SuperNova Standard Code Library

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Chapter 1

二维几何

1.1 Naive Tips

- 1. 注意舍入方式 (0.5 的舍入方向), 防止输出-0
- 2. 几何题注意多测试不对称数据
- 3. 整数几何注意避免出界
- 4. 符点几何注意 EPS 的使用
- 5. 公式化简后再代入
- 6. atan2(0,0)=0, atan2 的值域为 $[-\pi, \pi]$
- 7. 使用 acos, asin, sqrt 等函数时,注意定义域

1.2 几何公式

高维球

- 1. 体积 $V_0 = 1$, $V_{n+1} = S_n/(n+1)$
- 2. 表面积 $S_0 = 2$, $S_{n+1} = 2\pi V_n$

三角形

- 1. 半周长 P = (a+b+c)/2
- 2. 面积 $S = aH_a/2 = ab\sin(C)/2 = \sqrt{P(P-a)(P-b)(P-c)}$
- 3. 中线 $M_a = \sqrt{2(b^2 + c^2) a^2}/2 = \sqrt{b^2 + c^2 + 2bc\cos(A)}/2$
- 4. 角平分线 $T_a = \sqrt{bc((b+c)^2 a^2)}/(b+c) = 2bc\cos(A/2)/(b+c)$
- 5. 高线 $H_a = b\sin(C) = c\sin(B) = \sqrt{b^2 ((a^2 + b^2 c^2)/(2a))^2}$

6. 内切圆半径

$$r = S/P = \arcsin(B/2)\sin(C/2)/\sin((B+C)/2) = 4R\sin(A/2)\sin(B/2)\sin(C/2)$$
$$= \sqrt{(P-a)(P-b)(P-c)/P} = P\tan(A/2)\tan(B/2)\tan(C/2)$$

7. 外接圆半径 $R = abc/(4S) = a/(2\sin(A)) = b/(2\sin(B)) = c/(2\sin(C))$

四边形

D1, D2 为对角线, M 对角线中点连线, A 为对角线夹角

- 1. $a^2 + b^2 + c^2 + d^2 = D1^2 + D2^2 + 4M^2$
- 2. $S = D1D2\sin(A)/2$
- 3. 圆内接四边形 ac + bd = D1D2
- 4. 圆内接四边形, P 为半周长 $S = \sqrt{(P-a)(P-b)(P-c)(P-d)}$

正n边形

R 为外接圆半径,r 为内切圆半径

- 1. 中心角 $A = 2\pi/n$
- 2. 内角 $C = (n-2)\pi/n$
- 3. 边长 $a = 2\sqrt{R^2 r^2} = 2R\sin(A/2) = 2r\tan(A/2)$
- 4. 面积 $S = nar/2 = nr^2 \tan(A/2) = nR^2 \sin(A)/2 = na^2/(4\tan(A/2))$

员

- 1. 弧长 l = rA
- 2. 弦长 $a = 2\sqrt{2hr h^2} = 2r\sin(A/2)$
- 3. 弓形高 $h = r \sqrt{r^2 a^2/4} = r(1 \cos(A/2)) = \arctan(A/4)/2$
- 4. 扇形面积 $S1 = rl/2 = r^2A/2$
- 5. 弓形面积 $S2 = (rl a(r h))/2 = r^2(A \sin(A))/2$

棱柱

- 1. 体积 V = Ah , A 为底面积 , h 为高
- 2. 侧面积 S = lp , l 为棱长 , p 为直截面周长
- 3. 全面积 T = S + 2A

1.2. 几何公式

9

棱锥

- 1. 体积 V = Ah , A 为底面积 , h 为高
- 2. 正棱锥侧面积 S = lp , l 为棱长 , p 为直截面周长
- 3. 正棱锥全面积 T = S + 2A

棱台

- 1. 体积 $V = (A1 + A2 + \sqrt{A1A2})h/3$, A1, A2 为上下底面积 , h 为高
- 2. 正棱台侧面积 S=(p1+p2)l/2, p1,p2 为上下底面周长, l 为斜高
- 3. 正棱台全面积 T = S + A1 + A2

圆柱

- 1. 侧面积 $S=2\pi rh$
- 2. 全面积 $T = 2\pi r(h+r)$
- 3. 体积 $V = \pi r^2 h$

圆锥

- 1. 母线 $l = \sqrt{h^2 + r^2}$
- 2. 侧面积 $S = \pi r l$
- 3. 全面积 $T = \pi r(l + r)$
- 4. 体积 $V = \pi r^2 h/3$

圆台

- 1. 母线 $l = \sqrt{h^2 + (r1 r2)^2}$
- 2. 侧面积 $S = \pi(r1 + r2)l$
- 3. 全面积 $T = \pi r 1(l + r 1) + \pi r 2(l + r 2)$
- 4. 体积 $V = \pi(r1^2 + r2^2 + r1r2)h/3$

球

- 1. 全面积 $T = 4\pi r^2$
- 2. 体积 $V = 4\pi r^3/3$

球台

- 1. 侧面积 $S=2\pi rh$
- 2. 全面积 $T = \pi(2rh + r1^2 + r2^2)$
- 3. 体积 $V = \pi h(3(r1^2 + r2^2) + h^2)/6$

球扇形

```
1. 全面积 T = \pi r(2h + r0) , h 为球冠高 , r0 为球冠底面半径
```

```
2. 体积 V = 2\pi r^2 h/3
```

1.3 点类

```
1 #include <cmath>
2 #include <cstdio>
3 #include <vector>
4 #include <cstring>
5 #include <iostream>
   #include <algorithm>
   \#define for each (e,x) for (__typeof(x.begin()) e=x.begin(); e!=x.end();++e)
7
8
   using namespace std;
9
   const double PI = acos(-1.);
10
   const double EPS = 1e-8;
11
12
   inline int sign(double a) {
        return a < -EPS ? -1 : a > EPS;
13
14
   }
15
16
   struct Point {
17
        \mathbf{double} \ x\,,\ y\,;
18
        Point() {
19
20
        Point (double _x, double _y) :
21
                x(\underline{x}), y(\underline{y}) {
22
23
        Point operator+(const Point&p) const {
            return Point (x + p.x, y + p.y);
24
25
26
        Point operator-(const Point&p) const {
27
            return Point (x - p.x, y - p.y);
28
29
        Point operator*(double d) const {
30
            return Point (x * d, y * d);
31
32
        Point operator/(double d) const {
33
            return Point (x / d, y / d);
34
        bool operator < (const Point&p) const {
35
36
            int c = sign(x - p.x);
            if (c)
37
38
                 return c == -1;
39
            return sign(y - p.y) = -1;
40
        double dot(const Point&p) const {
41
```

1.3. 点类

```
42
               return x * p.x + y * p.y;
43
44
         double det(const Point&p) const {
               return x * p.y - y * p.x;
45
46
47
         double alpha() const {
48
               return atan2(y, x);
49
         double distTo(const Point&p) const {
50
               double dx = x - p.x, dy = y - p.y;
51
52
               return hypot(dx, dy);
53
         double alphaTo(const Point&p) const {
54
55
               double dx = x - p.x, dy = y - p.y;
56
               return atan2(dy, dx);
57
          //clockwise
58
59
         Point rotAlpha (const double & alpha, const Point & Point (0, 0)) const {
               \mathbf{double} \ \ nx = \cos(alpha) \ \ ^* \ \ (x - o.x) + \sin(alpha) \ \ ^* \ \ (y - o.y);
60
               double ny = -\sin(alpha) * (x - o.x) + \cos(alpha) * (y - o.y);
61
               return Point(nx, ny) + o;
62
63
64
         Point rot90() const {
              return Point(-y, x);
65
66
67
         Point unit() {
               return *this / abs();
68
69
70
         void read() {
               scanf("%lf%lf", &x, &y);
71
72
73
         double abs() {
74
               return hypot(x, y);
75
76
         double abs2() {
              return x * x + y * y;
77
78
         void write() {
79
               cout << "(" << x << "," << y << ")" << endl;
80
81
82
    };
84 \ \ \textit{\#define} \ \ \text{cross} \left( \text{p1}, \text{p2}, \text{p3} \right) \ \left( \left( \text{p2}.\text{x} - \text{p1}.\text{x} \right) * \left( \text{p3}.\text{y} - \text{p1}.\text{y} \right) - \left( \text{p3}.\text{x} - \text{p1}.\text{x} \right) * \left( \text{p2}.\text{y} - \text{p1}.\text{y} \right) \right) \\
    \#define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
85
86
    Point isSS (Point p1, Point p2, Point q1, Point q2) {
87
88
         double a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
         return (p1 * a2 + p2 * a1) / (a1 + a2);
89
90
```

```
91
         double minDiff(double a, double b) // a, b in[0, 2 * PI]
92
93
                    return min(abs(a - b), 2 * PI - abs(a - b));
94
95
                         基本操作
         1.4
         顺时针或逆时针传入一个凸多边形,返回被半平面 \overline{q1q^2} 逆时针方向切割掉之后的凸多边形
         vector < Point > convexCut (const vector < Point > &ps , Point q1 , Point q2) {
  1
  2
                    vector < Point > qs;
  3
                    int n = ps.size();
  4
                    for (int i = 0; i < n; ++i) {
                                Point p1 = ps[i], p2 = ps[(i + 1) \% n];
  5
  6
                                int d1 = crossOp(q1, q2, p1), d2 = crossOp(q1, q2, p2);
  7
                                if (d1 >= 0)
  8
                                          qs.push_back(p1);
 9
                                if (d1 * d2 < 0)
10
                                          qs.push_back(isSS(p1, p2, q1, q2));
11
12
                    return qs;
13
         返回 ps 的有向面积
         double calcArea(const vector<Point>&ps) {
  1
  2
                    int n = ps. size();
  3
                    double ret = 0;
  4
                    for (int i = 0; i < n; ++i) {
  5
                                ret += ps[i].det(ps[(i + 1) \% n]);
  6
  7
                    return ret / 2;
  8
         }
         返回点集 ps 组成的凸包
 1
         vector<Point> convexHull(vector<Point> ps) {
  2
                    int n = ps.size();
  3
                    if (n <= 1)
  4
                               return ps;
  5
                     sort(ps.begin(), ps.end());
  6
                    vector < Point > qs;
                    \begin{tabular}{ll} \beg
  7
  8
                               while (qs.size() > 1 \&\& crossOp(qs[qs.size()-2],qs.back(),ps[i]) \le 0)
 9
                                           qs.pop_back();
10
                    for (int i = n - 2, t = qs.size(); i \ge 0; qs.push_back(ps[i--])) {
11
12
                                while ((int) qs. size() > t \&\& crossOp(qs[(int) qs. size() -2], qs. back(), ps[i]) \le
13
                                           qs.pop_back();
```

14

}

```
15
        qs.pop_back();
16
        return qs;
17
   }
   返回凸包 ps 的直径
   double convexDiameter(const vector < Point > &ps) {
1
2
        int n = ps.size();
3
        int is = 0, js = 0;
4
        for (int i = 1; i < n; ++i) {
            if (ps[i].x > ps[is].x)
5
6
                 is = i;
7
            if (ps[i].x < ps[js].x)
8
                 js = i;
9
10
        double maxd = ps[is].distTo(ps[js]);
11
        int i = is, j = js;
12
        do {
             \mbox{\bf if} \ ((\,ps\,[\,(\,i\,+\,1)\,\,\%\,\,n\,]\,\,-\,\,ps\,[\,i\,]\,)\,.\,\det(\,ps\,[\,(\,j\,+\,1)\,\,\%\,\,n\,]\,\,-\,\,ps\,[\,j\,]\,)\,>=\,0) 
13
14
                (++j) \% = n;
15
            else
                 (++i) \% = n;
16
            maxd = max(maxd, ps[i].distTo(ps[j]));
17
        } while (i != is || j != js);
18
19
        return maxd;
20
   判断点 p 在线段 q1q2 上,端点重合返回 true
  int on Segment (Point p, Point q1, Point q2)
3
        return crossOp(q1, q2, p) == 0 \&\& sign((p - q1).dot(p - q2)) <= 0;
4
   }
   判断线段 p1p2 和 q1q2 是否严格相交, 重合或端点相交返回 false
   int isIntersect (Point p1, Point p2, Point q1, Point q2)
2
   {
        return crossOp(p1, p2, q1) * crossOp(p1, p2, q2) < 0 && crossOp(q1, q2, p1) *
3
            cross(q1, q2, p2) < 0;
4 }
   判断直线 p1p2 和 q1q2 是否平行
   int is Parallel (Point p1, Point p2, Point q1, Point q2)
2
        return sign((p2 - p1).det(q2 - q1)) == 0;
3
4
   返回点 p 到直线 uv 的距离
1 double distPointToLine(Point p, Point u, Point v)
2
        return abs((u - p).det(v - p)) / u.distTo(v);
3
4 }
```

```
判断点 q 是否在简单多边形 p 内部, 边界返回 false
   int insidePolygon (Point q, vector < Point > &p)
2
   {
3
        int n = p.size();
        for(int i = 0; i < n; ++ i) {
4
             if (onSegment(q, p[i], p[(i + 1) % n])) return false;
5
 6
7
        Point q2;
 8
        double offsite = LIM;
9
        for( ; ; ) {
             int flag = true;
10
             int rnd = rand() \% 10000;
11
             q2.x = cos(rnd)^* * offsite;
12
             q2.y = \sin(rnd) * offsite;
13
             for(int i = 0; i < n; ++ i) {
14
15
                  if (onSegment(p[i], q, q2)) {
16
                      flag = false;
17
                      break;
18
                  }
19
             if (flag) break;
20
21
22
        int cnt = 0;
23
        for(int i = 0; i < n; ++ i)
24
             cnt += isIntersect(p[i], p[(i + 1) \% n], q, q2);
25
        return cnt & 1;
26
27
   判断直线 1112 是否与圆相交,相切返回 true
1
   int isIntersectLineToCircle(Point c, double r, Point 11, Point 12)
2
3
        return (distPointToLine(c, 11, 12) - r) \le 0;
 4
   }
   判断圆与线段是否有公共点,线段在圆内部返回 true
   int isIntersectSegmentToCircle(Point c, double r, Point p1, Point p2)
 2
   {
 3
        if ((distPointToLine(c, p1, p2) - r) > 0) return false;
        if (\operatorname{sign}(c.\operatorname{dist}\operatorname{To}(p1) - r) \le 0 \mid | \operatorname{sign}(c.\operatorname{dist}\operatorname{To}(p2) - r) \le 0) return true;
 4
 5
        Point c2 = (p2 - p1) \cdot rot 90() + c;
6
        return crossOp(c, c2, p1) * crossOp(c, c2, p2) \le 0;
7
   }
   判断圆与圆是否相交,外切或内切返回 true
   int isIntersectCircleToCircle(Point c1, double r1, Point c2, double r2)
 1
2
3
        double dis = c1.distTo(c2);
        return \operatorname{sign}(\operatorname{dis} - \operatorname{abs}(r1 - r2)) >= 0 \&\& \operatorname{sign}(\operatorname{dis} - (r1 + r2)) <= 0;
 4
```

1.5. **球面** 15

```
5 }
  求直线与圆的两个交点
  void intersectionLineToCircle(Point c, double r, Point l1, Point l2, Point& p1, Point
      & p2) {
2
       Point c2 = c + (12 - 11) \cdot rot 90();
3
       c2 = isSS(c, c2, l1, l2);
4
       double t = sqrt(r * r - (c2 - c).abs2());
       p1 = c2 + (l2 - l1).unit() * t;
5
       p2 = c2 - (12 - 11) \cdot unit() * t;
6
7
  }
  求圆与圆的两个交点
  void intersection Circle To Circle (Point c1, double r1, Point c2, double r2, Point &p1,
      Point &p2) {
       double t = (1 + (r1 * r1 - r2 * r2) / (c1 - c2).abs2()) / 2;
2
3
       Point u = c1 + (c2 - c1) * t;
4
       Point v = u + (c2 - c1).rot90();
       intersectionLineToCircle(c1, r1, u, v, p1, p2);
5
 }
6
         球面
  1.5
  计算圆心角 lat 表示纬度,-90 \le w \le 90,\ln g 表示经度
  返回两点所在大圆劣弧对应圆心角,0 \le angle \le \pi
  double angle (double lng1, double lat1, double lng2, double lat2) {
       double dlng = abs(lng1 - lng2) * PI / 180;
2
       while (dlng >= PI + PI) dlng -= PI + PI;
3
4
       if (dlng > PI) dlng = PI + PI - dlng;
       lat1 *= PI / 180, lat2 *= PI / 180;
5
       return a\cos(\cos(\operatorname{lat}1) * \cos(\operatorname{lat}2) * \cos(\operatorname{dlng}) + \sin(\operatorname{lat}1) * \sin(\operatorname{lat}2));
6
7
  }
  计算直线距离, r 为球半径
  double line_dist(double r, double lng1, double lat1, double lng2, double lat2) {
1
       double dlng = abs(lng1 - lng2) * PI / 180;
2
3
       \mathbf{while}(d \log >= \mathrm{PI} + \mathrm{PI}) \ d \log = \mathrm{PI} + \mathrm{PI};
4
       if (d lng > PI) d lng = PI + PI - d lng;
       lat1 *= PI / 180, lat2 *= PI / 180;
5
       return r * sqrt(2 - 2 * (cos(lat1) * cos(lat2) * cos(dlng) + sin(lat1) * sin(lat2)
6
           )));
7 }
  计算球面距离, r 为球半径
  inline double sphere dist (double r, double lng1, double lat1, double lng2, double lat2) {
2
       return r * angle(lng1, lat1, lng2, lat2);
3
  }
```

