21         p1 = pnt;
22         if (++p1 == a.end())
23             break;
24         p2 = p1;
25         if (++p1 == a.end())
26             break;
27         if (det(point(p2) - p, point(p1) - p) < 0)
28             break;
29     }
30     for ( ; ; a.erase(p2)) {
31         if ((p1 = pnt) == a.begin())
32             break;
33         if (--p1 == a.begin())
34             break;
35         p2 = p1--;
36         if (det(point(p2) - p, point(p1) - p) > 0)

```

```

37         break;
38     }
39 }
`upperHull ← (x,y)` `lowerHull ← (x,-y)`

```

3.3 farmland

```

1
2  const int N = 11111, M = 111111 * 4;
3
4  struct eglist {
5      int other[M], succ[M], last[M], sum;
6      void clear() {
7          memset(last, -1, sizeof(last));
8          sum = 0;
9      }
10     void addEdge(int a, int b) {
11         other[sum] = b, succ[sum] = last[a], last[a] = sum++;
12         other[sum] = a, succ[sum] = last[b], last[b] = sum++;
13     }
14 }e;
15
16 int n, m;
17 struct point {
18     int x, y;
19     point(int x, int y) : x(x), y(y) {}
20     point() {}
21     friend point operator -(point a, point b) {
22         return point(a.x - b.x, a.y - b.y);
23     }
24     double arg() {
25         return atan2(y, x);
26     }
27 }points[N];
28
29 vector<pair<int, double> > vecs;
30 vector<int> ee[M];
31 vector<pair<double, pair<int, int> > > edges;
32 double length[M];
33 int tot, father[M], next[M], visit[M];
34
35 int find(int x) {
36     return father[x] == x ? x : father[x] = find(father[x]);
37 }
38
39 long long det(point a, point b) {
40     return 1LL * a.x * b.y - 1LL * b.x * a.y;
41 }

```



```

42
43 double dist(point a, point b) {
44     return sqrt(1.0 * (a.x - b.x) * (a.x - b.x) + 1.0 * (a.y - b.y) * (a.y - b.y));
45 }
46
47 int main() {
48     scanf("%d%d", &n, &m);
49     e.clear();
50     for(int i = 1; i <= n; i++) {
51         scanf("%d%d", &points[i].x, &points[i].y);
52     }
53     for(int i = 1; i <= m; i++) {
54         int a, b;
55         scanf("%d%d", &a, &b);
56         e.addEdge(a, b);
57     }
58     for(int x = 1; x <= n; x++) {
59         vector<pair<double, int> > pairs;
60         for(int i = e.last[x]; ~i; i = e.succ[i]) {
61             int y = e.other[i];
62             pairs.push_back(make_pair((points[y] - points[x]).arg(), i));
63         }
64         sort(pairs.begin(), pairs.end());
65         for(int i = 0; i < (int)pairs.size(); i++) {
66             next[pairs[(i + 1) % (int)pairs.size()].second ^ 1] = pairs[i].second;
67         }
68     }
69     memset(visit, 0, sizeof(visit));
70     tot = 0;
71     for(int start = 0; start < e.sum; start++) {
72         if (visit[start])
73             continue;
74         long long total = 0;
75         int now = start;
76         vecs.clear();
77         while(!visit[now]) {
78             visit[now] = 1;
79             total += det(points[e.other[now ^ 1]], points[e.other[now]]);
80             vecs.push_back(make_pair(now / 2, dist(points[e.other[now ^ 1]], points[e
                .other[now]])));
81             now = next[now];
82         }
83         if (now == start && total > 0) {
84             ++tot;
85             for(int i = 0; i < (int)vecs.size(); i++) {
86                 ee[vecs[i].first].push_back(tot);
87             }
88         }
89     }

```

```

90
91     for(int i = 0; i < e.sum / 2; i++) {
92         int a = 0, b = 0;
93         if (ee[i].size() == 0)
94             continue;
95         else if (ee[i].size() == 1) {
96             a = ee[i][0];
97         } else if (ee[i].size() == 2) {
98             a = ee[i][0], b = ee[i][1];
99         }
100         edges.push_back(make_pair(dist(points[e.other[i * 2]], points[e.other[i * 2 +
101             1]]), make_pair(a, b)));
102     }
103     sort(edges.begin(), edges.end());
104     for(int i = 0; i <= tot; i++)
105         father[i] = i;
106     double ans = 0;
107     for(int i = 0; i < (int)edges.size(); i++) {
108         int a = edges[i].second.first, b = edges[i].second.second;
109         double v = edges[i].first;
110         if (find(a) != find(b)) {
111             ans += v;
112             father[father[a]] = father[b];
113         }
114     }
115     printf("%.5f\n", ans);
116 }

```

3.4 farmland 完全体

```

1
2  const int MAXN = 200;
3  const int MAXV = MAXN * MAXN;
4  const int MAXE = MAXV * 6;
5  const double eps = 1e-8;
6
7  int sign(double x) {
8      return x < -eps ? -1 : x > eps;
9  }
10
11  struct Point {
12      double x, y;
13
14      Point(int x, int y) : x(x), y(y) {}
15      Point() {}
16
17      Point &operator +=(const Point &o) {
18          x += o.x;

```

```

19         y += o.y;
20         return *this;
21     }
22
23     Point &operator --=(const Point &o) {
24         x -= o.x;
25         y -= o.y;
26         return *this;
27     }
28
29     Point &operator *=(double k) {
30         x *= k;
31         y *= k;
32         return *this;
33     }
34
35     Point &operator /=(double k) {
36         x /= k;
37         y /= k;
38         return *this;
39     }
40
41     double norm2() const {
42         return x * x + y * y;
43     }
44
45     double norm() const {
46         return sqrt(norm2());
47     }
48
49     double arg() const {
50         return atan2(y, x);
51     }
52
53     bool on(const Point &, const Point &) const;
54     bool in(const vector<Point> &) const;
55 };
56
57 bool operator <(const Point &a, const Point &b) {
58     return sign(a.x - b.x) < 0 || sign(a.x - b.x) == 0 && sign(a.y - b.y) < 0;
59 }
60
61 bool operator ==(const Point &a, const Point &b) {
62     return sign(a.x - b.x) == 0 && sign(a.y - b.y) == 0;
63 }
64
65 Point operator +(Point a, const Point &b) {
66     return a += b;
67 }

```

```

68
69 Point operator -(Point a, const Point &b) {
70     return a - b;
71 }
72
73 Point operator /(Point a, double k) {
74     return a /= k;
75 }
76
77 Point operator *(Point a, double k) {
78     return a *= k;
79 }
80
81 Point operator *(double k, Point a) {
82     return a *= k;
83 }
84
85 double det(const Point &a, const Point &b) {
86     return a.x * b.y - b.x * a.y;
87 }
88
89 double dot(const Point &a, const Point &b) {
90     return a.x * b.x + a.y * b.y;
91 }
92
93 bool parallel(const Point &a, const Point &b, const Point &c, const Point &d) {
94     return sign(det(b - a, d - c)) == 0;
95 }
96
97 Point intersect(const Point &a, const Point &b, const Point &c, const Point &d) {
98     double s1 = det(b - a, c - a);
99     double s2 = det(b - a, d - a);
100    return (c * s2 - d * s1) / (s2 - s1);
101 }
102
103 bool Point::on(const Point &a, const Point &b) const {
104     const Point &p = *this;
105     return sign(det(p - a, p - b)) == 0 && sign(dot(p - a, p - b)) <= 0;
106 }
107
108 bool Point::in(const vector<Point> &polygon) const {
109     const Point &p = *this;
110     int n = polygon.size();
111     int count = 0;
112     for (int i = 0; i < n; ++ i) {
113         const Point &a = polygon[i];
114         const Point &b = polygon[(i + 1) % n];
115         if (p.on(a, b)){
116             return false;

```

```

117     }
118     int t0 = sign(det(a - p, b - p));
119     int t1 = sign(a.y - p.y);
120     int t2 = sign(b.y - p.y);
121     count += t0 > 0 && t1 <= 0 && t2 > 0;
122     count -= t0 < 0 && t2 <= 0 && t1 > 0;
123 }
124 return count != 0;
125 }
126
127 struct eglis {
128     int other[MAXE], succ[MAXE], last[MAXE], sum;
129     set<pair<int, int> > Edges;
130     void clear() {
131         memset(last, -1, sizeof(last));
132         sum = 0;
133         Edges.clear();
134     }
135     void addEdge(int a, int b) {
136         if (Edges.count(make_pair(a, b)))
137             return;
138         Edges.insert(make_pair(a, b));
139         other[sum] = b, succ[sum] = last[a], last[a] = sum;
140         sum++;
141     }
142     void _addEdge(int a, int b) {
143         addEdge(a, b);
144         addEdge(b, a);
145     }
146 }e, topo;
147
148 vector<Point> Points;
149
150 Point segments[MAXE][2];
151 double W, H;
152 int n, next[MAXE];
153 vector<double> areas, allAreas;
154 vector<vector<Point> > regions;
155
156 void addSegment(Point a, Point b) {
157     segments[n][0] = a;
158     segments[n][1] = b;
159     n++;
160 }
161
162 int getPointID(const Point &p) {
163     return lower_bound(Points.begin(), Points.end(), p) - Points.begin();
164 }
165

```

```

166 const int VERTEX = 0;
167 const int EDGE = 1;
168 const int REGION = 2;
169
170 int getID(int type, int id) {
171     if (type == VERTEX) {
172         return id;
173     }
174     if (type == EDGE) {
175         return id + Points.size();
176     }
177     if (type == REGION) {
178         return id + Points.size() + e.sum / 2;
179     }
180     assert(false);
181 }
182
183 double getArea(int id) {
184     id -= Points.size() + e.sum / 2;
185     return id < 0 ? 0 : areas[id];
186 }
187
188 int locate(const Point &p) {
189     for (int i = 0; i < e.sum; i += 2) {
190         if (p.on(Points[e.other[i]], Points[e.other[i ^ 1]])) {
191             return getID(EDGE, i >> 1);
192         }
193     }
194     int best = -1;
195     for (int i = 0; i < regions.size(); ++i) {
196         if (p.in(regions[i]) && (best == -1 || allAreas[best] > allAreas[i])) {
197             best = i;
198         }
199     }
200     return getID(REGION, best);
201 }
202
203 vector<string> colorNames;
204 map<string, int> colorIDs;
205
206 int getColorID(const char *color) {
207     if (!colorIDs.count(color)) {
208         colorNames.push_back(color);
209         int newID = colorIDs.size();
210         colorIDs[color] = newID;
211     }
212     return colorIDs[color];
213 }
214

```

```

215 int color[MAXV * 10];
216
217 void paint(const Point &p, const char * c) {
218     int start = locate(p);
219     int old = color[start];
220     int cid = getColorID(c);
221     if (old == cid)
222         return;
223     queue<int> q;
224     q.push(start);
225     color[start] = cid;
226     while (!q.empty()) {
227         int x = q.front();
228         q.pop();
229         for (int i = topo.last[x]; ~i; i = topo.succ[i]) {
230             int y = topo.other[i];
231             if (color[y] == old) {
232                 color[y] = cid;
233                 q.push(y);
234             }
235         }
236     }
237 }
238
239 int main() {
240     freopen("input.txt", "r", stdin);
241     //freopen("output.txt", "w", stdout);
242     scanf("%lf%lf%lf", &W, &H, &n);
243     for (int i = 0; i < n; i++) {
244         scanf("%lf%lf%lf%lf", &segments[i][0].x, &segments[i][0].y, &segments[i]
                ][1].x, &segments[i][1].y);
245     }
246     addSegment(Point(0, 0), Point(W, 0));
247     addSegment(Point(W, 0), Point(W, H));
248     addSegment(Point(W, H), Point(0, H));
249     addSegment(Point(0, H), Point(0, 0));
250
251     for (int i = 0; i < n; i++) {
252         Points.push_back(segments[i][0]);
253         Points.push_back(segments[i][1]);
254         for (int j = 0; j < i; j++) {
255             if (!parallel(segments[i][0], segments[i][1], segments[j][0], segments[j]
                ][1])) {
256                 Point p = intersect(segments[i][0], segments[i][1], segments[j][0],
                segments[j][1]);
257                 if (p.on(segments[i][0], segments[i][1]) && p.on(segments[j][0],
                segments[j][1])) {
258                     Points.push_back(p);
259                 }

```

```

260     }
261 }
262 }
263 sort(Points.begin(), Points.end());
264 Points.erase(unique(Points.begin(), Points.end()), Points.end());
265
266 e.clear();
267 for (int i = 0; i < n; i++) {
268     vector<pair<double, int> > pairs;
269     for (int j = 0; j < Points.size(); j++) {
270         if (Points[j].on(segments[i][0], segments[i][1]))
271             pairs.push_back(make_pair((Points[j] - segments[i][0]).norm(), j));
272     }
273     sort(pairs.begin(), pairs.end());
274     for (int i = 1; i < pairs.size(); i++) {
275         e.addEdge(pairs[i - 1].second, pairs[i].second);
276         e.addEdge(pairs[i].second, pairs[i - 1].second);
277     }
278 }
279
280 for (int u = 0; u < Points.size(); u++) {
281     vector<pair<double, int> > pairs;
282     for (int iter = e.last[u]; ~iter; iter = e.succ[iter]) {
283         pairs.push_back(make_pair((Points[e.other[iter]] - Points[u]).arg(), iter));
284     }
285     sort(pairs.begin(), pairs.end());
286     for (int i = 0; i < pairs.size(); i++) {
287         next[pairs[(i + 1) % pairs.size()].second ^ 1] = pairs[i].second;
288     }
289 }
290
291 vector<pair<Point, double> > waits;
292 static bool visit[MAXV];
293 memset(visit, 0, sizeof(visit));
294 for (int start = 0; start < e.sum; ++start) {
295     if (!visit[start]) {
296         int v = start;
297         double totalArea = 0;
298         vector<Point> region;
299         for (; !visit[v]; v = next[v]) {
300             visit[v] = true;
301             totalArea += det(Points[e.other[v ^ 1]], Points[e.other[v]]);
302             region.push_back(Points[e.other[v]]);
303         }
304
305         if (sign(totalArea) > 0) {
306             regions.push_back(region);
307             areas.push_back(totalArea);

```



```

308         allAreas.push_back(totalArea);
309     } else {
310         waits.push_back(make_pair(region.front(), -totalArea));
311     }
312 }
313 }
314
315 //build
316 topo.clear();
317 for (int i = 0; i < e.sum; i++) {
318     topo._addEdge(getID(EDGE, i >> 1), getID(VERTEX, e.other[i]));
319 }
320 for (int i = 0; i < regions.size(); i++) {
321     topo._addEdge(getID(REGION, i), getID(VERTEX, getPointID(regions[i].front())))
322         );
323 }
324 for (int iter = 0; iter < waits.size(); iter++) {
325     const Point &p = waits[iter].first;
326     int best = -1;
327     for (int i = 0; i < regions.size(); i++) {
328         if (p.in(regions[i]) && (best == -1 || allAreas[best] > allAreas[i])) {
329             best = i;
330         }
331     }
332     if (best != -1) {
333         areas[best] -= waits[iter].second;
334         topo._addEdge(getID(REGION, best), getID(VERTEX, getPointID(p)));
335     }
336 }
337
338 getColorID("white");
339 getColorID("black");
340 getColorID("__COLOR__");
341
342 for (int i = 0; i < regions.size(); i++) {
343     color[getID(REGION, i)] = getColorID("white");
344 }
345 for (int i = 0; i < Points.size(); i++) {
346     color[getID(VERTEX, i)] = getColorID("black");
347 }
348 for(int i = 0; i < e.sum / 2; i++) {
349     color[getID(EDGE, i)] = getColorID("black");
350 }
351 paint(Point(0, 0), "__COLOR__");
352 int m;
353 scanf("%d", &m);
354 while (m --) {
355     Point p;

```

```

356     char buffer[16];
357     scanf("%lf%lf%s", &p.x, &p.y, buffer);
358     paint(p, buffer);
359 }
360
361 map<string, double> answer;
362 for (int i = 0; i < Points.size() + (e.sum >> 1) + regions.size(); ++i) {
363     const string &name = colorNames[color[i]];
364     if (name != "__COLOR__") {
365         answer[name] += getArea(i);
366     }
367 }
368 for (map<string, double> :: iterator iter = answer.begin(); iter != answer.end();
369     ++ iter) {
370     printf("%s%.8lf\n", iter->first.c_str(), 0.5 * iter->second);
371 }

```

3.5 半平面交

```

1 struct Border {
2     point p1, p2; double alpha;
3     Border() : p1(), p2(), alpha(0.0) {}
4     Border(const point &a, const point &b): p1(a), p2(b), alpha( atan2(p2.y - p1.y,
5         p2.x - p1.x) ) {}
6     bool operator == (const Border &b) const {
7         return sign(alpha - b.alpha) == 0;
8     }
9     bool operator < (const Border &b) const {
10         int c = sign(alpha - b.alpha); if (c != 0) return c > 0;
11         return sign(det(b.p2 - b.p1, p1 - b.p1)) >= 0;
12     }
13 };
14 point isBorder(const Border &a, const Border &b) { // a and b should not be parallel
15     point is;
16     lineIntersect(a.p1, a.p2, b.p1, b.p2, is);
17     return is;
18 }
19 bool checkBorder(const Border &a, const Border &b, const Border &me) {
20     point is;
21     lineIntersect(a.p1, a.p2, b.p1, b.p2, is);
22     return sign(det(me.p2 - me.p1, is - me.p1)) > 0;
23 }
24 double HPI(int N, Border border[]) {
25     static Border que[MAXN * 2 + 1]; static point ps[MAXN];
26     int head = 0, tail = 0, cnt = 0; // [head, tail)
27     sort(border, border + N);
28     N = unique(border, border + N) - border;

```

```

28     for (int i = 0; i < N; ++i) {
29         Border &cur = border[i];
30         while (head + 1 < tail && !checkBorder(que[tail - 2], que[tail - 1], cur))
31             --tail;
32         while (head + 1 < tail && !checkBorder(que[head], que[head + 1], cur))
33             ++head;
34         que[tail++] = cur;
35     }
36     while (head + 1 < tail && !checkBorder(que[tail - 2], que[tail - 1], que[head]))
37         --tail;
38     while (head + 1 < tail && !checkBorder(que[head], que[head + 1], que[tail - 1]))
39         ++head;
40     if (tail - head <= 2)
41         return 0.0;
42     //Foru(i, a, b) : a <= i < b
43     Foru(i, head, tail)
44         ps[cnt++] = isBorder(que[i], que[(i + 1 == tail) ? (head) : (i + 1)]);
45     double area = 0;
46     Foru(i, 0, cnt)
47         area += det(ps[i], ps[(i + 1) % cnt]);
48     return fabs(area * 0.5); // or (-area * 0.5)
49 }

```

3.6 三维绕轴旋转

```

1  const double pi = acos(-1.0);
2  int n, m; char ch1; bool flag;
3  double a[4][4], s1, s2, x, y, z, w, b[4][4], c[4][4];
4  double sqr(double x)
5  {
6      return x*x;
7  }
8  int main()
9  {
10     scanf("%d\n", &n);
11     memset(b, 0, sizeof(b));
12     b[0][0] = b[1][1] = b[2][2] = b[3][3] = 1; //initial matrix
13     for(int i = 1; i <= n; i++)
14     {
15         scanf("%c", &ch1);
16         if(ch1 == 'T')
17         {
18             scanf("%lf %lf %lf\n", &x, &y, &z); //plus each coordinate by a number (x,
19                 y, z)
20             memset(a, 0, sizeof(a));
21             a[0][0] = 1; a[3][0] = x;
22             a[1][1] = 1; a[3][1] = y;
23             a[2][2] = 1; a[3][2] = z;

```

```

23     a[3][3] = 1;
24 }else if(ch1 == 'S')
25 {
26     scanf("%lf%lf%lf\n", &x, &y, &z); //multiply each coordinate by a number
        (x, y, z)
27     memset(a, 0, sizeof(a));
28     a[0][0] = x;
29     a[1][1] = y;
30     a[2][2] = z;
31     a[3][3] = 1;
32 }else
33 {
34     scanf("%lf%lf%lf%lf\n", &x, &y, &z, &w);
35     //大拇指指向x轴正方向时, 4指弯曲由y轴正方向指向z轴正方向
36     //大拇指沿着原点到点(x, y, z)的向量, 4指弯曲方向旋转w度
37     w = w*pi/180;
38     memset(a, 0, sizeof(a));
39     s1 = x*x+y*y+z*z;
40     a[3][3] = 1;
41     a[0][0] = ((y*y+z*z)*cos(w)+x*x)/s1;          a[0][1] = x*y*(1-cos(w))/
        s1+z*sin(w)/sqrt(s1); a[0][2] = x*z*(1-cos(w))/s1-y*sin(w)/sqrt(s1);
42     a[1][0] = x*y*(1-cos(w))/s1-z*sin(w)/sqrt(s1); a[1][1] = ((x*x+z*z)*cos(
        w)+y*y)/s1;          a[1][2] = y*z*(1-cos(w))/s1+x*sin(w)/sqrt(s1);
43     a[2][0] = x*z*(1-cos(w))/s1+y*sin(w)/sqrt(s1); a[2][1] = y*z*(1-cos(w))/
        s1-x*sin(w)/sqrt(s1); a[2][2] = ((x*x+y*y)*cos(w)+z*z)/s1;
44 }
45 memset(c, 0, sizeof(c));
46 for(int i = 0; i < 4; i++)
47     for(int j = 0; j < 4; j++)
48         for(int k = 0; k < 4; k++)
49             c[i][j] += b[i][k]*a[k][j];
50 memcpy(b, c, sizeof(c));
51 }
52 scanf("%d", &m);
53 for(int i = 1; i <= m; i++)
54 {
55     scanf("%lf%lf%lf", &x, &y, &z); //initial vector
56     printf("%lf%lf%lf\n", x*b[0][0]+y*b[1][0]+z*b[2][0]+b[3][0], x*b[0][1]+y*b
        [1][1]+z*b[2][1]+b[3][1], x*b[0][2]+y*b[1][2]+z*b[2][2]+b[3][2]);
57 }
58 return 0;
59 }

```

3.7 点到凸包切线

???

3.8 直线凸包交点

```

1  int n;
2  double eps(1e-8);
3  int sign(const double & x) {
4      return (x > eps) - (x + eps < 0);
5  }
6  struct Point {
7      double x, y;
8      void scan() {
9          scanf("%lf%lf", &x, &y);
10     }
11     void print() {
12         printf("%lf_ %lf\n", x, y);
13     }
14     Point() {}
15     Point(const double & x, const double & y) : x(x), y(y) {}
16 }
17
18 };
19 Point operator + (const Point & a, const Point & b) {
20     return Point(a.x + b.x, a.y + b.y);
21 }
22 Point operator - (const Point & a, const Point & b) {
23     return Point(a.x - b.x, a.y - b.y);
24 }
25 Point operator * (const double & a, const Point & b) {
26     return Point(a * b.x, a * b.y);
27 }
28 double operator * (const Point & a, const Point & b) {
29     return a.x * b.y - a.y * b.x;
30 }
31 bool isUpper(const Point & a) {
32     return sign(a.x) < 0 or sign(a.x) == 0 and sign(a.y > 0);
33 }
34 Point crs(const Point & as, const Point & at, const Point & bs, const Point & bt) {
35     if(sign((at - as) * (bt - bs)) == 0) {
36         return bs;
37     }
38     double lambda((bs - as) * (bt - bs) / ((at - as) * (bt - bs)));
39     return as + lambda * (at - as);
40 }
41 struct reca {
42     Point a[50000];
43     double s[50000];
44     Point & operator [] (int x) {
45         assert(x % n < 50000);
46         return a[x % n];
47     }

```

```

48 void init() {
49     s[0] = a[0] * a[1];
50     for(int i(1); i < n; i++) {
51         s[i] = s[i - 1] + a[i] * (i == n - 1 ? a[0] : a[i + 1]);
52     }
53 }
54
55 double getS(int le, int ri) {
56     if(le > ri)
57         return 0;
58     le %= n;
59     ri %= n;
60     if(le <= ri) {
61         return s[ri] - (le ? s[le - 1] : 0);
62     } else {
63         return getS(le, n - 1) + getS(0, ri);
64     }
65 }
66 } a;
67
68 int lowerBound(int le, int ri, const Point & dir) {
69     while(le < ri) {
70         int mid((le + ri) / 2);
71         if(sign((a[mid + 1] - a[mid]) * dir) >= 0) {
72             le = mid + 1;
73         } else {
74             ri = mid;
75         }
76     }
77     return le;
78 }
79 int boundLower(int le, int ri, const Point & s, const Point & t) {
80     while(le < ri) {
81         int mid((le + ri + 1) / 2);
82         if(sign((a[mid] - s) * (t - s)) >= 0) {
83             le = mid;
84         } else {
85             ri = mid - 1;
86         }
87     }
88     return le;
89 }
90 bool check(const Point & a, const Point & b, const Point & c, const Point & d) {
91     return sign((a - c) * (d - c)) * sign((b - c) * (d - c)) <= 0;
92 }
93 bool f[55555];
94 int main() {
95     scanf("%d", &n);
96     for(int i(0); i < n; i++) {

```