1.6 半平面交

```
struct Border {
1
2
        Point p1, p2;
3
        double alpha;
4
        void setAlpha() {
5
            alpha = atan2(p2.y - p1.y, p2.x - p1.x);
6
7
        void read() {
8
            p1.read();
            p2.read();
9
10
            setAlpha();
        }
11
12
   };
13
14
   int n;
   const int MAX_N_BORDER = 20000 + 10;
15
16
   Border border [MAX_N_BORDER];
17
18
   bool operator < (const Border&a, const Border&b) {
19
        int c = sign(a.alpha - b.alpha);
20
        if (c != 0)
21
            return c = 1;
22
        return crossOp(b.p1,b.p2,a.p1) >= 0;
23
   }
24
25
   bool operator==(const Border&a, const Border&b) {
26
        return sign(a.alpha - b.alpha) == 0;
27
   }
28
29
   const double LARGE = 10000;
30
31
   void add(double x, double y, double nx, double ny) {
32
        border[n].p1 = Point(x, y);
        border[n].p2 = Point(nx, ny);
33
        border [n]. setAlpha();
34
35
        n++;
36
   }
37
   Point isBorder (const Border&a, const Border&b) {
38
39
        return is SS(a.p1, a.p2, b.p1, b.p2);
40
   }
41
42
   Border que [MAX_N_BORDER];
43
   int qh, qt;
44
45
   bool check (const Border&a, const Border&b, const Border&me) {
46
        Point is = isBorder(a, b);
47
        return crossOp(me.p1,me.p2,is) > 0;
```

1.6. 半平面交 17

```
48
   }
49
50
    void convexIntersection() {
51
         qh = qt = 0;
52
         sort(border, border + n);
53
         n = unique(border, border + n) - border;
54
         for (int i = 0; i < n; ++i) {
              Border cur = border[i];
55
              while (qh + 1 < qt \&\& ! check(que[qt - 2], que[qt - 1], cur))
56
57
              while (qh + 1 < qt \&\& ! check(que[qh], que[qh + 1], cur))
58
59
                  ++qh;
              que[qt++] = cur;
60
61
          \mbox{while } (qh + 1 < qt \&\& ! check (que [qt - 2], que [qt - 1], que [qh])) 
62
63
         while (qh + 1 < qt \&\& !check(que[qh], que[qh + 1], que[qt - 1]))
64
65
             ++qh;
66
    }
67
68
    void calcArea() {
         static Point ps[MAX_N_BORDER];
69
70
         int cnt = 0;
71
72
         if (qt - qh \ll 2)
73
              puts("0.0");
74
              return;
75
         }
76
77
         for (int i = qh; i < qt; ++i) {
78
              int next = i + 1 = qt ? qh : i + 1;
79
              ps[cnt++] = isBorder(que[i], que[next]);
         }
80
81
82
         double area = 0;
         \  \  \, \textbf{for} \  \, (\, \textbf{int} \  \, \textbf{i} \, = \, 0\,; \  \, \textbf{i} \, < \, \textbf{cnt}\,; \, \, +\!\!\!\!\! +\!\!\!\! \textbf{i}\,) \  \, \{\,
83
              area += ps[i].det(ps[(i + 1) \% cnt]);
84
85
         }
86
         area /= 2;
         area = fabsl(area);
87
88
         cout.setf(ios::fixed);
89
         cout.precision(1);
90
         cout << area << endl;</pre>
91
92
93
    void halfPlaneIntersection()
94
95
         cin >> n;
96
         for (int i = 0; i < n; ++i) {
```

```
97
             border[i].read();
98
99
        add(0, 0, LARGE, 0);
        add(LARGE, 0, LARGE, LARGE);
100
        add (LARGE, LARGE, 0, LARGE);
101
102
        add(0, LARGE, 0, 0);
103
104
         convexIntersection();
105
         calcArea();
106
```

1.7 最小圆覆盖

```
1 #include < cmath >
   #include < cstdio >
3 #include<algorithm>
4 using namespace std;
   const double eps=1e-6;
   struct couple
6
7
       double x, y;
8
9
       couple(){}
10
       couple (const double &xx, const double &yy)
11
12
           x = xx; y = yy;
13
   } a[100001];
14
   int n;
15
   bool operator < (const couple & a, const couple & b)
16
17
18
       return a.x < b.x - eps or (abs(a.x - b.x) < eps and a.y < b.y - eps);
19
   bool operator = (const couple & a, const couple & b)
20
21
   {
       return !(a < b) and !(b < a);
22
23
   inline couple operator - (const couple &a, const couple &b)
24
25
   {
       return couple(a.x-b.x, a.y-b.y);
26
27
   }
28
   inline couple operator + (const couple &a, const couple &b)
29
       return couple(a.x+b.x, a.y+b.y);
30
31
   inline couple operator * (const couple &a, const double &b)
32
33
       return couple(a.x*b, a.y*b);
34
35
   inline couple operator / (const couple &a, const double &b)
```

1.7. 最小圆覆盖 19

```
37
38
       return a*(1/b);
39
  inline double operator * (const couple &a, const couple &b)
40
41
       return a.x*b.y-a.y*b.x;
42
43
44
   inline double len(const couple &a)
45
       return a.x*a.x+a.y*a.y;
46
47
48
   inline double di2(const couple &a, const couple &b)
49
       return (a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y);
50
51
   inline double dis (const couple &a, const couple &b)
52
53
54
       return sqrt((a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y));
55
   struct circle
56
57
58
       double r; couple c;
59
  inline bool inside (const couple & x)
60
61
       return di2(x, cir.c) < cir.r*cir.r+eps;
62
63
   }
64
   inline void p2c(int x, int y)
65
66
       cir.c.x = (a[x].x+a[y].x)/2;
67
       cir.c.y = (a[x].y+a[y].y)/2;
68
       cir.r = dis(cir.c, a[x]);
69
   inline void p3c(int i, int j, int k)
70
71
       couple x = a[i], y = a[j], z = a[k];
72
       cir.r = sqrt(di2(x,y)*di2(y,z)*di2(z,x))/fabs(x*y+y*z+z*x)/2;
73
74
       len(z))/2);
75
       cir.c = couple(t3*t2, t1*t3)/(t1*t2);
76
   inline circle mi()
77
78
   {
79
       sort(a + 1, a + 1 + n);
80
       n = unique(a + 1, a + 1 + n) - a - 1;
81
       if(n == 1)
82
83
           cir.c = a[1];
84
           cir.r = 0;
```

```
85
              return cir;
          }
86
87
          random\_shuffle(a + 1, a + 1 + n);
88
          p2c(1, 2);
          for(int i = 3; i \le n; i++)
89
90
               if (! inside (a[i]))
91
92
                   p2c(1, i);
93
                    for (int j = 2; j < i; j++)
94
                        \mathbf{if}(!\operatorname{inside}(a[j]))
95
96
                             p2c(i, j);
                             for (int k = 1; k < j; k++)
97
98
                                  if (! inside (a[k]))
99
                                       p3c(i,j, k);
                        }
100
101
102
          return cir;
103
    }
```

1.8 求直线与凸包的交点

1.8.1 tEJtM

```
1 #include < cstring >
2 #include < cstdio >
3 #include<cmath>
4 #include < algorithm >
   using namespace std;
6
   struct couple
7
   {
8
       double x, y;
9
       couple(){}
10
       couple(const double \& \_x, const double \& \_y) : x(\_x), y(\_y) \{\}
       void scan() {scanf("%lf%lf", &x, &y); }
11
12
   cp1, cp2, x, y;
   double operator * (const couple & a, const couple & b) {return a.x * b.y - a.y * b.x
13
       ;}
   couple operator - (const couple & a, const couple & b) {return couple(a.x - b.x, a.y
14
      - b.y);}
15
   couple operator + (const couple & a, const couple & b) {return couple(a.x + b.x, a.y
      + b.y);
   couple operator * (const double & a, const couple & b) {return couple(a * b.x, a * b.
16
   bool les(const couple & a, const couple & b) {return a.x < b.x or a.x == b.x and a.y
17
      < b.y; 
18
   bool mor(const couple & a, const couple & b) {return a.x > b.x or a.x == b.x and a.y
      > b.y;
   int n, m, mxi, mni, t1, t2, c1, c2, mi;
```

1.8. 求直线与凸包的交点 21

```
20 double eps = 1e-12;
   int sign (const double & x) {return x > eps?1:x < -eps?-1:0;}
22
   couple cross (const couple &a, const couple &b, const couple &c, const couple &d)
23
        if(sign((b-a) * (d-c)) == 0) return a;
24
        double lambda = (c - a) * (d - c) / ((b - a) * (d - c));
25
        return a + lambda * (b - a);
26
27
   double s [50001];
28
29
   struct convex polygon
30 {
31
        couple a[50000];
32
        couple & operator [] (int x) {return a[(x % n + n) % n];}
        int get_max(bool (*cmp)(const couple & a, const couple & b)) {int rtn = 0; for(
33
            int i = 1; i < n; i++) if(cmp(a[i], a[rtn])) rtn = i; return rtn;
34
    } a;
35
   int check(int id)
36
   {
37
        return (sign((y-x) * (a[id-1] - a[id]))) * sign((y-x) * (a[id+1] - a[id])
            = 0? - sign((y - x) * (a[id + 1] - a[id])) : sign((sign((y - x) * (a[id - 1] - a[id]))) : sign((sign((y - x) * (a[id - 1] - a[id])))) : sign((sign((y - x) * (a[id - 1] - a[id])))) : sign((sign((y - x) * (a[id - 1] - a[id])))))
            a[id]))) - sign((y - x) * (a[id + 1] - a[id])));
38
39 int check1(int id)
40 {
        return sign((y - x) * (a[id] - x)) * sign((y - x) * (a[id + 1] - x)) <= 0.0: sign
41
            ((y - x) * (a[id] - x));
42
43
   int di(int (*check)(int), int le, int ri)
44
45
        int nor = check(le), mid;
46
        if(le > ri) ri += n;
        while (le != ri)
47
48
             mid = (le + ri) / 2;
49
             if(0 = check(mid)) return mid;
50
             else if (nor = check (mid)) le = mid + 1;
51
             else ri = mid - 1;
52
53
54
        return le;
55
56 double area (int le, int ri)
57
        le \% n; ri \% n;
58
        return (le \leq ri)?(s[ri] - s[le]):(s[n] - s[le] + s[ri]);
59
60
61
   int main()
62
        freopen ("sgu345.in", "r", stdin);
63
64
        scanf("%d", &n);
```

```
65
        for(int i = 1; i \le n; i++)
66
            a[i].scan();
67
            if(i >= 3 \text{ and } fabs((a[i] - a[i - 1]) * (a[i - 1] - a[i - 2])) < eps)
68
69
70
                a[i - 1] = a[i];
71
                i --; n--;
72
73
        s[0] = 0;
74
75
        for(int i = 1; i \le n; i++)
76
            s[i] = s[i - 1] + a[i - 1] * a[i];
77
78
79
        mni = a.get_max(les);
80
        mxi = a.get_max(mor);
81
        scanf ("%d", &m);
82
        for (int i = 1; i \le m; i++)
83
84
            x.scan(); y.scan();
            if(check(mni) = 0 \text{ or } check(mxi) = 0)
85
86
87
                if(check(mxi) == 0) mi = mxi; else mi = mni;
88
                t1 = mi;
89
                t2 = di(check, mi + 1, mi - 1);
90
            }else
91
92
                t1 = di(check, mni, mxi);
                t2 = di(check, mxi, mni);
93
94
95
            c1 = di(check1, t1, t2);
96
            c2 = di(check1, t2, t1);
97
            if (check1(c1)) and check1(c2) { printf("0\n"); continue;}
98
            cp1 = cross(a[c1], a[c1 + 1], x, y);
            cp2 = cross(a[c2], a[c2 + 1], x, y);
99
            100
                [c2 + 1]) / 2);
101
102
        fclose (stdin);
103
        return 0;
104
    1.8.2 Seraphim
    double calc(point a, point b) {
 2
        double k=a \tan 2 (b.y-a.y, b.x-a.x); if (k<0) k+=2*pi;return k;
 3
    /\!\!/= the convex must compare y, then \pounds \neg xa[0] is the lower-right point
    //=== three is no 3 points in line. a[] is convex 0\sim n-1
```

1.8. 求直线与凸包的交点 23

```
\mathbf{void} \ \ \mathbf{prepare} \ (\ \mathbf{point} \ \ \mathbf{a} \ [\ ] \ \ , \\ \mathbf{double} \ \ \mathbf{w} \ [\ ] \ , \\ \mathbf{int} \ \ \& \mathbf{n}) \ \ \{
  6
  7
                   int i; rep(i,n) a[i+n]=a[i];
  8
                   a[2*n]=a[0];
                   rep(i,n) \{ w[i] = calc(a[i],a[i+1]); w[i+n] = w[i]; \}
  9
10
        int find(double k,int n , double w[]){
11
                    \begin{tabular}{ll} \be
12
13
                   while (1 \le r) { mid=(1+r)/2; if (w[mid] > k) r=mid-1; else l=mid+1;
14
                   r=1;
15
        int dic(const point &a, const point &b, int l, int r, point c[]) {
16
17
                   int s; if (area(a,b,c[1])<0) s=-1; else s=1; int mid;
18
                   while (l \le r) {
                             mid = (l+r)/2; if (area(a,b,c[mid])*s <= 0) r=mid-1;
19
20
                             else l=mid+1;
21
                   r=1;
22
        }
23
        point get (const point &a, const point &b, point s1, point s2) {
24
                   double k1, k2; point tmp; k1=area(a,b,s1); k2=area(a,b,s2);
25
                   if (cmp(k1)==0) return s1; if (cmp(k2)==0) return s2;
                   tmp = (s1*k2 - s2*k1) / (k2-k1);
26
27
                   return tmp;
28
29
        bool line_cross_convex(point a, point b ,point c[] , int n, point &cp1, point &cp2 ,
                 double w[]) {
30
                   int i, j;
31
                   i=find(calc(a,b),n,w);
32
                   j = find(calc(b,a),n,w);
33
                   double k1, k2;
34
                   k1=area(a,b,c[i]); k2=area(a,b,c[j]);
35
                   if (cmp(k1)*cmp(k2)>0) return false; //no\ cross
36
                   if (cmp(k1)==0 | | cmp(k2)==0) {
37
                             //cross a point or a line in the convex
38
                             if (cmp(k1) == 0) {
39
                                       if (cmp(area(a,b,c[i+1]))==0) \{cp1=c[i]; cp2=c[i+1];\}
40
                                       else cp1=cp2=c[i];
                                       return true;
41
42
43
                             if (cmp(k2) == 0) {
                                       if (cmp(area(a,b,c[j+1]))==0) \{cp1=c[j]; cp2=c[j+1];
44
45
                                       else cp1=cp2=c[i];
46
                             }return true;
47
                   if (i>j) swap(i,j); int x,y;
48
49
                   x=dic(a,b,i,j,c); y=dic(a,b,j,i+n,c);
                   cp1 = get\left(a\,,b\,,c\,[\,x\,-1\,]\,,c\,[\,x\,]\,\right)\,;\  \  cp2 = get\left(a\,,b\,,c\,[\,y\,-1\,]\,,c\,[\,y\,]\,\right)\,;
50
                   return true;
51
52
      }
```

1.9 点到凸包的切线

```
1 #include < cstring >
2 #include < cstdio >
   #include<algorithm>
    using namespace std;
5
    struct couple
 6
7
         long long x, y;
8
         couple(){}
9
         couple(\mathbf{const}\ \mathbf{long}\ \mathbf{long}\ \&\ \underline{\hspace{0.1cm}}x,\ \mathbf{const}\ \mathbf{long}\ \mathbf{long}\ \&\underline{\hspace{0.1cm}}y)\ \{x=\underline{\hspace{0.1cm}}x;\ y=\underline{\hspace{0.1cm}}y;\}
10
         void scan() { scanf("%lld%lld", &x, &y);}
         void print() { printf("%lld \\n", x, y);}
11
    } q1[111111], *q, q2[111111], a[111111], x; long long ans, ans1, s1[111111], s2[111111],
12
13
    int n, Q, cl1, cl2, cl, mid, lb, bs[2], frm, to;
14
    couple operator + (const couple & a, const couple & b)
15
    \{return couple (a.x + b.x, a.y + b.y); \}
    couple operator - (const couple & a, const couple & b)
17
    \{return couple (a.x - b.x, a.y - b.y); \}
18
    long long operator * (const couple & a, const couple & b)
19
    \{return a.x * b.y - a.y * b.x;\}
20
    bool operator < (const couple & a, const couple & b)
21
22
    \{return a.x < b.x  or a.x == b.x  and a.y < b.y; <math>\}
    typedef bool (* func) (const couple & a, const couple & b);
23
    bool lss (const couple & a, const couple & b) {return a < b;}
    bool grt(const couple & a, const couple & b) {return b < a;}
    void psh(int i)
26
27
         \mathbf{while}\,(\,c\,l \,>\, 1 \,\,\mathbf{\,and\,\,}\,(\,a\,[\,i\,] \,\,-\,\,q\,[\,c\,l\,]\,) \,\,\,*\,\,\,(\,q\,[\,c\,l\,] \,\,-\,\,q\,[\,c\,l \,\,-\,\,1\,]\,) \,\,<=\,0) \,\,c\,l\,--;
28
29
         q[++cl] = a[i];
30
31
    bool check (int mid)
32
    {
         return (x - q[mid]) * (q[mid + 1] - x) < 0;
33
34
35
    func cmp;
    void calc()
36
37
    {
38
         lb = lower\_bound(q + 1, q + 1 + cl, x, cmp) - q;
39
         if(lb = cl + 1 or lb = 1 or (q[lb] - x) * (x - q[lb - 1]) > 0)
40
41
               bs[0] = 1; bs[1] = lb - 1;
              while (bs [0] < bs [1] - 1)
42
43
                   mid = (bs[0] + bs[1]) / 2;
44
45
                   bs[check(mid)] = mid;
46
47
              frm = check(bs[0])?bs[0]:bs[1];
```

1.9. 点到凸包的切线

25

```
48
            bs[0] = lb - 1; bs[1] = cl - 1;
49
            while (bs [0] < bs [1] - 1)
50
51
                mid = (bs[0] + bs[1]) / 2;
                bs[!check(mid)] = mid;
52
53
            to = check(bs[1])?bs[1]:bs[0];
54
55
            if(!frm) ans1 += 0 * (x * q[1]);
            else if (to == cl) ans1 += 0 * (q[cl1] * x);
56
            else ans 1 += q[frm] * x + x * q[to + 1] - s[to] + s[frm - 1];
57
58
        }
59
60
   int main()
61
   {
62
        scanf("%d%d", &n, &Q);
63
        for(int i = 1; i \le n; i++) a[i].scan();
64
        sort(a + 1, a + 1 + n);
65
        q = q1; s = s1;
66
        c1 = 0;
67
        for(int i = 1; i \le n; i++)
68
69
            psh(i);
70
        }
71
        s[0] = 0;
        for (int i = 1; i < c1; i++) s[i] = s[i-1] + q[i] * q[i+1];
72
73
        cl1 = cl;
74
        q = q2; s = s2;
75
        c1 = 0;
76
        for(int i = n; i >= 1; i--)
77
        {
78
            psh(i);
79
        }
80
        s[0] = 0;
81
        for (int i = 1; i < c1; i++) s[i] = s[i-1] + q[i] * q[i+1];
82
        c12 = c1;
        ans = s1[c11 - 1] + s2[c12 - 1];
83
        for (int i = 1; i \le Q; i++)
84
85
86
            x.scan();
87
            ans1 = ans;
88
            cl = cl1; q = q1; s = s1; cmp = lss;
89
            calc();
            c1 = c12; q = q2; s = s2; cmp = grt;
90
91
            calc();
            ans1 = abs(ans1);
92
93
            printf("%lld.%c\n", ans1 / 2, ans1 % 2 == 1?'5':'0');
94
        fclose (stdin);
95
96
        return 0;
```

97 }

1.10 **判断圆存在交集** *NlogK*

```
传入 n 个圆 , 圆心存在 cir 中 , 半径存在 radius 中 , nlogk 判断是否存在交集
```

```
double sx, sy, d;
3
   vector < Point > cir;
   vector < double > radius;
6
   int isIntersectCircleToCircle(Point c1, double r1, Point c2, double r2)
7
8
        double dis = c1. distTo(c2);
9
        return sign (dis -(r1 + r2)) \leq 0;
10
   }
11
12
   void getRange(double x, Point &c, double r, double &retl, double &retr)
13
   {
        double tmp = sqrt(max(r * r - (c.x - x) * (c.x - x), 0.0));
14
15
        retl = c.y - tmp; retr = c.y + tmp;
16
   }
17
   int checkInLine(double x)
18
19
   {
20
        double minR = INF, maxL = -INF;
21
        double tmpl, tmpr;
22
        for(int i = 0; i < n; ++ i) {
23
             if (sign(cir[i].x + radius[i] - x) < 0 \mid | sign(cir[i].x - radius[i] - x) > 0)
24
                 return false;
25
             getRange(x, cir[i], radius[i], tmpl, tmpr);
26
             \max L = \max(tmpl, \max L);
27
             \min R = \min(tmpr, \min R);
28
             if (maxL > minR) return false;
29
30
        return true;
31
   }
32
33
   int shouldGoLeft(double x)
34
   {
35
        if (checkInLine(x)) return 2;
36
        int onL = 0, onR = 0;
37
        for(int i = 0; i < n; ++ i)
             if (sign(cir[i].x + radius[i] - x) < 0) onL = 1;
38
              \mbox{\bf if} \ ( \, sign \, ( \, cir \, [ \, i \, ] \, . \, x \, - \, radius \, [ \, i \, ] \, - \, x ) \, > \, 0 ) \ onR \, = \, 1; 
39
40
        if (onL && onR) return -1;
41
42
        if (onL) return 1;
43
        if (onR) return 0;
44
```

1.11. 圆与三角形的交面积

```
45
        double minR = INF, maxL = -INF, tmpl, tmpr;
46
        int idMinR , idMaxL;
47
48
        for(int i = 0; i < n; ++ i) {
             getRange\left(x\,,\ cir\left[\,i\,\right]\,,\ radius\left[\,i\,\right]\,,\ tmpl\,,\ tmpr\,\right);
49
             if (tmpr < minR)  {
50
51
                 minR = tmpr;
52
                 idMinR = i;
53
             if (tmpl > maxL)  {
54
                 \max L = tmpl;
55
56
                 idMaxL = i;
             }
57
58
59
        if (! isIntersectCircleToCircle(cir[idMinR], radius[idMinR], cir[idMaxL], radius[
            idMaxL]))
60
             return -1;
61
        Point p1, p2;
62
        intersectionCircleToCircle(cir[idMinR], radius[idMinR], cir[idMaxL], radius[
            idMaxL], p1, p2);
63
        return (p1.x < x);
64
   }
65
66 int hasIntersectionCircles()
67
    {
68
        double l = -INF, r = INF, mid;
        for(int i = 0; i < 100; ++ i) {
69
             mid = (l + r) * 0.5;
70
             int tmp = shouldGoLeft(mid);
71
72
             if (tmp < 0) return 0;
             if (tmp == 2) return 1;
73
74
             if (tmp) r = mid;
75
             else l = mid;
76
        }
        mid = (l + r) * 0.5;
77
        return checkInLine(mid);
78
   }
79
```

1.11 圆与三角形的交面积

```
1 #include<cstring>
2 #include<cstdio>
3 #include<algorithm>
4 #include<cmath>
5 using namespace std;
6 const double eps = 1e-12, PI = acos(-1.);
7 int sign(double x)
8 {
```

```
return x < -eps? -1:(x > eps? 1:0);
9
10
   struct triple
11
12
13
         double x, y, z;
14
         triple(){}
15
         triple (const double & _x, const double & _y, const double & _z) : x(_x), y(_y), z
             (_z){}
         void scan() {scanf("%lf%lf%lf", &x, &y, &z);}
16
17
         void print (char ch) { printf("%lf \\%lf \\%lf \\capsilon lf \\capsilon c", x, y, z, ch); }
         double sqrlen() const {return x * x + y * y + z * z;}
18
19
         double len() const {return sqrt(sqrlen());}
20
    } p1, p2, p3, dir, co;
21
    double sign(triple x)
22
   {
         \mathbf{return} \ \operatorname{sign}(\mathbf{x}.\mathbf{x}) = 0?(\operatorname{sign}(\mathbf{x}.\mathbf{y}) = 0?\operatorname{sign}(\mathbf{x}.\mathbf{z}):\operatorname{sign}(\mathbf{x}.\mathbf{y})):\operatorname{sign}(\mathbf{x}.\mathbf{x});
23
24
   }
25
   triple operator + (const triple & a, const triple & b)
26
         return triple (a.x + b.x, a.y + b.y, a.z + b.z);
27
28
    triple operator - (const triple & a, const triple & b)
29
30
         return triple (a.x - b.x, a.y - b.y, a.z - b.z);
31
32
33
   triple operator * (const double & a, const triple & b)
34
    {
         return triple(a * b.x, a * b.y, a * b.z);
35
36
37
    triple operator * (const triple & a, const triple & b)
38
    {
         return triple (a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x
39
             );
    }
40
    double operator % (const triple & a, const triple & b)
41
42
         return a.x * b.x + a.y * b.y + a.z * b.z;
43
44
45
46
    double t, ans, r;
47
    double fix (double x)
48
         if(x > 1) return 1;
49
         else if (x < -1) return -1;
50
51
         else return x;
52
    double calc(triple pa, triple pb)
53
54
55
              if(pa.len() < pb.len()) swap(pa, pb);
```

```
56
                                   if(pb.len() < eps) return 0;
  57
                                   double a, b, c, B, C, sinB, cosB, sinC, cosC, S, h, theta;
  58
                                   a = pb.len();
                                   b = pa.len();
  59
                                   c = (pb - pa).len();
  60
  61
                                   cosB = fix(pb \% (pb - pa) / a / c);
  62
                                   sinB = fix((pb * (pb - pa)).len() / a / c);
                                   B = a\cos(\cos B);
  63
                                   cosC = fix(pa \% pb / a / b);
  64
                                   sinC = fix((pa * pb).len() / a / b);
  65
  66
                                   C = a\cos(\cos C);
  67
                                   if(a > r)
  68
                                               S = C / 2 * r * r;
  69
                                               h = a * b * sinC / c;
  70
                                               if(h < r \text{ and } B < PI / 2) S = (acos(h / r) * r * r - h * sqrt(r * r 
  71
                                                           h));
  72
                                   else if(b > r)
  73
  74
                                               theta = PI - B - a\sin(fix(sinB / r * a));
                                               S = .5 * a * r * sin(theta) + (C - theta) / 2 * r * r;
  75
  76
  77
                                               S = .5 * sinC * a * b;
                                   //printf("\% lf \mid n", S);
  78
  79
                                   return S;
  80
  81 int main()
  82
            {
  83
                        p1.scan();
  84
                        p2.scan();
  85
                        p3.scan();
                        dir = (p2 - p1) * (p3 - p1);
  86
                        double t = dir \% p1 / (dir \% dir);
  87
  88
                        co = t * dir;
  89
                        //co.print(' \mid n');
                        if(co.sqrlen() > 10000)
  90
  91
  92
                                   printf("0\n");
  93
                                   return 0;
  94
                        r = sqrt(10000 - co.sqrlen());
  95
  96
                        p1 = p1 - co;
  97
                        p2 = p2 - co;
                        p3 = p3 - co;
  98
 99
                        double ans = 0;
100
                        ans += \operatorname{calc}(p1, p2) * \operatorname{sign}(p1 * p2);
                        ans += \operatorname{calc}(p2, p3) * \operatorname{sign}(p2 * p3);
101
                        ans += calc(p3, p1) * sign(p3 * p1);
102
103
                        printf("%.10f\n", fabs(ans));
```

```
104 fclose(stdin);
105 return 0;
106 }
```

1.12 圆与圆的交并面积

```
1 #include < cstring >
2 #include<cstdio>
3 #include<algorithm>
4 #include<cmath>
5 #include<vector>
6 using namespace std;
7
   double pi = a\cos(-1.0), eps = 1e-12;
   double sqr(const double & a) {return a * a;}
8
9
   double ans [1111];
   int sign (const double & a) {return a > eps?1:a < -eps?-1:0;}
10
   int n, cnt;
11
12
   struct couple
13
   {
14
       double x, y;
15
       couple(){}
16
       couple (const double \& \_x, const double \& \_y) : x(\_x), y(\_y) \{\}
17
       void scan() {scanf("%lf%lf", &x, &y);}
18
       double sqrlen() {return sqr(x) + sqr(y);}
19
       double len() {return sqrt(sqrlen());}
20
       couple rev() {return couple(y, -x);}
21
       couple zoom(const double & d) {double lambda = d / len(); return couple(lambda *
           x, lambda * y);}
22
   } dvd;
23
   double atan2(const couple & x) {return atan2(x.y, x.x);}
24
   couple operator - (const couple & a, const couple & b)
25
26
       return couple (a.x - b.x, a.y - b.y);
27
   }
   couple operator + (const couple & a, const couple & b)
28
29
   {
       return couple (a.x + b.x, a.y + b.y);
30
31
32
   double operator * (const couple & a, const couple & b)
33
   {
       return a.x * b.y - a.y * b.x;
34
35
   }
36
   couple operator * (const double & a, const couple & b)
37
       return couple(a * b.x, a * b.y);
38
39
40
   struct circle
41
   {
42
       double r; couple o;
```

1.12. 圆与圆的交并面积 31

```
43
        circle(){}
44
        void scan() {o.scan(); scanf("%lf", &r);}
   } cir[1111];
45
46
   struct arc
47
48
        double theta;
49
        int delta;
50
        couple p;
        arc(const double & _theta, const couple & _p, int _d) :theta(_theta), p(_p),
51
           delta(d){}
52
   };
53
   bool operator < (const arc & a, const arc & b) {return a.theta < b.theta;}
   vector<arc> vec;
   void psh(const double t1, const couple p1, const double t2, const couple p2)
56
   {
57
        if(t1 < t2)
58
59
            vec.push_back(arc(t1, p1, 1));
            vec.push\_back(arc(t2, p2, -1));
60
61
        }else
62
63
            vec.push back(arc(t1, p1, 1));
64
            vec.push\_back(arc(pi, dvd, -1));
65
            vec.push\_back(arc(-pi, dvd, 1));
            vec.push_back(arc(t2, p2, -1));
66
        }
67
68
   }
69
   int main()
70
   {
        freopen("cirut.in", "r", stdin);
71
72
73
        scanf("%d", &n);
74
        for (int i = 1; i \le n; i++) cir [i]. scan(), ans [i] = 0;
75
        for(int i = 1; i \le n; i++)
76
            vec.clear();
77
            dvd = cir[i].o - couple(cir[i].r, 0);
78
79
            vec.push\_back(arc(-pi, dvd, 1));
80
            for(int j = 1; j \le n; j++) if(j != i)
81
82
                double d = (cir[j].o - cir[i].o).sqrlen();
                if(d \le sqr(cir[j].r - cir[i].r))
83
84
                {
                    if(cir[i].r < cir[j].r)
85
86
                         psh(-pi, dvd, pi, dvd);
                else if(d < sqr(cir[j].r + cir[i].r))
87
88
                    double lambda = 0.5 * (1 + (sqr(cir[i].r) - sqr(cir[j].r))/d);
89
90
                    couple cp = cir[i].o + lambda * (cir[j].o - cir[i].o);
```

```
91
                     couple frm = cp + (cir[j].o - cir[i].o).rev().zoom(sqrt(sqr(cir[i].r))
                         - (cp - cir[i].o).sqrlen());
92
                     couple to = cp - (cir[i].o - cir[i].o).rev().zoom(sqrt(sqr(cir[i].r)
                        - (cp - cir[i].o).sqrlen()));
                     psh(atan2(frm - cir[i].o), frm, atan2(to - cir[i].o), to);
93
                 }
94
95
96
            sort(vec.begin() + 1, vec.end());
97
            vec.push\_back(arc(pi, dvd, -1));
98
            cnt = 0;
99
            for (int j = 0; j + 1 < vec. size(); j++)
100
                 cnt += vec[j].delta;
101
                 double theta = vec[j + 1]. theta - vec[j]. theta;
102
                 ans[cnt] += sqr(cir[i].r) * (theta - sin(theta)) * 0.5;
103
                 ans [cnt] += vec[j].p * vec[j + 1].p * 0.5;
104
105
            }
106
        }
107
        ans [n + 1] = 0;
        for (int i = 1; i \le n; i++) printf ("[%d] = \%.3lf\n", i, ans [i] - ans[i+1]);
108
109
        fclose (stdin);
110
        return 0;
111
```

1.13 Farmland

1.13.1 Logic_IU

```
1 #include < cstdio >
   #include < cstring >
 3 #include<vector>
 4 #include<cmath>
   #include<iostream>
   #include<algorithm>
7
8
   using namespace std;
9
   #define for each (e, x) for (\underline{\phantom{a}} type of (x. begin()) e = x. begin(); e != x. end(); ++ e
10
11
   typedef long long LL;
12
13
   typedef unsigned long long ULL;
   typedef pair<int, int> PII;
14
15
   const int N = 200 + 10;
16
17
18
   struct Point
19
   {
20
        double x, y;
21
        Point() {}
```

1.13. FARMLAND

33

```
22
        Point (double _x, double _y) {
23
             x = _x; y = _y;
24
25
        Point operator - (const Point &that) const {
26
             return Point (x - that.x, y - that.y);
27
28
        double det(const Point &that) const {
29
             return x * that.y - y * that.x;
30
31
        double alpha() {
32
             return atan2(y, x);
33
34
        void read() {
             scanf("\%lf\%lf", \&x, \&y);
35
36
37
   };
38
39 int n, m;
40 int vis[N][N];
41 int prev[N][N];
42 int in [N];
43 Point point [N], o;
44 \operatorname{vector} < \operatorname{int} > \operatorname{adj}[N];
45 vector < int > sqn;
46
47 int cmp(const int &u, const int &v)
48
   {
49
        Point pu = point[u] - o, pv = point[v] - o;
50
        return pu.alpha() < pv.alpha();
   }
51
52
   double calcArea (vector<int> &ps)
53
54
55
        double area = 0;
        for(int i = 0; i < (int)ps.size(); ++ i) {
56
             int j = i = (int)ps.size() - 1 ? 0 : i + 1;
57
             area += point[ps[i]].det(point[ps[j]]);
58
59
60
        return area;
61
   }
63 void dfs(int u, int v)
64
         \textbf{if} \ (\ vis\ [\ u\ ]\ [\ v\ ]) \ \ \textbf{return}\ ; 
65
66
        vis[u][v] = true;
67
        sqn.push_back(u);
68
        int w = prev[u][v];
69
        dfs(v, w);
70 }
```

```
71
72
    void solve()
73
    {
74
         cin >> n;
75
         for(int i = 0; i < n; ++ i) {
76
             adj[i].clear();
77
78
         \mathbf{int}\ u\,,\ v\,;
79
         for(int i = 0; i < n; ++ i) {
80
             cin \gg u; --u;
81
             point[u].read();
82
             int tot; cin >> tot;
             for(int j = 0; j < tot; ++ j)  {
83
                  scanf("%d", &v); -- v;
84
85
                  adj[u].push_back(v);
86
             }
87
         }
88
         cin >> m;
89
90
         for(int i = 0; i < n; ++ i)  {
91
             o = point[i];
92
             sort(adj[i].begin(), adj[i].end(), cmp);
93
94
         for(int i = 0; i < n; ++ i)
95
96
             for (int j = 0; j < (int) adj[i]. size(); ++ j) {
97
                  vis [i] [adj [i] [j]] = false;
                  int tmp = j = 0 ? adj[i].size() - 1 : j - 1;
98
                  prev[adj[i][j]][i] = adj[i][tmp];
99
100
             }
101
         }
102
103
         int ret = 0;
104
         for(int i = 0; i < n; ++ i)
105
             for(int j = 0; j < (int)adj[i].size(); ++ j) {
                  int v = adj[i][j];
106
                  if (vis[i][v]) continue;
107
                  sqn.clear();
108
109
                  dfs(i, v);
110
                  int flag = true;
111
                  if (calcArea(sqn) > 0) {
                      memset(in, 0, sizeof in);
112
                      for(int k = 0; k < (int)sqn.size(); ++ k) {
113
114
                           v = sqn[k];
                           if (in[v]) {
115
116
                               flag = false;
                               {\bf break}\,;
117
118
119
                           in[v] = true;
```