```

97         //printf("%d\n", n);
98         a[i].scan();
99         //return 0;
100     }
101     //return 0;
102     for(int i(0); i < n; i++) {
103         int d(sign((a[i + 1] - a[i]) * (a[i + 2] - a[i + 1])));
104         if(d) {
105             if(d < 0) {
106                 reverse(a.a, a.a + n);
107             }
108             break;
109         }
110     }
111     for(int i(0); i < n; i++) {
112         if(!sign(a[i].x - a[i + 1].x) and !sign(a[i].y - a[i + 1].y)) {
113             f[i] = false;
114         } else {
115             f[i] = true;
116         }
117     }
118     int n1(0);
119     for(int i(0); i < n; i++) {
120         if(f[i]) {
121             a[n1++] = a[i];
122         }
123     }
124     n = n1;
125     //现在a必须是严格逆时针凸包
126     a.init();
127     int i1, j1;
128     for(int i(0); i < n; i++) {
129         if(isUpper(a[i + 1] - a[i])) {
130             for(int j(i + 1); j != i; ++j %= n) {
131                 if(!isUpper(a[j + 1] - a[j])) {
132                     i1 = i; j1 = j;
133                     break;
134                 }
135             }
136             break;
137         }
138     }
139     if(i1 > j1) {
140         j1 += n;
141     }
142     int m;
143     scanf("%d", &m);
144     for(int i(0); i < m; i++) {
145         Point s, t;

```

```

146     s.scan(); t.scan();
147     if(!isUpper(t - s)) {
148         swap(t, s);
149     }
150     int i3(lowerBound(i1, j1, t - s));
151     int j3(lowerBound(j1, i1 + n, s - t));
152     int i4(lowerBound(i3, j3, s, t));
153     int j4(lowerBound(j3, i3 + n, t, s));
154     if(check(a[i4], a[i4 + 1], s, t)) {
155         Point p1(crs(s, t, a[i4], a[i4 + 1]));
156         Point p2(crs(s, t, a[j4], a[j4 + 1]));
157         if(sign(p1.x - p2.x) or sign(p1.y - p2.y)) {
158             assert(i4 % n != j4 % n);
159             double area1(p1 * a[i4 + 1] + a.getS(i4 + 1, j4 - 1) + a[j4] * p2 +
160                 p2 * p1);
161             double area2(p2 * a[j4 + 1] + a.getS(j4 + 1, i4 + n - 1) + a[i4] * p1
162                 + p1 * p2);
163             printf("%.6f\n", min(fabs(area1), fabs(area2)) / 2);
164         }else {
165             printf("0.000000\n");
166         }
167     }else {
168         printf("0.000000\n");
169     }
170 }

```

3.9 exhausted_robot 凸多边形卡壳 + 凸多边形交

```

1  double eps(1e-8);
2  int sign(const double & x) {
3      return (x > eps) - (x + eps < 0);
4  }
5  bool equal(const double & x, const double & y) {
6      return x + eps > y and y + eps > x;
7  }
8  struct Point {
9      double x, y;
10     Point () {
11     }
12     Point(const double & x, const double & y) : x(x), y(y) {
13     }
14     void scan() {
15         scanf("%lf%lf", &x, &y);
16     }
17     double sqrlen() const {
18         return x * x + y * y;
19     }

```



```

20     double len() const {
21         return sqrt(sqrten());
22     }
23     Point zoom(const double & l) const {
24         double lambda(1 / len());
25         return Point(lambda * x, lambda * y);
26     }
27     Point rev() const {
28         return Point(-y, x);
29     }
30     void print() const {
31         printf("(%f_ %f)\n", x, y);
32     }
33 };
34
35 vector<Point> blocks[22], denied[22], robot;
36
37 vector<pair<double, int> > vec;
38
39 bool f[111];
40
41 Point operator - (const Point & a, const Point & b) {
42     return Point(a.x - b.x, a.y - b.y);
43 }
44 Point operator + (const Point & a, const Point & b) {
45     return Point(a.x + b.x, a.y + b.y);
46 }
47 Point operator * (const double & a, const Point & b) {
48     return Point(a * b.x, a * b.y);
49 }
50 double operator * (const Point & a, const Point & b) {
51     return a.x * b.y - a.y * b.x;
52 }
53 double operator % (const Point & a, const Point & b) {
54     return a.x * b.x + a.y * b.y;
55 }
56
57 bool operator < (const Point & a, const Point & b) {
58     if(!equal(a.x, b.x))
59         return a.x < b.x;
60     else if(!equal(a.y, b.y));
61         return a.y < b.y;
62     return false;
63 }
64 bool operator == (const Point & a, const Point & b) {
65     return equal(a.x, b.x) and equal(a.y, b.y);
66 }
67
68 void scan(vector<Point> & vec) {

```

```

69     vec.clear();
70     int x;
71     scanf("%d", &x);
72     for(int i(0); i < x; i++) {
73         Point tmp;
74         tmp.scan();
75         vec.push_back(tmp);
76     }
77 }
78
79 Point intersect(const Point & as, const Point & ad, const Point & bs, const Point &
    bd) {
80     double lambda((bs - as) * bd / (ad * bd));
81     return as + lambda * ad;
82 }
83
84 void cut(vector<Point> & vec, const Point & s, const Point & d) {
85     vector<Point> vec1;
86     for(int i(0); i < (int)vec.size(); i++) {
87         if(sign((vec[i] - s) * d) <= 0) {
88             vec1.push_back(vec[i]);
89         }
90         if(sign((vec[i] - s) * d) * sign((vec[(i + 1) % (int)vec.size()] - s) * d) <
            0) {
91             vec1.push_back(intersect(s, d, vec[i], vec[(i + 1) % (int)vec.size()] -
                vec[i]));
92         }
93     }
94     vec = vec1;
95 }
96
97 int mi;
98
99 Point getMax(const Point & norm) {
100     Point res(robot[0]);
101     mi = 0;
102     for(int i(0); i < (int)robot.size(); i++) {
103         if(sign(robot[i] % norm - res % norm) > 0) {
104             res = robot[i];
105             mi = i;
106         }
107     }
108     return res;
109 }
110
111 bool vecCmp(const pair<double, int> & a, const pair<double, int> & b) {
112     if(!equal(a.first, b.first))
113         return a.first < b.first;
114     else

```

```

115         return a.second > b.second;
116     }
117
118     bool vecEq1(const pair<double, int> & a, const pair<double, int> & b) {
119         return equal(a.first, b.first) and a.second == b.second;
120     }
121
122     void print(const vector<Point> & vec) {
123         printf("print:\n");
124         for(int i(0); i < (int)vec.size(); i++) {
125             vec[i].print();
126         }
127         printf("endprint\n");
128     }
129
130     void getConvex(vector<Point> & vec) {
131         sort(vec.begin(), vec.end());
132         vector<Point> vec1;
133         for(int i(0); i < (int)vec.size(); i++) {
134             while(vec1.size() >= 2 and sign((vec1.back() - vec1[(int)vec1.size() - 2]) *
135                 (vec[i] - vec1.back())) <= 0)
136                 vec1.pop_back();
137             vec1.push_back(vec[i]);
138         }
139         vector<Point> vec2;
140         for(int i((int)vec.size() - 1); i >= 0; i--) {
141             while(vec2.size() >= 2 and sign((vec2.back() - vec2[(int)vec2.size() - 2]) *
142                 (vec[i] - vec2.back())) <= 0)
143                 vec2.pop_back();
144             vec2.push_back(vec[i]);
145         }
146         vec.clear();
147         for(int i(0); i + 1 < (int)vec1.size(); i++)
148             vec.push_back(vec1[i]);
149         for(int i(0); i + 1 < (int)vec2.size(); i++)
150             vec.push_back(vec2[i]);
151     }
152
153     int main() {
154         int tst;
155         scanf("%d", &tst);
156         for(int qq(1); qq <= tst; qq++) {
157             int n;
158             scanf("%d", &n);
159             for(int i(0); i < n; i++)
160                 scan(blocks[i]);
161             scan(robot);
162             double x1, y1, x2, y2;
163             scanf("%lf%lf%lf%lf", &x1, &y1, &x2, &y2);

```

```

162 x1 += robot[0].x - getMax(Point(-1, 0)).x;
163 y1 += robot[0].y - getMax(Point(0, -1)).y;
164 x2 -= getMax(Point(1, 0)).x - robot[0].x;
165 y2 -= getMax(Point(0, 1)).y - robot[0].y;
166 double ans((x2 - x1) * (y2 - y1));
167 for(int i(0); i < n; i++) {
168     int siz(blocks[i].size());
169     denied[i].clear();
170     int p1, p2;
171     p1 = 0;
172     getMax((blocks[i][1] - blocks[i][0]).rev());
173     p2 = mi;
174     denied[i].push_back(blocks[i][0] + robot[0] - robot[mi]);
175     for(int j1(1), j2(mi); j1 != p1 or j2 != p2; ) {
176         denied[i].push_back(blocks[i][j1] + robot[0] - robot[j2]);
177         Point dir((blocks[i][(j1 + 1) % (int)blocks[i].size()] - blocks[i][j1]
178             ).rev());
179         getMax(dir);
180         if(equal(robot[j2] % dir, robot[mi] % dir))
181             ++j1 %= (int)blocks[i].size();
182         else
183             ++j2 %= (int)robot.size();
184     }
185     for(int i(0); i < n; i++) {
186         cut(denied[i], Point(x1, y1), Point(x2 - x1, 0));
187         cut(denied[i], Point(x2, y1), Point(0, y2 - y1));
188         cut(denied[i], Point(x2, y2), Point(x1 - x2, 0));
189         cut(denied[i], Point(x1, y2), Point(0, y1 - y2));
190         for(int j(0); j < (int)denied[i].size(); j++) {
191             f[j] = !(denied[i][j] == denied[i][(j + 1) % (int)denied[i].size()]);
192         }
193         getConvex(denied[i]);
194         denied[i].push_back(denied[i].front());
195     }
196     for(int i(0); i < n; i++) {
197         for(int j(0); j + 1 < (int)denied[i].size(); j++) {
198             vec.clear();
199             vec.push_back(make_pair(0., 0));
200             vec.push_back(make_pair(1., 0));
201             Point norm(denied[i][j + 1] - denied[i][j]);
202             Point a(denied[i][j]), b(denied[i][j + 1]);
203             norm = norm.zoom(1 / norm.len());
204             for(int k(0); k < n; k++) if(k != i) {
205                 int sz(vec.size());
206                 for(int l(0); l + 1 < (int)denied[k].size(); l++) {
207                     Point c(denied[k][l]), d(denied[k][l + 1]);
208                     int s1(sign((c - a) * norm));
209                     int s2(sign((d - a) * norm));

```

```

210         if(!s1 and !s2 and k < i and sign((d - c) % norm) > 0) {
211             vec.push_back(make_pair((c - a) % norm, 1));
212             vec.push_back(make_pair((d - a) % norm, -1));
213         } else if(s1 <= 0 and s2 > 0 or s1 > 0 and s2 <= 0) {
214             double a1((d - c) * (a - c));
215             double a2((d - c) * (b - c));
216             vec.push_back(make_pair(a1 / (a1 - a2), (s1 < 0 or s2 >
217                                     0)?1:-1));
218         }
219     }
220     sort(vec.begin(), vec.end(), vecCmp);
221     int cnt(0);
222     double tot(0);
223     for(int k(0); k + 1 < (int)vec.size(); k++) {
224         cnt += vec[k].second;
225         if(cnt == 0 and sign(vec[k].first) >= 0 and sign(vec[k + 1].first
226                     - 1) <= 0) {
227             tot += vec[k + 1].first - vec[k].first;
228         }
229         ans -= tot * (denied[i][j] * denied[i][j + 1]) / 2;
230     }
231 }
232 printf("Case_#%d: %.3f\n", qq, ans);
233 }
234 }

```

3.10 判断圆存在交集 $O(n\log k)$

传入 n 个圆, 圆心存在 `cir` 中, 半径存在 `radius` 中, $n\log k$ 判断是否存在交集

```

1  int n;
2  double sx, sy, d;
3  vector<Point> cir;
4  vector<double> radius;
5
6  int isIntersectCircleToCircle(Point c1, double r1, Point c2, double r2)
7  {
8      double dis = c1.distTo(c2);
9      return sign(dis - (r1 + r2)) <= 0;
10 }
11
12 void getRange(double x, Point &c, double r, double &retl, double &retr)
13 {
14     double tmp = sqrt(max(r * r - (c.x - x) * (c.x - x), 0.0));
15     retl = c.y - tmp; retr = c.y + tmp;
16 }
17

```

```

18 int checkInLine(double x)
19 {
20     double minR = INF, maxL = -INF;
21     double tmpL, tmpR;
22     for(int i = 0; i < n; ++ i) {
23         if (sign(cir[i].x + radius[i] - x) < 0 || sign(cir[i].x - radius[i] - x) > 0)
24             return false;
25         getRange(x, cir[i], radius[i], tmpL, tmpR);
26         maxL = max(tmpL, maxL);
27         minR = min(tmpR, minR);
28         if (maxL > minR) return false;
29     }
30     return true;
31 }
32
33 int shouldGoLeft(double x)
34 {
35     if (checkInLine(x)) return 2;
36     int onL = 0, onR = 0;
37     for(int i = 0; i < n; ++ i) {
38         if (sign(cir[i].x + radius[i] - x) < 0) onL = 1;
39         if (sign(cir[i].x - radius[i] - x) > 0) onR = 1;
40     }
41     if (onL && onR) return -1;
42     if (onL) return 1;
43     if (onR) return 0;
44
45     double minR = INF, maxL = -INF, tmpL, tmpR;
46     int idMinR, idMaxL;
47
48     for(int i = 0; i < n; ++ i) {
49         getRange(x, cir[i], radius[i], tmpL, tmpR);
50         if (tmpR < minR) {
51             minR = tmpR;
52             idMinR = i;
53         }
54         if (tmpL > maxL) {
55             maxL = tmpL;
56             idMaxL = i;
57         }
58     }
59     if (! isIntersectCircleToCircle(cir[idMinR], radius[idMinR], cir[idMaxL], radius[
        idMaxL]))
60         return -1;
61     Point p1, p2;
62     intersectionCircleToCircle(cir[idMinR], radius[idMinR], cir[idMaxL], radius[
        idMaxL], p1, p2);
63     return (p1.x < x);
64 }

```

```

65
66 int hasIntersectionCircles()
67 {
68     double l = -INF, r = INF, mid;
69     for(int i = 0; i < 100; ++ i) {
70         mid = (l + r) * 0.5;
71         int tmp = shouldGoLeft(mid);
72         if (tmp < 0) return 0;
73         if (tmp == 2) return 1;
74         if (tmp) r = mid;
75         else l = mid;
76     }
77     mid = (l + r) * 0.5;
78     return checkInLine(mid);
79 }

```

3.11 最小覆盖球

```

1  double eps(1e-8);
2  int sign(const double & x) {
3      return (x > eps) - (x + eps < 0);
4  }
5  bool equal(const double & x, const double & y) {
6      return x + eps > y and y + eps > x;
7  }
8  struct Point {
9      double x, y, z;
10     Point() {
11     }
12     Point(const double & x, const double & y, const double & z) : x(x), y(y), z(z){
13     }
14     void scan() {
15         scanf("%lf%lf%lf", &x, &y, &z);
16     }
17     double sqrlen() const {
18         return x * x + y * y + z * z;
19     }
20     double len() const {
21         return sqrt(sqrlen());
22     }
23     void print() const {
24         printf("(%lf_ %lf_ %lf)\n", x, y, z);
25     }
26 } a[33];
27 Point operator + (const Point & a, const Point & b) {
28     return Point(a.x + b.x, a.y + b.y, a.z + b.z);
29 }
30 Point operator - (const Point & a, const Point & b) {

```

```

31     return Point(a.x - b.x, a.y - b.y, a.z - b.z);
32 }
33 Point operator * (const double & x, const Point & a) {
34     return Point(x * a.x, x * a.y, x * a.z);
35 }
36 double operator % (const Point & a, const Point & b) {
37     return a.x * b.x + a.y * b.y + a.z * b.z;
38 }
39 Point operator * (const Point & a, const Point & b) {
40     return Point(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x)
41         ;
42 }
43 struct Circle {
44     double r;
45     Point o;
46     Circle() {
47         o.x = o.y = o.z = r = 0;
48     }
49     Circle(const Point & o, const double & r) : o(o), r(r) {
50     }
51     void scan() {
52         o.scan();
53         scanf("%lf", &r);
54     }
55     void print() const {
56         o.print();
57         printf("%lf\n", r);
58     }
59 };
60 struct Plane {
61     Point nor;
62     double m;
63     Plane(const Point & nor, const Point & a) : nor(nor){
64         m = nor % a;
65     }
66 };
67 Point intersect(const Plane & a, const Plane & b, const Plane & c) {
68     Point c1(a.nor.x, b.nor.x, c.nor.x), c2(a.nor.y, b.nor.y, c.nor.y), c3(a.nor.z, b
        .nor.z, c.nor.z), c4(a.m, b.m, c.m);
69     return 1 / ((c1 * c2) % c3) * Point((c4 * c2) % c3, (c1 * c4) % c3, (c1 * c2) %
        c4);
70 }
71 bool in(const Point & a, const Circle & b) {
72     return sign((a - b.o).len() - b.r) <= 0;
73 }
74 bool operator < (const Point & a, const Point & b) {
75     if(!equal(a.x, b.x)) {
76         return a.x < b.x;
77     }

```



```

77     if(!equal(a.y, b.y)) {
78         return a.y < b.y;
79     }
80     if(!equal(a.z, b.z)) {
81         return a.z < b.z;
82     }
83     return false;
84 }
85 bool operator == (const Point & a, const Point & b) {
86     return equal(a.x, b.x) and equal(a.y, b.y) and equal(a.z, b.z);
87 }
88 vector<Point> vec;
89 Circle calc() {
90     if(vec.empty()) {
91         return Circle(Point(0, 0, 0), 0);
92     } else if(1 == (int)vec.size()) {
93         return Circle(vec[0], 0);
94     } else if(2 == (int)vec.size()) {
95         return Circle(0.5 * (vec[0] + vec[1]), 0.5 * (vec[0] - vec[1]).len());
96     } else if(3 == (int)vec.size()) {
97         double r((vec[0] - vec[1]).len() * (vec[1] - vec[2]).len() * (vec[2] - vec
98             [0]).len() / 2 / fabs(((vec[0] - vec[2]) * (vec[1] - vec[2])).len()));
99         return Circle(intersect(Plane(vec[1] - vec[0], 0.5 * (vec[1] + vec[0])),
100             Plane(vec[2] - vec[1], 0.5 * (vec[2] + vec[1])),
101             Plane((vec[1] - vec[0]) * (vec[2] - vec[0]), vec[0])), r);
102     } else {
103         Point o(intersect(Plane(vec[1] - vec[0], 0.5 * (vec[1] + vec[0])),
104             Plane(vec[2] - vec[0], 0.5 * (vec[2] + vec[0])),
105             Plane(vec[3] - vec[0], 0.5 * (vec[3] + vec[0]))));
106         return Circle(o, (o - vec[0]).len());
107     }
108 }
109 Circle miniBall(int n) {
110     Circle res(calc());
111     for(int i(0); i < n; i++) {
112         if(!in(a[i], res)) {
113             vec.push_back(a[i]);
114             res = miniBall(i);
115             vec.pop_back();
116             if(i) {
117                 Point tmp(a[i]);
118                 memmove(a + 1, a, sizeof(Point) * i);
119                 a[0] = tmp;
120             }
121         }
122     }
123     return res;
124 }
125 int main() {

```

```

125     int n;
126     for(;;) {
127         scanf("%d", &n);
128         if(!n) {
129             break;
130         }
131         for(int i(0); i < n; i++) {
132             a[i].scan();
133         }
134         sort(a, a + n);
135         n = unique(a, a + n) - a;
136         vec.clear();
137         printf("%.10f\n", miniBall(n).r);
138     }
139 }

```

3.12 最小覆盖圆

```

1  #include<cmath>
2  #include<cstdio>
3  #include<algorithm>
4  using namespace std;
5  const double eps=1e-6;
6  struct couple
7  {
8      double x, y;
9      couple(){}
10     couple(const double &xx, const double &yy)
11     {
12         x = xx; y = yy;
13     }
14 } a[100001];
15 int n;
16 bool operator < (const couple & a, const couple & b)
17 {
18     return a.x < b.x - eps or (abs(a.x - b.x) < eps and a.y < b.y - eps);
19 }
20 bool operator == (const couple & a, const couple & b)
21 {
22     return !(a < b) and !(b < a);
23 }
24 inline couple operator - (const couple &a, const couple &b)
25 {
26     return couple(a.x-b.x, a.y-b.y);
27 }
28 inline couple operator + (const couple &a, const couple &b)
29 {
30     return couple(a.x+b.x, a.y+b.y);

```

```

31 }
32 inline couple operator * (const couple &a, const double &b)
33 {
34     return couple(a.x*b, a.y*b);
35 }
36 inline couple operator / (const couple &a, const double &b)
37 {
38     return a*(1/b);
39 }
40 inline double operator * (const couple &a, const couple &b)
41 {
42     return a.x*b.y-a.y*b.x;
43 }
44 inline double len(const couple &a)
45 {
46     return a.x*a.x+a.y*a.y;
47 }
48 inline double di2(const couple &a, const couple &b)
49 {
50     return (a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y);
51 }
52 inline double dis(const couple &a, const couple &b)
53 {
54     return sqrt((a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y));
55 }
56 struct circle
57 {
58     double r; couple c;
59 } cir;
60 inline bool inside(const couple &x)
61 {
62     return di2(x, cir.c) < cir.r*cir.r+eps;
63 }
64 inline void p2c(int x, int y)
65 {
66     cir.c.x = (a[x].x+a[y].x)/2;
67     cir.c.y = (a[x].y+a[y].y)/2;
68     cir.r = dis(cir.c, a[x]);
69 }
70 inline void p3c(int i, int j, int k)
71 {
72     couple x = a[i], y = a[j], z = a[k];
73     cir.r = sqrt(di2(x,y)*di2(y,z)*di2(z,x))/fabs(x*y+y*z+z*x)/2;
74     couple t1((x-y).x, (y-z).x), t2((x-y).y, (y-z).y), t3((len(x)-len(y))/2, (len(y)-len(z))/2);
75     cir.c = couple(t3*t2, t1*t3)/(t1*t2);
76 }
77 inline circle mi()
78 {

```



```

20 Point centre[2001];
21 double atan2(const Point & x) {
22     return atan2(x.y, x.x);
23 }
24 Point operator - (const Point & a, const Point & b) {
25     return Point(a.x - b.x, a.y - b.y);
26 }
27 Point operator + (const Point & a, const Point & b) {
28     return Point(a.x + b.x, a.y + b.y);
29 }
30 double operator * (const Point & a, const Point & b) {
31     return a.x * b.y - a.y * b.x;
32 }
33 Point operator * (const double & a, const Point & b) {
34     return Point(a * b.x, a * b.y);
35 }
36 double operator % (const Point & a, const Point & b) {
37     return a.x * b.x + a.y * b.y;
38 }
39 struct circle {
40     double r; Point o;
41     circle() {}
42     void scan() {
43         o.scan();
44         scanf("%lf", &r);
45     }
46 } cir[2001];
47 struct arc {
48     double theta;
49     int delta;
50     Point p;
51     arc() {};
52     arc(const double & theta, const Point & p, int d) : theta(theta), p(p), delta(d)
53         {}
54 } vec[4444];
55 int nV;
56 inline bool operator < (const arc & a, const arc & b) {
57     return a.theta + eps < b.theta;
58 }
59 int cnt;
60 inline void psh(const double t1, const Point p1, const double t2, const Point p2) {
61     if(t2 + eps < t1)
62         cnt++;
63     vec[nV++] = arc(t1, p1, 1);
64     vec[nV++] = arc(t2, p2, -1);
65 }
66 inline double cub(const double & x) {
67     return x * x * x;
68 }

```

```

68 inline void combine(int d, const double & area, const Point & o) {
69     if(sign(area) == 0) return;
70     centre[d] = 1 / (ans[d] + area) * (ans[d] * centre[d] + area * o);
71     ans[d] += area;
72 }
73 bool equal(const double & x, const double & y) {
74     return x + eps > y and y + eps > x;
75 }
76 bool equal(const Point & a, const Point & b) {
77     return equal(a.x, b.x) and equal(a.y, b.y);
78 }
79 bool equal(const circle & a, const circle & b) {
80     return equal(a.o, b.o) and equal(a.r, b.r);
81 }
82 bool f[2001];
83 int main() {
84     //freopen("hdu4895.in", "r", stdin);
85     int n, m, index;
86     while(EOF != scanf("%d%d%d", &m, &n, &index)) {
87         index--;
88         for(int i(0); i < m; i++) {
89             a[i].scan();
90         }
91         for(int i(0); i < n; i++) {
92             cir[i].scan(); //n个圆
93         }
94         for(int i(0); i < n; i++) { //这一段在去重圆 能加速 删掉不会错
95             f[i] = true;
96             for(int j(0); j < n; j++) if(i != j) {
97                 if(equal(cir[i], cir[j]) and i < j or !equal(cir[i], cir[j]) and cir[
                    i].r < cir[j].r + eps and (cir[i].o - cir[j].o).sqrten() < sqr(cir
                    [i].r - cir[j].r) + eps) {
98                     f[i] = false;
99                     break;
100                 }
101             }
102         }
103         int n1(0);
104         for(int i(0); i < n; i++)
105             if(f[i])
106                 cir[n1++] = cir[i];
107         n = n1; //去重圆结束
108         fill(ans, ans + n + 1, 0); //ans[i]表示被圆覆盖至少i次的面积
109         fill(centre, centre + n + 1, Point(0, 0)); //centre[i]表示上面ans[i]部分的重心
110         for(int i(0); i < m; i++)
111             combine(0, a[i] * a[(i + 1) % m] * 0.5, 1. / 3 * (a[i] + a[(i + 1) % m]));
112         for(int i(0); i < n; i++) {
113             dvd = cir[i].o - Point(cir[i].r, 0);

```