1.13. FARMLAND 35

```
120
                        \mathbf{if} ((\mathbf{int}) \operatorname{sqn.size}() == \mathbf{m})
121
122
                             ret += flag;
123
                   }
              }
124
125
126
          cout << ret << endl;</pre>
127
128
129 int main()
130 {
131
          int T; cin >> T;
132
          for (int i = 1; i \ll T; ++ i) {
133
              solve();
134
135
          return 0;
136
     1.13.2 tEJtM
 1 #include < cstring >
 2 #include < cstdio >
 3 #include < cmath >
 4 #include<vector>
 5 #include<algorithm>
 6 #include<map>
 7 using namespace std;
 8 double eps = 1e-12;
    struct couple
 9
 10
 11
          int x, y;
 12
          couple(){}
 13
          couple(int \underline{x}, int \underline{y}) : x(\underline{x}), y(\underline{y}) \{\}
 14
          void scan() { scanf("%d%d", &x, &y);}
    } a[222], c;
 16 int operator * (const couple & x, const couple & y) {return x.x * y.y - x.y * y.x;}
     int operator % (const couple & x, const couple & y) {return x.x * y.x + x.y * y.y;}
    couple operator - (const couple & x, const couple & y) {return couple(x.x - y.x, x.y
 18
         -y.y);}
   int k, n, x, y, ans, x1, Q, id[222];
 19
 20 bool flag, flag1;
    int area;
    vector<int> gen;
23 \operatorname{vector} < \operatorname{int} > \operatorname{vec} [222];
24 vector <bool> f [222];
 25 map<int, int> mp;
26 struct Polar
27
28
          couple o;
 29
          Polar (const couple & \_o) : o(\_o) {}
```

```
30
         bool operator () (const couple & a, const couple & b)
31
              return atan2((a - o).y, (a - o).x) < atan2((b - o).y, (b - o).x);
32
33
34
         bool operator () (int x, int y)
35
36
              return this->operator () (a[x], a[y]);
37
         }
38
    };
39
   int main()
40
   {
         freopen("01.in", "r", stdin);
41
         scanf("%d", \&Q);
42
43
         for (int qq = 1; qq \ll Q; qq++)
44
45
              scanf("%d", &n);
              mp.clear();
46
47
              for (int i = 1; i \le n; i++)
48
                   scanf("%d", &id[i]);
49
50
                   a[i].scan();
51
                   vec[i].clear();
52
                   f[i].clear();
                   scanf("%d", &x);
53
                   \mathbf{for}(\mathbf{int} \ \mathbf{j} = 0; \ \mathbf{j} < \mathbf{x}; \ \mathbf{j++}) \ \{\mathbf{scanf}(\text{``%d''}, \&\mathbf{y}); \ \mathbf{vec}[\mathbf{i}]. \ \mathbf{push\_back}(\mathbf{y}); \ \mathbf{f}[\mathbf{i}].
54
                       push_back(true);}
55
              scanf("%d", &k);
56
              for(int i = 1; i \le n; i++)
57
58
                   sort (vec[i].begin(), vec[i].end(), Polar(a[i]));
59
              for(int i = 1; i \le n; i++) for(int j = 0; j < vec[i].size(); j++) if(f[i][j])
60
                   1)
61
62
                   x = i;
63
                   y = j;
64
                   gen.clear();
65
                   for (;;) {
66
                        f[x][y] = false;
67
                        gen.push_back(x);
68
                        x1 = x;
                        x = vec[x][y];
69
70
                        y = lower_bound(vec[x].begin(), vec[x].end(), x1, Polar(a[x])) - vec[
                            x ] . begin ();
71
                        y = (y + 1) \% vec[x]. size();
72
                        if(x = i \text{ and } y = j) \text{ break}; //break \text{ when } x = i \text{ and } y = j, \text{ not only}
                            x == i!
73
                   if(gen.size() != k) continue;
74
```

1.13. FARMLAND 37

```
75
                                                                                                                                                      gen.push_back(gen.front());
 76
                                                                                                                                                      area = 0;
                                                                                                                                                       for(int i = 0; i + 1 < gen.size(); i++) area += a[gen[i]] * a[gen[i + 1]] + a[gen[i]] + 
 77
                                                                                                                                                                                         1]]; //printf("%d %d %lf \n", gen[i], gen[i + 1], a[gen[i]] * a[gen[i + 1]] * a[gen[i]] 
                                                                                                                                                                                         1]]);}
 78
                                                                                                                                                       if(area >= 0) continue;
  79
                                                                                                                                                       flag = true;
 80
                                                                                                                                                       for(int i = 0; i + 2 < gen.size(); i++) \{for(int j = i + 1; j + 1 < gen.
                                                                                                                                                                                      size(); j++) if(gen[i] = gen[j]) {flag = false; break;} if(flag = false)
                                                                                                                                                                                      false) break;}
81
                                                                                                                                                      ans += flag;
 82
 83
                                                                                                                printf("%d\n", ans);
 84
                                                                         fclose(stdin);
 85
                                                                         return 0;
 86
87 }
```

38 CHAPTER 1. 二维几何

Chapter 2

三维几何

2.1 **三维几何** Seraphim Version

2.1.1 基本操作

```
//vlen(point3\ P): length\ of\ vector;\ zero(double\ x): if\ fabs(x) < eps)\ return\ true;
  double vlen (point3 p);
  //平面法向量
4
   point3 pvec(point3 s1, point3 s2, point3 s3){return det((s1-s2),(s2-s3));}
   //共线 check
   int dots_inline(point3 p1, point3 p2, point3 p3){
7
        return vlen (\det(p1-p2, p2-p3)) < eps; 
8
   //共平面 check
9
   int dots onplane (point 3 a, point 3 b, point 3 c, point 3 d) {
10
        return zero (dot(pvec(a,b,c),d-a));
11
   //在线段上check(end point inclusive)
   int dot_online_in(point3 p, line3 l)
   int dot_online_in(point3 p,point3 l1,point3 l2){return zero(vlen(det(p-l1,p-l2)))&&(
       11.x-p.x)*(12.x-p.x)<eps&&(11.y-p.y)*(12.y-p.y)<eps&&(11.z-p.z)*(12.z-p.z)<eps;
14
   //在线段上check(end point exclusive)
  int dot_online_ex(point3 p, line3 l)
   int dot_online_ex(point3 p, point3 l1, point3 l2){ return dot_online_in(p, l1, l2)&&(!
       zero (p.x-l1.x) | | ! zero (p.y-l1.y) | | ! zero (p.z-l1.z) ) && (!zero (p.x-l2.x) | | ! zero (p.y-l2.
       y) | | ! zero(p.z-12.z) ;
17
   //一个点是否在三角形里 check (in clusive)
18
   int dot_inplane_in(point3 p, plane3 s)
   int dot_inplane_in(point3 p, point3 s1, point3 s2, point3 s3){
21
        return zero (vlen (det (s1-s2, s1-s3))-vlen (det (p-s1, p-s2))-
22
            vlen(det(p-s2, p-s3))-vlen(det(p-s3, p-s1)));
23
24
   //一个点是否在三角形里 check (exclusive)
25 int dot_inplane_ex(point3 p, plane3 s)
   int dot_inplane_ex(point3 p, point3 s1, point3 s2, point3 s3){
```

```
27
        return dot_inplane_in(p,s1,s2,s3) & vlen(det(p-s1,p-s2)) > eps &
28
            vlen(det(p-s2, p-s3)) > eps&&vlen(det(p-s3, p-s1)) > eps;
29
30
   //check if two point and a segment in one plane have the same side
   int same_side(point3 p1, point3 p2, point3 l1, point3 l2)
31
32
   int same_side(point3 p1, point3 p2, line3 l){
33
        return dot(det(1.a-l.b,p1-l.b),det(1.a-l.b,p2-l.b))>eps;
34
35
   //check if two point and a segment in one plane have the opposite side
36
   int opposite side (point3 p1, point3 p2, point3 l1, point3 l2)
   int opposite_side(point3 p1, point3 p2, line3 l){
37
38
        return dot(det(l.a-l.b,p1-l.b), det(l.a-l.b,p2-l.b))<-eps;
39
40
   //check if two point is on the same side of a plane
41
   int same_side(point3 p1,point3 p2,point3 s1,point3 s2,point3 s3)
42
   int same_side(point3 p1, point3 p2, plane3 s){
43
        return dot(pvec(s), p1-s.a)*dot(pvec(s), p2-s.a)>eps;
44
45
   //check if two point is on the opposite side of a plane
   int opposite_side(point3 p1, point3 p2, point3 s1, point3 s2, point3 s3)
46
   int opposite_side(point3 p1,point3 p2,plane3 s){
47
48
        return dot(pvec(s), p1-s.a)*dot(pvec(s), p2-s.a)<-eps;
49
50
   //check if two straight line is parallel
51
   int parallel (point3 u1, point3 u2, point3 v1, point3 v2)
   int parallel(line3 u, line3 v){
                                       return vlen(det(u.a-u.b,v.a-v.b)) < eps;
53
   //check if two plane is parallel
54
   int parallel (point 3 u1, point 3 u2, point 3 u3, point 3 v1, point 3 v2, point 3 v3)
   int parallel(plane3 u, plane3 v){return vlen(det(pvec(u), pvec(v)))<eps;}</pre>
55
   //check if a plane and a line is parallel
56
57
   int parallel (point 3 l1, point 3 l2, point 3 s1, point 3 s2, point 3 s3)
   int parallel(line3 1,plane3 s){ return zero(dot(1.a-1.b,pvec(s))); }
58
59
   //check if two line is perpendicular
   int perpendicular (point3 u1, point3 u2, point3 v1, point3 v2)
60
   int perpendicular(line3 u, line3 v){return zero(dot(u.a-u.b,v.a-v.b)); }
61
   //check if two plane is perpendicular
62
63
   int perpendicular (point3 u1, point3 u2, point3 u3, point3 v1, point3 v2, point3 v3)
64
   int perpendicular(plane3 u, plane3 v){
                                              return zero (dot(pvec(u), pvec(v))); }
65
   //check if plane and line is perpendicular
   int perpendicular (point3 11, point3 12, point3 s1, point3 s2, point3 s3)
66
67
   int perpendicular (line 3 l, plane 3 s) {return vlen (det (l.a-l.b, pvec(s))) < eps;}
   //check 两条线段是否有交点(end point inclusive)
68
   int intersect_in (point3 u1, point3 u2, point3 v1, point3 v2)
69
   int intersect_in(line3 u, line3 v){
70
71
        if (!dots_onplane(u.a,u.b,v.a,v.b)) return 0;
72
        if (!dots_inline(u.a,u.b,v.a)||!dots_inline(u.a,u.b,v.b))
73
            return ! same_side (u.a, u.b, v) \&\&! same_side (v.a, v.b, u);
74
        return dot_online_in(u.a,v) | | dot_online_in(u.b,v) | |
   dot\_online\_in(v.a, u) | | dot\_online\_in(v.b, u);
```

```
76
77
    //check 两条线段是否有交点(end point exclusive)
   int intersect_ex(point3 u1, point3 u2, point3 v1, point3 v2)
79 int intersect_ex(line3 u, line3 v){
        80
81
    opposite_side(v.a,v.b,u);
82
    }
83
    //线段和三角形是否有交点check(end point and border inclusive)
84 int intersect_in(point3 l1, point3 l2, point3 s1, point3 s2, point3 s3)
    int intersect_in(line3 l, plane3 s){
86
        return !same_side(1.a,1.b,s)&&!same_side(s.a,s.b,1.a,1.b,s.c)&&
87
            !same_side(s.b,s.c,l.a,l.b,s.a)&&!same_side(s.c,s.a,l.a,l.b,s.b);
88
    }
89
    //线段和三角形是否有交点check(end point and border exclusive)
    int intersect_ex(point3 l1, point3 l2, point3 s1, point3 s2, point3 s3)
    int intersect_ex(line3 l, plane3 s){
91
        return opposite_side(1.a, 1.b, s)&&opposite_side(s.a, s.b, 1.a, 1.b, s.c)&&
92
            opposite_side(s.b,s.c,l.a,l.b,s.a)&&opposite_side(s.c,s.a,l.a,l.b,s.b);}
93
    //calculate the intersection of two line
    //Must you should ensure they are co-plane and not parallel
    point3 intersection (point3 u1, point3 u2, point3 v1, point3 v2)
95
96
    point3 intersection(line3 u, line3 v){
97
        point3 ret=u.a;
        double t = ((u.a.x-v.a.x)*(v.a.y-v.b.y)-(u.a.y-v.a.y)*(v.a.x-v.b.x))
98
99
                 /((u.a.x-u.b.x)*(v.a.y-v.b.y)-(u.a.y-u.b.y)*(v.a.x-v.b.x));
100
    ret += (u.b-u.a)*t;
                         \mathbf{return} \ \ \mathbf{ret} \ ;
101
    }
102
    //calculate the intersection of plane and line
103
    point3 intersection (point3 11, point3 12, point3 s1, point3 s2, point3 s3)
104
    point3 intersection (line3 1, plane3 s) {
105
        point3 ret=pvec(s);
    double t = (ret.x*(s.a.x-l.a.x)+ret.y*(s.a.y-l.a.y)+ret.z*(s.a.z-l.a.z))/
106
            (ret.x*(1.b.x-1.a.x)+ret.y*(1.b.y-1.a.y)+ret.z*(1.b.z-1.a.z));
107
108
        ret=1.a + (1.b-1.a)*t;
                                    return ret;
109
    }
110
    //calculate the intersection of two plane
    bool intersection (plane3 pl1 , plane3 pl2 , line3 &li) {
111
112
        if (parallel(pl1, pl2)) return false;
113
        li.a=parallel(pl2.a,pl2.b, pl1) ? intersection(pl2.b,pl2.c, pl1.a,pl1.b,pl1.c) :
            intersection (pl2.a, pl2.b, pl1.a, pl1.b, pl1.c);
114
        point3 fa; fa=det(pvec(pl1),pvec(pl2));
115
        li.b=li.a+fa;
116
        return true;
117
118
    //distance from point to line
    double ptoline (point3 p, point3 11, point3 12)
119
120
    double ptoline (point3 p, line3 1) {
121
        return vlen (det (p-l.a, l.b-l.a))/distance(l.a, l.b);}
122
    //distance from point to plane
```

```
123
    double ptoplane (point 3 p, plane 3 s) {
124
        return fabs (dot(pvec(s),p-s.a))/vlen(pvec(s));}
125
    double ptoplane (point3 p, point3 s1, point3 s2, point3 s3)
126
    //distance between two line 当
                                         u,平行时有问题v
    double linetoline (line3 u, line3 v) {
127
128
        point3 n=det(u.a-u.b,v.a-v.b); return fabs(dot(u.a-v.a,n))/vlen(n);
129
130
    double linetoline (point 3 u1, point 3 u2, point 3 v1, point 3 v2)
    //cosine value of the angle formed by two lines
131
132
    double angle cos(line3 u, line3 v){
        return dot(u.a-u.b, v.a-v.b)/vlen(u.a-u.b)/vlen(v.a-v.b);
133
134
    double angle_cos(point3 u1, point3 u2, point3 v1, point3 v2)
135
    //cosine value of the angle formed by two planes
136
    double angle_cos(plane3 u, plane3 v){
137
        return dot(pvec(u), pvec(v))/vlen(pvec(u))/vlen(pvec(v));
138
139
    double angle_cos(point3 u1, point3 u2, point3 u3, point3 v1, point3 v2, point3 v3)
140
    //cosine value of the angle formed by plane and line
    double angle_sin(line3 l, plane3 s){
141
142
        return dot(1.a-1.b, pvec(s))/vlen(1.a-1.b)/vlen(pvec(s));}
    double angle_sin(point3 l1, point3 l2, point3 s1, point3 s2, point3 s3)
143
           三维旋转操作
    2.1.2
    a 点绕 Ob 向量, 逆时针旋转弧度 angle, sin(angle), cos(angle) 先求出来,减少精度问题。
 1
    point e1, e2, e3;
    point Rotate (point a, point b, double angle) {
 3
        b. std();//单位化,注意不能为b(0,0,0)
        e3=b; double lens=a*e3;//dot(a,e3)
 4
 5
        e1=a - e3*lens; if (e1.len()>(1e-8)) e1.std(); else return a;
 6
        e2=e1/e3; //det(e1, e3)
 7
        double x1, y1, x, y;
        y1=a*e1; x1=a*e2;
 8
 9
        x=x1*cos(angle) - y1*sin(angle);
 10
        y=x1*sin(angle) + y1*cos(angle);
11
        return e3*lens + e1*y + e2*x;
12
   }
    2.1.3 三维凸包随机增量
 1 #include<iostream>
 2 #include < cstring >
 3 #include<algorithm>
 4 #include<vector>
```

5 #include < cmath > 6 #include < cstdio >

9 #define Eps 1E-8

using namespace std;