```

114         nV = 0;
115         vec[nV++] = arc(-pi, dvd, 1);
116         cnt = 0;
117         for(int j(0); j < n; j++) if(j != i) {
118             double d = (cir[j].o - cir[i].o).sqrln();
119             if(d < sqr(cir[j].r - cir[i].r) + eps) {
120                 if(cir[i].r + i * eps < cir[j].r + j * eps)
121                     psh(-pi, dvd, pi, dvd);
122             } else if(d + eps < sqr(cir[j].r + cir[i].r)) {
123                 double lambda = 0.5 * (1 + (sqr(cir[i].r) - sqr(cir[j].r)) / d);
124                 Point cp(cir[i].o + lambda * (cir[j].o - cir[i].o));
125                 Point nor((cir[j].o - cir[i].o).rev().zoom(sqrt(sqr(cir[i].r) - (
126                     cp - cir[i].o).sqrln())));
127                 Point frm(cp + nor);
128                 Point to(cp - nor);
129                 psh(atan2(frm - cir[i].o), frm, atan2(to - cir[i].o), to);
130             }
131         }
132         sort(vec + 1, vec + nV);
133         vec[nV++] = arc(pi, dvd, -1);
134         for(int j = 0; j + 1 < nV; j++) {
135             cnt += vec[j].delta;
136             //if(cnt == 1) { //如果只算ans[1]和centre[1], 可以加这个if加速.
137                 double theta(vec[j + 1].theta - vec[j].theta);
138                 double area(sqr(cir[i].r) * theta * 0.5);
139                 combine(cnt, area, cir[i].o + 1. / area / 3 * cub(cir[i].r) *
140                     Point(sin(vec[j + 1].theta) - sin(vec[j].theta), cos(vec[j].
141                         theta) - cos(vec[j + 1].theta)));
142                 combine(cnt, -sqr(cir[i].r) * sin(theta) * 0.5, 1. / 3 * (cir[i].
143                     o + vec[j].p + vec[j + 1].p));
144                 combine(cnt, vec[j].p * vec[j + 1].p * 0.5, 1. / 3 * (vec[j].p +
145                     vec[j + 1].p));
146             //}
147         }
148     } //板子部分结束 下面是题目
149     combine(0, -ans[1], centre[1]);
150     for(int i = 0; i < m; i++) {
151         if(i != index)
152             (a[index] - Point((a[i] - a[index]) * (centre[0] - a[index]), (a[i] -
153                 a[index]) % (centre[0] - a[index])).zoom((a[i] - a[index]).len()
154                 ).print();
155         else
156             a[i].print();
157     }
158 }
159 }
160 fclose(stdin);
161 return 0;
162 }

```

3.14 三维跨立实验 + 点到线段的垂足在线段上 + 分数类

```

1 long long gcd(long long a, long long b) {
2     return b?gcd(b, a % b):a;
3 }
4 struct frac {
5     long long x, y;
6     frac() {}
7     frac(const long long & xx, const long long & yy) : x(xx), y(yy) {
8         long long d(gcd(x, y));
9         x /= d; y /= d;
10        if(y < 0)
11            y = -y, x = -x;
12    }
13    void print() const {
14        printf("%lld/%lld\n", x, y);
15    }
16 };
17 frac operator + (const frac & a, const frac & b) {
18     //long long y = a.y / gcd(a.y, b.y) * b.y;
19     //return frac(y / a.y * a.x + y / b.y * b.x, y); //这里可以减小中间结果, 以避免爆
20     //long long.
21     return frac(a.x * b.y + b.x * a.y, a.y * b.y);
22 }
23 frac operator - (const frac & a, const frac & b) {
24     //long long y = a.y / gcd(a.y, b.y) * b.y;
25     //return frac(y / a.y * a.x - y / b.y * b.x, y);
26     return frac(a.x * b.y - b.x * a.y, a.y * b.y);
27 }
28 frac operator * (const frac & a, const frac & b) {
29     //long long v(gcd(a.x, b.y)), w(gcd(a.y, b.x));
30     //return frac((a.x / v) * (b.x / w), (a.y / w) * (b.y / v));
31     return frac(a.x * b.x, a.y * b.y);
32 }
33 frac operator / (const frac & a, const frac & b) {
34     //long long v(gcd(a.x, b.x)), w(gcd(a.y, b.y));
35     //return frac((a.x / v) * (b.y / w), (a.y / w) * (b.x / v));
36     return frac(a.x * b.y, a.y * b.x);
37 }
38 bool operator < (const frac & a, const frac & b) {
39     return a.x * b.y < b.x * a.y;
40 }
41 bool operator == (const frac & a, const frac & b) {
42     return a.x * b.y == b.x * a.y;
43 }
44 bool operator <= (const frac & a, const frac & b) {
45     return a.x * b.y <= b.x * a.y;
46 }

```



```

46
47 frac sqr(const frac & a) {
48     return a * a;
49 }
50 struct Point {
51     frac x, y, z;
52     Point () {}
53     void scan() {cin >> x.x >> y.x >> z.x; x.y = y.y = z.y = 1;}
54     Point(const frac & x, const frac & y, const frac & z) :x(x), y(y), z(z) {}
55     frac sqrlen() {return x * x + y * y + z * z;}
56     void print() const {printf("{");x.print(); y.print(); z.print();printf("}\n");}
57 } a, b, c, d;
58 Point operator - (const Point & a, const Point & b) {
59     return Point(a.x - b.x, a.y - b.y, a.z - b.z);
60 }
61 Point operator + (const Point & a, const Point & b) {
62     return Point(a.x + b.x, a.y + b.y, a.z + b.z);
63 }
64 Point operator * (const frac & a, const Point & b) {
65     return Point(a * b.x, a * b.y, a * b.z);
66 }
67 frac operator % (const Point & a, const Point & b) {
68     return a.x * b.x + a.y * b.y + a.z * b.z;
69 }
70 Point operator * (const Point & a, const Point & b) {
71     return Point(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x)
72     ;
73 }
74 bool _ (const Point & a) {
75     return a.x == frac(0, 1) and a.y == frac(0, 1) and a.z == frac(0, 1);
76 }
77 void check(frac & ans, const Point & a, const Point & s, const Point & t) {
78     if(sign((a - s) % (t - s)) * sign((a - t) % (t - s)) <= 0) {//
79         点到线段的垂足在线段上(端点含)
80         ans = min(ans, ((a - s) * (t - s)).sqrlen() / (t - s).sqrlen());//
81         点到直线距离
82     }
83 }
84 int sign(const frac & a) {
85     return a.x < 0?-1:a.x > 0;
86 }
87 int main() {
88     int tst;
89     scanf("%d", &tst);
90     for(int qq = 1; qq <= tst; qq++) {
91         a.scan(); b.scan();
92         c.scan(); d.scan();//线段(a->b), (c->d)
93         frac ans = (a - c).sqrlen();
94         ans = min(ans, (a - d).sqrlen());
95     }
96 }

```

```

92     ans = min(ans, (b - c).sqrln());
93     ans = min(ans, (b - d).sqrln());
94     Point nor;
95     if(!_ (nor = (b - a) * (d - c)))//线段平行
96         if(sign((c - a) * (d - a) % nor) * sign((c - b) * (d - b) % nor) <= 0 and
            sign((a - c) * (b - c) % nor) * sign((a - d) * (b - d) % nor) <= 0)//
            三维跨立实验
97         ans = min(ans, sqr(nor % (c - a)) / nor.sqrln());
98     check(ans, a, c, d);
99     check(ans, b, c, d);
100    check(ans, c, a, b);
101    check(ans, d, a, b);
102    cout << ans.x << '□' << ans.y << endl;
103 }
104 return 0;
105 }

```

3.15 平面图形的转动惯量计算

```

1  int n, m;
2  double eps = 1e-8;
3  int sign(const double & x) {
4      return x < -eps?-1:x > eps;
5  }
6  struct Point {
7      double x, y;
8      void scan() {
9          scanf("%lf%lf", &x, &y);
10     }
11     void print() {
12         printf("(%f□%f)\n", x, y);
13     }
14     Point(const double & x, const double & y) : x(x), y(y) {}
15     Point() {}
16     double len() {return sqrt(x * x + y * y);}
17     Point rev() {return Point(-y, x);}
18 } a[222], b[222];
19 Point operator + (const Point & a, const Point & b) {
20     return Point(a.x + b.x, a.y + b.y);
21 }
22 Point operator - (const Point & a, const Point & b) {
23     return Point(a.x - b.x, a.y - b.y);
24 }
25 Point operator * (const double & a, const Point & b) {
26     return Point(a * b.x, a * b.y);
27 }
28 double operator % (const Point & a, const Point & b) {

```

```

29     return a.x * b.x + a.y * b.y;
30 }
31 double operator * (const Point & a, const Point & b) {
32     return a.x * b.y - a.y * b.x;
33 }
34 double sqr(const double & x) {
35     return x * x;
36 }
37 double cub(const double & x) {
38     return x * x * x;
39 }
40 double calc(const double & Y, const double & c0, const double & c1, const double & c2
, const double & c3) {
41     return Y * c0 + 0.5 * Y * Y * c1 + Y * Y * Y * c2 / 3 + Y * Y * Y * Y * c3 / 4;
42 }
43 int main() {
44     scanf("%d%d", &n, &m);
45     for(int i = 1; i <= n; i++) {
46         a[i].scan();
47     }
48     a[0] = a[n];
49     double area(0);
50     for(int i = 1; i <= n; i++) {
51         area += (a[i - 1] * a[i]);
52     }
53     for(int i = 1; i <= m; i++) {
54         b[i].scan();
55     }
56     double ans(0);
57     for(int i = 1; i <= m; i++) {
58         vector<Point> vec(a + 1, a + 1 + n);
59         for(int j = 1; j <= m; j++) if(j != i) {
60             vector<Point> vec1;
61             Point mid(0.5 * (b[i] + b[j])), dir((b[j] - b[i]).rev());
62             for(int k = 0; k < (int)vec.size(); k++) {
63                 if(sign((vec[k] - mid) * dir) <= 0)
64                     vec1.push_back(vec[k]);
65                 Point dir1(vec[(k + 1) % (int)vec.size()] - vec[k]);
66                 if(sign((vec[k] - mid) * dir) * sign((vec[(k + 1) % (int)vec.size()]
- mid) * dir) < 0) {
67                     double lambda((mid - vec[k]) * dir / (dir1 * dir));
68                     vec1.push_back(vec[k] + lambda * dir1);
69                 }
70             }
71             vec = vec1;
72         }
73         for(int j = 0; j < (int)vec.size(); j++)
74             vec[j] = vec[j] - b[i];
75         for(int j = 0; j < (int)vec.size(); j++){

```

```

76     double X1(vec[j].len()), X(vec[(j + 1) % (int)vec.size()] % vec[j] / vec[
77         j].len()), Y(vec[j] * vec[(j + 1) % (int)vec.size()] / vec[j].len());
78     //若是vec[j].len()为0 或者Y为0 则转动惯量为0
79     //旋转中心在原点 三角形((0, 0), vec[j], vec[j + 1])的转动惯量, 其中若vec[
80         j] * vec[j + 1] < 0求出来的是转动惯量的相反数.
81     ans += calc(Y, cub(X1) / 3, sqr(X1) * (X - X1) / Y, X1 * sqr((X - X1) / Y
82         ), (cub((X - X1) / Y) - cub(X / Y)) / 3);
83     ans += calc(Y, 0, 0, X1, -X1 / Y);
84 }
85 printf("%.10f\n", ans / area * 2);
86 fclose(stdin);
87 return 0;
88 }

```

3.16 凸多边形内的最大圆 $O(n \log n)$

```

1  double eps(1e-8);
2  int sign(const double & x) {
3      return x < -eps?-1:x > eps;
4  }
5  struct Point {
6      double x, y;
7      Point() {}
8      Point(const double & x, const double & y) : x(x), y(y) {}
9      double sqrlen() const {
10         return x * x + y * y;
11     }
12     double len() const {
13         return sqrt(sqrlen());
14     }
15     void scan() {
16         scanf("%lf%lf", &x, &y);
17     }
18     void print() const {
19         printf("(%.10f, %.10f)\n", x, y);
20     }
21 };
22 Point operator + (const Point & a, const Point & b) {
23     return Point(a.x + b.x, a.y + b.y);
24 }
25 Point operator - (const Point & a, const Point & b) {
26     return Point(a.x - b.x, a.y - b.y);
27 }

```

```

29 }
30 Point operator * (const double & a, const Point & b) {
31     return Point(a * b.x, a * b.y);
32 }
33 double operator * (const Point & a, const Point & b) {
34     return a.x * b.y - a.y * b.x;
35 }
36 struct Line {
37     Point s, d;
38     Line() {
39     }
40     Line(const Point & s, const Point & d) : s(s), d(d) {
41     }
42 };
43 Point crs(const Line & a, const Line & b) {
44     double lambda((b.s - a.s) * b.d / (a.d * b.d));
45     return a.s + lambda * a.d;
46 }
47 struct reca {
48     Point a, b;
49     int prv, nxt;
50     Point d() const {
51         return b - a;
52     }
53     double calc();
54 } a[11111];
55 reca (&c)[11111](a);
56 double reca::calc() {
57     if(sign(d() * c[prv].d()) and sign(d() * c[nxt].d())) {
58         double len1(c[prv].d().len()), len2(d().len()), len3(c[nxt].d().len());
59         Point cp(crs(Line(a, 1 / (len1 + len2) * (len2 * c[prv].a + len1 * b) - a),
60                 Line(b, 1 / (len2 + len3) * (len3 * a + len2 * c[nxt].b) - b)));
61         return fabs((cp - a) * d() / d().len());
62     } else
63         return 1e100;
64 }
65 double val[11111];
66 bool f[11111];
67 int main() {
68     int n;
69     scanf("%d", &n);
70     for(int i(0); i < n; i++) {
71         a[i].a.scan();
72     }
73     for(int i(0); i < n; i++) {
74         a[i].b = a[(i + 1) % n].a;
75         a[i].prv = (i + n - 1) % n;
76         a[i].nxt = (i + 1) % n;

```

```

77     }
78     priority_queue<pair<double, int>, vector<pair<double, int> >, greater<pair<double
    , int> > > hp;
79     for(int i(0); i < n; i++) {
80         hp.push(make_pair(val[i] = a[i].calc(), i));
81     }
82     for(int i(1); i <= n - 3; i++) {
83         int prv(a[hp.top().second].prv), nxt(a[hp.top().second].nxt);
84         a[prv].nxt = nxt;
85         a[nxt].prv = prv;
86         if(sign(a[prv].d() * a[nxt].d()))
87             a[prv].b = a[nxt].a = crs(Line(a[prv].a, a[prv].d()), Line(a[nxt].a, a[
                nxt].d()));
88         f[hp.top().second] = true;
89         hp.pop();
90         hp.push(make_pair(val[prv] = a[prv].calc(), prv));
91         hp.push(make_pair(val[nxt] = a[nxt].calc(), nxt));
92         while(f[hp.top().second] or val[hp.top().second] != hp.top().first)
93             hp.pop();
94     }
95     int y(hp.top().second);
96     printf("%f\n", min(min(val[a[y].prv], val[a[y].nxt]), val[y]));
97 }

```

3.17 三维凸包

```

1  const double eps = 1e-8;
2  int mark[1005][1005];
3  Point info[1005];
4  int n, cnt;
5  double mix(const Point &a, const Point &b, const Point &c) {
6      return a.dot(b.cross(c));
7  }
8  double area(int a, int b, int c) {
9      return ((info[b] - info[a]).cross(info[c] - info[a])).length();
10 }
11 double volume(int a, int b, int c, int d) {
12     return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]);
13 }
14 struct Face {
15     int a, b, c;
16     Face() {}
17     Face(int a, int b, int c): a(a), b(b), c(c) {}
18     int &operator [](int k) { return k==0?a:k==1?b:c; }
19 };
20 vector <Face> face;
21 inline void insert(int a, int b, int c) { face.push_back(Face(a, b, c)); }
22 void add(int v) {
23     vector <Face> tmp;
24     int a, b, c;
25     cnt++;

```

```

23     for (int i = 0; i < SIZE(face); i++) {
24         a = face[i][0]; b = face[i][1]; c = face[i][2];
25         if (Sign(volume(v, a, b, c)) < 0)
26             mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] =
27                 mark[a][c] = cnt;
28         else tmp.push_back(face[i]);
29     }
30     face = tmp;
31     for (int i = 0; i < SIZE(tmp); i++) {
32         a = face[i][0]; b = face[i][1]; c = face[i][2];
33         if (mark[a][b] == cnt) insert(b, a, v);
34         if (mark[b][c] == cnt) insert(c, b, v);
35         if (mark[c][a] == cnt) insert(a, c, v);
36     }
37 }
38 int Find() {
39     for (int i = 2; i < n; i++) {
40         Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
41         if (ndir == Point()) continue;
42         swap(info[i], info[2]);
43         for (int j = i + 1; j < n; j++)
44             if (Sign(volume(0, 1, 2, j)) != 0) {
45                 swap(info[j], info[3]);
46                 insert(0, 1, 2); insert(0, 2, 1);
47                 return 1;
48             }
49     }
50     return 0;
51 }
52 int main() {
53     for (; scanf("%d", &n) == 1; ) {
54         for (int i = 0; i < n; i++)
55             info[i].Input();
56         sort(info, info + n);
57         n = unique(info, info + n) - info;
58         face.clear();
59         random_shuffle(info, info + n);
60         if (Find()) {
61             memset(mark, 0, sizeof(mark));
62             cnt = 0;
63             for (int i = 3; i < n; i++) add(i);
64             vector<Point> Ndir;
65             for (int i = 0; i < SIZE(face); ++i) {
66                 Point p = (info[face[i][0]] - info[face[i][1]]).cross
67                     (info[face[i][2]] - info[face[i][1]]);
68                 p = p / p.length();
69                 Ndir.push_back(p);
70             }
71             sort(Ndir.begin(), Ndir.end());

```

```

72         int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
73         printf("%d\n", ans);
74     } else {
75         printf("1\n");
76     }
77 }
78 }

```

3.18 点在多边形内

```

1 bool in_polygon(const point &p, const vector<point> &poly) {
2     int n = (int)poly.size();
3     int counter = 0;
4     for (int i = 0; i < n; ++i) {
5         point a = poly[i], b = poly[(i + 1) % n];
6         if (point_on_line(p, line(a, b)))
7             return false; // bounded excluded
8         int x = sign(det(p - a, b - a));
9         int y = sign(a.y - p.y);
10        int z = sign(b.y - p.y);
11        if (x > 0 && y <= 0 && z > 0)
12            counter++;
13        if (x < 0 && z <= 0 && y > 0)
14            counter--;
15    }
16    return counter != 0;
17 }

```

3.19 三角形的内心

```

1 point incenter(const point &a, const point &b, const point &c) {
2     double p = (a - b).length() + (b - c).length() + (c - a).length();
3     return (a * (b - c).length() + b * (c - a).length() + c * (a - b).length()) / p;
4 }

```

3.20 三角形的外心

```

1 point circumcenter(const point &a, const point &b, const point &c) {
2     point p = b - a, q = c - a, s(dot(p, p) / 2, dot(q, q) / 2);
3     double d = det(p, q);
4     return a + point(det(s, point(p.y, q.y)), det(point(p.x, q.x), s)) / d;
5 }

```


3.21 三角形的垂心

```

1 point orthocenter(const point &a, const point &b, const point &c) {
2     return a + b + c - circumcenter(a, b, c) * 2.0;
3 }

```

3.22 V 图

```

1 const int AIX = 5;
2 const int MAXM = AIX * MAXN;
3
4 struct point {
5     double x, y;
6     int index;
7     struct Edge *in;
8     point(double _x = 0, double _y = 0) : x(_x), y(_y) {}
9 };
10 inline bool operator< (const point &a, const point &b) {
11     return a.x < b.x || (sgn(a.x - b.x) == 0 && a.y < b.y);
12 }
13 inline double cross(const point &a, const point &b, const point &c) { return det
14     (b - a, c - a); }
15 struct Edge {
16     point *Org, *Dest;
17     Edge *Onext, *Oprev, *Dnext, *Dprev;
18 };
19 inline point* Other(const Edge *e, const point *p) { return e->Org == p ?
20     e->Dest : e->Org; }
21 inline Edge* Next(const Edge *e, const point *p) { return e->Org == p ? e->Onext
22     : e->Dnext; }
23 inline Edge* Prev(const Edge *e, const point *p) { return e->Org == p ? e->Oprev
24     : e->Dprev; }
25 struct gEdge {
26     int u, v;
27     double w;
28     gEdge() {}
29     gEdge(int _u, int _v, double _w) : u(_u), v(_v), w(_w) {}
30 };
31 inline bool operator< (const gEdge &a, const gEdge &b) { return a.w < b.w; }
32 point p[MAXN], *Q[MAXN];
33 Edge mem[AIX * MAXN], *elist[AIX * MAXN];
34 static int nfree;
35 //Alloc memory
36 inline void Alloc_Memory(const int &n) {
37     nfree = AIX * n;
38     Edge *e = mem;
39     for (int i = 0; i < nfree; ++i)

```

```

40     elist[i] = e++;
41 }
42 //Add an edge to a ring of edges
43 inline void Splice(Edge *a, Edge *b, point *v) {
44     Edge *next;
45     if (a->Org == v)
46         next = a->Onext, a->Onext = b;
47     else
48         next = a->Dnext, a->Dnext = b;
49     if (next->Org == v)
50         next->Oprev = b;
51     else
52         next->Dprev = b;
53     if (b->Org == v)
54         b->Onext = next, b->Oprev = a;
55     else
56         b->Dnext = next, b->Dprev = a;
57 }
58 //Initialise a new edge
59 inline Edge *MakeEdge(point *u, point *v) {
60     Edge *e = elist[--nfree];
61     e->Onext = e->Oprev = e->Dnext = e->Dprev = e;
62     e->Org = u, e->Dest = v;
63     if (!u->in)
64         u->in = e;
65     if (!v->in)
66         v->in = e;
67     return e;
68 }
69 //Creates a new edge and adds it to two rings of edges.
70 inline Edge *Join(Edge *a, point *u, Edge *b, point *v, int side) {
71     Edge *e = MakeEdge(u, v);
72     if (side == 1) {
73         if (a->Org == u)
74             Splice(a->Oprev, e, u);
75         else
76             Splice(a->Dprev, e, u);
77         Splice(b, e, v);
78     }
79     else {
80         Splice(a, e, u);
81         if (b->Org == v)
82             Splice(b->Oprev, e, v);
83         else
84             Splice(b->Dprev, e, v);
85     }
86     return e;
87 }
88 //Remove an edge

```

```

89 inline void Remove(Edge *e) {
90     point *u = e->Org, *v = e->Dest;
91     if (u->in == e)
92         u->in = e->Onext;
93     if (v->in == e)
94         v->in = e->Dnext;
95     if (e->Onext->Org == u)
96         e->Onext->Oprev = e->Oprev;
97     else
98         e->Onext->Dprev = e->Oprev;
99     if (e->Oprev->Org == u)
100         e->Oprev->Onext = e->Onext;
101     else
102         e->Oprev->Dnext = e->Onext;
103     if (e->Dnext->Org == v)
104         e->Dnext->Oprev = e->Dprev;
105     else
106         e->Dnext->Dprev = e->Dprev;
107     if (e->Dprev->Org == v)
108         e->Dprev->Onext = e->Dnext;
109     else
110         e->Dprev->Dnext = e->Dnext;
111     elist[nfree++] = e;
112 }
113 //Determines the lower tangent of two triangulations
114 inline void Low_tangent(Edge *e_l, point *o_l, Edge *e_r, point *o_r, Edge
115     **l_low, point **OL, Edge **r_low, point **OR) {
116     point *d_l = Other(e_l, o_l), *d_r = Other(e_r, o_r);
117     while (true) {
118         if (cross(*o_l, *o_r, *d_l) < -EPS) {
119             e_l = Prev(e_l, d_l);
120             o_l = d_l;
121             d_l = Other(e_l, o_l);
122         }
123         else if (cross(*o_l, *o_r, *d_r) < -EPS) {
124             e_r = Next(e_r, d_r);
125             o_r = d_r;
126             d_r = Other(e_r, o_r);
127         }
128         else
129             break;
130     }
131     *OL = o_l, *OR = o_r;
132     *l_low = e_l, *r_low = e_r;
133 }
134 inline void Merge(Edge *lr, point *s, Edge *rl, point *u, Edge **tangent) {
135     double cot_L, cot_R, N1, cot_N, P1, cot_P;
136     point l1, l2, r1, r2, uu, vv;
137     point *O, *D, *OR, *OL;

```

```

138 Edge *B, *L, *R;
139 Low_tangent(lr, s, r1, u, &L, &OL, &R, &OR);
140 *tangent = B = Join(L, OL, R, OR, 0);
141 O = OL, D = OR;
142 do {
143     Edge *El = Next(B, O), *Er = Prev(B, D), *next, *prev;
144     point *l = Other(El, O), *r = Other(Er, D);
145     l1 = *O - *l, l2 = *D - *l, r1 = *O - *r, r2 = *D - *r;
146     double cl = det(l1, l2), cr = det(r1, r2);
147     bool BL = cl > EPS, BR = cr > EPS;
148     if (!BL && !BR)
149         break;
150     if (BL) {
151         double dl = dot(l1, l2);
152         cot_L = dl / cl;
153         do {
154             next = Next(El, O);
155             uu = *O - *Other(next, O);
156             vv = *D - *Other(next, O);
157             N1 = det(uu, vv);
158             if (!(N1 > EPS))
159                 break;
160             cot_N = dot(uu, vv) / N1;
161             if (cot_N > cot_L)
162                 break;
163             Remove(El);
164             El = next;
165             cot_L = cot_N;
166         }
167         while (true);
168     }
169     if (BR) {
170         double dr = dot(r1, r2);
171         cot_R = dr / cr;
172         do {
173             prev = Prev(Er, D);
174             uu = *O - *Other(prev, D);
175             vv = *D - *Other(prev, D);
176             P1 = det(uu, vv);
177             if !(P1 > EPS)
178                 break;
179             cot_P = dot(uu, vv) / P1;
180             if (cot_P > cot_R)
181                 break;
182             Remove(Er);
183             Er = prev;
184             cot_R = cot_P;
185         }
186         while (true);

```

```

187     }
188     l = Other(E1, O); r = Other(Er, D);
189     if (!BL || (BL && BR && cot_R < cot_L)) {
190         B = Join(B, O, Er, r, 0);
191         D = r;
192     }
193     else {
194         B = Join(E1, l, B, D, 0);
195         O = l;
196     }
197 }
198 while (true);
199 }
200 inline void Divide(int s, int t, Edge **L, Edge **R) {
201     Edge *a, *b, *c, *ll, *lr, *rl, *rr, *tangent;
202     int n = t - s + 1;
203     if (n == 2)
204         *L = *R = MakeEdge(Q[s], Q[t]);
205     else if (n == 3) {
206         a = MakeEdge(Q[s], Q[s + 1]);
207         b = MakeEdge(Q[s + 1], Q[t]);
208         Splice(a, b, Q[s + 1]);
209         double v = cross(*Q[s], *Q[s + 1], *Q[t]);
210         if (v > EPS) {
211             c = Join(a, Q[s], b, Q[t], 0);
212             *L = a, *R = b;
213         }
214         else if (v < -EPS) {
215             c = Join(a, Q[s], b, Q[t], 1);
216             *L = c, *R = c;
217         }
218         else
219             *L = a, *R = b;
220     }
221     else if (n > 3) {
222         int split = (s + t) / 2;
223         Divide(s, split, &ll, &lr);
224         Divide(split + 1, t, &rl, &rr);
225         Merge(lr, Q[split], rl, Q[split + 1], &tangent);
226         if (tangent->Org == Q[s])
227             ll = tangent;
228         if (tangent->Dest == Q[t])
229             rr = tangent;
230         *L = ll; *R = rr;
231     }
232 }
233 int task, n, m, k, root[MAXN];
234 gEdge E[MAXM], MST[MAXN];
235 inline int Make_Graph() {

```

```

236     Edge *start, *e;
237     int M = 0;
238     point *u, *v;
239     for(int i = 0; i < n; ++i) {
240         u = p + i;
241         start = e = u->in;
242         do {
243             v = Other(e, u);
244             if (u < v)
245                 E[M++] = gEdge(u - p + 1, v - p + 1, dis(*u, *v));
246             e = Next(e, u);
247         }
248         while(e != start);
249     }
250     return M;
251 }
252 int find_root(const int &x) { return root[x] ? root[x] = find_root(root[x]) : x;
253     }
254 inline bool merge(const int &x, const int &y) {
255     int p = find_root(x), q = find_root(y);
256     if (p != q) {
257         root[p] = q;
258         return true;
259     }
260     else
261         return false;
262 }
263 inline void kruskal(gEdge *E, int m, int n, gEdge* MST) {
264     for (int i = 1; i <= n; ++i)
265         root[i] = 0;
266     sort(E, E + m);
267     int tot = 0;
268     for (int i = 0; i < m; ++i)
269         if (merge(E[i].u, E[i].v))
270             MST[tot++] = E[i];
271 }
272 inline void MinimumEuclideanSpanningTree(point* p, int n, gEdge* MST) {
273     Alloc_Memory(n);
274     sort(p, p + n);
275     for (int i = 0; i < n; ++i)
276         Q[i] = p + i;
277     Edge *L, *R;
278     Divide(0, n - 1, &L, &R);
279     m = Make_Graph();
280     kruskal(E, m, n, MST);
281 }
282 int main() {
283     for (scanf("%d", &task); task--; ) {
284         scanf("%d", &k);

```

```
285     for (n = 0; scanf("%lf", &p[n].x) == 1 && p[n].x != -1; ++n) {
286         scanf("%lf", &p[n].y);
287         p[n].in = NULL;
288         p[n].index = n;
289     }
290     if (n == 1) {
291         printf("0\n");
292         continue;
293     }
294     MinimumEuclideanSpaningTree(p, n, MST);
295     printf("%d\n", int(ceil(k > n ? 0 : MST[n - k - 1].w) + EPS));
296 }
297 }
```


Chapter 4

数据结构

4.1 KD 树

```
1
2 曼哈顿距离版，欧几里得只需要把sqr改成x*x即可。
3 tested on bzoj 2648, 2626
4
5 namespace k_dimensional_tree {
6     int const N = ;
7
8     struct point {
9         int x, y, id;
10    };
11
12    inline long long sqr(const long long &x) {
13        return abs(x);
14    }
15
16    inline long long dist(const point &a, const point &b) {
17        return sqr(a.x - b.x) + sqr(a.y - b.y);
18    }
19
20    struct rectangle {
21        int lx, rx, ly, ry;
22        inline void set(const point &p) {
23            lx = rx = p.x;
24            ly = ry = p.y;
25        }
26        inline void mergy(const point &p) {
27            lx = min(lx, p.x);
28            rx = max(rx, p.x);
29            ly = min(ly, p.y);
30            ry = max(ry, p.y);
31        }
32    }
```

```

32     inline void mergy(const rectangle &r) {
33         lx = min(lx, r.lx);
34         rx = max(rx, r.rx);
35         ly = min(ly, r.ly);
36         ry = max(ry, r.ry);
37     }
38     /* minimum distance */
39     inline long long dist(const point &p) {
40         if (p.x <= lx && p.y <= ly) {
41             return sqr(p.x - lx) + sqr(p.y - ly);
42         }
43         if (p.x <= rx && p.y <= ly) {
44             return sqr(p.y - ly);
45         }
46         if (p.x >= rx && p.y <= ly) {
47             return sqr(p.x - rx) + sqr(p.y - ly);
48         }
49         if (p.x >= rx && p.y <= ry) {
50             return sqr(p.x - rx);
51         }
52         if (p.x >= rx && p.y >= ry) {
53             return sqr(p.x - rx) + sqr(p.y - ry);
54         }
55         if (p.x >= lx && p.y >= ry) {
56             return sqr(p.y - ry);
57         }
58         if (p.x <= lx && p.y >= ry) {
59             return sqr(p.x - lx) + sqr(p.y - ry);
60         }
61         if (p.x <= lx && p.y >= ly) {
62             return sqr(p.x - lx);
63         }
64         return 0;
65     }
66     /* maximum distance */
67     inline long long dist(const point &p) {
68         long long ret = 0;
69         ret += max(sqr(rx - p.x), sqr(lx - p.x));
70         ret += max(sqr(ry - p.y), sqr(ly - p.y));
71         return ret;
72     }
73 };
74
75 struct node {
76     int child[2];
77     point p;
78     rectangle r;
79     inline void set(const point &_p) {
80         p = _p;

```

```

81         r.set(p);
82         child[0] = child[1] = 0;
83     }
84 };
85
86 int size;
87 point a[N];
88 node tree[N];
89
90 inline bool xcompare(const point &a, const point &b) {
91     return a.x < b.x || a.x == b.x && a.y < b.y;
92 }
93
94 inline bool ycompare(const point &a, const point &b) {
95     return a.y < b.y || a.y == b.y && a.x < b.x;
96 }
97
98 inline int build(int left, int right, bool dim = 0) {
99     int x = ++size, mid = left + right >> 1;
100     nth_element(a + left, a + mid, a + right, dim ? xcompare : ycompare);
101     tree[x].set(a[mid]);
102     if (left < mid) {
103         tree[x].child[0] = build(left, mid, dim ^ 1);
104         tree[x].r.mergy(tree[tree[x].child[0]].r);
105     }
106     if (mid + 1 < right) {
107         tree[x].child[1] = build(mid + 1, right, dim ^ 1);
108         tree[x].r.mergy(tree[tree[x].child[1]].r);
109     }
110     return x;
111 }
112
113 inline int insert(int x, const point &p, bool dim = 0) {
114     if (x == 0) {
115         tree[++size].set(p);
116         return size;
117     }
118     tree[x].r.mergy(p);
119     if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
120         tree[x].child[0] = insert(tree[x].child[0], p, dim ^ 1);
121     } else {
122         tree[x].child[1] = insert(tree[x].child[1], p, dim ^ 1);
123     }
124     return x;
125 }
126
127 /* query minimum */
128 inline void query(int x, const point &p, long long &ret, bool dim = 0) {
129     if (tree[x].r.dist(p) >= ret) {

```

```

130         return;
131     }
132     ret = min(ret, dist(tree[x].p, p));
133     if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
134         if (tree[x].child[0]) {
135             query(tree[x].child[0], p, ret, dim ^ 1);
136         }
137         if (tree[x].child[1]) {
138             query(tree[x].child[1], p, ret, dim ^ 1);
139         }
140     } else {
141         if (tree[x].child[1]) {
142             query(tree[x].child[1], p, ret, dim ^ 1);
143         }
144         if (tree[x].child[0]) {
145             query(tree[x].child[0], p, ret, dim ^ 1);
146         }
147     }
148 }
149
150 /* query maximum */
151 inline void query(int x, const point &p, long long &ret, bool dim = 0) {
152     if (tree[x].r.dist(p) <= ret) {
153         return;
154     }
155     ret = max(ret, dist(tree[x].p, p));
156     if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
157         if (tree[x].child[1]) {
158             query(tree[x].child[1], p, ret, dim ^ 1);
159         }
160         if (tree[x].child[0]) {
161             query(tree[x].child[0], p, ret, dim ^ 1);
162         }
163     } else {
164         if (tree[x].child[0]) {
165             query(tree[x].child[0], p, ret, dim ^ 1);
166         }
167         if (tree[x].child[1]) {
168             query(tree[x].child[1], p, ret, dim ^ 1);
169         }
170     }
171 }
172
173 /* query kth-minimum */
174 inline void query(int x, const point &p, int k, pair<long long, int> ret[], bool
175     dim = 0) {
176     if (tree[x].r.dist(p) > ret[k].first) {
177         return;
178     }

```

```

178     pair<long long, int> val = make_pair(dist(tree[x].p, p), tree[x].p.id);
179     for (int i = 1; i <= k; ++i) {
180         if (val < ret[i]) {
181             for (int j = k + 1; j > i; --j) {
182                 ret[j] = ret[j - 1];
183             }
184             ret[i] = val;
185             break;
186         }
187     }
188     if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
189         if (tree[x].child[0]) {
190             query(tree[x].child[0], p, k, ret, dim ^ 1);
191         }
192         if (tree[x].child[1]) {
193             query(tree[x].child[1], p, k, ret, dim ^ 1);
194         }
195     } else {
196         if (tree[x].child[1]) {
197             query(tree[x].child[1], p, k, ret, dim ^ 1);
198         }
199         if (tree[x].child[0]) {
200             query(tree[x].child[0], p, k, ret, dim ^ 1);
201         }
202     }
203 }
204
205 /* query kth-maximum */
206 inline void query(int x, const point &p, int k, pair<long long, int> ret[], bool
207     dim = 0) {
208     if (tree[x].r.dist(p) < ret[k].first) {
209         return;
210     }
211     pair<long long, int> val = make_pair(dist(tree[x].p, p), -tree[x].p.id);
212     for (int i = 1; i <= k; ++i) {
213         if (val > ret[i]) {
214             for (int j = k + 1; j > i; --j) {
215                 ret[j] = ret[j - 1];
216             }
217             ret[i] = val;
218             break;
219         }
220     }
221     if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
222         if (tree[x].child[1]) {
223             query(tree[x].child[1], p, k, ret, dim ^ 1);
224         }
225         if (tree[x].child[0]) {
226             query(tree[x].child[0], p, k, ret, dim ^ 1);
227         }
228     }
229 }

```

```

226     }
227   } else {
228     if (tree[x].child[0]) {
229       query(tree[x].child[0], p, k, ret, dim ^ 1);
230     }
231     if (tree[x].child[1]) {
232       query(tree[x].child[1], p, k, ret, dim ^ 1);
233     }
234   }
235 }
236
237 inline void clear() {
238     size = 0;
239 }
240 }

```

4.2 树链剖分

```

1 namespace heavy_light_decomposition {
2     int const N = ;
3
4     int n;
5     vector<int> adj[N];
6     int father[N], height[N], size[N], son[N], top[N], idx[N], num[N];
7
8     inline void prepare() {
9         vector<int> queue;
10        queue.push_back(1);
11        father[1] = height[1] = 0;
12        for (int head = 0; head < (int)queue.size(); ++head) {
13            int x = queue[head];
14            for (int i = 0; i < (int)adj[x].size(); ++i) {
15                int y = adj[x][i];
16                if (y != father[x]) {
17                    queue.push_back(y);
18                    height[y] = height[x] + 1;
19                    father[y] = x;
20                }
21            }
22        }
23        for (int i = n - 1; i >= 0; --i) {
24            int x = queue[i];
25            size[x] = 1;
26            son[x] = -1;
27            for (int j = 0; j < (int)adj[x].size(); ++j) {
28                int y = adj[x][j];
29                if (y != father[x]) {
30                    size[x] += size[y];

```

```

31         if (son[x] == -1 || size[son[x]] < size[y]) {
32             son[x] = y;
33         }
34     }
35 }
36 }
37 int tot = 0;
38 fill(top + 1, top + n + 1, 0);
39 for (int i = 0; i < n; ++i) {
40     int x = queue[i];
41     if (top[x] == 0) {
42         for (int y = x; y != -1; y = son[y]) {
43             top[y] = x;
44             idx[y] = ++tot;
45             num[tot] = //data[y];
46         }
47     }
48 }
49 build(1, 1, n);
50 }
51
52 inline void handle(int x, int y) {
53     for (; true; ) {
54         if (top[x] == top[y]) {
55             if (x == y) {
56                 handle(1, 1, n, idx[x], idx[x]);
57             } else {
58                 if (height[x] < height[y]) {
59                     handle(1, 1, n, idx[x], idx[y]);
60                 } else {
61                     handle(1, 1, n, idx[y], idx[x]);
62                 }
63             }
64             break;
65         }
66         if (height[top[x]] > height[top[y]]) {
67             handle(1, 1, n, idx[top[x]], idx[x]);
68             x = father[top[x]];
69         } else {
70             handle(1, 1, n, idx[top[y]], idx[y]);
71             y = father[top[y]];
72         }
73     }
74 }
75 }

```

4.3 可持久化左偏树

```

1 Node * persiMerge(Node * a, Node * b) {
2     if(!a) return b;
3     if(!b) return a;
4     Node * res;
5     if(a->v < b->v) {
6         res = new Node(*a);
7         res->s[1] = persiMerge(b, res->s[1]);
8     }else {
9         res = new Node(*b);
10        res->s[1] = persiMerge(a, res->s[1]);
11    }
12    if(!res->s[0] or res->s[1] and res->s[0]->l < res->s[1]->l)
13        swap(res->s[0], res->s[1]);
14    res->l = res->s[1]?res->s[1]->l + 1:0;
15    return res;
16 }

```

4.4 treap

```

1 namespace treap {
2     struct node {
3         node *left, *right;
4         int key;
5         int size, count, aux;
6         inline node(int _aux) {
7             left = right = 0;
8             key = size = count = 0;
9             aux = _aux;
10        }
11        inline void update() {
12            this->size = this->left->size + this->count + this->right->size;
13        }
14    };
15
16    node *null;
17
18    inline void print(node *&x) {
19        if (x == null) {
20            return;
21        }
22        print(x->left);
23        printf("%d_", x->key);
24        print(x->right);
25    }
26
27    inline node* create(int key) {
28        node *x = new node(rand() % INT_MAX);
29        x->key = key;

```



```

30     x->count = x->size = 1;
31     x->left = x->right = null;
32     return x;
33 }
34
35 inline void left_rotate(node *&x) {
36     node *y = x->right;
37     x->right = y->left;
38     y->left = x;
39     x->update();
40     y->update();
41     x = y;
42 }
43
44 inline void right_rotate(node *&x) {
45     node *y = x->left;
46     x->left = y->right;
47     y->right = x;
48     x->update();
49     y->update();
50     x = y;
51 }
52
53 inline void insert(node *&x, int key) {
54     if (x == null) {
55         x = create(key);
56         return;
57     }
58     if (x->key == key) {
59         x->count++;
60     } else if (x->key > key) {
61         insert(x->left, key);
62         if (x->left->aux < x->aux) {
63             right_rotate(x);
64         }
65     } else {
66         insert(x->right, key);
67         if (x->right->aux < x->aux) {
68             left_rotate(x);
69         }
70     }
71     x->update();
72 }
73
74 inline void erase(node *&x, int key) {
75     if (x == null) {
76         return;
77     }
78     if (x->key == key) {

```

```

79         if (x->count > 1) {
80             x->count--;
81         } else if (x->left == null && x->right == null) {
82             delete(x);
83             x = null;
84             return;
85         } else if (x->left->aux < x->right->aux) {
86             right_rotate(x);
87             erase(x->right, key);
88         } else {
89             left_rotate(x);
90             erase(x->left, key);
91         }
92     } else if (x->key > key) {
93         erase(x->left, key);
94     } else {
95         erase(x->right, key);
96     }
97     x->update();
98 }
99
100 inline void prepare() {
101     null = new node(INT_MAX);
102 }
103 }

```

4.5 functional_treap

```

1 namespace functional_treap {
2     struct node {
3         int size;
4         node *left, *right;
5         inline node(node *_left, node *_right) {
6             left = _left;
7             right = _right;
8         }
9         inline node* update() {
10             size = left->size + 1 + right->size;
11             return this;
12         }
13         inline pair<node*, node*> split(int);
14     };
15
16     node* null;
17
18     inline bool random(int x, int y) {
19         return rand() % (x + y) < x;
20     }

```

```

21
22     inline node* mergy(node* x, node* y) {
23         if (x == null) {
24             return y;
25         }
26         if (y == null) {
27             return x;
28         }
29         if (random(x->size, y->size)) {
30             x->right = mergy(x->right, y);
31             return x->update();
32         }
33         y->left = mergy(x, y->left);
34         return y->update();
35     }
36
37     inline pair<node*, node*> node::split(int n) {
38         if (this == null) {
39             return make_pair(null, null);
40         }
41         if (n <= left->size) {
42             pair<node*, node*> ret = left->split(n);
43             left = null;
44             return make_pair(ret.first, mergy(ret.second, this->update()));
45         }
46         pair<node*, node*> ret = right->split(n - left->size);
47         right = null;
48         return make_pair(mergy(this->update(), ret.first), ret.second);
49     }
50
51     inline void prepare() {
52         null = new node(null, null);
53         null->left = null->right = null;
54     }
55 }

```

4.6 LCT

```

1  namespace link_cut_tree {
2      struct node {
3          node *child[2], *father;
4          bool head, rev;
5          int val, sum, size;
6          inline node() {
7              head = rev = val = sum = size = 0;
8          }
9          inline void set(node *temp, int dir) {
10             child[dir] = temp;

```

```

11         temp->father = this;
12     }
13     inline int which() {
14         return father->child[1] == this;
15     }
16     inline void update() {
17         sum = val + child[0]->sum + child[1]->sum;
18         size = 1 + child[0]->size + child[1]->size;
19     }
20     inline void release() {
21         if (rev) {
22             child[0]->reverse();
23             child[1]->reverse();
24             rev = 0;
25         }
26     }
27     inline void reverse() {
28         if (size == 0) {
29             return;
30         }
31         rev ^= 1;
32         swap(child[0], child[1]);
33     }
34 };
35
36 node *null, *tree[N];
37
38 inline node* create(int val) {
39     node *temp = new node();
40     temp->val = temp->sum = val;
41     temp->size = 1;
42     temp->child[0] = temp->child[1] = temp->father = null;
43     temp->head = true;
44     return temp;
45 }
46
47 inline void rotate(node *root) {
48     node *father = root->father;
49     father->release();
50     root->release();
51     int dir = root->which();
52     father->set(root->child[!dir], dir);
53     if (father->head) {
54         father->head = false;
55         root->head = true;
56         root->father = father->father;
57     } else {
58         father->father->set(root, father->which());
59     }

```

```

60     root->set(father, !dir);
61     father->update();
62 }
63
64 inline void splay(node *root) {
65     for (root->release(); !root->head; ) {
66         if (root->father->head) {
67             rotate(root);
68         } else {
69             root->which() == root->father->which() ? (rotate(root->father),
70                 rotate(root)) : (rotate(root), rotate(root));
71         }
72     }
73     root->update();
74 }
75
76 inline void access(node *root) {
77     for (node *temp = null; root != null; temp = root, root = root->father) {
78         splay(root);
79         root->child[1]->head = true;
80         root->child[1] = temp;
81         root->child[1]->head = false;
82         root->update();
83     }
84 }
85
86 inline void link(int son, int father) {
87     access(tree[son]);
88     splay(tree[son]);
89     tree[son]->father = tree[father];
90     tree[son]->reverse();
91 }
92
93 inline void cut(int x, int y) {
94     access(tree[y]);
95     splay(tree[x]);
96     if (tree[x]->father == tree[y]) {
97         tree[x]->father = null;
98     } else {
99         access(tree[x]);
100        splay(tree[y]);
101        if (tree[y]->father == tree[x]) {
102            tree[y]->father = null;
103        }
104    }
105 }
106
107 inline void handle(int x, int y) {
108     access(tree[x]);

```

```

108     node *root = tree[y];
109     for (node *temp = null; root != null; temp = root, root = root->father) {
110         splay(root);
111         if (root->father == null) {
112             }
113             root->child[1]->head = true;
114             root->child[1] = temp;
115             root->child[1]->head = false;
116             root->update();
117         }
118     }
119 }
120
121 inline void init(int n, int val[]) {
122     for (int i = 1; i <= n; ++i) {
123         tree[i] = create(val[i]);
124     }
125 }
126
127 inline void prepare() {
128     null = new node();
129     null->child[0] = null->child[1] = null->father = null;
130 }
131 }

```

4.7 Splay

```

1 namespace splay {
2     struct node {
3         node *child[2], *father;
4         int val, sum, size;
5         inline node() {
6             val = sum = size = 0;
7         }
8         inline int which() {
9             return father->child[1] == this;
10        }
11        inline void set(node *temp, int dir) {
12            child[dir] = temp;
13            temp->father = this;
14        }
15        inline void update() {
16            sum = val + child[0]->sum + child[1]->sum;
17            size = 1 + child[0]->size + child[1]->size;
18        }
19        inline void release() {
20        }
21    }

```

```

22     };
23
24     node *null, *head;
25
26     inline void print(node *root) {
27         if (root == null) {
28             return;
29         }
30         print(root->child[0]);
31         printf("%d_", root->val);
32         print(root->child[1]);
33     }
34
35     inline node* create(int val = 0) {
36         node *temp = new node();
37         temp->val = val;
38         temp->child[0] = temp->child[1] = temp->father = null;
39         return temp;
40     }
41
42     inline void rotate(node *root) {
43         node *father = root->father;
44         int dir = root->which();
45         father->release();
46         root->release();
47         father->set(root->child[!dir], dir);
48         father->father->set(root, father->which());
49         root->set(father, !dir);
50         if (father == head) {
51             head = root;
52         }
53         father->update();
54     }
55
56     inline void splay(node *root, node *target) {
57         for (root->release(); root->father != target; ) {
58             if (root->father->father == target) {
59                 rotate(root);
60             } else {
61                 root->which() == root->father->which() ? (rotate(root->father),
62                                                         rotate(root)) : (rotate(root), rotate(root));
63             }
64             root->update();
65         }
66
67         inline int rank(node *root) {
68             splay(root, null);
69             return root->child[0]->size + 1;

```

```

70     }
71
72     inline node* find(int rank) {
73         node *now = head;
74         for (; now->child[0]->size + 1 != rank; ) {
75             now->release();
76             if (now->child[0]->size + 1 > rank) {
77                 now = now->child[0];
78             } else {
79                 rank -= now->child[0]->size + 1;
80                 now = now->child[1];
81             }
82         }
83         return now;
84     }
85
86     inline void splay(int left, int right) {
87         splay(find(right), null);
88         splay(find(left), head);
89     }
90
91     inline node* insert(int pos, int val) {
92         splay(pos, pos + 1);
93         node *now = head->child[0];
94         node *cur = create(val);
95         now->set(cur, 1);
96         splay(cur, null);
97         return head;
98     }
99
100    inline void insert(int pos, int n, int val[]) {
101        splay(pos, pos + 1);
102        node *now = head->child[0];
103        for (int i = 1; i <= n; ++i) {
104            node *cur = create(val[i]);
105            now->set(cur, 1);
106            now = cur;
107        }
108        splay(now, null);
109    }
110
111    inline void erase(node *root) {
112        int pos = rank(root);
113        splay(pos - 1, pos + 1);
114        head->child[0]->child[1] = null;
115        head->child[0]->update();
116        head->update();
117    }
118

```



```
119     inline int query(int left, int right) {
120         splay(left - 1, right + 1);
121         return head->child[0]->child[1]->sum;
122     }
123
124     inline void prepare() {
125         null = new node();
126         head = create();
127         node *tail = create();
128         head->set(tail, 1);
129         splay(tail, null);
130     }
131 }
```


Chapter 5

图论

5.1 Gabow 算法求点双连通分量 (非递归)

边 (u, v) 属于 $\min(\text{color}[u], \text{color}[v])$ 这个点双连通分量.