8 #define SIZE(X) (int(X.size()))

```
10 #define PI 3.14159265358979323846264338327950288
  inline int Sign(double x) {
12
       return x < -Eps ? -1 : (x > Eps ? 1 : 0);
13 }
   inline double Sqrt(double x) {
14
15
       return x < 0? 0 : sqrt(x);
16
17
   struct Point {
18
       double x, y, z;
19
       Point() {
20
           x = y = z = 0;
21
22
       Point (double x, double y, double z): x(x), y(y), z(z) {}
       bool operator <(const Point &p) const {
23
24
           return \ x < p.x \ | | \ x == p.x \&\& y < p.y \ | | \ x == p.x \&\& y == p.y \&\& z < p.z;
25
       bool operator ==(const Point &p) const {
26
27
           28
29
       Point operator +(const Point &p) const {
30
           return Point (x + p.x, y + p.y, z + p.z);
31
32
       Point operator -(const Point &p) const {
33
           return Point (x - p.x, y - p.y, z - p.z);
34
       Point operator *(const double k) const {
35
           return Point (x * k, y * k, z * k);
36
37
       Point operator /(const double k) const {
38
39
           return Point (x / k, y / k, z / k);
40
41
       Point cross (const Point &p) const {
           return Point(y * p.z - z * p.y, z * p.x - x * p.z, x * p.y - y * p.x);
42
43
       double dot(const Point &p) const {
44
           return x * p.x + y * p.y + z * p.z;
45
46
47
       double norm() {
48
           return dot(*this);
49
50
       double length() {
           return Sqrt(norm());
51
52
       void read() {
53
           scanf("%1f%1f%1f", &x, &y, &z);
54
55
56
       void write() {
           printf("(\%.10f, \%.10f, \%.10f) \ , x, y, z);
57
58
```

```
59
    };
60
    int mark[1005][1005];
    Point info [1005];
62
    int n, cnt;
    double mix(const Point &a, const Point &b, const Point &c) {
63
64
         return a.dot(b.cross(c));
65
66
    double area (int a, int b, int c) {
         \mathbf{return} \ ((\inf o [b] - \inf o [a]) . \operatorname{cross}(\inf o [c] - \inf o [a])) . \operatorname{length}();
67
68
69
    double volume(int a, int b, int c, int d) {
70
         return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]);
    }
71
    struct Face {
72
73
         int a, b, c;
74
         Face() {}
75
         Face(int a, int b, int c): a(a), b(b), c(c) {}
76
         int &operator [](int k) {
77
              if (k == 0) return a;
78
              if (k == 1) return b;
79
              return c;
         }
80
81
     };
82
    vector <Face> face;
    inline void insert(int a, int b, int c) {
83
84
         face.push_back(Face(a, b, c));
85
    }
86
    void add(int v) {
87
         vector <Face> tmp;
88
         int a, b, c;
89
         cnt ++;
90
         for (int i = 0; i < SIZE(face); i ++) {
91
              a = face[i][0];
              b = face[i][1];
92
93
              c = face[i][2];
94
              if (Sign(volume(v, a, b, c)) < 0)
                   \operatorname{mark}[a][b] = \operatorname{mark}[b][a] = \operatorname{mark}[b][c] = \operatorname{mark}[c][b] = \operatorname{mark}[c][a] =
95
96
                       mark[a][c] = cnt;
97
              else
98
                  tmp.push_back(face[i]);
99
100
         face = tmp;
         for (int i = 0; i < SIZE(tmp); i ++) {
101
              a = face[i][0];
102
              b = face[i][1];
103
              c = face[i][2];
104
              if (mark[a][b] = cnt) insert(b, a, v);
105
106
              if (\max[b][c] = cnt) insert(c, b, v);
107
              if (mark[c][a] = cnt) insert(a, c, v);
```

```
108
          }
109
     }
110
     int Find() {
111
          for (int i = 2; i < n; i ++) {
               Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
112
113
               if (ndir == Point())
114
                    continue;
115
               swap(info[i], info[2]);
               for (int j = i + 1; j < n; j ++)
116
                    if (Sign(volume(0, 1, 2, j)) != 0) {
117
                         swap(info[j], info[3]);
insert (0, 1, 2);
118
119
                         insert (0, 2, 1);
120
121
                         return 1;
122
123
124
          return 0;
125
     }
     int main() {
126
127
          double ans, ret;
128
          int Case;
          \mathbf{for} \ (\, \operatorname{scanf} \left(\, \text{``%d''} \,, \, \, \& \operatorname{Case} \,\right) \,; \ \operatorname{Case} \,; \ \operatorname{Case} \,, \, \, --) \ \left\{\, \right.
129
130
               scanf("%d", &n);
131
               for (int i = 0; i < n; i ++)
                    info[i].read();
132
133
               sort(info, info + n);
               n = unique(info, info + n) - info;
134
135
               face.clear();
               random_shuffle(info, info + n);
136
137
               ans = ret = 0;
138
               if (Find()) {
                    memset(mark, 0, sizeof(mark));
139
140
                    cnt = 0;
                    for (int i = 3; i < n; i ++) add(i);
141
                    int first = face [0][0];
142
                    for (int i = 0; i < SIZE(face); i ++) {
143
                         ret += area(face[i][0], face[i][1], face[i][2]);
144
145
                         ans += fabs(volume(first, face[i][0], face[i][1], face[i][2]));
146
                    }
147
                    ans \neq 6;
148
                    ret /= 2;
149
150
               printf("\%.3f\\n", ret, ans);
151
152
          return 0;
153
```

2.2 基本操作 tEJtM Version

```
1
   struct triple
2
3
        double x, y, z;
4
        triple(){}
        triple(const double & _x, const double & _y, const double & _z) : x(_x), y(_y), z(
5
        double len2() const {return x * x + y * y + z * z;}
6
7
        double len() const {return sqrt(len2());}
        void scan() {scanf("%lf%lf%lf", &x, &y, &z);}
8
9
   };
   triple operator + (const triple & a, const triple & b)
10
   \{return triple (a.x + b.x, a.y + b.y, a.z + b.z); \}
11
   triple operator - (const triple & a, const triple & b)
12
   \{return triple (a.x - b.x, a.y - b.y, a.z - b.z); \}
   triple operator * (const double & a, const triple & b)
14
   {return triple(a * b.x, a * b.y, a * b.z);}
15
   triple operator * (const triple & a, const triple & b)
16
   \{ \text{return triple} (a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x) \} \}
   double operator % (const triple & a, const triple & b)
   {return a.x * b.x + a.y * b.y + a.z * b.z;}
19
   struct line
20
21
22
        triple s, d;
23
        line(){}
        line(const triple \& \_s, const triple \& \_d) : s(\_s), d(\_d) {}
24
25
        triple operator () const {return d;}
26
   };
27
   struct plane
28
   {
29
        triple a, n;
30
        plane()
31
        plane(const triple & _a, const triple & _n) :a(_a), n(_n){}
32
        plane (const triple & a, const triple & b, const triple & c)
33
        \{a = \underline{a}; n = (b - a) * (b - c);\}//valid for non-colinear \underline{a}, \underline{b}, \underline{c}.
34
   };
   const double eps = 1e-12;
35
36
   int sign (const double & x)
   \{ \mathbf{return} \ x < -\mathbf{eps}? -1: x > \mathbf{eps}? 1: 0; \}
37
38
   //判断 相交平行垂直
39
40
  bool parallel(const triple & a, const triple & b)//向量平行
41
        return sign((a * b).len2()) == 0;
42
43
   bool orthogonal(const triple & a, const triple & b)//向量垂直
44
45
   {
        return sign(a \% b) = 0;
46
47
```

bool dis(const triple & a, const line & b)//点到直线距离 无正负

```
49
       return ((a - b.s) * b.d).len() / b.d.len();
50
   }//做三角形求高法
51
   bool perpendicular (const triple & a, const triple & b) //点到直线垂线
52
53
54
       return line (a, b.d * (b.s - a) * b.d);
   }//若是点在直线上则求出来方向为的直线0
55
   bool on(const triple & a, const line & b)//点在直线上
56
57
       return parallel(a - b.s, b.d);
58
59
   bool parallel(const line & a, const line & b)//直线平行
60
61
62
       return parallel(a.d, b.d);
63
   }//重合也算平行
64
   bool orthogonal(const line & a, const line & b)//直线垂直
65
66
       return orthogonal(a.d, b.d);
67
   double dis(const line & a, const line & b)//直线间最近距离 无正负
68
69
70
       triple nor = a.d * b.d;
       if(sign(nor.len2()) = 0) return dis(b.s, a); //平行直线距离
71
72
       else return nor % (a.s - b.s) / nor.len();//不平行直线最近距离
73
74
   bool intersect (const line & a, const line & b)//直线相交距离为:0
75
       return sign(dis(a, b)) == 0;
76
77
78
   triple intersection(const line & a, const line & b)//直线交点 假设不平行且交点存在
79
80
       double lambda = (b.s - a.s) * b.d % (a.d * b.d) / (a.d * b.d).len2();
81
       return a.s + lambda * a.d;
82
   }//若是不平行交点也不存在则求出来的是条直线最近距离两点中第一条直线上的那个点2
83
84
85
   bool on Ray (const triple & a, const line & b) //点在射线上 含
86
       return on(a, b) and sign((a - b.s) % (b.d)) \geq 0;
87
88
   bool on Seg(const triple & a, const triple & b, const triple & c)//点在线段上 含
89
90
       return on Ray(a, line(b, c - b)) and on Ray(a, line(c, b - c));
91
92
   ^{1}^{1}//有了上面个函数就可以处理射线^{2} 线段和直线相互之间存在交点的问题了
93
   //下面是有关平面的算法
94
95
   int dis(const triple & a, const plane & b)//点到平面距离 有正负
96
97
       return (a - b.a) \% b.n;
```

```
98
    }
   int above (const triple & a, const plane & b) //above_1 on_0 under_-1
99
100
        return sign(dis(a, b));//和法向同向的算是平面的上面
101
102
    bool parallel(const line & a, const plane & b)//直线和平面平行 重合也算平行
103
104
105
        return orthogonal(a.d, b.n);
106
107
    bool parallel (const plane & a, const plane & b) //平面和平面平行
108
109
        return parallel(a.n, b.n);
110
111
    bool intersect (const line & a, const plane & b) //直线和平面相交?
112
113
    {
        return !parallel(a, b) or sign(a.s * b.n - b.s * b.n) == 0; //不平行或在平面内部
114
115
    triple intersection (const line & a, const plane & b) //直线和平面的交点
116
117
        double lambda = b.n \% (b.a - a.s) / (a.d \% b.n);
118
119
        return a.s + lambda * a.d;
120
121
    line intersection (const plane & a, const plane & b) //平面和平面的交线
122
        return line(intersection(line(a.a, a.n * b.n * a.n)), a.n * b.n);
123
124
    }
```

2.3 点类 + 三维凸包 N^3+ 凸包求重心

```
1 #include < cstring >
    2 #include<cstdio>
    3 #include<vector>
    4 #include<algorithm>
    5 #include<set>
    6 #include<string>
    7
                 #include<cmath>
    8
                  using namespace std;
   9
                 multiset < string > st;
10
                  struct triple
11
                  {
12
                                          double x, y, z;
13
                                         double sqrlen() {return x * x + y * y + z * z;}
14
                                         double len() {return sqrt(sqrlen());}
15
                                           triple(){}
                                           \label{eq:continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous_continuous
16
17
                   } a[111];
                   char name [111] [211];
18
                   bool flag, ext[111];
```

```
int 1, real[111], cnt, n, f[111][111];
20
21
   struct plane
22
23
        int a [3];
        plane(int _x, int _y, int _z)
24
25
26
            a[0] = _x;
27
            a[1] = _y;
28
            a[2] = _z;
29
30
        int & operator [] (int x)
31
32
            return a[x];
33
34
   };
35
   vector < plane > surf;
   triple operator * (const triple & a, const triple & b)
37
        return triple (a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x
38
           );
39
   triple operator * (const double & lambda, const triple & b)
40
41
        return triple(lambda * b.x, lambda * b.y, lambda * b.z);
42
43
   double operator % (const triple & a, const triple & b)
44
45
        return a.x * b.x + a.y * b.y + a.z * b.z;
46
47
   triple operator - (const triple & a, const triple & b)
48
49
        return triple (a.x - b.x, a.y - b.y, a.z - b.z);
50
51
   triple operator + (const triple & a, const triple & b)
52
53
        return triple (a.x + b.x, a.y + b.y, a.z + b.z);
54
55
56
   double volume (const triple & o, int j)//volume of a tetrahedron := {a point and a
       triangle undersurface \}
57
        return (a[surf[j][0]] - o) * (a[surf[j][1]] - o) % (a[surf[j][2]] - o); // can be
58
           negative
59
   double volume(int i, int j)
60
61
        return volume(a[i], j);
62
63
   double above(int i, int j) {return volume(i, j) > 0;} //point above plane
64
   double on (int i, int j) {return volume(i, j) = 0;}//point on plane
```

```
void print(const triple & x, char ch)
66
67
    {
        printf("(\%lf, ...\%lf, ...\%lf)\%c", x.x, x.y, x.z, ch);
68
69
    double dis(const triple & o, int j)//point to plane
70
71
    {
        72
           surf[j][0]])).len());
73
    }
74
   int main()
75
    {
76
        double ans = 0;
77
        for (int cv = 1; cv \ll 2; cv++)
78
79
            scanf("%d", &n);
80
            for(int i = 1; i \le n; i++)
81
                scanf("%lf%lf", &a[i].x, &a[i].y, &a[i].z);
82
83
            }
84
            //-> degenerate checking
            flag = false;
85
            for (int i = 3; i \le n; i++)
86
87
                if(((a[1] - a[i]) * (a[2] - a[i])).sqrlen() != 0)
88
89
                    swap(a[3], a[i]);
90
                    swap(real[i], real[3]);
91
92
                    for(int j = 4; j \le n; j++)
93
                        if((a[1] - a[j]) * (a[2] - a[j]) % (a[3] - a[j]) != 0)
94
95
96
                            swap(a[4], a[j]);
97
                            swap(real[4], real[j]);
98
                            flag = true;
99
                            break;
                        }
100
101
102
                    break;
103
                }
104
105
106
107
                //degenerate!
            } else
108
109
            //->convex polyhedra
110
            memset(f, 0, sizeof(f));
111
112
            surf.clear();
113
            surf.push_back(plane(1, 2, 3));
```

```
114
              surf.push_back(plane(3, 2, 1));
115
              for (int i = 4; i <= n; i++)
116
117
                   vector < plane > tmp;
                   for(int j = 0; j < surf.size(); j++)
118
119
                       if (above(i, j))
120
121
                            for (int d = 0; d < 3; d++)
122
                                 f[surf[j][d]][surf[j][(d + 2) \% 3]] = i;
123
124
125
                       }else
126
                            tmp.push_back(surf[j]);
127
128
                   surf = tmp;
129
                   for(int j = surf.size() - 1; j >= 0; j--)
130
131
132
                       for (int d = 0; d < 3; d++)
                            \mathbf{if}(\,f\,[\,surf\,[\,j\,]\,[\,d\,]\,]\,[\,surf\,[\,j\,]\,[\,(\,d\,+\,1)\,\,\%\,\,3\,]\,] \,==\, i\,) \ surf\,.\,push\_back\,(\,plane)
133
                                (surf[j][(d + 1) \% 3], surf[j][d], i));
134
135
              //end\ convex\ polyhedra , result\ :=\ surf
136
137
              //->centre of gravity
138
              double svol = 0;
              triple qc(0, 0, 0);
139
140
              for (int i = 0; i < surf.size(); i++)
141
                   double vol1 = volume(1, i);
142
                   qc = qc + (vol1 / 4)^* (a[1] + a[surf[i][0]] + a[surf[i][1]] + a[surf[i][1]]
143
                      |[2]|;
144
                   svol += vol1;
145
              }
146
              qc = (1 / svol) * qc;
              double mn = 1e9;
147
              for (int i = 0; i < surf.size(); i++)
148
149
150
                  mn = min(mn, dis(qc, i));
151
152
              ans += mn;
              //end centre of gravity
153
              //}
154
155
         printf("\%.5f\n", ans);
156
157
         fclose (stdin);
158
         return 0;
159
   }
```

2.4 三维旋转

```
//sgu265
2 #include < cstring >
3 #include<cstdio>
4 #include<cmath>
5 #include<algorithm>
6
   using namespace std;
7
   const double pi = acos(-1.0);
8 int n, m; char ch1; bool flag;
   double a[4][4], s1, s2, x, y, z, w, b[4][4], c[4][4];
   double sqr(double x)
10
11
12
        return x*x;
13
14
   int main()
15
   {
        \operatorname{scanf}("%d \ n", \&n);
16
17
        memset(b, 0, sizeof(b));
        b[0][0] = b[1][1] = b[2][2] = b[3][3] = 1; //initial matrix
18
19
        for(int i = 1; i \le n; i++)
20
21
            scanf("%c", &ch1);
22
            if(ch1 = 'T')
23
24
                 //plus each coordinate by a number (x, y, z)
25
                \operatorname{scanf}("\% \operatorname{lf}_{\square}\% \operatorname{lf}_{\backslash} ", \&x, \&y, \&z);
26
                memset(a, 0, sizeof(a));
27
                a[0][0] = 1; a[3][0] = x;
28
                a[1][1] = 1; a[3][1] = y;
29
                a[2][2] = 1; a[3][2] = z;
30
                a[3][3] = 1;
            else if(ch1 = 'S')
31
32
33
                 //multiply each coordinate by a number (x, y, z)
                 34
                 memset(a, 0, sizeof(a));
35
36
                a[0][0] = x;
37
                a[1][1] = y;
38
                a[2][2] = z;
39
                a[3][3] = 1;
40
            }else
41
42
                 //rotate in a clockwise about the ray from the origin through (x, y, z);
                 scanf("%lf_\%lf_\%lf\n", &x, &y, &z, &w);
43
44
                w = w*pi/180;
45
                memset(a, 0, sizeof(a));
                s1 = x*x+y*y+z*z;
46
47
                a[3][3] = 1;
```