```
1  int color[222222], siz[222222], cnt[222222];
2  long long ans[222222];
3  vector<int> edges[222222];
4  vector<pair<int, int> > st0, st2;
5  vector<int> st1;
6  void psh(int v) {
7      st0.push_back(make_pair(v, 0));
8      color[v] = st1.size();
9      st1.push_back(v);
10 }
11 int main() {
12     freopen("travel.in", "r", stdin);
13     freopen("travel.out", "w", stdout);
14     int n, m;
15     scanf("%d%d", &n, &m);
16     for(int i(1); i <= m; i++) {
17         int x, y;
18         scanf("%d%d", &x, &y);
19         edges[x].push_back(y);
20         edges[y].push_back(x);
21     }
22     int c(n);
23     fill(color + 1, color + 1 + n, 0);
24     fill(ans + 1, ans + 1 + n, 0);
25     fill(cnt + 1, cnt + 1 + n, 0);
26     fill(siz + 1, siz + 1 + n, 0);
27     for(int i(1); i <= n; i++) if(!color[i]) {
28         psh(i);
29         while(!st0.empty()) {
30
```

```

31     int v(st0.back().first), p(st0.back().second++);
32     if(p != (int)edges[v].size()) {
33         int y(edges[v][p]);
34         if(!color[y]) {
35             psh(y);
36             st2.push_back(make_pair(color[v], color[y]));
37         }else
38             while(!st2.empty() and st2.back().first > color[y])
39                 st2.pop_back();
40     }else {
41         st0.pop_back();
42         siz[v]++;
43         if(color[v] == 1)
44             color[v] = c;
45         else {
46             int fa(st0.back().first);
47             if(st2.back().second == color[v]) {
48                 st2.pop_back();
49                 color[v] = ++c;
50                 while(st1.back() != v) {
51                     color[st1.back()] = c;
52                     st1.pop_back();
53                 }
54                 st1.pop_back();
55                 ans[fa] += (long long)cnt[fa] * siz[v];
56                 cnt[fa] += siz[v];
57             }
58             siz[fa] += siz[v];
59         }
60         ans[v] += (long long)(n - cnt[v]) * cnt[v] + n - cnt[v] - 1;
61     }
62 }
63 }
64 for(int i(1); i <= n; i++) {
65     cout << ans[i] << endl; //ans[i]: 删去点 i 后, 无法连通的 {a, b} 数, 其中 a, b
66                             //为图中不同节点且无序.
67 }
68 fclose(stdin);
69 fclose(stdout);
70 return 0;
71 }

```

5.2 Hopcroft Karp 求二分图最大匹配 $O(EV^{0.5})$

```

1 // hint :: 全部都是 0base
2 // 用的时候, 建好边, 左边 n 个点, 右边 m 个点, 直接调用 maxMatch 即可
3

```

```
4  const int N = 3333;
5
6  vector<int> e[N];
7  int pairx[N], pairy[N], level[N];
8  int n, m;
9
10 bool dfs(int x) {
11     for(int i = 0; i < (int)e[x].size(); i++) {
12         int y = e[x][i];
13         int w = pairy[y];
14         if (w == -1 || level[x] + 1 == level[w] && dfs(w)) {
15             pairx[x] = y;
16             pairy[y] = x;
17             return true;
18         }
19     }
20     level[x] = -1;
21     return false;
22 }
23
24 int maxMatch() {
25     fill(pairx, pairx + n, -1);
26     fill(pairy, pairy + m, -1);
27
28     for(int answer = 0; ; ) {
29         vector<int> queue;
30         for(int i = 0; i < n; i++) {
31             if (pairx[i] == -1) {
32                 level[i] = 0;
33                 queue.push_back(i);
34             } else {
35                 level[i] = -1;
36             }
37         }
38
39         for(int head = 0; head < (int)queue.size(); head++) {
40             int x = queue[head];
41             for(int i = 0; i < (int)e[x].size(); i++) {
42                 int y = e[x][i];
43                 int w = pairy[y];
44                 if (w != -1 && level[w] < 0) {
45                     level[w] = level[x] + 1;
46                     queue.push_back(w);
47                 }
48             }
49         }
50
51         int delta = 0;
52         for(int i = 0; i < n; i++) {
```

```

53         if (pairx[i] == -1 && dfs(i)) {
54             delta++;
55         }
56     }
57     if (delta == 0) {
58         return answer;
59     } else {
60         answer += delta;
61     }
62 }
63 }
64
65 int solve() {
66     int timing;
67     scanf("%d", &timing);
68
69     static int x[N], y[N], s[N];
70     scanf("%d", &n);
71     for(int i = 0; i < n; i++) {
72         scanf("%d_%d_%d", &x[i], &y[i], &s[i]);
73         e[i].clear();
74     }
75
76     scanf("%d", &m);
77     for(int i = 0; i < m; i++) {
78         int xx, yy;
79         scanf("%d_%d", &xx, &yy);
80         for(int j = 0; j < n; j++) {
81             if (timing * timing * s[j] * s[j] >= (xx - x[j]) * (xx - x[j]) + (yy - y[
82                 j]) * (yy - y[j])) {
83                 e[j].push_back(i);
84             }
85         }
86     }
87     return maxMatch();
88 }
89
90 int main() {
91     freopen("input.txt", "r", stdin);
92     int test;
93     scanf("%d", &test);
94     while(test--) {
95         static int testCount = 0;
96         printf("Scenario_%d:\n", ++testCount);
97         printf("%d\n", solve());
98         puts("");
99     }
100     return 0;

```

101 }

5.3 最小树形图

```

1  const int maxn=1100;
2
3  int n,m , g[maxn][maxn] , used[maxn] , pass[maxn] , eg[maxn] , more , queue[maxn];
4
5  void combine (int id , int &sum ) {
6      int tot = 0 , from , i , j , k ;
7      for ( ; id!=0 && !pass[ id ] ; id=eg[id] ) {
8          queue[tot++]=id ; pass[id]=1;
9      }
10     for ( from=0; from<tot && queue[from]!=id ; from++);
11     if ( from==tot ) return ;
12     more = 1 ;
13     for ( i=from ; i<tot ; i++) {
14         sum+=g[eg[queue[i]]][queue[i]] ;
15         if ( i!=from ) {
16             used[queue[i]]=1;
17             for ( j = 1 ; j <= n ; j++) if ( !used[j] )
18                 if ( g[queue[i]][j]<g[id][j] ) g[id][j]=g[queue[i]][j] ;
19         }
20     }
21     for ( i=1; i<=n ; i++) if ( !used[i] && i!=id ) {
22         for ( j=from ; j<tot ; j++){
23             k=queue[j];
24             if ( g[i][id]>g[i][k]-g[eg[k]][k] ) g[i][id]=g[i][k]-g[eg[k]][k];
25         }
26     }
27 }
28
29 int mdst( int root ) { // return the total length of MDST
30     int i , j , k , sum = 0 ;
31     memset ( used , 0 , sizeof ( used ) ) ;
32     for ( more =1; more ; ) {
33         more = 0 ;
34         memset (eg,0,sizeof(eg)) ;
35         for ( i=1 ; i <= n ; i ++ ) if ( !used[i] && i!=root ) {
36             for ( j=1 , k=0 ; j <= n ; j ++ ) if ( !used[j] && i!=j )
37                 if ( k==0 || g[j][i] < g[k][i] ) k=j ;
38             eg[i] = k ;
39         }
40         memset(pass,0,sizeof(pass));
41         for ( i=1; i<=n ; i++) if ( !used[i] && !pass[i] && i!= root ) combine ( i ,
            sum ) ;
42     }
43     for ( i =1; i<=n ; i ++ ) if ( !used[i] && i!= root ) sum+=g[eg[i]][i];

```

```

44     return sum ;
45 }
46
47
48 int main(){
49     freopen("input.txt","r",stdin);
50     freopen("output.txt","w",stdout);
51     int i,j,k,test,cases;
52     cases=0;
53     scanf("%d",&test);
54     while (test){
55         test--;
56         //if (n==0) break;
57         scanf("%d%d",&n,&m);
58         //memset(g,60,sizeof(g));
59         foru(i,1,n)
60             foru(j,1,n) g[i][j]=1000001;
61         foru(i,1,m) {
62             scanf("%d%d",&j,&k);
63             j++;k++;
64             scanf("%d",&g[j][k]);
65         }
66         cases++;
67         printf("Case_#%d: ",cases);
68         k=mdst(1);
69         if (k>1000000) printf("Possums!\n"); //===no
70         else printf("%d\n",k);
71     }
72
73     return 0;
74 }

```

5.4 KM

```

1  #include <cstdio>
2  #include <cstdlib>
3  #include <algorithm>
4  #include <vector>
5  #include <cstring>
6  #include <string>
7  #include <iostream>
8
9  #define foreach(e, x) for(__typeof(x.begin()) e = x.begin(); e != x.end(); ++e)
10
11 using namespace std;
12
13 const int N = 333;
14 const int INF = (1 << 30);

```



```

15
16 int mat[N][N], lx[N], ly[N], vx[N], vy[N], slack[N];
17 int n, match[N];
18
19 bool find(int x) {
20     vx[x] = 1;
21     for(int i = 1; i <= n; i++) {
22         if (vy[i]) {
23             continue;
24         }
25         int temp = lx[x] + ly[i] - mat[x][i];
26         if (temp == 0) {
27             vy[i] = 1;
28             if (match[i] == -1 || find(match[i])) {
29                 match[i] = x;
30                 return true;
31             }
32         } else {
33             slack[i] = min(slack[i], temp);
34         }
35     }
36     return false;
37 }
38
39 int KM() {
40     for(int i = 1; i <= n; i++) {
41         lx[i] = -INF;
42         ly[i] = 0;
43         match[i] = -1;
44         for(int j = 1; j <= n; j++) {
45             lx[i] = max(lx[i], mat[i][j]);
46         }
47     }
48     for(int i = 1; i <= n; i++) {
49         for(int j = 1; j <= n; j++) {
50             slack[j] = INF;
51         }
52         for(; ; ) {
53             memset(vx, 0, sizeof(vx));
54             memset(vy, 0, sizeof(vy));
55             for(int j = 1; j <= n; j++) {
56                 slack[j] = INF;
57             }
58             if (find(i)) {
59                 break;
60             }
61             int delta = INF;
62             for(int j = 1; j <= n; j++) {
63                 if (!vy[j]) {

```

```

64         delta = min(delta, slack[j]);
65     }
66 }
67 for(int j = 1; j <= n; j++) {
68     if (vx[j]) {
69         lx[j] -= delta;
70     }
71     if (vy[j]) {
72         ly[j] += delta;
73     } else {
74         slack[j] -= delta;
75     }
76 }
77 }
78 }
79 int answer = 0;
80 for(int i = 1; i <= n; i++) {
81     answer += mat[match[i]][i];
82 }
83 return answer;
84 }
85
86 int main() {
87     while(scanf("%d", &n) != EOF) {
88         for(int i = 1; i <= n; i++) {
89             for(int j = 1; j <= n; j++) {
90                 scanf("%d", &mat[i][j]);
91             }
92         }
93         printf("%d\n", KM());
94     }
95     return 0;
96 }

```

5.5 扩展 KM

```

1  #include <cstdio>
2  #include <cstdlib>
3  #include <algorithm>
4  #include <iostream>
5  #include <cstring>
6  using namespace std;
7
8  const int N = 205;
9  const int inf = 1000000000;
10
11 int a[N], b[N], c[N][N], vx[N], vy[N], w[N][N], dx[N], dy[N];
12 int ans, m, n, slack[N], lk[N], next[N];

```

```

13
14 bool hungary(int x) {
15     vx[x] = 1;
16     for(int i = 1; i <= n; i++) {
17         if (vy[i])
18             continue;
19         int delta = dx[x] + dy[i] - w[x][i];
20         if (delta == 0) {
21             vy[i] = 1;
22             if (b[i]) {
23                 lk[x] = i;
24                 next[x] = 0;
25                 return true;
26             }
27             for(int j = 1; j <= m; j++) {
28                 if (vx[j])
29                     continue;
30                 if (c[j][i] && hungary(j)) {
31                     lk[x] = i;
32                     next[x] = j;
33                     return true;
34                 }
35             }
36         } else {
37             slack[i] = min(slack[i], delta);
38         }
39     }
40     return false;
41 }
42
43 void travel(int x) {
44     int flow = a[x];
45     for(int i = x; i; i = next[i]) {
46         if (next[i])
47             flow = min(flow, c[next[i]][lk[i]]);
48         else
49             flow = min(flow, b[lk[i]]);
50     }
51     a[x] -= flow;
52     for(int i = x; i; i = next[i]) {
53         if (next[i])
54             c[next[i]][lk[i]] -= flow;
55         else
56             b[lk[i]] -= flow;
57         c[i][lk[i]] += flow;
58     }
59 }
60
61 int Main() {

```

```

62     scanf("%d%d", &m, &n);
63     for(int i = 1; i <= m; i++)
64         scanf("%d", &a[i]);
65     for(int i = 1; i <= n; i++)
66         scanf("%d", &b[i]);
67     for(int i = 1; i <= m; i++)
68         for(int j = 1; j <= n; j++) {
69             scanf("%d", &w[i][j]);
70             w[i][j] *= -1;
71             c[i][j] = 0;
72         }
73     memset(dy, 0, sizeof(dy));
74     for(int i = 1; i <= m; i++) {
75         dx[i] = -inf;
76         for(int j = 1; j <= n; j++)
77             dx[i] = max(dx[i], w[i][j]);
78     }
79     for(int i = 1; i <= m; i++) {
80         while(1) {
81             for(int j = 1; j <= n; j++)
82                 slack[j] = inf;
83             while (a[i]) {
84                 fill(vx + 1, vx + m + 1, 0);
85                 fill(vy + 1, vy + n + 1, 0);
86                 if (hungary(i))
87                     travel(i);
88             }
89             break;
90         }
91         if (!a[i])
92             break;
93         int delta = inf;
94         for(int j = 1; j <= n; j++)
95             if (!vy[j])
96                 delta = min(delta, slack[j]);
97         for(int j = 1; j <= m; j++)
98             if (vx[j])
99                 dx[j] -= delta;
100         for(int j = 1; j <= n; j++)
101             if (vy[j])
102                 dy[j] += delta;
103     }
104 }
105 long long ans = 0;
106 for(int i = 1; i <= m; i++)
107     for(int j = 1; j <= n; j++) {
108         ans += (long long)c[i][j] * w[i][j];
109     }
110 cout << -ans << endl;

```

```

111     return 0;
112 }
113
114 int main() {
115     int testCount;
116     scanf("%d", &testCount);
117     while(testCount--) {
118         Main();
119     }
120     return 0;
121 }

```

5.6 度限制生成树

```

1  const int N = 55, M = 1010, INF = 1e8;
2  int n, m, S, K, ans, cnt, Best[N], fa[N], FE[N];
3  int f[N], p[M], t[M], c[M], o, Cost[N];
4  bool u[M], d[M];
5  pair<int, int> MinCost[N];
6  struct Edge {
7      int a, b, c;
8      bool operator < (const Edge & E) const { return c < E.c; }
9  }E[M];
10 vector<int> SE;
11 inline int F(int x) { return fa[x] == x ? x : fa[x] = F(fa[x]); }
12 inline void AddEdge(int a, int b, int C) {
13     p[++o] = b; c[o] = C;
14     t[o] = f[a]; f[a] = o;
15 }
16 void dfs(int i, int father) {
17     fa[i] = father;
18     if (father == S) Best[i] = -1;
19     else {
20         Best[i] = i;
21         if (Cost[Best[father]] > Cost[i]) Best[i] = Best[father];
22     }
23     for (int j = f[i]; j; j = t[j])
24         if (!d[j] && p[j] != father) {
25             Cost[p[j]] = c[j];
26             FE[p[j]] = j;
27             dfs(p[j], i);
28         }
29 }
30 inline void Kruskal() {
31     cnt = n - 1; ans = 0; o = 1;
32     for (int i = 1; i <= n; i++) fa[i] = i, f[i] = 0;
33     sort(E + 1, E + m + 1);
34     for (int i = 1; i <= m; i++) {

```

```

35     if (E[i].b == S) swap(E[i].a, E[i].b);
36     if (E[i].a != S && F(E[i].a) != F(E[i].b)) {
37         fa[F(E[i].a)] = F(E[i].b);
38         ans += E[i].c;
39         cnt--;
40         u[i] = true;
41         AddEdge(E[i].a, E[i].b, E[i].c);
42         AddEdge(E[i].b, E[i].a, E[i].c);
43     }
44 }
45 for (int i = 1; i <= n; i++) MinCost[i] = make_pair(INF, INF);
46 for (int i = 1; i <= m; i++)
47     if (E[i].a == S) {
48         SE.push_back(i);
49         MinCost[F(E[i].b)] = min(MinCost[F(E[i].b)], make_pair(E[i].c, i));
50     }
51 for (int i = 1; i <= n; i++)
52     if (i != S && fa[i] == i) {
53         dfs(E[MinCost[i].second].b, S);
54         u[MinCost[i].second] = true;
55         ans += MinCost[i].first;
56     }
57 }
58 bool Solve() {
59     Kruskal();
60     for (int i = cnt + 1; i <= K && i <= n; i++) {
61         int MinD = INF, MinID = -1;
62         for (int j = (int) SE.size() - 1; j >= 0; j--)
63             if (u[SE[j]])
64                 SE.erase(SE.begin() + j);
65         for (int j = 0; j < (int) SE.size(); j++) {
66             int tmp = E[SE[j]].c - Cost[Best[E[SE[j]].b]];
67             if (tmp < MinD) {
68                 MinD = tmp;
69                 MinID = SE[j];
70             }
71         }
72         if (MinID == -1) return false;
73         if (MinD >= 0) break;
74         ans += MinD;
75         u[MinID] = true;
76         d[FE[Best[E[MinID].b]]] = d[FE[Best[E[MinID].b]] ^ 1] = true;
77         dfs(E[MinID].b, S);
78     }
79     return true;
80 }

```

5.7 一般图匹配

```

1  const int N = 300;
2  int n, Next[N], f[N], mark[N], visited[N], Link[N], Q[N], head, tail;
3  vector <int> E[N];
4  int getf(int x) { return f[x] == x ? x : f[x] = getf(f[x]); }
5  void merge(int x, int y) { x = getf(x); y = getf(y); if (x != y) f[x] = y; }
6  int LCA(int x, int y) {
7      static int flag = 0;
8      flag++;
9      for (; ; swap(x, y)) if (x != -1) {
10         x = getf(x);
11         if (visited[x] == flag) return x;
12         visited[x] = flag;
13         if (Link[x] != -1) x = Next[Link[x]];
14         else x = -1;
15     }
16 }
17 void go(int a, int p) {
18     while (a != p) {
19         int b = Link[a], c = Next[b];
20         if (getf(c) != p) Next[c] = b;
21         if (mark[b] == 2) mark[Q[tail++]] = b;
22         if (mark[c] == 2) mark[Q[tail++]] = c;
23         merge(a, b); merge(b, c); a = c;
24     }
25 }
26 void find(int s) {
27     for (int i = 0; i < n; i++) {
28         Next[i] = -1; f[i] = i;
29         mark[i] = 0; visited[i] = -1;
30     }
31     head = tail = 0; Q[tail++] = s; mark[s] = 1;
32     for (; head < tail && Link[s] == -1; ) {
33         for (int i = 0, x = Q[head++]; i < (int)E[x].size(); i++) {
34             if (Link[x] != E[x][i] && getf(x) != getf(E[x][i]) && mark[E[x][i]] != 2)
35             {
36                 int y = E[x][i];
37                 if (mark[y] == 1) {
38                     int p = LCA(x, y);
39                     if (getf(x) != p) Next[x] = y;
40                     if (getf(y) != p) Next[y] = x;
41                     go(x, p);
42                     go(y, p);
43                 }
44                 else if (Link[y] == -1) {
45                     Next[y] = x;
46                     for (int j = y; j != -1; ) {
47                         int k = Next[j];

```



```

21         if (i == n - 1) {
22             if (best > w[zj]) best = w[zj];
23             for (i = 0; i < n; i++)
24                 g[v[i]][pv] = g[pv][v[i]] +=
25                     g[v[zj]][v[i]];
26             v[zj] = v[--n];
27             break;
28         }
29         pv = v[zj];
30         for (j = 1; j < n; j++)
31             if (!a[v[j]])
32                 w[j] += g[v[zj]][v[j]];
33     }
34 }
35 return best;
36 }

```

5.9 Hamilton 回路

```

1  bool graph[N][N];
2  int n, l[N], r[N], next[N], last[N], s, t;
3  char buf[10010];
4  void cover(int x) { l[r[x]] = l[x]; r[l[x]] = r[x]; }
5  int adjacent(int x) {
6      for (int i = r[0]; i <= n; i = r[i]) if (graph[x][i]) return i;
7      return 0;
8  }
9  int main() {
10     scanf("%d\n", &n);
11     for (int i = 1; i <= n; ++i) {
12         gets(buf);
13         string str = buf;
14         istringstream sin(str);
15         int x;
16         while (sin >> x) {
17             graph[i][x] = true;
18         }
19         l[i] = i - 1;
20         r[i] = i + 1;
21     }
22     for (int i = 2; i <= n; ++i)
23         if (graph[1][i]) {
24             s = 1;
25             t = i;
26             cover(s);
27             cover(t);
28             next[s] = t;
29             break;

```

```

30     }
31     while (true) {
32         int x;
33         while (x = adjacent(s)) {
34             next[x] = s;
35             s = x;
36             cover(s);
37         }
38         while (x = adjacent(t)) {
39             next[t] = x;
40             t = x;
41             cover(t);
42         }
43         if (!graph[s][t]) {
44             for (int i = s, j; i != t; i = next[i])
45                 if (graph[s][next[i]] && graph[t][i]) {
46                     for (j = s; j != i; j = next[j])
47                         last[next[j]] = j;
48                     j = next[s];
49                     next[s] = next[i];
50                     next[t] = i;
51                     t = j;
52                     for (j = i; j != s; j = last[j])
53                         next[j] = last[j];
54                     break;
55                 }
56         }
57         next[t] = s;
58         if (r[0] > n)
59             break;
60         for (int i = s; i != t; i = next[i])
61             if (adjacent(i)) {
62                 s = next[i];
63                 t = i;
64                 next[t] = 0;
65                 break;
66             }
67     }
68     for (int i = s; ; i = next[i]) {
69         if (i == 1) {
70             printf("%d", i);
71             for (int j = next[i]; j != i; j = next[j])
72                 printf("␣%d", j);
73             printf("␣%d\n", i);
74             break;
75         }
76         if (i == t)
77             break;
78     }

```

79 }

5.10 弦图判定

```

1  int n, m, first[1001], l, next[2000001], where[2000001], f[1001], a[1001], c[1001], L
    [1001], R[1001],
2  v[1001], idx[1001], pos[1001];
3  bool b[1001][1001];
4
5  int read(){
6      char ch;
7      for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
8      int cnt = 0;
9      for (; ch >= '0' && ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
10     return(cnt);
11 }
12
13 inline void makelist(int x, int y){
14     where[++l] = y;
15     next[l] = first[x];
16     first[x] = l;
17 }
18
19 bool cmp(const int &x, const int &y){
20     return(idx[x] < idx[y]);
21 }
22
23 int main(){
24     //freopen("1015.in", "r", stdin);
25     // freopen("1015.out", "w", stdout);
26     for (;;)
27     {
28         n = read(); m = read();
29         if (!n && !m) return 0;
30         memset(first, 0, sizeof(first)); l = 0;
31         memset(b, false, sizeof(b));
32         for (int i = 1; i <= m; i++)
33         {
34             int x = read(), y = read();
35             if (x != y && !b[x][y])
36             {
37                 b[x][y] = true; b[y][x] = true;
38                 makelist(x, y); makelist(y, x);
39             }
40         }
41         memset(f, 0, sizeof(f));
42         memset(L, 0, sizeof(L));
43         memset(R, 255, sizeof(R));

```

```

44 L[0] = 1; R[0] = n;
45 for (int i = 1; i <= n; i++) c[i] = i, pos[i] = i;
46 memset(idx, 0, sizeof(idx));
47 memset(v, 0, sizeof(v));
48 for (int i = n; i; --i)
49 {
50     int now = c[i];
51     R[f[now]]--;
52     if (R[f[now]] < L[f[now]]) R[f[now]] = -1;
53     idx[now] = i; v[i] = now;
54     for (int x = first[now]; x; x = next[x])
55         if (!idx[where[x]])
56         {
57             swap(c[pos[where[x]]], c[R[f[where[x]]]]);
58             pos[c[pos[where[x]]]] = pos[where[x]];
59             pos[where[x]] = R[f[where[x]]];
60             L[f[where[x]] + 1] = R[f[where[x]]]--;
61             if (R[f[where[x]]] < L[f[where[x]]]) R[f[where[x]]] = -1;
62             if (R[f[where[x]] + 1] == -1)
63                 R[f[where[x]] + 1] = L[f[where[x]] + 1];
64             ++f[where[x]];
65         }
66 }
67 bool ok = true;
68 //v是完美消除序列.
69 for (int i = 1; i <= n && ok; i++)
70 {
71     int cnt = 0;
72     for (int x = first[v[i]]; x; x = next[x])
73         if (idx[where[x]] > i) c[++cnt] = where[x];
74     sort(c + 1, c + cnt + 1, cmp);
75     bool can = true;
76     for (int j = 2; j <= cnt; j++)
77         if (!b[c[1]][c[j]])
78         {
79             ok = false;
80             break;
81         }
82 }
83 if (ok) printf("Perfect\n");
84 else printf("Imperfect\n");
85 printf("\n");
86 }
87 }

```

5.11 弦图求团数

```

1  int n, m, first[100001], next[2000001], where[2000001], l, L[100001], R[100001], c
    [100001], f[100001],
2  pos[100001], idx[100001], v[100001], ans;
3
4  inline void makelist(int x, int y){
5      where[++l] = y;
6      next[l] = first[x];
7      first[x] = l;
8  }
9
10 int read(){
11     char ch;
12     for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
13     int cnt = 0;
14     for (; ch >= '0' && ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
15     return(cnt);
16 }
17
18 int main(){
19     freopen("1006.in", "r", stdin);
20     freopen("1006.out", "w", stdout);
21     memset(first, 0, sizeof(first)); l = 0;
22     n = read(); m = read();
23     for (int i = 1; i <= m; i++)
24     {
25         int x, y;
26         x = read(); y = read();
27         makelist(x, y); makelist(y, x);
28     }
29     memset(L, 0, sizeof(L));
30     memset(R, 255, sizeof(R));
31     memset(f, 0, sizeof(f));
32     memset(idx, 0, sizeof(idx));
33     for (int i = 1; i <= n; i++) c[i] = i, pos[i] = i;
34     L[0] = 1; R[0] = n; ans = 0;
35     for (int i = n; i; --i)
36     {
37         int now = c[i], cnt = 1;
38         idx[now] = i; v[i] = now;
39         if (--R[f[now]] < L[f[now]]) R[f[now]] = -1;
40         for (int x = first[now]; x; x = next[x])
41             if (!idx[where[x]])
42             {
43                 swap(c[pos[where[x]]], c[R[f[where[x]]]]);
44                 pos[c[pos[where[x]]]] = pos[where[x]];
45                 pos[where[x]] = R[f[where[x]]];
46                 L[f[where[x]] + 1] = R[f[where[x]]]--;
47                 if (R[f[where[x]]] < L[f[where[x]]]) R[f[where[x]]] = -1;

```

```

48         if (R[f[where[x]] + 1] == -1) R[f[where[x]] + 1] = L[f[where[x]] +
49             1];
50         ++f[where[x]];
51     }
52     else ++cnt;
53     ans = max(ans, cnt);
54 }
55 printf("%d\n", ans);
56 }

```

5.12 有根树的同构

```

1 //http://acm.sdut.edu.cn/judgeonline/showproblem?problem_id=1861 ÓÐ, ùÊ÷µÄĪ~¹¹
2 const int mm=1051697,p=4773737;
3 int m,n,first[101],where[10001],next[10001],l,hash[10001],size[10001],pos[10001];
4 long long f[10001],rt[10001];
5 bool in[10001];
6
7 inline void makelist(int x,int y){
8     where[++l]=y;
9     next[l]=first[x];
10    first[x]=l;
11 }
12
13
14 inline void hashwork(int now){
15     int a[1001],v[1001],tot=0;
16     size[now]=1;
17     for (int x=first[now];x;x=next[x])
18     {
19         hashwork(where[x]);
20         a[++tot]=f[where[x]];
21         v[tot]=size[where[x]];
22         size[now]+=size[where[x]];
23     }
24     a[++tot]=size[now];
25     v[tot]=1;
26     int len=0;
27     for (int i=1;i<=tot;i++)
28         for (int j=i+1;j<=tot;j++)
29             if (a[j]<a[i])
30             {
31                 int u=a[i];a[i]=a[j];a[j]=u;
32                 u=v[i];v[i]=v[j];v[j]=u;
33             }
34     f[now]=1;
35     for (int i=1;i<=tot;i++)
36     {

```

```

37         f[now]=(f[now]*a[i])%p*rt[len]%p;
38         len+=v[i];
39     }
40 }
41
42 int main(){
43     //freopen("1.txt","r",stdin);
44     //freopen("2.txt","w",stdout);
45     scanf("%d%d",&n,&m);
46     rt[0]=1;
47     for (int i=1;i<=100;i++)
48         rt[i]=(rt[i-1]*mm)%p;
49     for (int i=1;i<=n;i++)
50     {
51         memset(first,0,sizeof(first));
52         memset(in,false,sizeof(in));
53         l=0;
54         for (int j=1;j<=m;j++)
55         {
56             int x,y;
57             scanf("%d%d",&x,&y);
58             makelist(x,y);
59             in[y]=true;
60         }
61         int root=0;
62         for (int j=1;j<=m;j++)
63             if (!in[j])
64             {
65                 root=j;
66                 break;
67             }
68         memset(size,0,sizeof(size));
69         memset(f,0,sizeof(f));
70         hashwork(root);
71         hash[i]=f[root];
72     }
73     for (int i=1;i<=n;i++) pos[i]=i;
74     memset(in,false,sizeof(in));
75     for (int i=1;i<=n;i++)
76         if (!in[i])
77         {
78             printf("%d",i);
79             for (int j=i+1;j<=n;j++)
80                 if (hash[j]==hash[i])
81                 {
82                     in[j]=true;
83                     printf("=%d",j);
84                 }
85             printf("\n");

```

```

86     }
87 }

```

5.13 zkw 费用流

```

1  #include <cstdio>
2  #include <cstdlib>
3  #include <algorithm>
4  #include <cstring>
5  #include <cmath>
6  using namespace std;
7
8  const int N = 105 << 2, M = 205 * 205 * 2;
9  const int inf = 1000000000;
10
11 struct edgelist {
12     int other[M], succ[M], last[N], cap[M], cost[M], sum;
13     void clear() {
14         memset(last, -1, sizeof(last));
15         sum = 0;
16     }
17     void _addEdge(int a, int b, int c, int d) {
18         other[sum] = b, succ[sum] = last[a], last[a] = sum, cost[sum] = d, cap[sum++]
            = c;
19     }
20     void addEdge(int a, int b, int c, int d) {
21         _addEdge(a, b, c, d);
22         _addEdge(b, a, 0, -d);
23     }
24 }e;
25
26 int n, m, S, T, tot, totFlow, totCost;
27 int dis[N], slack[N], visit[N], cur[N];
28
29 int modlable() {
30     int delta = inf;
31     for(int i = 1; i <= T; i++) {
32         if (!visit[i] && slack[i] < delta)
33             delta = slack[i];
34         slack[i] = inf;
35         cur[i] = e.last[i];
36     }
37     if (delta == inf)
38         return 1;
39     for(int i = 1; i <= T; i++)
40         if (visit[i])
41             dis[i] += delta;
42     return 0;

```



```

43 }
44
45 int dfs(int x, int flow) {
46     if (x == T) {
47         totFlow += flow;
48         totCost += flow * (dis[S] - dis[T]);
49         return flow;
50     }
51     visit[x] = 1;
52     int left = flow;
53     for(int &i = cur[x]; ~i; i = e.succ[i])
54         if (e.cap[i] > 0 && !visit[e.other[i]]) {
55             int y = e.other[i];
56             if (dis[y] + e.cost[i] == dis[x]) {
57                 int delta = dfs(y, min(left, e.cap[i]));
58                 e.cap[i] -= delta;
59                 e.cap[i ^ 1] += delta;
60                 left -= delta;
61                 if (!left)
62                     return flow;
63             } else {
64                 slack[y] = min(slack[y], dis[y] + e.cost[i] - dis[x]);
65             }
66         }
67     return flow - left;
68 }
69
70 pair<int, int> minCost() {
71     totFlow = 0, totCost = 0;
72     fill(dis + 1, dis + T + 1, 0);
73     for(int i = 1; i <= T; i++)
74         cur[i] = e.last[i];
75     do {
76         do {
77             fill(visit + 1, visit + T + 1, 0);
78         } while(dfs(S, inf));
79     } while(!modlable());
80     return make_pair(totFlow, totCost);
81 }
82
83 void run() {
84     scanf("%d%d", &m, &n);
85     e.clear();
86     S = m + n + 1, T = m + n + 2;
87     tot = 0;
88     for(int i = 1; i <= m; i++) {
89         int times;
90         scanf("%d", &times);
91         e.addEdge(S, i, times, 0);

```

```
92     }
93     for(int i = 1; i <= n; i++) {
94         int times;
95         scanf("%d", &times);
96         e.addEdge(i + m, T, times, 0);
97     }
98     for(int i = 1; i <= m; i++)
99         for(int j = 1; j <= n; j++) {
100             int cost;
101             scanf("%d", &cost);
102             e.addEdge(i, j + m, inf, cost);
103         }
104     pair<int, int> tmp = minCost();
105     printf("%d\n", tmp.second);
106 }
107
108 int main() {
109     int Test;
110     scanf("%d", &Test);
111     for(; Test--; run());
112     return 0;
113 }
```

Chapter 6

字符串

6.1 扩展 KMP

传入字符串 s 和长度 N , $\text{next}[i]=\text{LCP}(s, s[i..N-1])$

```
1 void z(char *s, int *next, int N)
2 {
3     int j = 0, k = 1;
4     while (j + 1 < N && s[j] == s[j + 1]) ++ j;
5     next[0] = N - 1; next[1] = j;
6     for(int i = 2; i < N; ++ i) {
7         int far = k + next[k] - 1, L = next[i - k];
8         if (L < far - i + 1) next[i] = L;
9         else {
10             j = max(0, far - i + 1);
11             while (i + j < N && s[j] == s[i + j]) ++ j;
12             next[i] = j; k = i;
13         }
14     }
15 }
```

6.2 后缀数组

字符串后面会自动加上一个最小字符 $\backslash 0$.

```
1 const int N = 4 * int(1e5) + 10;
2
3 int n, m;
4 int sa[N], ta[N], tb[N], *rank = ta, *tmp = tb;
5 int height[N], myLog[N], f[N][20];
6 int str[N];
7
8 bool cmp(int i, int j, int l) {
9     return tmp[i] == tmp[j] && tmp[i + l] == tmp[j + l];
10 }
```

```

11
12 void radixSort() {
13     static int w[N];
14     fill(w, w + m, 0);
15     for (int i = 0; i < n; i++) {
16         w[rank[i]]++;
17     }
18     for (int i = 1; i < m; i++) {
19         w[i] += w[i - 1];
20     }
21     for (int i = n - 1; i >= 0; i--) {
22         sa[--w[rank[tmp[i]]]] = tmp[i];
23     }
24 }
25
26 void suffixArray() {
27     for (int i = 0; i < n; i++) {
28         rank[i] = str[i];
29         tmp[i] = i;
30     }
31     radixSort();
32     for (int j = 1, i, p; j < n; j <= 1, m = p) {
33         for (i = n - j, p = 0; i < n; i++) {
34             tmp[p++] = i;
35         }
36         for (i = 0; i < n; i++) {
37             if (sa[i] >= j) {
38                 tmp[p++] = sa[i] - j;
39             }
40         }
41         radixSort();
42         for (swap(tmp, rank), rank[sa[0]] = 0, i = p = 1; i < n; i++) {
43             rank[sa[i]] = cmp(sa[i - 1], sa[i], j) ? p - 1 : p++;
44         }
45     }
46     for (int i = 0, j, k = 0; i < n; ++i, k = max(k - 1, 0)) {
47         if (rank[i]) {
48             j = sa[rank[i] - 1];
49             for (; str[i + k] == str[j + k]; k++);
50             height[rank[i]] = k;
51         }
52     }
53     for (int i = 2; i <= n; i++) {
54         myLog[i] = myLog[i >> 1] + 1;
55     }
56     for (int i = 1; i < n; i++) {
57         f[i][0] = height[i];
58     }
59     for (int j = 1; 1 << j <= n; j++) {

```

```

60         for (int i = 1; i + (1 << j) <= n; i++) {
61             f[i][j] = min(f[i][j - 1], f[i + (1 << j - 1)][j - 1]);
62         }
63     }
64 }
65
66 int lcp(int l, int r) {
67     if (l > r) {
68         return 0;
69     }
70     int len = myLog[r - l + 1];
71     return min(f[l][len], f[r - (1 << len) + 1][len]);
72 }
73
74 int nBase, mBase;
75 int cnt[N];
76 char buf[N];
77
78 int pos(int x) {
79     return x / (mBase << 1 | 1);
80 }
81
82 int main() {
83     n = 0;
84     m = 256;
85     scanf("%d%d", &nBase, &mBase);
86     for (int i = 0; i < nBase; i++) {
87         scanf("%s", buf);
88         for (int j = 0; j < mBase; j++) {
89             str[n++] = buf[j];
90         }
91         for (int j = 0; j < mBase; j++) {
92             str[n++] = buf[j];
93         }
94         str[n++] = i < nBase - 1 ? m++ : 0;
95     }
96     suffixArray();
97     int result = 0, total = 0;
98     for (int i = 0, j = 0; i < n; i++) {
99         for (; j < n && total < nBase; j++) {
100             int p = pos(sa[j]);
101             total += cnt[p]++ == 0;
102         }
103         if (total == nBase) {
104             result = max(result, lcp(i + 1, j - 1));
105         }
106         int p = pos(sa[i]);
107         total -= --cnt[p] == 0;
108     }

```

```

109     result = min(result, mBase);
110     printf("%d\n", result);
111     vector<int> ans(n);
112     total = 0;
113     memset(cnt, 0, sizeof(cnt));
114     for (int i = 0, j = 0; i < n; i++) {
115         for (; j < n && total < nBase; j++) {
116             int p = pos(sa[j]);
117             total += cnt[p]++ == 0;
118         }
119         if (total == nBase && lcp(i + 1, j - 1) >= result) {
120             for (int k = i; k < j; k++) {
121                 int p = pos(sa[k]);
122                 ans[p] = sa[k] % (mBase << 1 | 1);
123             }
124             break;
125         }
126         int p = pos(sa[i]);
127         total -= cnt[p] == 0;
128     }
129     for (int i = 0; i < nBase; i++) {
130         printf("%d\n", ans[i] % mBase + 1);
131     }
132 }

```

6.3 DC3

```

1  //`DC3 待排序的字符串放在 r 数组中，从 r[0]到 r[n-1]，长度为 n，且最大值小于 m。`
2  //`约定除 r[n-1]外所有的 r[i]都大于 0，r[n-1]=0。`
3  //`函数结束后，结果放在 sa 数组中，从 sa[0]到 sa[n-1]。`
4  //`r 必须开长度乘 3`
5  #define maxn 10000
6  #define F(x) ((x)/3+((x)%3==1?0:tb))
7  #define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
8
9  int wa[maxn],wb[maxn],wv[maxn],wss[maxn];
10 int s[maxn*3],sa[maxn*3];
11 int c0(int *r,int a,int b)
12 {
13     return r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];
14 }
15 int c12(int k,int *r,int a,int b)
16 {
17     if(k==2) return r[a]<r[b]||r[a]==r[b]&&c12(1,r,a+1,b+1);
18     else return r[a]<r[b]||r[a]==r[b]&&wv[a+1]<wv[b+1];
19 }
20 void sort(int *r,int *a,int *b,int n,int m)

```

```

21 {
22     int i;
23     for(i=0;i<n;i++) wv[i]=r[a[i]];
24     for(i=0;i<m;i++) wss[i]=0;
25     for(i=0;i<n;i++) wss[wv[i]]++;
26     for(i=1;i<m;i++) wss[i]+=wss[i-1];
27     for(i=n-1;i>=0;i--) b[--wss[wv[i]]]=a[i];
28 }
29 void dc3(int *r,int *sa,int n,int m)
30 {
31     int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
32     r[n]=r[n+1]=0;
33     for(i=0;i<n;i++)
34         if(i%3!=0) wa[tbc++]=i;
35     sort(r+2,wa,wb,tbc,m);
36     sort(r+1,wb,wa,tbc,m);
37     sort(r,wa,wb,tbc,m);
38     for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)
39         rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
40     if (p<tbc) dc3(rn,san,tbc,p);
41     else for (i=0;i<tbc;i++) san[rn[i]]=i;
42     for (i=0;i<tbc;i++)
43         if(san[i]<tb) wb[ta++]=san[i]*3;
44     if(n%3==1) wb[ta++]=n-1;
45     sort(r,wb,wa,ta,m);
46     for(i=0;i<tbc;i++)
47         wv[wb[i]]=G(san[i])=i;
48     for(i=0,j=0,p=0;i<ta && j<tbc;p++)
49         sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
50     for(;i<ta;p++) sa[p]=wa[i++];
51     for(;j<tbc;p++) sa[p]=wb[j++];
52 }
53
54 int main(){
55     int n,m=0;
56     scanf("%d",&n);
57     for (int i=0;i<n;i++) scanf("%d",&s[i]),s[i]++,m=max(s[i]+1,m);
58     printf("%d\n",m);
59     s[n++]=0;
60     dc3(s,sa,n,m);
61     for (int i=0;i<n;i++) printf("%d_",sa[i]);printf("\n");
62 }

```

6.4 AC 自动机

```

1 namespace aho_corasick_automation {
2     int const N = ;
3     struct node {

```

```

4      node *next[N], *fail;
5      int count;
6      inline node() {
7          memset(next, 0, sizeof(next));
8          fail = 0;
9          count = 0;
10     }
11 };
12
13 node *root;
14
15 inline int idx(char x) {
16     return x - 'a';
17 }
18
19 inline void insert(node *x, char *str) {
20     int len = (int)strlen(str);
21     for (int i = 0; i < len; ++i) {
22         int c = idx(str[i]);
23         if (!x->next[c]) {
24             x->next[c] = new node();
25         }
26         x = x->next[c];
27     }
28     x->count++;
29 }
30
31 inline void build() {
32     vector<node*> queue;
33     queue.push_back(root->fail = root);
34     for (int head = 0; head < (int)queue.size(); ++head) {
35         node* x = queue[head];
36         for (int i = 0; i < N; ++i) {
37             if (x->next[i]) {
38                 x->next[i]->fail = (x == root) ? root : x->fail->next[i];
39                 x->next[i]->count += x->next[i]->fail->count;
40                 queue.push_back(x->next[i]);
41             } else {
42                 x->next[i] = (x == root) ? root : x->fail->next[i];
43             }
44         }
45     }
46 }
47
48 inline void prepare() {
49     root = new node();
50 }
51 }

```


6.5 极长回文子串

```

1  //CF17 - E
2  typedef long long int64;
3  const int N = 4 * int(1e6) + 111;
4  const int mod = 51123987;
5  int n;
6  int input[N];
7  int start[N], finish[N];
8  int f[N];
9  int64 ans;
10 void prepare() {
11     int k = 0;
12     for (int i = 0; i < n; ++i) {
13         if (k + f[k] < i) {
14             int &l = f[i] = 0;
15             for (; i - l - 1 >= 0 && i + l + 1 < n && input[i - l - 1] ==
16                 input[i + l + 1]; l++);
17             k = i;
18         } else {
19             int &l = f[i] = f[k - (i - k)];
20             if (i + l >= k + f[k]) {
21                 l = min(l, k + f[k] - i);
22                 for (; i - l - 1 >= 0 && i + l + 1 < n && input[i - l - 1] ==
23                     input[i + l + 1]; l++);
24                 k = i;
25             }
26         }
27         int l = i - f[i], r = i + f[i];
28         l += l & 1;
29         r -= r & 1;
30         if (l <= r) {
31             l /= 2;
32             r /= 2;
33             int mid1 = l + r >> 1;
34             int mid2 = mid1 + ((l + r) & 1);
35             start[l]++;
36             start[mid1 + 1]--;
37             finish[mid2]++;
38             finish[r + 1]--;
39             ans = (ans + (r - l) / 2 + 1) % mod;
40         }
41     }
42 }
43 int main() {
44     scanf("%d", &n);
45     for (int i = 0; i < n; ++i) {
46         input[i << 1] = getchar();
47         if (i < n - 1)

```

```

48         input[i << 1 | 1] = '*';
49     }
50     n = n * 2 - 1;
51     prepare();
52     ans = ans * (ans - 1) / 2 % mod;
53     n = (n + 1) / 2;
54     int sum = 0;
55     for (int i = 0; i < n; ++i) {
56         if (i) {
57             start[i] = (start[i] + start[i - 1]) % mod;
58             finish[i] = (finish[i] + finish[i - 1]) % mod;
59         }
60         ans = (ans - (int64)start[i] * sum % mod) % mod;
61         sum = (sum + finish[i]) % mod;
62     }
63     cout << (ans + mod) % mod << endl;
64 }

```

6.6 后缀自动机 --多个串的最长公共子串

```

1
2  const int N = 255555;
3  const int C = 36;
4
5  struct Node {
6      Node *next[C], *fail;
7      int count, len, dp, dp2;
8      void clear() {
9          for(int i = 0; i < C; i++)
10             next[i] = NULL;
11             len = count = 0;
12             fail = NULL;
13     }
14 };
15
16 Node *tail, *q[N * 2], pool[N * 2], *head;
17 int used = 0, top = 0;
18 char bufer[N * 2];
19
20 Node *newNode() {
21     pool[used++].clear();
22     return &pool[used - 1];
23 }
24
25 void add(int x) {
26     Node *np = newNode(), *p = tail;
27     tail = np;
28     np->len = p->len + 1;

```

```

29     for(; p && !p->next[x]; p = p->fail)
30         p->next[x] = np;
31     if (!p)
32         np->fail = head;
33     else if (p->len + 1 == p->next[x]->len)
34         np->fail = p->next[x];
35     else {
36         Node *q = p->next[x], *nq = newNode();
37         *nq = *q;
38         nq->len = p->len + 1;
39         q->fail = np->fail = nq;
40         for(; p && p->next[x] == q; p = p->fail)
41             p->next[x] = nq;
42     }
43 }
44
45 int main() {
46     scanf("%s", bufer);
47     int length = strlen(bufer);
48     head = tail = newNode();
49     for(int i = 0; i < length; i++)
50         add(bufer[i] - 'a');
51     for(int i = 0; i < used; i++)
52         pool[i].count = 0, pool[i].dp = pool[i].len;
53     int number = 0;
54     while(scanf("%s", bufer) == 1) {
55         number++;
56         length = strlen(bufer);
57         Node *iter = head;
58         int cur = 0;
59         top = 0;
60         for(int i = 0; i < length; i++) {
61             int x = bufer[i] - 'a';
62             while(iter != head && !iter->next[x])
63                 iter = iter->fail, cur = iter->len;
64             if (iter->next[x]) {
65                 cur++;
66                 iter = iter->next[x];
67             }
68             q[top++] = iter;
69             if (iter->count == number - 1) {
70                 iter->count = number;
71                 iter->dp2 = cur;
72             } else if (iter->count == number) {
73                 iter->dp2 = max(iter->dp2, cur);
74             } else {
75                 top--;
76             }
77         }

```

```

78     for(int i = 0; i < top; i++) {
79         q[i]->dp = min(q[i]->dp, q[i]->dp2);
80     }
81 }
82 int ans = 0;
83 for(int i = 0; i < used; i++)
84     if (pool[i].count == number)
85         ans = max(ans, pool[i].dp);
86 printf("%d\n", ans);
87 return 0;
88 }

```

6.7 后缀自动机 --多次询问串在母串中的出现次数

```

1
2 const int N = 255555;
3 const int C = 36;
4
5 struct Node {
6     Node *next[C], *fail;
7     int count, len;
8     void clear() {
9         for(int i = 0; i < C; i++)
10             next[i] = NULL;
11         len = count = 0;
12         fail = NULL;
13     }
14 };
15
16 Node *tail, *q[N * 2], pool[N * 2], *head;
17 int used = 0;
18 char bufer[N * 2];
19 int buc[N * 2], f[N * 2];
20
21 Node *newNode() {
22     pool[used++].clear();
23     return &pool[used - 1];
24 }
25
26 void add(int x) {
27     Node *np = newNode(), *p = tail;
28     tail = np;
29     np->len = p->len + 1;
30     for(; p && !p->next[x]; p = p->fail)
31         p->next[x] = np;
32     if (!p)
33         np->fail = head;
34     else if (p->len + 1 == p->next[x]->len)

```