2.5. 最小球覆盖 53

```
48
                                                     a[0][0] = ((y^*y+z^*z)^*\cos(w)+x^*x)/s1;
49
                                                     a[0][1] = x^*y^*(1-\cos(w))/s1+z^*\sin(w)/sqrt(s1);
50
                                                     a[0][2] = x*z*(1-\cos(w))/s1-y*\sin(w)/sqrt(s1);
                                                     a[1][0] = x*y*(1-\cos(w))/s1-z*\sin(w)/sqrt(s1);
51
                                                     a[1][1] = ((x*x+z*z)*cos(w)+y*y)/s1;
52
                                                                               = y*z*(1-\cos(w))/s1+x*\sin(w)/sqrt(s1);
53
                                                     a [1][2]
                                                     a[2][0] = x*z*(1-\cos(w))/s1+y*\sin(w)/sqrt(s1);
54
55
                                                     a[2][1] = y*z*(1-cos(w))/s1-x*sin(w)/sqrt(s1);
                                                     a[2][2] = ((x*x+y*y)*cos(w)+z*z)/s1;
56
57
                                       memset(c, 0, sizeof(c));
58
59
                                       for (int i = 0; i < 4; i++)
                                                     for(int j = 0; j < 4; j++)
60
                                                                   for (int k = 0; k < 4; k++)
61
62
                                                                                c[i][j] += b[i][k]*a[k][j];
63
                                      memcpy(b, c, sizeof(c));
64
                         }
65
                         scanf("%d", &m);
66
                         for (int i = 1; i \le m; i++)
67
                                       scanf("%lf%lf%lf", &x, &y, &z);//initial vector
68
                                        printf("\%lf_{\bot}\%lf_{\bot}\%lf_{h}", x*b[0][0] + y*b[1][0] + z*b[2][0] + b[3][0], x*b[0][1] + y*b[1][0] + b[3][0] + b[3
69
                                                   [1][1] + z*b[2][1] + b[3][1], x*b[0][2] + y*b[1][2] + z*b[2][2] + b[3][2]);
70
71
                         return 0;
72
```

2.5 最小球覆盖

```
1 #include<iostream>
2 #include < cstring >
  #include < algorithm >
  #include<cstdio>
  #include<cmath>
6
7
   using namespace std;
8
9
   const int eps = 1e-8;
10
   struct Tpoint
11
12
   {
13
       double x, y, z;
14
   };
15
16
   int npoint, nouter;
17
18
   Tpoint pt[200000], outer[4], res;
   double radius, tmp;
   inline double dist (Tpoint p1, Tpoint p2) {
```

```
21
        double dx=p1.x-p2.x, dy=p1.y-p2.y, dz=p1.z-p2.z;
22
        return ( dx*dx + dy*dy + dz*dz );
23
   }
   inline double dot(Tpoint p1, Tpoint p2) {
24
25
        return p1.x*p2.x + p1.y*p2.y + p1.z*p2.z;
26
27
   void ball() {
28
        Tpoint q[3]; double m[3][3], sol[3], L[3], det;
29
        \mathbf{int} \quad i \ , j \ ;
        res.x = res.y = res.z = radius = 0;
30
31
        switch ( nouter ) {
32
            case 1: res=outer[0]; break;
33
            case 2:
                     res.x=(outer[0].x+outer[1].x)/2;
34
35
                     res.y=(outer[0].y+outer[1].y)/2;
36
                     res.z=(outer[0].z+outer[1].z)/2;
                     radius=dist(res, outer[0]);
37
38
                     break;
39
            case 3:
40
                     for (i=0; i<2; ++i)
                         q[i].x=outer[i+1].x-outer[0].x;
41
42
                         q[i].y=outer[i+1].y-outer[0].y;
43
                         q[i].z=outer[i+1].z-outer[0].z;
44
45
                     for (i=0; i<2; ++i) for (j=0; j<2; ++j)
46
                         m[i][j] = dot(q[i], q[j]) *2;
47
                     for (i=0; i<2; ++i) sol[i]=dot(q[i], q[i]);
48
                     if (fabs(det=m[0][0]*m[1][1]-m[0][1]*m[1][0]) < eps)
49
                         return;
                    L[0] = (sol[0]*m[1][1] - sol[1]*m[0][1]) / det;
50
51
                    L[1] = (sol[1]*m[0][0] - sol[0]*m[1][0]) / det;
52
                     res.x=outer[0].x+q[0].x*L[0]+q[1].x*L[1];
53
                     res.y=outer[0].y+q[0].y*L[0]+q[1].y*L[1];
54
                     res.z=outer[0].z+q[0].z*L[0]+q[1].z*L[1];
55
                     radius=dist (res, outer [0]);
56
                     break;
57
            case 4:
                     for (i=0; i<3; ++i) {
58
59
                         q[i].x=outer[i+1].x-outer[0].x;
60
                         q[i].y=outer[i+1].y-outer[0].y;
61
                         q[i].z=outer[i+1].z-outer[0].z;
62
                         sol[i] = dot(q[i], q[i]);
63
64
                     for (i=0; i<3;++i)
                         for (j=0; j<3;++j) m[i][j]=dot(q[i],q[j])*2;
65
66
                     det = m[0][0]*m[1][1]*m[2][2]
67
                         + m[0][1]*m[1][2]*m[2][0]
                         + m[0][2]*m[2][1]*m[1][0]
68
69
                         - m[0][2]*m[1][1]*m[2][0]
```

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```
70
                          - m[0][1]*m[1][0]*m[2][2]
71
                          - m[0][0]*m[1][2]*m[2][1];
72
                      if ( fabs(det)<eps ) return;</pre>
73
                      for (j=0; j<3; ++j) {
                           for (i=0; i<3; ++i) m[i][j]=sol[i];
74
                           L[j] = (m[0][0]*m[1][1]*m[2][2]
75
                                   + m[0][1]*m[1][2]*m[2][0]
76
77
                                   + m[0][2]*m[2][1]*m[1][0]
                                   - m[0][2]*m[1][1]*m[2][0]
78
79
                                   - m[0][1]*m[1][0]*m[2][2]
80
                                   - m[0][0]*m[1][2]*m[2][1]
                                ) / det;
81
82
                           for (i=0; i<3; ++i)
                               m[i][j] = dot(q[i], q[j]) *2;
83
84
                      }
85
                      res=outer [0];
86
                      for (i=0; i<3; ++i)
87
                           res.x += q[i].x * L[i];
                           res.y += q[i].y * L[i];
88
                           res.z \leftarrow q[i].z * L[i];
89
90
                      radius=dist(res, outer[0]);
91
92
         }
93
94
    void minball(int n) {
95
         ball();
         //printf("(\%.3 lf, \%.3 lf, \%.3 lf) \%.3 lf \ "", res.x, res.y, res.z, radius);
96
97
         if (nouter < 4)
98
             for (int i=0; i< n; ++i)
99
                  if (dist(res, pt[i])-radius>eps) {
100
                      outer [nouter]=pt[i];
101
                      ++nouter;
102
                      minball(i);
103
                      --nouter;
                      if (i>0) {
104
105
                           Tpoint Tt = pt[i];
                           memmove(\&pt[1], \&pt[0], sizeof(Tpoint)*i);
106
107
                           pt[0] = Tt;
108
                      }
109
                  }
110
    }
    void solve()
111
112
    {
113
         for (int i=0; i < npoint; i++) scanf("%lf%lf%lf",&pt[i].x,&pt[i].y,&pt[i].z);
114
         random_shuffle(pt, pt + npoint);
115
         radius=-1;
116
         for (int i=0; i < npoint; i++)
117
             if (dist(res,pt[i])-radius>eps){
118
                  nouter=1;
```

```
outer [0] = pt [i];
119
120
                    minball(i);
               }
121
122
          }
          printf("\%.5f\n", sqrt(radius));
123
124
     int main(){
   for( ; cin >> npoint && npoint; )
        solve();
125
126
127
128
          return 0;
129 }
```

Chapter 3

图论

3.1 Dijkstra

求 s 到其他点的最短路

```
int used [MAX_N] , dis [MAX_N];
2
    void dijstra(int s) {
3
         fill(dis, dis + N, INF); dis[s] = 0;
4
         priority_queue<pair<int, int>> que;
5
         que.push(make_pair(-dis[s], s));
6
         while (!que.empty()) {
7
              int u = que.top().second; que.pop();
8
              if (used[u]) continue;
9
              used[u] = true;
              foreach (e, E[u])
10
                    if (dis[u] + e \rightarrow w < dis[e \rightarrow t]) {
11
12
                         dis[e\rightarrow t] = dis[u] + e\rightarrow w;
                         que.push\left(\,make\_pair(-\,d\,is\,[\,e-\!\!>\!\!t\,]\;,\;\;e-\!\!>\!\!t\,)\,\right);
13
14
15
16
   }
```

3.2 最大流

iSAP 算法求 S 到 T 的最大流 , 点数为 cntN , 边表存储在 *E[] 中

```
1  struct Edge
2  {
3     int t, c;
4     Edge *n, *r;
5  } *E[MAX_V], edges[MAX_M], *totEdge;
6
7  Edge* makeEdge(int s, int t, int c)
8  {
9     Edge *e = totEdge ++;
```

```
10
         e \rightarrow t = t; e \rightarrow c = c; e \rightarrow n = E[s];
11
         return E[s] = e;
12
    }
13
    void addEdge(int s, int t, int c)
14
15
16
         Edge *p = makeEdge(s, t, c), *q = makeEdge(t, s, 0);
17
         p->r = q; q->r = p;
    }
18
19
20
    int maxflow()
21
    {
22
                                     [MAX_V];
          static int
                         cnt
23
                                     [MAX_V];
          static int
                         h
24
                                     [MAX_V];
          static int
                         que
                                     [MAX_V];
25
          static int
                         aug
          static Edge *cur
26
                                     [MAX_V];
27
          static Edge *prev
                                     [MAX_V];
28
          fill(h, h + cntN, cntN);
29
         memset(cnt, 0, sizeof cnt);
         int qt = 0, qh = 0; h[T] = 0;
30
31
          for(que[qt ++] = T; qh < qt;)
32
               int u = que[qh ++];
33
              ++ cnt[h[u]];
               for (Edge *e = E[u]; e; e = e \rightarrow n)
34
35
                    if (e->r->c \&\& h[e->t] = cntN) {
36
                         h[e->t] = h[u] + 1;
37
                         que[qt ++] = e->t;
                    }
38
39
         memcpy(\,cur\;,\;\;E,\;\;\mathbf{sizeof}\;\;E)\;;
40
41
         aug[S] = INF; Edge *e;
42
          int flow = 0, u = S;
43
          while (h[S] < cntN) {
44
               for(e = cur[u]; e; e = e->n)
                    if (e->c \&\& h[e->t] + 1 == h[u])
45
46
                         break;
47
               if (e) {
48
                    \mathbf{int} \ v = e -\!\!> \!\! t \; ;
                    \operatorname{cur}[\mathbf{u}] = \operatorname{prev}[\mathbf{v}] = \mathbf{e};
49
50
                    \operatorname{aug}[v] = \min(\operatorname{aug}[u], e \rightarrow c);
                    if ((u = v) == T) {
51
52
                         int by = aug[T];
53
                         while (u != S) {
54
                               Edge *p = prev[u];
55
                               p\rightarrow c -= by;
56
                               p\rightarrow r\rightarrow c += by;
57
                               u = p \rightarrow r \rightarrow t;
58
                         }
```

3.3. 上下界流 59

```
59
                       flow += by;
60
                  }
61
             } else {
                  if (!-- cnt[h[u]]) return flow;
62
                  h[u] = cntN;
63
64
                  for(e = E[u]; e; e = e->n)
65
                       if (e->c \&\& h[u] > h[e->t] + 1)
66
                           h[u] = h[e->t] + 1, cur[u] = e;
67
                  ++ \operatorname{cnt}[h[u]];
                  if (u != S) u = prev[u] -> r -> t;
68
69
             }
70
        return flow;
71
   }
72
```

3.3 上下界流

上下界无源汇可行流: 不用添 T—>S, 判断是否流量平衡

上下界无源汇可行流: 添 T—>S (下界 0 , 上界 oo) , 判断是否流量平衡

上下界最小流: 不添 T—>S 先流一遍,再添 T—>S (下界 0 , 上界 ∞) 在残图上流一遍,答案为 S—>T 的流量值上下界最大流: 添 T—>S (下界 0 , 上界 ∞) 流一遍,再在残图上流一遍 S 到 T 的最大流,答案为前者的 S—>T 的值 + 残图中 S—>T 的最大流

3.3.1 上下界无源汇可行流

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #include <ctime>
5 #include <cmath>
6 #include <iostream>
  #include <algorithm>
9
   using namespace std;
10
11
   struct {
12
          int x, y, down, up, what;
13
   } a[100001];
14
   int S, T, DS, DT, n, m, out [100001], what [100001], first [501], pre [501], way [501],
      len, dist[501], c[501], ans, flow[201], where[100001], next[100001], v[100001], 1,
        cnt;
16
17
   inline void makelist(int x, int y, int z, int q){
18
       where [++1] = y;
19
       v[1] = z;
       what [1] = q;
20
```

```
21
          next[l] = first[x];
22
          first[x] = 1;
23
    }
24
    bool check(){
25
          memset(dist, 0, sizeof(dist));
26
          dist[DS] = 1; c[1] = DS;
27
28
          for (int k = 1, l = 1; l <= k; l++)
29
                int m = c[1];
30
31
                if (m == DT)
32
33
                     len = dist[m] + 1;
34
                     return(true);
35
               for (int x = first[m]; x; x = next[x])
36
                     if (v[x] \&\& !dist[where[x]]) dist[where[x]] = dist[m] + 1, c[++k] = where
37
                          [x];
38
          }
39
          return(false);
40
41
42
    inline void dinic(int now){
43
          if (now == DT)
44
45
                int Minflow = 1 \ll 30;
               for (; now != DS; now = pre[now]) Minflow = min(Minflow, v[way[now]]);
46
47
               ans += Minflow;
                for (now = DT; now != DS; now = pre[now])
48
49
                     \begin{array}{ll} v \left[ way \left[ now \right] \right] \stackrel{}{-}{=} & Minflow; \\ v \left[ way \left[ now \right] \stackrel{\wedge}{-} 1 \right] \stackrel{}{+}{=} & Minflow; \end{array}
50
51
52
                     if (!v[way[now]]) len = dist[now];
53
               }
54
               return;
55
          \mathbf{for} \ (\mathbf{int} \ x = \ \mathsf{first} \ [\mathsf{now}] \, ; \ x ; \ x = \ \mathsf{next} \, [\, x \, ] \, )
56
57
                if (v[x] \&\& dist[now] + 1 = dist[where[x]])
58
                {
                     pre[where[x]] = now;
59
60
                     \text{way}[\text{where}[x]] = x;
61
                     dinic (where [x]);
62
                     if (dist[now] >= len) return;
                     len = dist[DT] + 1;
63
64
65
          dist[now] = -1;
    }
66
67
```

int main(){

3.3. 上下界流 61

```
69
                       freopen ("194.in", "r", stdin);
                       freopen ("194. out", "w", stdout);
70
71
                  scanf("%d%d", &n, &m);
72
                  memset(flow, 0, sizeof(flow));
                  for (int i = 1; i \le m; i++)
73
74
                            scanf("%d\%d\%d\%d", \&a[i].x, \&a[i].y, \&a[i].down, \&a[i].up);\\
75
76
                            flow[a[i].y] += a[i].down;
                            flow[a[i].x] -= a[i].down;
77
                  }
78
79
                  cnt = 0:
80
                  memset(first, 0, sizeof(first)); l = 1;
                  S = 1; T = n; DS = 0; DT = n + 1; cnt = 0;
81
82
                  for (int i = 1; i \le n; i++)
                            if (flow[i] > 0) makelist (DS, i, flow[i], 0), makelist (i, DS, 0, 0), cnt +=
83
                                    flow[i];
84
                                                          else makelist(i, DT, abs(flow[i]), 0), makelist(DT, i, 0, 0);
85
                        makelist(T, S, 1 \ll 30, 0); makelist(S, T, 0, 0);
                  for (int i = 1; i \le m; i++) makelist(a[i].x, a[i].y, a[i].up - a[i].down, i),
86
87
                                                                                          makelist(a[i].y, a[i].x, 0, i);
                  ans = 0;
88
89
                  for (; check();) dinic(DS);
90
                  if (ans != cnt) printf("NO\n");
91
                  else
92
                            printf("YES\n");
93
94
                            for (int i = 3; i \le 1; i += 2)
95
                                      if (what[i]) out[what[i]] = v[i];
                            for (int i = 1; i \le m; i++) printf("%d\n", a[i].down + out[i]);
96
97
                  }
98
                       上下界最大流
        3.3.2
  1 #include <cstdio>
  2 #include <cstdlib>
  3
      #include <cstring>
  4 #include <ctime>
  5 #include <cmath>
  6 #include <iostream>
  7 #include <algorithm>
  9
       using namespace std;
10
       int n, m, S, T, DS, DT, a[1001], first [1501], next [100001], where [100001], v[100001],
11
                   what [100001],
        1, c[1501], dist[1501], len, pre[1501], way[1501], flow[1501], out[100001], tot, cnt, flow[1501], fl
12
13
       inline void makelist(int x, int y, int z, int q){
```

```
15
         where[++1] = y;
16
         v[1] = z;
17
         what [1] = q;
         next[l] = first[x];
18
         first[x] = 1;
19
20
    }
21
22
    bool check(int S, int T){
23
         memset(dist, 0, sizeof(dist));
24
         c[1] = S; dist[S] = 1;
25
         for (int k = 1, l = 1; l <= k; l++)
26
27
              int m = c[1];
28
              if (m == T)
29
              {
30
                   len = dist[m] + 1;
31
                   return(true);
32
33
              for (int x = first[m]; x; x = next[x])
                   if (v[x] && ! dist[where[x]])
34
35
                         dist[where[x]] = dist[m] + 1;
36
37
                        c[++k] = where[x];
38
                   }
39
40
         return(false);
41
    }
42
    inline void dinic(int now, int S, int T){
43
44
         if (now == T)
45
              int Minflow = 1 \ll 30;
46
47
              for (; now != S; now = pre[now]) Minflow = min(Minflow, v[way[now]]);
48
              ans += Minflow;
49
              for (now = T; now != S; now = pre[now])
50
                   \begin{array}{l} v \, [\, way \, [\, now \, ] \, ] \, \stackrel{}{-}{=} \, \begin{array}{l} Minflow \, ; \\ v \, [\, way \, [\, now \, ] \, & \stackrel{}{\cap} \, 1 \, ] \, & += \, Minflow \, ; \end{array}
51
52
53
                   if (!v[way[now]]) len = dist[now];
54
              }
              return;
55
56
57
         for (int x = first [now]; x; x = next [x])
              if (v[x] \&\& dist[where[x]] = dist[now] + 1)
58
59
60
                   pre[where[x]] = now;
61
                   way[where[x]] = x;
                   dinic(where[x], S, T);
62
63
                   if (dist[now] >= len) return;
```

3.3. 上下界流 63

```
64
                 len = dist[T] + 1;
65
         dist[now] = -1;
66
67
    }
68
69
    int main(){
           freopen("3229.in", "r", stdin);
freopen("3229.out", "w", stdout);
70
    //
71
    //
72
         for (;;)
73
             if (scanf("%d%d", &n, &m) != 2) return 0;
74
75
             memset(first, 0, sizeof(first)); l = 1;
             memset(flow, 0, sizeof(flow));
76
             S = 0; T = n + m + 1; DS = T + 1; DT = DS + 1;
77
78
             for (int i = 1; i \le m; i++)
79
                  scanf("%d", &a[i]);
80
81
                  flow[S] = a[i]; flow[i] += a[i];
                  makelist(S, i, 1 \ll 30, 0); makelist(i, S, 0, 0);
82
83
             tot = 0;
84
             for (int i = 1; i \le n; i++)
85
86
                  int C, D;
87
                  scanf("%d%d", &C, &D);
88
                  if (D) makelist (m + i, T, D, 0), makelist (T, m + i, 0, 0);
89
90
                  for (int j = 1; j <= C; j++)
91
                  {
92
                      int idx, x, y;
93
                      scanf("%d%d%d", &idx, &x, &y);
94
                      idx++;
                      flow[idx] = x; flow[i + m] += x;
95
96
                      out[++tot] = x;
                      if (y != x) makelist (idx, i + m, y - x, tot), makelist (i + m, idx, 0, y)
97
                           tot);
                 }
98
             }
99
100
             cnt = 0;
101
             for (int i = S; i \ll T; i++)
                  if (flow[i] > 0) makelist (DS, i, flow[i], 0), makelist (i, DS, 0, 0), cnt
102
                     += flow [i];
                  else makelist(i, DT, abs(flow[i]), 0), makelist(DT, i, 0, 0);
103
             makelist(T, S, 1 \ll 30, 0); makelist(S, T, 0, 0);
104
105
             for (; check(DS, DT);) dinic(DS, DS, DT);
106
             if (ans != cnt)
107
108
                  printf("-1\n\n");
109
110
                  continue;
```

```
111
               }
112
               else
113
114
                    v[1] = v[1 - 1] = 0;
                    for (; \operatorname{check}(S, T);) \operatorname{dinic}(S, S, T);
115
116
                    printf("%d\n", ans);
117
                    for (int i = 3; i \le 1; i += 2)
118
                         if (what [i]) out [what [i]] += v[i];
                    for (int i = 1; i \le tot; i++) printf("%d\n", out[i]);
119
120
                    printf("\n");
121
               }
          }
122
123
            上下界最小流
     3.3.3
    #include <cstdio>
  1
  2 #include <cstdlib>
  3 #include <cstring>
  4 #include <ctime>
  5
    #include <cmath>
  6
    #include <iostream>
  7
    #include <algorithm>
 8
 9
     using namespace std;
 10
 11
     struct {
 12
              int x, y, down, up;
     } a[10001];
 13
     \mathbf{int} \ \mathrm{out} \, [100001] \, , \ \mathrm{what} \, [100001] \, , \ \mathrm{cnt} \, , \ \mathrm{S}, \ \mathrm{T}, \ \mathrm{DS}, \ \mathrm{DT}, \ 1 \, , \ \mathrm{ans} \, , \ \mathrm{n}, \ \mathrm{m}, \ \mathrm{flow} \, [101] \, , \ \mathrm{first}
 14
          [201], next [100001], where [100001], v[100001], dist [201], c[201], pre [201], way
          [201], len;
 15
 16
     int read(){
 17
          char ch;
          for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
 18
 19
          int cnt = 0;
 20
          for (; ch >= '0' && ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
 21
          return(cnt);
 22
     }
 23
 24
     inline void makelist(int x, int y, int z, int q){
 25
          where[++1] = y;
 26
          v[1] = z;
          what [1] = q;
 27
          next[l] = first[x];
 28
 29
          first[x] = 1;
 30
     }
 31
```

inline void makemap() {

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```
33
          memset(first, 0, sizeof(first)); l = 1;
34
          S = 1, T = n, DS = 0, DT = n + 1; cnt = 0;
35
          for (int i = 1; i \le n; i++)
                if (flow[i] > 0) makelist(DS, i, flow[i], 0), makelist(i, DS, 0, 0), cnt +=
36
                     flow[i];
                \mathbf{else} \ \ \mathbf{makelist} \, (\, \mathbf{i} \, , \, \, \mathbf{DT}, \, \, \mathbf{abs} \, (\, \mathbf{flow} \, [\, \mathbf{i} \, ]\, ) \, , \, \, \mathbf{0}) \, , \, \, \mathbf{makelist} \, (\mathbf{DT}, \, \, \mathbf{i} \, , \, \, \mathbf{0} \, , \, \, \mathbf{0}) \, ;
37
38
          39
                                                    makelist(a[i].y, a[i].x, 0, i);
    }
40
41
42
     bool check(){
43
          memset(dist, 0, sizeof(dist));
           dist[DS] = 1; c[1] = DS;
44
45
          for (int k = 1, l = 1; l <= k; l++)
46
47
                int m = c[1];
48
                \mathbf{if} \pmod{\mathrm{DT}}
49
                     len = dist[m] + 1;
50
                    return(true);
51
52
53
                for (int x = first[m]; x; x = next[x])
                       \begin{tabular}{ll} \bf if & (v[x] & & !dist[where[x]]) & dist[where[x]] & = dist[m] + 1, & c[++k] & = where \\ \end{tabular} 
54
                           [x];
55
56
          return (false);
    }
57
58
     inline void dinic(int now){
59
60
           if (now == DT)
61
62
                int Minflow = 1 \ll 30;
63
                for (; now != DS; now = pre[now]) Minflow = min(Minflow, v[way[now]]);
                ans += Minflow;
64
                for (now = DT; now != DS; now = pre[now])
65
66
                      \begin{array}{l} v \left[ \left. way \left[ \left. now \right. \right] \right. \right] -= \left. \begin{array}{l} Minflow \, ; \\ v \left[ \left. way \left[ \left. now \right. \right] \right. \right] \, += \, Minflow \, ; \end{array} \right. \end{array}
67
68
69
                      if (!v[way[now]]) len = dist[now];
70
71
                return;
72
73
          for (int x = first [now]; x; x = next [x])
                if (dist[where[x]] = dist[now] + 1 & v[x])
74
75
76
                      pre[where[x]] = now;
                      way[where[x]] = x;
77
78
                      dinic (where [x]);
79
                      if (dist [now] >= len) return;
```

```
80
                 len = dist[DT] + 1;
81
82
         dist[now] = -1;
83
    }
84
85
    inline void network(){
86
        for (; check();) dinic(DS);
87
    }
88
89
    int main(){
       // freopen ("176. in", "r", stdin);
90
       // freopen ("176. out", "w", stdout);
91
         scanf("%d%d", &n, &m);
92
        memset(flow, 0, sizeof(flow));
93
         for (int i = 1; i \le m; i++)
94
95
96
             a[i].x = read(), a[i].y = read(), a[i].up = read();
97
             int status = read();
98
             if (status) a[i].down = a[i].up;
99
             else a[i].down = 0;
             flow[a[i].y] += a[i].down;
100
             flow[a[i].x] = a[i].down;
101
102
         }
103
        makemap();
104
        ans = 0;
105
        network();
         makelist(T, S, 1 \ll 30, 0); makelist(S, T, 0, 0);
106
107
         network();
         if (ans != cnt)
108
109
             printf("Impossible\n");
110
             return 0;
111
112
113
         printf("%d\n", v[1]);
         for (int i = 3; i <= 1; i += 2)
114
             if (what[i]) out[what[i]] = v[i];
115
         for (int i = 1; i \le m; i++)
116
117
118
             printf("%d", a[i].down + out[i]);
119
             if (i != m) printf("_{\sqcup}");
120
             else printf("\n");
121
         }
122
    }
    3.3.4 上下界有源汇可行流
 1 #include <cstdio>
 2 #include <cstdlib>
```

3 #include <cstring> 4 #include <ctime> 3.3. 上下界流 67

```
5 #include <cmath>
6 #include <iostream>
7 #include <algorithm>
9
   using namespace std;
10
   int test, n, m, Q, first [501], a1[201], a2[201], flow [501], next [100001], where
11
       [100001], v[100001], len,
   1, dist [501], c[501], up [201] [201], down [201] [201], S, T, DS, DT, ans, out [201] [201],
12
        pre [501], way [501];
13
14
   inline void makelist(int x, int y, int z){
        where [++1] = y;
15
        v[1] = z;
16
17
        next[l] = first[x];
        first[x] = 1;
18
19
   }
20
21
   bool check(){
22
        memset(dist, 0, sizeof(dist));
23
        dist[DS] = 1; c[1] = DS;
24
        for (int k = 1, l = 1; l <= k; l++)
25
26
            int m = c[1];
27
            if (m == DT)
28
                len = dist[m] + 1;
29
30
                return(true);
31
            for (int x = first[m]; x; x = next[x])
32
33
                if (v[x] && ! dist[where[x]])
34
35
                    dist[where[x]] = dist[m] + 1;
36
                    c[++k] = where[x];
37
38
39
        return(false);
40
41
42
   inline void dinic(int now){
        if (now == DT)
43
44
            int Minflow = 1 \ll 30;
45
            for (; now != DS; now = pre[now]) Minflow = min(Minflow, v[way[now]]);
46
47
            ans += Minflow;
            for (now = DT; now != DS; now = pre[now])
48
49
50
                v[way[now]] -= Minflow;
51
                v[way[now] ^ 1] += Minflow;
```

```
52
                 if (!v[way[now]]) len = dist[now];
53
             }
54
             return;
55
56
        for (int x = first[now]; x; x = next[x])
57
             if (v[x] \&\& dist[now] + 1 = dist[where[x]])
58
59
                 pre[where[x]] = now;
                 \text{way}[\text{where}[x]] = x;
60
                 dinic (where [x]);
61
62
                 if (dist[now] >= len) return;
                 len = dist[DT] + 1;
63
64
        dist[now] = -1;
65
66
   }
67
68
   int main(){
69
      // freopen ("2396. in", "r", stdin);
70
          freopen ("2396. out", "w", stdout);
        scanf("%d", &test);
71
        for (int uu = 1; uu \le test; uu++)
72
73
74
             scanf("%d%d", &m, &m);
             for (int i = 1; i \le n; i++) scanf("%d", &a1[i]);
75
76
             for (int i = 1; i \le m; i++) scanf("%d", &a2[i]);
77
             memset(up, 127, sizeof(up));
             memset(down, 0, sizeof(down));
78
79
             \operatorname{scanf}("%d", \&Q);
             for (int i = 1; i \ll Q; i++)
80
81
             {
82
                 int x, y, z;
83
                 char str [2];
84
                 scanf("%d%d%s%d", &x, &y, str, &z);
85
                 int L1, L2, R1, R2;
86
                 if (x == 0) L1 = 1, R1 = n;
87
                 else L1 = R1 = x;
                 if (y == 0) L2 = 1, R2 = m;
88
                 else L2 = R2 = y;
89
90
                 for (int j = L1; j \ll R1; j++)
                      for (int k = L2; k \le R2; k++)
91
                           if (str[0] = '>') down[j][k] = max(down[j][k], z + 1);
92
                           else if (str[0] = '<') up[j][k] = min(up[j][k], z - 1);
93
                           else down[j][k] = max(down[j][k], z), up[j][k] = min(up[j][k], z)
94
95
             bool ok = true;
96
             \label{eq:formula} \mbox{for } (\mbox{int} \ \ i \ = \ 1; \ \ i \ <= \ n \ \&\& \ ok \ ; \ \ i \ ++)
97
98
                 for (int j = 1; j \le m; j++)
99
                      if (down[i][j] > up[i][j])
```

3.3. 上下界流 69

```
100
                       {
101
                            ok = false;
102
                            break;
103
              if (!ok)
104
105
                 printf("IMPOSSIBLE\n");
106
107
                 if (uu != test) printf("\n");
108
                 continue;
109
              memset(flow, 0, sizeof(flow));
110
111
              memset(first, 0, sizeof(first)); l = 1;
              S = 0; T = n + m + 1;
112
              for (int i = 1; i \le n; i++) flow[S] -= a1[i], flow[i] += a1[i];
113
              for (int i = 1; i \le m; i++) flow[i + n] = a2[i], flow[T] += a2[i];
114
115
              for (int i = 1; i <= n; i++)
                   \quad \mathbf{for} \ (\mathbf{int} \ \mathbf{j} \ = \ 1; \ \mathbf{j} \ <= \ \mathbf{m}; \ \mathbf{j} +\!\!\!\! +)
116
117
                       flow[i] -= down[i][j]; flow[j + n] += down[i][j];
118
                       if (down[i][j] != up[i][j]) makelist(i, j + n, up[i][j] - down[i][j])
119
                                                        makelist(i + n, i, 0);
120
121
                   }
              DS = T + 1; DT = DS + 1;
122
              int cnt = 0;
123
124
              for (int i = S; i \leftarrow T; i++)
                   if (flow[i] > 0) makelist (DS, i, flow[i]), makelist (i, DS, 0), cnt +=
125
                      flow[i];
                   else if (flow[i] < 0) makelist(i, DT, abs(flow[i])), makelist(DT, i, 0);
126
127
              makelist(T, S, 1 \ll 30); makelist(S, T, 0);
128
              ans = 0:
              for (; check();) dinic(DS);
129
130
              if (ans != cnt)
131
132
                   printf("IMPOSSIBLE\n");
                   if (uu != test) printf("\n");
133
134
                   continue;
135
136
              for (int i = 1; i \le n; i++)
                   for (int x = first[i]; x; x = next[x])
137
138
                       if (\text{where } [x] >= n + 1 \&\& \text{where } [x] <= n + m)
                           down[i][where[x] - n] += v[x^1];
139
              for (int i = 1; i \le n; i++)
140
                   for (int j = 1; j \le m; j++)
141
142
                   {
143
                        printf("%d", down[i][j]);
                       if \ (j \ != \ m) \ printf("_{\sqcup}");
144
145
                       else printf("\n");
146
                   }
```

3.4 费用流

3.4.1 Logic_IU+ **负费用路**

注意图的初始化,费用和流的类型依题目而定

```
1 int flow, cost;
3
   struct Edge
 4
        \mathbf{int} \quad t \ , \quad c \ , \quad w;
5
6
        Edge *n, *r;
7
    *totEdge, edges[MAX_M], *E[MAX_V];
8
9
   Edge* makeEdge(int s, int t, int c, int w)
10
    {
11
        Edge *e = totEdge ++;
12
        e \rightarrow t = t; e \rightarrow c = c; e \rightarrow w = w; e \rightarrow n = E[s];
13
        return E[s] = e;
14
    }
15
16
   void addEdge(int s, int t, int c, int w)
17
        Edge *st = makeEdge(s, t, c, w), *ts = makeEdge(t, s, 0, -w);
18
19
        st->r = ts; ts->r = st;
20
    }
21
22 int SPFA()
23
   {
24
         static int que [MAX_V];
25
         static int aug [MAX_V];
26
         static int in [MAX_V];
27
         static int dist[MAX V];
28
         static Edge *prev[MAX_V];
29
         int qh = 0, qt = 0;
30
31
         int u, v;
32
         fill(dist, dist + cntN, INF); dist[S] = 0;
33
         fill(in, in + cntN, 0); in[S] = true;
34
         que[qt ++] = S; aug[S] = INF;
35
         for (; qh!= qt;) {
             u = que[qh]; qh = (qh + 1) \% MAX_N;
36
37
             for(Edge *e = E[u]; e; e = e->n) {
38
                  if (! e->c) continue;
39
                  v = e \rightarrow t;
                  if (dist[v] > dist[u] + e \rightarrow w) {
40
```

3.4. 费用流

71