```

35     np->fail = p->next[x];
36     else {
37         Node *q = p->next[x], *nq = newNode();
38         *nq = *q;
39         nq->len = p->len + 1;
40         q->fail = np->fail = nq;
41         for(; p && p->next[x] == q; p = p->fail)
42             p->next[x] = nq;
43     }
44 }
45
46 int main() {
47     scanf("%s\n", bufer);
48     int length = strlen(bufer);
49     head = tail = newNode();
50     for(int i = 0; i < length; i++)
51         add(bufer[i] - 'a');
52     for(int i = 0; i < used; ++i)
53         ++buc[pool[i].len];
54     for(int i = 1; i <= length; i++)
55         buc[i] += buc[i - 1];
56     for(int i = used - 1; i >= 0; i--)
57         q[--buc[pool[i].len]] = &pool[i];
58     Node *iter = head;
59     for(int i = 0; i < length; ++i)
60         (iter = iter->next[bufer[i] - 'a'])->count++;
61     for(int i = used - 1; i > 0; --i) {
62         f[q[i]->len] = max(f[q[i]->len], q[i]->count);
63         q[i]->fail->count += q[i]->count;
64     }
65     for(int i = length - 1; i > 0; --i) {
66         f[i] = max(f[i + 1], f[i]);
67     }
68     for(int i = 1; i <= length; i++)
69         printf("%d\n", f[i]);
70     return 0;
71 }

```

6.8 循环串的最小表示

```

1 struct cyc_string
2 {
3     int n, offset;
4     char str[max_length];
5     char & operator [] (int x)
6     {return str[((offset + x) % n)];}
7     cyc_string(){offset = 0;}
8 };

```

```
9 void minimum_circular_representation(cyc_string & a)
10 {
11     int i = 0, j = 1, dlt = 0, n = a.n;
12     while(i < n and j < n and dlt < n)
13     {
14         if(a[i + dlt] == a[j + dlt]) dlt++;
15         else
16         {
17             if(a[i + dlt] > a[j + dlt]) i += dlt + 1; else j += dlt + 1;
18             dlt = 0;
19         }
20     }
21     a.offset = min(i, j);
22 }
23 int main()
24 {return 0;}
```

Chapter 7

Others

7.1 快速求逆

```
1 int inverse(int x, int modulo) {
2     if(x == 1)
3         return 1;
4     return (long long)(modulo - modulo / x) * inverse(modulo % x, modulo) % modulo;
5 }
```

7.2 求某年某月某日星期几

```
1 int whatday(int d, int m, int y)
2 {
3     int ans;
4     if (m == 1 || m == 2) {
5         m += 12; y --;
6     }
7     if ((y < 1752) || (y == 1752 && m < 9) || (y == 1752 && m == 9 && d < 3))
8         ans = (d + 2 * m + 3 * (m + 1) / 5 + y + y / 4 + 5) % 7;
9     else ans = (d + 2 * m + 3 * (m + 1) / 5 + y + y / 4 - y / 100 + y / 400) % 7;
10    return ans;
11 }
```

7.3 LL*LL%LL

```
1 LL multiplyMod(LL a, LL b, LL P) { // `需要保证 a 和 b 非负`
2     LL t = (a * b - LL((long double)a / P * b + 1e-3) * P) % P;
3     return t < 0 : t + P : t;
4 }
```

7.4 next_nCk

```

1 void nCk(int n, int k) {
2     for (int comb = (1 << k) - 1; comb < (1 << n); ) {
3         // ...
4         {
5             int x = comb & -comb, y = comb + x;
6             comb = (((comb & ~y) / x) >> 1) | y;
7         }
8     }
9 }

```

7.5 单纯形

test on uva 12567

```

1 const double eps = 1e-8;
2 // max{c * x | Ax <= b, x >= 0}的解, 无解返回空的vector, 否则就是解.
3 vector<double> simplex(vector<vector<double>> &A, vector<double> b, vector<double> c
4 ) {
5     int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
6     vector<vector<double>> D(n + 2, vector<double>(m + 1));
7     vector<int> ix(n + m);
8     for(int i = 0; i < n + m; i++) {
9         ix[i] = i;
10    }
11    for(int i = 0; i < n; i++) {
12        for(int j = 0; j < m - 1; j++) {
13            D[i][j] = -A[i][j];
14        }
15        D[i][m - 1] = 1;
16        D[i][m] = b[i];
17        if (D[r][m] > D[i][m]) {
18            r = i;
19        }
20    }
21    for(int j = 0; j < m - 1; j++) {
22        D[n][j] = c[j];
23    }
24    D[n + 1][m - 1] = -1;
25    for(double d; ; ) {
26        if (r < n) {
27            swap(ix[s], ix[r + m]);
28            D[r][s] = 1. / D[r][s];
29            for(int j = 0; j <= m; j++) {
30                if (j != s) {
31                    D[r][j] *= -D[r][s];

```



```

32         }
33     }
34     for(int i = 0; i <= n + 1; i++) {
35         if (i != r) {
36             for(int j = 0; j <= m; j++) {
37                 if (j != s) {
38                     D[i][j] += D[r][j] * D[i][s];
39                 }
40             }
41             D[i][s] *= D[r][s];
42         }
43     }
44 }
45 r = -1, s = -1;
46 for(int j = 0; j < m; j++) {
47     if (s < 0 || ix[s] > ix[j]) {
48         if (D[n + 1][j] > eps || D[n + 1][j] > -eps && D[n][j] > eps) {
49             s = j;
50         }
51     }
52 }
53 if (s < 0) {
54     break;
55 }
56 for(int i = 0; i < n; i++) {
57     if (D[i][s] < -eps) {
58         if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -eps
59             || d < eps && ix[r + m] > ix[i + m]) {
60
61             r = i;
62         }
63     }
64 }
65
66 if (r < 0) {
67     return vector<double> ();
68 }
69 }
70 if (D[n + 1][m] < -eps) {
71     return vector<double> ();
72 }
73
74 vector<double> x(m - 1);
75 for(int i = m; i < n + m; i++) {
76     if (ix[i] < m - 1) {
77         x[ix[i]] = D[i - m][m];
78     }
79 }
80 return x;

```

```
81 }
```

7.6 曼哈顿最小生成树

```
1  /*
2  `只需要考虑每个点的  $pi/4*k - pi/4*(k+1)$  的区间内的第一个点，这样只有  $4n$  条无向边。`
3  */
4  const int maxn = 100000+5;
5  const int Inf = 1000000005;
6  struct TreeEdge
7  {
8      int x,y,z;
9      void make( int _x,int _y,int _z ) { x=_x; y=_y; z=_z; }
10 } data[maxn*4];
11
12 inline bool operator < ( const TreeEdge& x,const TreeEdge& y ){
13     return x.z<y.z;
14 }
15
16 int x[maxn],y[maxn],px[maxn],py[maxn],id[maxn],tree[maxn],node[maxn],val[maxn],fa[
    maxn];
17 int n;
18 inline bool compare1( const int a,const int b ) { return x[a]<x[b]; }
19 inline bool compare2( const int a,const int b ) { return y[a]<y[b]; }
20 inline bool compare3( const int a,const int b ) { return (y[a]-x[a]<y[b]-x[b] || y[a]
    ]-x[a]==y[b]-x[b] && y[a]>y[b]); }
21 inline bool compare4( const int a,const int b ) { return (y[a]-x[a]>y[b]-x[b] || y[a]
    ]-x[a]==y[b]-x[b] && x[a]>x[b]); }
22 inline bool compare5( const int a,const int b ) { return (x[a]+y[a]>x[b]+y[b] || x[a]
    ]+y[a]==x[b]+y[b] && x[a]<x[b]); }
23 inline bool compare6( const int a,const int b ) { return (x[a]+y[a]<x[b]+y[b] || x[a]
    ]+y[a]==x[b]+y[b] && y[a]>y[b]); }
24 void Change_X()
25 {
26     for(int i=0;i<n;++i) val[i]=x[i];
27     for(int i=0;i<n;++i) id[i]=i;
28     sort(id,id+n,compare1);
29     int cntM=1, last=val[id[0]]; px[id[0]]=1;
30     for(int i=1;i<n;++i)
31     {
32         if(val[id[i]]>last) ++cntM,last=val[id[i]];
33         px[id[i]]=cntM;
34     }
35 }
36 void Change_Y()
37 {
38     for(int i=0;i<n;++i) val[i]=y[i];
```

```

39     for(int i=0;i<n;++i) id[i]=i;
40     sort(id,id+n,compare2);
41     int cntM=1, last=val[id[0]]; py[id[0]]=1;
42     for(int i=1;i<n;++i)
43     {
44         if(val[id[i]]>last) ++cntM,last=val[id[i]];
45         py[id[i]]=cntM;
46     }
47 }
48 inline int absValue( int x ) { return (x<0)?-x:x; }
49 inline int Cost( int a,int b ) { return absValue(x[a]-x[b])+absValue(y[a]-y[b]); }
50 int find( int x ) { return (fa[x]==x)?x:(fa[x]=find(fa[x])); }
51 int main()
52 {
53     // freopen("input.txt", "r", stdin);
54     // freopen("output.txt", "w", stdout);
55
56     int test=0;
57     while( scanf("%d",&n)!=EOF && n )
58     {
59         for(int i=0;i<n;++i) scanf("%d%d",x+i,y+i);
60         Change_X();
61         Change_Y();
62
63         int cntE = 0;
64         for(int i=0;i<n;++i) id[i]=i;
65         sort(id,id+n,compare3);
66         for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;
67         for(int i=0;i<n;++i)
68         {
69             int Min=Inf, Tnode=-1;
70             for(int k=py[id[i]];k<=n;k+=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=
                node[k];
71             if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
72             int tmp=x[id[i]]+y[id[i]];
73             for(int k=py[id[i]];k;k-=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i]
                ];
74         }
75         sort(id,id+n,compare4);
76         for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;
77         for(int i=0;i<n;++i)
78         {
79             int Min=Inf, Tnode=-1;
80             for(int k=px[id[i]];k<=n;k+=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=
                node[k];
81             if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
82             int tmp=x[id[i]]+y[id[i]];
83             for(int k=px[id[i]];k;k-=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i]
                ];

```

```

84     }
85     sort(id,id+n,compare5);
86     for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;
87     for(int i=0;i<n;++i)
88     {
89         int Min=Inf, Tnode=-1;
90         for(int k=px[id[i]];k;k=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=node[k];
91         if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
92         int tmp=-x[id[i]]+y[id[i]];
93         for(int k=px[id[i]];k<=n;k+=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i];
94     }
95     sort(id,id+n,compare6);
96     for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;
97     for(int i=0;i<n;++i)
98     {
99         int Min=Inf, Tnode=-1;
100        for(int k=py[id[i]];k<=n;k+=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=
            node[k];
101        if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
102        int tmp=-x[id[i]]+y[id[i]];
103        for(int k=py[id[i]];k;k=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i];
104    }
105
106    long long Ans = 0;
107    sort(data,data+cntE);
108    for(int i=0;i<n;++i) fa[i]=i;
109    for(int i=0;i<cntE;++i) if(find(data[i].x)!=find(data[i].y))
110    {
111        Ans += data[i].z;
112        fa[fa[data[i].x]]=fa[data[i].y];
113    }
114
115    cout<<"Case_"<<test<<":_"<<"Total_Weight_="<<Ans<<endl;
116 }
117 return 0;
118 }

```

7.7 最长公共子序列

7.7.1 最长公共子序列

```

1  const int dx[]={0,-1,0,1};
2  const int dy[]={1,0,-1,0};
3  const string ds="ENWS";
4  char G[52][52];

```

```

5  char A[22222], B[22222], buf[22222];
6  int n, m;
7
8  typedef unsigned long long ll;
9
10 const int M = 62;
11 const int maxn = 20010;
12 const int maxt = 130;
13 const int maxl = maxn / M + 10;
14 const ll Top = ((ll) 1 << (M));
15 const ll Topless = Top - 1;
16 const ll underTop = ((ll) 1 << (M - 1));
17 typedef ll bitarr[maxl];
18 bitarr comp[maxt], row[2], X;
19
20 void get(char *S){
21     int L,x,y,sz=0;
22     scanf("%d%d%d",&L,&x,&y),x--,y--;
23     //scanf("%s",buf);
24     S[sz++]=G[x][y];
25     for(int i=0;i<L;i++){
26         char ch;
27         scanf("%c",&ch);
28         int pos=ds.find(ch);
29         x+=dx[pos],y+=dy[pos];
30         if (x < 0 || y < 0 || x >= n || y >= m) for(;;);
31         S[sz++]=G[x][y];
32     }
33     S[sz]=0;
34 }
35
36 bool calc[maxt];
37
38 void prepare() {
39
40     int u, p;
41     memset(calc, 0, sizeof(calc));
42     for (int i = 0; i < m; i++) {
43         u = B[i];
44         if (calc[u]) continue; //=====仅对所有字符集 , 每次一次
45         calc[u] = 1;
46         memset(comp[u], 0, sizeof(comp[u]));
47         for (p = 0; p < n; p++) if (u == A[p]) comp[u][p / M] ^= ((ll) 1 << (p % M));
48     }
49 }
50
51 void solve() {
52     prepare();
53     memset(row, 0, sizeof(row));

```

```

54     int prev, curt;
55     int i, u, p, c, cc;
56     int Ln = (n / M) + 1;
57     prev = 0;
58     for (i = 0; i < m; i++) {
59         curt = 1 - prev; u = B[i];
60         for (p = 0; p < Ln; p++) X[p] = row[prev][p] | comp[u][p];
61         c = 0;
62         for (p = 0; p < Ln; p++) {
63             cc = (row[prev][p] & underTop) > 0;
64             row[prev][p] = ((row[prev][p] & (underTop - 1)) << 1) + c;
65             c = cc;
66         }
67         for (p = 0; p < Ln; p++) {
68             if (row[prev][p] != Topless) {
69                 row[prev][p]++;
70                 break;
71             }
72             row[prev][p] = 0;
73         }
74         c = 0;
75         for (p = 0; p < Ln; p++) {
76             if (X[p] >= row[prev][p] + c)
77                 row[prev][p] = X[p] - (row[prev][p] + c), c = 0;
78             else
79                 row[prev][p] = Top + X[p] - (row[prev][p] + c), c = 1;
80         }
81         for (p = 0; p < Ln; p++)
82             row[curt][p] = X[p] & (row[prev][p] ^ X[p]);
83         prev = curt;
84     }
85     int ret = 0;
86     for (i = 0; i < n; i++)
87         if (row[prev][i / M] & ((11) 1 << (i % M))) ret++;
88 // printf("%d %d %d\n", n, m, ret);
89 //=====ret 就是最长公共子序列。
90 printf("%d_ %d\n", n - ret, m - ret);
91 }
92
93 int main(){
94     int tests=0,T;
95     scanf("%d",&T);
96     while(T--){
97         scanf("%d%d",&n,&m);
98         for(int i=0;i<n;i++)
99             for (int j = 0; j < m; j++)
100                 scanf("_%c",&G[i][j]);
101         get(A),get(B);
102

```

```

103         printf("Case_□d:□", ++tests);
104 //         printf("A = %s\n, B = %s\n", A, B);
105         n = strlen(A), m = strlen(B);
106         //n = 20000; m = 20000;
107         //for (int i = 0; i < m; i++) A[i] = B[i] = 'A';
108         //A[m] = B[m] = 0;
109         solve();
110     }
111 }

```

7.8 环状最长公共子序列

```

1  const int N = 2222;
2
3  int a[N], b[N];
4  int n, dp[N][N], from[N][N];
5
6  int run() {
7      scanf("%d", &n);
8      for(int i = 1; i <= n; i++) {
9          scanf("%d", &a[i]);
10         a[i + n] = a[i];
11         b[n - i + 1] = a[i];
12     }
13     memset(from, 0, sizeof(from));
14     int ans = 0;
15     for(int i = 1; i <= 2 * n; i++) {
16         from[i][0] = 2;
17         int upleft = 0, up = 0, left = 0;
18         for(int j = 1; j <= n; j++) {
19             upleft = up;
20             if (a[i] == b[j]) {
21                 upleft++;
22             } else {
23                 upleft = INT_MIN;
24             }
25             if (from[i - 1][j])
26                 up++;
27             int mm = max(up, max(left, upleft));
28             if (mm == left) {
29                 from[i][j] = 0;
30             } else if (mm == upleft)
31                 from[i][j] = 1;
32             else
33                 from[i][j] = 2;
34             left = mm;
35         }
36         if (i >= n) {

```

```

37     int count = 0;
38     for(int x = i, y = n; y; ) {
39         if (from[x][y] == 1) {
40             x--; y--;
41             count++;
42         } else if (from[x][y] == 0)
43             y--;
44         else
45             x--;
46     }
47     ans = max(ans, count);
48     int x = i - n + 1;
49     from[x][0] = 0;
50     int y = 0;
51     for(; y <= n && from[x][y] == 0; y++);
52     for(; x <= i; x++) {
53         from[x][y] = 0;
54         if (x == i) {
55             break;
56         }
57         for(; y <= n; ++y) {
58             if (from[x + 1][y] == 2) {
59                 break;
60             }
61             if (y + 1 <= n && from[x + 1][y + 1] == 1) {
62                 y++;
63                 break;
64             }
65         }
66     }
67 }
68 }
69 if (n)
70     printf("%d\n", ans);
71 return n;
72 }
73
74 int main() {
75     for(; run(); );
76     return 0;
77 }

```

7.9 长方体表面两点最近距离

```

1  int r;
2  void turn(int i, int j, int x, int y, int z, int x0, int y0, int L, int W, int H) {
3      if (z==0) {
4          int R = x*x+y*y;

```



```

5         if (R<r) r=R;
6     }
7     else{
8         if(i>=0 && i< 2)
9             turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
10        if(j>=0 && j< 2)
11            turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
12        if(i<=0 && i>-2)
13            turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
14        if(j<=0 && j>-2)
15            turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
16    }
17 }
18 int main(){
19     int L, H, W, x1, y1, z1, x2, y2, z2;
20     cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
21     if (z1!=0 && z1!=H)
22         if (y1==0 || y1==W)
23             swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
24     else
25         swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
26     if (z1==H) z1=0, z2=H-z2;
27     r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
28     cout<<r<<endl;
29     return 0;
30 }

```

7.10 插头 DP

```

1  #include <cstdio>
2  #include <cstdlib>
3  #include <algorithm>
4  #include <vector>
5  #include <iostream>
6  using namespace std;
7
8  typedef long long int64;
9  typedef pair<int, long long> State;
10 const int MAXN = 8;
11
12 char map[MAXN + 10][MAXN + 10];
13 int n, m, lastx, lasty;
14 int64 ans;
15 vector<State> vec[2];
16
17
18 void mergy(int cur) {
19     sort(vec[cur].begin(), vec[cur].end());

```

```

20     int size = 0;
21     for(int i = 0, j = 0; i < vec[cur].size(); i = j) {
22         vec[cur][size] = vec[cur][i];
23         j = i + 1;
24         while(j < vec[cur].size() && vec[cur][j].first == vec[cur][size].first)
25             vec[cur][size].second += vec[cur][j].second, j++;
26         size++;
27     }
28     vec[cur].resize(size);
29 }
30
31 void next_line(int cur) {
32     int size = 0;
33     for(int i = 0; i < vec[cur].size(); i++) {
34         int sta = vec[cur][i].first;
35         if ((sta >> (m << 1)) == 0) {
36             vec[cur][size] = vec[cur][i];
37             vec[cur][size].first <= 2;
38             size++;
39         }
40     }
41     vec[cur].resize(size);
42 }
43
44 inline int replace(int sta, int pos, int v) {
45     return (sta & ~(3 << (pos << 1))) | (v << (pos << 1));
46 }
47
48 inline int replace(int &sta, int pos, int v1, int v2) {
49     int res = replace(sta, pos, v1);
50     res = replace(res, pos + 1, v2);
51     return res;
52 }
53
54 int Trans(int sta, int pos) {
55     int cnt = 1, v = (sta >> (pos << 1) & 3);
56     if (v == 1) {
57         sta = replace(sta, pos, 0, 0);
58         for(int i = pos + 2; ; i++) {
59             if ((sta >> (i << 1) & 3) == 1)
60                 cnt++;
61             else if ((sta >> (i << 1) & 3) == 2)
62                 cnt--;
63             if (cnt == 0)
64                 return replace(sta, i, 1);
65         }
66     } else {
67         sta = replace(sta, pos, 0, 0);
68         for(int i = pos - 1; ; i--) {

```

```

69         if ((sta >> (i << 1) & 3) == 1)
70             cnt--;
71         else if ((sta >> (i << 1) & 3) == 2)
72             cnt++;
73         if (cnt == 0)
74             return replace(sta, i, 2);
75     }
76 }
77 }
78
79 void dp_block(int i, int j, int cur) {
80     for(int s = 0; s < vec[cur].size(); s++) {
81         int sta = vec[cur][s].first;
82         int64 val = vec[cur][s].second;
83         int left = (sta >> (j << 1)) & 3, up = (sta >> ((j + 1) << 1)) & 3;
84         if (left == 0 && up == 0) {
85             vec[cur ^ 1].push_back(State(sta, val));
86         }
87     }
88 }
89
90 void dp_blank(int i, int j, int cur) {
91     for(int s = 0; s < vec[cur].size(); s++) {
92         int sta = vec[cur][s].first;
93         int64 val = vec[cur][s].second;
94         int left = (sta >> (j << 1)) & 3, up = (sta >> ((j + 1) << 1)) & 3, ns = 0;
95         if (left && up) {
96             if (left == 2 && up == 1) {
97                 vec[cur ^ 1].push_back(State(replace(sta, j, 0, 0), val));
98             } else if (left == 1 && up == 2) {
99                 if (replace(sta, j, 0, 0) == 0 && i == lastx && j == lasty)
100                     ans += val;
101             } else if (left == 1 && up == 1) {
102                 vec[cur ^ 1].push_back(State(Trans(sta, j), val));
103             } else if (left == 2 && up == 2) {
104                 vec[cur ^ 1].push_back(State(Trans(sta, j), val));
105             }
106         } else if (left || up) {
107             vec[cur ^ 1].push_back(State(sta, val));
108             vec[cur ^ 1].push_back(State(replace(sta, j, up, left), val));
109         } else {
110             vec[cur ^ 1].push_back(State(replace(sta, j, 1, 2), val));
111         }
112     }
113 }
114
115 void show(int cur) {
116     for(int i = 0; i < vec[cur].size(); i++)
117         printf("%d_%I64d\n", vec[cur][i].first, vec[cur][i].second);

```

```

118     printf("step\n");
119 }
120
121 int main() {
122     freopen("input.txt", "r", stdin);
123     while(scanf("%d%d", &n, &m) == 2) {
124         ans = 0;
125         lastx = lasty = -1;
126         gets(map[0]);
127         for(int i = 0; i < n; i++) {
128             scanf("%s", map[i]);
129             for(int j = 0; j < m; j++) {
130                 if (map[i][j] == '.') {
131                     lastx = i, lasty = j;
132                 }
133             }
134         }
135         if (lastx == -1) {
136             printf("0\n");
137             continue;
138         }
139         int cur = 0;
140         vec[cur].clear();
141         vec[cur].push_back(State(0, 1));
142         for(int i = 0; i < n; i++) {
143             for(int j = 0; j < m; j++) {
144                 vec[cur ^ 1].clear();
145                 if (map[i][j] == '.')
146                     dp_blank(i, j, cur);
147                 else
148                     dp_block(i, j, cur);
149                 cur ^= 1;
150                 mergy(cur);
151                 //show(cur);
152             }
153             next_line(cur);
154         }
155         cout << ans << endl;
156     }
157     return 0;
158 }

```

7.11 最大团搜索

Int $g[][]$ 为图的邻接矩阵。 $MC(V)$ 表示点集 V 的最大团令 $S_i = v_i, v_{i+1}, \dots, v_n$, $mc[i]$ 表示 $MC(S_i)$ 倒着算 $mc[i]$, 那么显然 $MC(V) = mc[1]$ 此外有 $mc[i] = mc[i+1]$ or $mc[i] = mc[i+1] + 1$

```

1 void init(){
2     int i, j;

```

```

3     for (i=1; i<=n; ++i) for (j=1; j<=n; ++j) scanf("%d", &g[i][j]);
4 }
5 void dfs(int size){
6     int i, j, k;
7     if (len[size]==0) {
8         if (size>ans) {
9             ans=size; found=true;
10        }
11        return;
12    }
13    for (k=0; k<len[size] && !found; ++k) {
14        if (size+len[size]-k<=ans) break;
15        i=list[size][k];
16        if (size+mc[i]<=ans) break;
17        for (j=k+1, len[size+1]=0; j<len[size]; ++j)
18            if (g[i][list[size][j]]) list[size+1][len[size+1]++]=list[size][j];
19        dfs(size+1);
20    }
21 }
22 void work(){
23     int i, j;
24     mc[n]=ans=1;
25     for (i=n-1; i; --i) {
26         found=false;
27         len[1]=0;
28         for (j=i+1; j<=n; ++j) if (g[i][j]) list[1][len[1]++]=j;
29         dfs(1);
30         mc[i]=ans;
31     }
32 }
33 void print(){
34     printf("%d\n", ans);
35 }

```

7.12 Dancing Links

```

1 namespace dancing_links {
2     int const N = , M = , G = ;
3
4     struct node {
5         int col, row, left, right, up, down;
6         inline void clear() {
7             col = row = left = right = up = down = 0;
8         }
9     } grid[G];
10
11     int n, m, tot;
12     int cnt[M], head[N], tail[N];

```

```

13
14 inline void prepare() {
15     tot = m + 1;
16     for (int i = 1; i <= n; ++i) {
17         head[i] = tail[i] = 0;
18     }
19     for (int i = 1; i <= m + 1; ++i) {
20         grid[i].col = i;
21         grid[i].left = i - 1;
22         grid[i].right = i + 1;
23         grid[i].up = i;
24         grid[i].down = i;
25         cnt[i] = 0;
26     }
27     grid[1].left = m + 1;
28     grid[m + 1].right = 1;
29 }
30
31 inline void remove(int x) {
32     grid[grid[x].right].left = grid[x].left;
33     grid[grid[x].left].right = grid[x].right;
34     for (int y = grid[x].down; y != x; y = grid[y].down) {
35         for (int z = grid[y].right; z != y; z = grid[z].right) {
36             cnt[grid[z].col]--;
37             grid[grid[z].down].up = grid[z].up;
38             grid[grid[z].up].down = grid[z].down;
39         }
40     }
41 }
42
43 inline void resume(int x) {
44     for (int y = grid[x].up; y != x; y = grid[y].up) {
45         for (int z = grid[y].left; z != y; z = grid[z].left) {
46             cnt[grid[z].col]++;
47             grid[grid[z].up].down = z;
48             grid[grid[z].down].up = z;
49         }
50     }
51     grid[grid[x].right].left = x;
52     grid[grid[x].left].right = x;
53 }
54
55 inline void add(int x, int y) {
56     tot++;
57     cnt[y]++;
58     if (!head[x]) {
59         head[x] = tot;
60     }
61     if (!tail[x]) {

```

```

62         tail[x] = tot;
63     }
64     grid[tot].row = x; grid[tot].col = y;
65     grid[tot].up = grid[y].up; grid[grid[y].up].down = tot;
66     grid[tot].down = y; grid[y].up = tot;
67     grid[tot].left = tail[x]; grid[tail[x]].right = tot;
68     grid[tot].right = head[x]; grid[head[x]].left = tot;
69     tail[x] = tot;
70 }
71
72 inline bool dfs(int dep) {
73     if (grid[m + 1].right == m + 1) {
74         return true;
75     }
76     int x = grid[m + 1].right;
77     for (int i = x; i != m + 1; i = grid[i].right) {
78         if (cnt[i] < cnt[x]) {
79             x = i;
80         }
81     }
82     if (!cnt[x]) {
83         return false;
84     }
85     remove(x);
86     for (int i = grid[x].down; i != x; i = grid[i].down) {
87         for (int j = grid[i].right; j != i; j = grid[j].right) {
88             remove(grid[j].col);
89         }
90         if (dfs(dep + 1)) {
91             return true;
92         }
93         for (int j = grid[i].left; j != i; j = grid[j].left) {
94             resume(grid[j].col);
95         }
96     }
97     resume(x);
98     return false;
99 }
100
101 inline void clear() {
102     for (int i = 1; i <= tot; ++i) {
103         grid[i].clear();
104     }
105 }
106 }

```

7.13 极大团计数

Bool g[][] 为图的邻接矩阵, 图点的标号由 1 至 n。

```

1 void dfs(int size){
2     int i, j, k, t, cnt, best = 0;
3     bool bb;
4     if (ne[size]==ce[size]){
5         if (ce[size]==0) ++ans;
6         return;
7     }
8     for (t=0, i=1; i<=ne[size]; ++i) {
9         for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)
10            if (!g[list[size][i]][list[size][j]]) ++cnt;
11        if (t==0 || cnt<best) t=i, best=cnt;
12    }
13    if (t && best<=0) return;
14    for (k=ne[size]+1; k<=ce[size]; ++k) {
15        if (t>0){
16            for (i=k; i<=ce[size]; ++i) if (!g[list[size][t]][list[size][i]]) break;
17            swap(list[size][k], list[size][i]);
18        }
19        i=list[size][k];
20        ne[size+1]=ce[size+1]=0;
21        for (j=1; j<k; ++j)if (g[i][list[size][j]]) list[size+1][++ne[size+1]]=list[
22            size][j];
23        for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)
24            if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
25        dfs(size+1);
26        ++ne[size];
27        --best;
28        for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;
29        if (t==0 || cnt<best) t=k, best=cnt;
30        if (t && best<=0) break;
31    }
32 }
33 void work(){
34     int i;
35     ne[0]=0; ce[0]=0;
36     for (i=1; i<=n; ++i) list[0][++ce[0]]=i;
37     ans=0;
38     dfs(0);
39 }

```


Chapter 8

Hints

8.1 积分表

$$\arcsin x \rightarrow \frac{1}{\sqrt{1-x^2}}$$

$$\arccos x \rightarrow -\frac{1}{\sqrt{1-x^2}}$$

$$\arctan x \rightarrow \frac{1}{1+x^2}$$

$$a^x \rightarrow \frac{a^x}{\ln a}$$

$$\sin x \rightarrow -\cos x$$

$$\cos x \rightarrow \sin x$$

$$\tan x \rightarrow -\ln \cos x$$

$$\sec x \rightarrow \ln \tan\left(\frac{x}{2} + \frac{\pi}{4}\right)$$

$$\tan^2 x \rightarrow \tan x - x$$

$$\csc x \rightarrow \ln \tan \frac{x}{2}$$

$$\sin^2 x \rightarrow \frac{x}{2} - \frac{1}{2} \sin x \cos x$$

$$\cos^2 x \rightarrow \frac{x}{2} + \frac{1}{2} \sin x \cos x$$

$$\sec^2 x \rightarrow \tan x$$

$$\frac{1}{\sqrt{a^2-x^2}} \rightarrow \arcsin \frac{x}{a}$$

$$\csc^2 x \rightarrow -\cot x$$

$$\frac{1}{a^2-x^2} (|x| < |a|) \rightarrow \frac{1}{2a} \ln \frac{a+x}{a-x}$$

$$\frac{1}{x^2-a^2} (|x| > |a|) \rightarrow \frac{1}{2a} \ln \frac{x-a}{x+a}$$

$$\sqrt{a^2 - x^2} \rightarrow \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \arcsin \frac{x}{a}$$

$$\frac{1}{\sqrt{x^2 + a^2}} \rightarrow \ln(x + \sqrt{a^2 + x^2})$$

$$\sqrt{a^2 + x^2} \rightarrow \frac{x}{2} \sqrt{a^2 + x^2} + \frac{a^2}{2} \ln(x + \sqrt{a^2 + x^2})$$

$$\frac{1}{\sqrt{x^2 - a^2}} \rightarrow \ln(x + \sqrt{x^2 - a^2})$$

$$\sqrt{x^2 - a^2} \rightarrow \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \ln(x + \sqrt{x^2 - a^2})$$

$$\frac{1}{x\sqrt{a^2 - x^2}} \rightarrow -\frac{1}{a} \ln \frac{a + \sqrt{a^2 - x^2}}{x}$$

$$\frac{1}{x\sqrt{x^2 - a^2}} \rightarrow \frac{1}{a} \arccos \frac{a}{x}$$

$$\frac{1}{x\sqrt{a^2 + x^2}} \rightarrow -\frac{1}{a} \ln \frac{a + \sqrt{a^2 + x^2}}{x}$$

$$\frac{1}{\sqrt{2ax - x^2}} \rightarrow \arccos(1 - \frac{x}{a})$$

$$\frac{x}{ax + b} \rightarrow \frac{x}{a} - \frac{b}{a^2} \ln(ax + b)$$

$$\sqrt{2ax - x^2} \rightarrow \frac{x - a}{2} \sqrt{2ax - x^2} + \frac{a^2}{2} \arcsin(\frac{x}{a} - 1)$$

$$\frac{1}{x\sqrt{ax + b}} (b < 0) \rightarrow \frac{2}{\sqrt{-b}} \arctan \sqrt{\frac{ax + b}{-b}}$$

$$x\sqrt{ax + b} \rightarrow \frac{2(3ax - 2b)}{15a^2} (ax + b)^{\frac{3}{2}}$$

$$\frac{1}{x\sqrt{ax + b}} (b > 0) \rightarrow \frac{1}{\sqrt{b}} \ln \frac{\sqrt{ax + b} - \sqrt{b}}{\sqrt{ax + b} + \sqrt{b}}$$

$$\frac{x}{\sqrt{ax + b}} \rightarrow \frac{2(ax - 2b)}{3a^2} \sqrt{ax + b}$$

$$\frac{1}{x^2\sqrt{ax + b}} \rightarrow -\frac{\sqrt{ax + b}}{bx} - \frac{a}{2b} \int \frac{dx}{x\sqrt{ax + b}}$$

$$\frac{\sqrt{ax + b}}{x} \rightarrow 2\sqrt{ax + b} + b \int \frac{dx}{x\sqrt{ax + b}}$$

$$\frac{1}{\sqrt{(ax + b)^n}} (n > 2) \rightarrow \frac{-2}{a(n - 2)} \cdot \frac{1}{\sqrt{(ax + b)^{n-2}}}$$

$$\frac{1}{ax^2 + c} (a > 0, c > 0) \rightarrow \frac{1}{\sqrt{ac}} \arctan(x\sqrt{\frac{a}{c}})$$

$$\frac{x}{ax^2 + c} \rightarrow \frac{1}{2a} \ln(ax^2 + c)$$

$$\begin{aligned}
\frac{1}{ax^2+c}(a+, c-) &\rightarrow \frac{1}{2\sqrt{-ac}} \ln \frac{x\sqrt{a}-\sqrt{-c}}{x\sqrt{a}+\sqrt{-c}} \\
\frac{1}{x(ax^2+c)} &\rightarrow \frac{1}{2c} \ln \frac{x^2}{ax^2+c} \\
\frac{1}{ax^2+c}(a-, c+) &\rightarrow \frac{1}{2\sqrt{-ac}} \ln \frac{\sqrt{c}+x\sqrt{-a}}{\sqrt{c}-x\sqrt{-a}} \\
x\sqrt{ax^2+c} &\rightarrow \frac{1}{3a} \sqrt{(ax^2+c)^3} \\
\frac{1}{(ax^2+c)^n}(n>1) &\rightarrow \frac{x}{2c(n-1)(ax^2+c)^{n-1}} + \frac{2n-3}{2c(n-1)} \int \frac{dx}{(ax^2+c)^{n-1}} \\
\frac{x^n}{ax^2+c}(n\neq 1) &\rightarrow \frac{x^{n-1}}{a(n-1)} - \frac{c}{a} \int \frac{x^{n-2}}{ax^2+c} dx \\
\frac{1}{x^2(ax^2+c)} &\rightarrow \frac{-1}{cx} - \frac{a}{c} \int \frac{dx}{ax^2+c} \\
\frac{1}{x^2(ax^2+c)^n}(n\geq 2) &\rightarrow \frac{1}{c} \int \frac{dx}{x^2(ax^2+c)^{n-1}} - \frac{a}{c} \int \frac{dx}{(ax^2+c)^n} \\
\sqrt{ax^2+c}(a>0) &\rightarrow \frac{x}{2}\sqrt{ax^2+c} + \frac{c}{2\sqrt{a}} \ln(x\sqrt{a}+\sqrt{ax^2+c}) \\
\sqrt{ax^2+c}(a<0) &\rightarrow \frac{x}{2}\sqrt{ax^2+c} + \frac{c}{2\sqrt{-a}} \arcsin(x\sqrt{\frac{-a}{c}}) \\
\frac{1}{\sqrt{ax^2+c}}(a>0) &\rightarrow \frac{1}{\sqrt{a}} \ln(x\sqrt{a}+\sqrt{ax^2+c}) \\
\frac{1}{\sqrt{ax^2+c}}(a<0) &\rightarrow \frac{1}{\sqrt{-a}} \arcsin(x\sqrt{\frac{-a}{c}}) \\
\sin^2 ax &\rightarrow \frac{x}{2} - \frac{1}{4a} \sin 2ax \\
\cos^2 ax &\rightarrow \frac{x}{2} + \frac{1}{4a} \sin 2ax \\
\frac{1}{\sin ax} &\rightarrow \frac{1}{a} \ln \tan \frac{ax}{2} \\
\frac{1}{\cos^2 ax} &\rightarrow \frac{1}{a} \tan ax \\
\frac{1}{\cos ax} &\rightarrow \frac{1}{a} \ln \tan(\frac{\pi}{4} + \frac{ax}{2}) \\
\ln(ax) &\rightarrow x \ln(ax) - x \\
\sin^3 ax &\rightarrow \frac{-1}{a} \cos ax + \frac{1}{3a} \cos^3 ax \\
\cos^3 ax &\rightarrow \frac{1}{a} \sin ax - \frac{1}{3a} \sin^3 ax \\
\frac{1}{\sin^2 ax} &\rightarrow -\frac{1}{a} \cot ax
\end{aligned}$$

$$x \ln(ax) \rightarrow \frac{x^2}{2} \ln(ax) - \frac{x^2}{4}$$

$$\cos ax \rightarrow \frac{1}{a} \sin ax$$

$$x^2 e^{ax} \rightarrow \frac{e^{ax}}{a^3} (a^2 x^2 - 2ax + 2)$$

$$(\ln(ax))^2 \rightarrow x(\ln(ax))^2 - 2x \ln(ax) + 2x$$

$$x^2 \ln(ax) \rightarrow \frac{x^3}{3} \ln(ax) - \frac{x^3}{9}$$

$$x^n \ln(ax) \rightarrow \frac{x^{n+1}}{n+1} \ln(ax) - \frac{x^{n+1}}{(n+1)^2}$$

$$\sin(\ln ax) \rightarrow \frac{x}{2} [\sin(\ln ax) - \cos(\ln ax)]$$

$$\cos(\ln ax) \rightarrow \frac{x}{2} [\sin(\ln ax) + \cos(\ln ax)]$$

8.2 数学公式

组合公式

- fibonacci
 - $f_0 = 0, f_1 = 1$
 - $f_{n+2}f_n - f_{n+1}^2 = (-1)^{n+1}$
 - $f_{-n} = (-1)^{n-1}f_n$
 - $f_{n+k} = f_k f_{n+1} + f_{k-1} f_n$
 - $\gcd(f_m, f_n) = f_{\gcd(m, n)}$
 - $f_m | f_n^2 \Leftrightarrow n f_n | m$
- $\sum_{k=1}^n (2k-1)^2 = \frac{n(4n^2-1)}{3}$
- $\sum_{k=1}^n k^3 = (\frac{n(n+1)}{2})^2$
- $\sum_{k=1}^n (2k-1)^3 = n^2(2n^2-1)$
- $\sum_{k=1}^n k^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30}$
- $\sum_{k=1}^n k^5 = \frac{n^2(n+1)^2(2n^2+2n-1)}{12}$
- $\sum_{k=1}^n k(k+1) = \frac{n(n+1)(n+2)}{3}$
- $\sum_{k=1}^n k(k+1)(k+2) = \frac{n(n+1)(n+2)(n+3)}{4}$
- $\sum_{k=1}^n k(k+1)(k+2)(k+3) = \frac{n(n+1)(n+2)(n+3)(n+4)}{5}$
- 错排: $D_n = n!(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \dots + \frac{(-1)^n}{n!}) = (n-1)(D_{n-2} - D_{n-1})$

8.3 平面几何公式

三角形

1. 半周长 $P = (a + b + c)/2$

2. 面积 $S = aH_a/2 = ab \sin(C)/2 = \sqrt{P(P-a)(P-b)(P-c)}$

3. 中线 $M_a = \sqrt{2(b^2 + c^2) - a^2}/2 = \sqrt{b^2 + c^2 + 2bc \cos(A)}/2$

4. 角平分线 $T_a = \sqrt{bc((b+c)^2 - a^2)}/(b+c) = 2bc \cos(A/2)/(b+c)$

5. 高线 $H_a = b \sin(C) = c \sin(B) = \sqrt{b^2 - ((a^2 + b^2 - c^2)/(2a))^2}$

6. 内切圆半径

$$r = S/P = \arcsin(B/2) \sin(C/2) / \sin((B+C)/2) = 4R \sin(A/2) \sin(B/2) \sin(C/2) \\ = \sqrt{(P-a)(P-b)(P-c)/P} = P \tan(A/2) \tan(B/2) \tan(C/2)$$

7. 外接圆半径 $R = abc/(4S) = a/(2 \sin(A)) = b/(2 \sin(B)) = c/(2 \sin(C))$

四边形

$D1, D2$ 为对角线, M 为对角线中点连线, A 为对角线夹角

1. $a^2 + b^2 + c^2 + d^2 = D1^2 + D2^2 + 4M^2$

2. $S = D1D2 \sin(A)/2$

3. 圆内接四边形 $ac + bd = D1D2$

4. 圆内接四边形, P 为半周长 $S = \sqrt{(P-a)(P-b)(P-c)(P-d)}$

正 n 边形

R 为外接圆半径, r 为内切圆半径

1. 中心角 $A = 2\pi/n$

2. 内角 $C = (n-2)\pi/n$

3. 边长 $a = 2\sqrt{R^2 - r^2} = 2R \sin(A/2) = 2r \tan(A/2)$

4. 面积 $S = nar/2 = nr^2 \tan(A/2) = nR^2 \sin(A)/2 = na^2/(4 \tan(A/2))$

圆

1. 弧长 $l = rA$

2. 弦长 $a = 2\sqrt{2hr - h^2} = 2r \sin(A/2)$

3. 弓形高 $h = r - \sqrt{r^2 - a^2/4} = r(1 - \cos(A/2)) = \arctan(A/4)/2$

4. 扇形面积 $S1 = rl/2 = r^2 A/2$

5. 弓形面积 $S2 = (rl - a(r-h))/2 = r^2(A - \sin(A))/2$

棱柱

1. 体积 $V = Ah$, A 为底面积, h 为高
2. 侧面积 $S = lp$, l 为棱长, p 为直截面周长
3. 全面积 $T = S + 2A$

棱锥

1. 体积 $V = Ah$, A 为底面积, h 为高
2. 正棱锥侧面积 $S = lp$, l 为棱长, p 为直截面周长
3. 正棱锥全面积 $T = S + 2A$

棱台

1. 体积 $V = (A_1 + A_2 + \sqrt{A_1 A_2})h/3$, A_1, A_2 为上下底面积, h 为高
2. 正棱台侧面积 $S = (p_1 + p_2)l/2$, p_1, p_2 为上下底面周长, l 为斜高
3. 正棱台全面积 $T = S + A_1 + A_2$

圆柱

1. 侧面积 $S = 2\pi rh$
2. 全面积 $T = 2\pi r(h + r)$
3. 体积 $V = \pi r^2 h$

圆锥

1. 母线 $l = \sqrt{h^2 + r^2}$
2. 侧面积 $S = \pi rl$
3. 全面积 $T = \pi r(l + r)$
4. 体积 $V = \pi r^2 h/3$

圆台

1. 母线 $l = \sqrt{h^2 + (r_1 - r_2)^2}$
2. 侧面积 $S = \pi(r_1 + r_2)l$
3. 全面积 $T = \pi r_1(l + r_1) + \pi r_2(l + r_2)$
4. 体积 $V = \pi(r_1^2 + r_2^2 + r_1 r_2)h/3$

球

1. 全面积 $T = 4\pi r^2$
2. 体积 $V = 4\pi r^3/3$

球台

1. 侧面积 $S = 2\pi rh$
2. 全面积 $T = \pi(2rh + r_1^2 + r_2^2)$
3. 体积 $V = \pi h(3(r_1^2 + r_2^2) + h^2)/6$

球扇形

1. 全面积 $T = \pi r(2h + r_0)$, h 为球冠高, r_0 为球冠底面半径
2. 体积 $V = 2\pi r^2 h/3$

8.4 网络流 Hints

下界: (u, v) 下界为 c : 超级源到 t 建流量为 c , s 到超级汇建流量为 c , (原来的汇到原来的源建无穷, 如果有), 流一遍超级源出边满了就存在可行流.

下界最大流 (有源汇): 上面的搞完从原来的源到原来的汇流一遍

下界最小流 (有源汇): 上面的搞完从原来的汇到原来的源流一遍

8.5 2-SAT Hints

每对点都选择强连通时 color 较小的

8.6 二分图相关 Hints

二分图最小覆盖集: 从右边的所有没有匹配过的点出发走增广路, 右边所有没有打上记号的点, 加上左边已经有记号的点.

最小覆盖数 = 最大匹配数.

8.7 java_hints

旧

```
1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4
5 class InputReader {
```

```

6     BufferedReader buff;
7     StringTokenizer tokenizer;
8
9     InputReader(InputStream stream) {
10         buff = new BufferedReader(new InputStreamReader(stream));
11         tokenizer = null;
12     }
13     boolean hasNext() {
14         while (tokenizer == null || !tokenizer.hasMoreTokens())
15             try {
16                 tokenizer = new StringTokenizer(buff.readLine());
17             }
18             catch (Exception e) {
19                 return false;
20             }
21         return true;
22     }
23     String next() {
24         if (!hasNext())
25             throw new RuntimeException();
26         return tokenizer.nextToken();
27     }
28     int nextInt() { return Integer.parseInt(next()); }
29     long nextLong() { return Long.parseLong(next()); }
30 }
31
32 class Node implements Comparable<Node> {
33     int key;
34     public int compareTo(Node o) {
35         if (key != o.key)
36             return key < o.key ? -1 : 1;
37         return 0;
38     }
39     public boolean equals(Object o) { return false; }
40     public String toString() { return ""; }
41     public int hashCode() { return key; }
42 }
43
44 class MyComparator implements Comparator<Node> {
45     public int compare(Node a, Node b) {
46         if (a.key != b.key)
47             return a.key < b.key ? -1 : 1;
48         return 0;
49     }
50 }
51
52 public class Main {
53     public static void main(String[] args) {
54         new Main().run();

```



```

55     }
56     void run() {
57         PriorityQueue<Integer> Q = new PriorityQueue<Integer>();
58         Q.offer(1); Q.poll(); Q.peek(); Q.size();
59
60         HashMap<Node, Integer> dict = new HashMap<Node, Integer>();
61         dict.entrySet(); dict.put(new Node(), 0); dict.containsKey(new Node());
62         //Map.Entry e = (Map.Entry)it.next(); e.getValue(); e.getKey();
63
64         HashSet<Node> h = new HashSet<Node>();
65         h.contains(new Node()); h.add(new Node()); h.remove(new Node());
66
67         Random rand = new Random();
68         rand.nextInt(); rand.nextDouble();
69
70         int temp = 0;
71         BigInteger a = BigInteger.ZERO, b = new BigInteger("1"), c =
72             BigInteger.valueOf(2);
73         a.remainder(b); a.modPow(b, c); a.pow(temp); a.intValue();
74         a.isProbablePrime(temp); // 1 - 1 / 2 ^ certainty
75         a.nextProbablePrime();
76
77         Arrays.asList(array);
78         Arrays.sort(array, fromIndex, toIndex, comparator);
79         Arrays.fill(array, fromIndex, toIndex, value);
80         Arrays.binarySearch(array, key, comparator); // found ? index : -
81             (insertPoint) - 1
82         Arrays.equals(array, array2);
83         Collection.toArray(arrayType[]);
84
85         Collections.copy(dest, src);
86         Collections.fill(collection, value);
87         Collections.max(collection, comparator);
88         Collections.replaceAll(list, oldValue, newValue);
89         Collections.reverse(list);
90         Collections.reverseOrder();
91         Collections.rotate(list, distance); // ----->
92         Collections.shuffle(list); // random_shuffle
93     }
94 }

```

新

```

1  import java.io.*;
2  import java.util.*;
3  import java.math.*;
4
5  public class Main {
6      public static void main(String[] args) {

```

```

7      InputStream inputStream = System.in;
8      OutputStream outputStream = System.out;
9      InputReader in = new InputReader(inputStream);
10     PrintWriter out = new PrintWriter(outputStream);
11     Task solver = new Task();
12     solver.solve(1, in, out);
13     out.close();
14 }
15 }
16
17 class Task {
18     public void solve(int testNumber, InputReader in, PrintWriter out) {
19
20     }
21 }
22
23 class InputReader {
24     public BufferedReader reader;
25     public StringTokenizer tokenizer;
26
27     public InputReader(InputStream stream) {
28         reader = new BufferedReader(new InputStreamReader(stream), 32768);
29         tokenizer = null;
30     }
31
32     public String next() {
33         while (tokenizer == null || !tokenizer.hasMoreTokens()) {
34             try {
35                 tokenizer = new StringTokenizer(reader.readLine());
36             } catch (IOException e) {
37                 throw new RuntimeException(e);
38             }
39         }
40         return tokenizer.nextToken();
41     }
42
43     public int nextInt() {
44         return Integer.parseInt(next());
45     }
46
47     public long nextLong() {
48         return Long.parseLong(next());
49     }
50 }

```

8.8 Usage_of_Rope

```

1 #include <ext/rope>

```

```
2 using __gnu_cxx::crope; using __gnu_cxx::rope;
3 a = b.substr(from, len);           // [from, from + len)
4 a = b.substr(from);                // [from, from]
5 b.c_str();                         // might lead to memory leaks
6 b.delete_c_str();                  // delete the c_str that created before
7 a.insert(p, str);                  // insert str before position p
8 a.erase(i, n);                     // erase [i, i + n)
```