```
41
                                      dist[v] = dist[u] + e \rightarrow w;
42
                                      \operatorname{aug}[v] = \min(\operatorname{aug}[u], e \rightarrow c);
43
                                      prev[v] = e;
                                      if (! in [v]) {
44
                                              in[v] = true;
45
                                              \mathbf{if} \hspace{0.1cm} (\hspace{0.1cm} \mathrm{qh} \hspace{0.1cm} != \hspace{0.1cm} \mathrm{qt} \hspace{0.1cm} \& \& \hspace{0.1cm} \mathrm{dist} \hspace{0.1cm} [\hspace{0.1cm} \mathrm{v} \hspace{0.1cm}] \hspace{0.1cm} <= \hspace{0.1cm} \mathrm{dist} \hspace{0.1cm} [\hspace{0.1cm} \mathrm{que} \hspace{0.1cm} [\hspace{0.1cm} \mathrm{qh} \hspace{0.1cm}] \hspace{0.1cm}] \hspace{0.1cm} ) \hspace{0.1cm} \hspace{0.1cm} \hspace{0.1cm} \{
46
47
                                                      qh = (qh - 1 + MAX_N) \% MAX_N;
48
                                                      que[qh] = v;
49
                                              } else {
50
                                                      que[qt] = v;
                                                      qt = (qt + 1) \% MAX_N;
51
52
                                              }
                                      }
53
                              }
54
55
56
                      in[u] = false;
57
              }
58
59
              if (dist[T] == INF) return false;
              cost += dist[T] * aug[T];
60
              flow += aug[T];
61
              \mathbf{for}\,(\,u\,=\,T\,;\ u\,:=\,S\,;\ )\ \{
62
63
                      prev[u]->c -= aug[T];
                      prev[u]->r->c += aug[T];
64
65
                      u = prev[u] -> r -> t;
66
67
              return true;
68
      }
69
70
      int minCostFlow()
71
      {
72
              flow = cost = 0;
73
              while (SPFA());
74
              return cost;
     }
75
```

3.4.2 shytangyuan+ZKW

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #include <ctime>
5 #include <cmath>
6 #include <iostream>
7 #include <algorithm>
8
9 using namespace std;
```

```
\textbf{int} \;\; n, \;\; m, \;\; S, \;\; T, \;\; slk\left[1001\right], \;\; dist\left[1001\right], \;\; first\left[1001\right], \;\; l, \;\; c\left[1000001\right], \;\; next\left[1000001\right],
11
        where [1000001], 11[1000001], v[1000001];
12
   bool b[1001];
   long long ans1, ans2;
13
14
15
   inline void makelist(int x, int y, int z, int p){
16
        where [++1] = y;
17
        11[1] = z;
        v[1] = p;
18
        next[l] = first[x];
19
20
        first[x] = 1;
21
   }
22
   inline void spfa(){
23
24
        memset(dist, 127, sizeof(dist));
25
        memset(b, false, sizeof(b));
26
        dist[T] = 0; c[1] = T;
27
        for (int k = 1, l = 1; l <= k; l++)
28
29
             int m = c[1];
             b[m] = false;
30
             for (int x = first[m]; x; x = next[x])
31
32
                  if (ll[x ^1] \&\& dist[m] - v[x] < dist[where[x]])
33
34
                     dist[where[x]] = dist[m] - v[x];
                     if (!b[where[x]]) b[where[x]] = true, c[++k] = where[x];
35
36
                  }
37
        }
   }
38
39
   int zkw work(int now, int cap){
40
        b [now] = true;
41
42
        if (now == T)
43
44
             ans1 += cap;
             ans2 += (long long) cap * dist[S];
45
46
             return(cap);
47
48
        int Left = cap;
        for (int x = first[now]; x; x = next[x])
49
50
             if (ll[x] && !b[where[x]])
                 if (dist[now] = dist[where[x]] + v[x])
51
52
53
                     int use = zkw_work(where[x], min(Left, ll[x]));
                     ll[x] = use; ll[x^1] += use;
54
55
                     Left -= use;
56
                     if (!Left) return(cap);
                 }
57
```

3.5. 强联通分量 73

```
58
                else slk[where[x]] = min(slk[where[x]], dist[where[x]] + v[x] - dist[now])
        return(cap - Left);
59
60
   }
61
62
   bool relax(){
63
        int Min = 1 << 30;
64
        for (int i = 0; i \le T; i++)
            if (!b[i]) Min = min(Min, slk[i]);
65
        if (Min == 1 << 30) return(false);
66
67
        for (int i = 0; i \le T; i++)
            if (b[i]) dist[i] += Min;
68
        return(true);
69
   }
70
71
72
   inline void zkw(){
73
        ans1 = ans2 = 0;
74
        spfa();
                  //hint memset(dist, 0, size of (dist)); if all values of edges are
            nonnegative
75
        for (;;)
76
            memset(slk, 127, sizeof(slk));
77
78
            for (;;)
79
            {
                 memset(b, false, sizeof(b));
80
81
                 if (!zkw_work(S, 1 \ll 30)) break;
82
83
            if (!relax()) break;
84
        printf("%I64d_{\perp}%I64d_{\uparrow}n", ans1, ans2);
85
86
   }
87
88
   int main(){
89
        scanf ("%d%d", &n, &m);
        S = 1; T = n;
90
        memset(first, 0, sizeof(first)); l = 1;
91
        for (int i = 1; i \le m; i++)
92
93
94
            int x, y, z, q;
            scanf("%d%d%d%d", &x, &y, &z, &q);
95
96
            makelist(x, y, z, q); makelist(y, x, 0, -q);
97
98
        zkw();
99
```

3.5 强联通分量

3.5.1 Logic_IU

N 个点的图求 SCC, totID 为时间标记, top 为栈顶, totCol 为强联通分量个数,注意初始化

```
int totID , totCol;
1
   int col [MAX_N] , low [MAX_N] , dfn [MAX_N] ;
   int top, stack [MAX_N], instack [MAX_N];
5
   int tarjan (int u)
6
7
        low[u] = dfn[u] = ++ totID;
8
         instack[u] = true; stack[++ top] = u;
9
10
         int v;
11
         foreach(it, adj[u]) {
             v = it -> first;
12
13
             \mathbf{if} \ (\mathrm{dfn} \, [\, v \, ] =\!\!\!\! -1)
                  low[u] = min(low[u], tarjan(v));
14
15
             else if (instack[v])
16
                  low[u] = min(low[u], dfn[v]);
        }
17
18
19
         if (low[u] = dfn[u]) {
20
             do {
21
                  v = \operatorname{stack} [\operatorname{top} --];
22
                  instack[v] = false;
23
                  col[v] = totCol;
24
             } while (v != u);
25
             ++ totCol;
         }
26
27
        return low[u];
28
   }
29
   void solve()
30
31
   {
32
         totID = totCol = top = 0;
33
         fill(dfn, dfn + N, 0);
34
         for(int i = 0; i < N; ++ i)
35
             if (! dfn[i])
36
                  tarjan(i);
37
   }
```

3.5.2 shytangyuan+ **手写栈**

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #include <ctime>
5 #include <cmath>
6 #include <iostream>
7 #include <algorithm>
```

3.5. 强联通分量 75

```
using namespace std;
10
   int n, m, first [10001], father [10001], dfn [10001], low [10001], c [10001], pos [10001],
       todo [10001],
   cnt, len, next[2000001], where [2000001], l, kuai, Max, color [10001], number;
12
13
   bool b[10001];
14
15
   int read(){
16
        char ch;
        for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
17
18
        int cnt = 0;
        for (; ch >= '0' \&\& ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
19
20
        return(cnt);
21
   }
22
23
   inline void makelist(int x, int y){
24
        where[++1] = y;
25
        next[l] = first[x];
26
        first[x] = 1;
27
   }
28
29
   inline void tarjan(int S){
30
        int now = S; todo[now] = first[now];
31
        for (;;)
32
33
            if (!now) return;
            if (first [now] = todo [now])
34
35
                b[now] = true;
36
                dfn[now] = low[now] = ++cnt;
37
38
                c[++len] = now; pos[now] = len;
39
40
            int x = todo[now];
            if (!x)
41
42
                if (father [now])
43
                     low [father [now]] = min(low [father [now]], low [now]);
44
45
                int delta = -1;
46
                if (father[now]) ++delta;
                for (int x = first[now]; x; x = next[x])
47
48
                     if (father[where[x]] = now)
                         if (low[where[x]] >= dfn[now]) ++delta;
49
                Max = max(Max, delta);
50
                if (low[now] = dfn[now])
51
52
53
                   ++number;
54
                   for (int i = pos[now]; i \le len; i++) color[c[i]] = number;
55
                   len = pos[now] - 1;
56
```

```
57
                 now = father[now];
58
                 continue;
59
             }
             todo[now] = next[todo[now]];
60
             if (father[now] != where[x])
61
62
                 if (!b[where[x]])
63
                 {
64
                      father[where[x]] = now;
65
                     now = where[x];
                     todo[now] = first[now];
66
67
                     continue;
68
69
                 else if (! color [where [x]]) low [now] = min(low [now], dfn [where [x]]);
70
        }
71
    }
72
73
    int main(){
74
       // freopen ("2117.in", "r", stdin);
75
       // freopen ("2117.out", "w", stdout);
76
        for (;;)
77
             n = read(); m = read();
78
79
             if (!n && !m) return 0;
             memset(first, 0, sizeof(first));
80
             1 = 0;
81
82
             for (int i = 1; i \le m; i++)
83
84
                 int x = read() + 1, y = read() + 1;
85
                 makelist(x, y);
86
                 makelist(y, x);
87
             }
             memset(dfn, 0, sizeof(dfn));
88
89
             memset(low, 0, sizeof(low));
90
             memset(color, 0, sizeof(color));
91
             memset(b, false, sizeof(b));
             memset(father, 0, sizeof(father));
92
             cnt = 0; len = 0;
93
94
             Max = - (1 \ll 30);
95
             kuai = 0; number = 0;
             for (int i = 1; i \le n; i++)
96
97
                 if (!b[i]) tarjan(i), ++kuai;
98
             printf("%d\n", kuai + Max);
99
        }
100
    }
```

3.6 KM

3.6.1 tEJtM

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```
1 // sgu206
 2 #include < cstring >
 3 #include<cstdio>
 4 #include<algorithm>
 5 using namespace std;
   struct recmap
 7
 8
         int y, c;
9
         recmap *next;
   } *p, ma1[1000], *id1[1001];
    \mathbf{int} \ n, \ m, \ l1 \ , \ l2 \ , \ c \, [1001] \ , \ i \ , \ x, \ y, \ z \ , \ g \, [401] \, [401] \ , \ gn \ , \ l1 \, [1001] \ , \ lr \, [1001] \ , \ rm \, [1001] \ ,
          exd, t;
    bool f[1001], vl[1001];
12
    void build(int x, int y)
13
14
    {
15
         ma1[++11] \cdot y = y;
16
         ma1[l1].next = id1[x];
17
         id1[x] = \&ma1[l1];
18
    }
19
    bool dfs(int v)
20
          if(v == y) return true;
21
22
         f[v] = false;
23
         for(recmap *p=id1[v]; p; p=p->next) if(f[p->y] and dfs(p->y))
24
               g \, [\, (\, p\text{-ma1}\,) \, > \, 1][\, i\, -n \, + \, 1] \,\, = \,\, c \, [\, (\, p\text{-ma1}\,) \, > \, 1] - z \, ;
25
26
              return true;
27
28
         return false;
29
   int hgry(int v)
30
31
32
33
         vl[v] = true;
         for(int u = 1; u \le gn; u++)
34
              if (f [u])
35
36
               {
                    if((t=ll[v]+lr[u] - g[v][u]) ==0)
37
38
                    {
39
                         f[u] = false;
                         if(rm[u] = 0 \text{ or } hgry(rm[u])) \text{ return } rm[u] = v;
40
41
                    else\ exd = min(exd, t);
42
43
         return 0;
44
45
    void KM()
46
    {
         memset(ll, 0x7f, sizeof(ll));
47
48
         memset(lr, 0, sizeof(lr));
```

```
49
          memset(rm, 0, sizeof(rm));
50
          for(int i = 1; i < n; i++)
51
52
               for (;;)
53
                     memset(vl, false, sizeof(vl));
54
55
                    memset(f, true, sizeof(f));
56
                    exd = 0x7fffffff;
                     if(hgry(i)) break;
57
                     for (int i = 1; i < n; i++) if (vl[i]) ll[i] -= exd;
58
59
                     for (int i = n; i \le m; i + +) if (!f[i-n+1]) lr[i-n+1] += exd;
60
               }
          }
61
62
    int main()
63
64
    {
          scanf("%d%d", &n, &m);
65
66
         memset(id1, 0, sizeof(id1));
67
          11 = 1;
68
          for(i = 1; i < n; i++)
69
               scanf("%d%d%d", &x, &y, &c[i]);
70
               build(x, y);
71
72
               build(y, x);
73
74
          memset(g, 0, sizeof(g));
          \mathbf{for} \left( \begin{smallmatrix} i \end{smallmatrix} = \begin{smallmatrix} n \end{smallmatrix} ; \quad i <= \begin{smallmatrix} m \end{smallmatrix} ; \quad i ++ \right)
75
76
77
               scanf("%d%d%d", &x, &y, &z);
78
               c[i] = z;
79
               memset(f, true, sizeof(f));
80
               dfs(x);
81
          }
82
         gn = max(n-1, m-n+1);
83
         KM();
          for (int i = 1; i < n; i++) printf ("%d\n", c[i]-ll[i]);
84
          \label{eq:formula} \mbox{for}\,(\mbox{int}\ i \ = \ n\,;\ i \ <= \ m;\ i \ ++)\ printf\,(\mbox{``%d}\n"\,,\ c\,[\,i\,]\ +\ lr\,[\,i-n+1])\,;
85
86
          return 0;
87
    }
    3.6.2 Logic IU
    求完备匹配的最大权匹配,建好的完全图用 w[][] 存储,点数为 N
    \mathbf{const} \quad \mathbf{int} \quad \mathbf{MAX} \mathbf{N} = 200 + 10;
 1
    const int INF = 10000000000;
 2
 3
 4 int N, flag;
 5 \quad \mathbf{int} \quad w[MAX_N][MAX_N];
    int fx [MAX_N], fy [MAX_N], lx [MAX_N], ly [MAX_N], slk [MAX_N], mat [MAX_N];
```

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```
int DFS(int x) {
9
        fx[x] = flag;
10
        for (int i = 1; i \le N; ++ i)
            if (lx[x] + ly[i] != w[x][i])
11
                slk[i] = min(slk[i], lx[x] + ly[i] - w[x][i]);
12
13
            else if (fy[i] != flag) {
14
                fy[i] = flag;
15
                if (mat[i] < 0 || DFS(mat[i])) {
16
                     mat[i] = x;
17
                     return true;
18
                }
19
20
        return false;
   }
21
22
23
   int KM()  {
24
        for(int i = 1; i \le N; ++ i)  {
25
            mat[i] = -1;
26
            fx[i] = 0; fy[i] = 0;
            ly[i] = 0; lx[i] = -INF;
27
28
            for (int j = 1; j \ll N; ++ j)
29
                lx[i] = max(lx[i], w[i][j]);
30
31
        for (int now = 1; now \leq N; ++ now) {
32
            ++ flag; for (int i = 1; i <= N; ++ i) slk[i] = INF;
33
            while (! DFS(now)) {
                int p(INF); for(int i = 1; i \le N; ++ i)
34
                     if (fy[i] != flag) p = min(p, slk[i]);
35
36
                for(int i = 1; i \le N; ++ i)
37
                     if (fx[i] = flag) lx[i] -= p;
                     if (fy[i] == flag) ly[i] += p;
38
39
                     slk[i] = INF;
40
41
                ++ flag;
            }
42
43
44
        long long ans = 0;
45
        for (int i = 1; i \le N; +++ i) ans += lx[i], ans += ly[i];
46
        return ans;
47
```

3.6.3 shytangyuan+ 邻接阵

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #include <ctime>
5 #include <cmath>
```

```
#include <iostream>
   #include <algorithm>
9
   using namespace std;
10
11
   const int oo = 1 \ll 30;
12
   int ans, value [501] [501], n, m, L[501], R[501], v[501];
13
   bool bx[501], by[501];
14
15
16
   bool find (int now) {
17
       bx[now] = true;
        for (int i = 1; i \ll m; i++)
18
            if (!by[i] && L[now] + R[i] == value[now][i])
19
20
21
               by[i] = true;
22
               if (!v[i] || find(v[i]))
23
24
                  v[i] = now;
25
                  return(true);
26
27
28
       return (false);
29
   }
30
31
   inline void km() {
32
       memset(L, 0, sizeof(L));
33
        memset(R, 0, sizeof(R));
34
        for (int i = 1; i \le n; i++)
35
            for (int j = 1; j \ll m; j++)
36
                L[i] = max(L[i], value[i][j]);
37
        ans = 0;
        memset(v, 0, sizeof(v));
38
39
        for (int i = 1; i \le \min(n, m); i++)
40
            for (;;)
41
                memset(bx, false, sizeof(bx));
42
43
                memset(by, false, sizeof(by));
44
                if (find(i)) break;
                int Min = oo;
45
                for (int j = 1; j \le n; j++)
46
47
                     if (bx[j])
48
                        for (int k = 1; k \le m; k++)
49
                            if (!by[k])
                               Min = min(Min, L[j] + R[k] - value[j][k]);
50
51
                for (int j = 1; j \le n; j++) if (bx[j]) L[j] = Min;
52
                for (int j = 1; j \le m; j++) if (by[j]) R[j] += Min;
53
54
        for (int i = 1; i \le n; i++)
```

3.6. KM 81

```
55
              for (int j = 1; j \le m; j++)
56
                  if (v[j] == i) ans += value[i][j];
57
         printf("%d\n", abs(ans));
58
    }
59
60
   int main(){
         61
62
         for (int i = 1; i \le n; i++)
              for (int j = 1; j \le m; j++) scanf("%d", &value[i][j]), value[i][j] = -value[
63
64
        km();
65
         for (int i = 1; i \le n; i++)
              \  \  \, \mathbf{for}\  \  \, (\,\mathbf{int}\  \  \, \mathbf{j}\  \, =\  \, 1\,;\  \  \, \mathbf{j}\  \, <=\, m;\  \  \, \mathbf{j}\, +\! +)
66
67
                  value[i][j] = -value[i][j];
68
        km();
   }
69
70
   /*hint 500 * 500 1.5s
72 can solve problems whose n \neq m
   must be complete graph, or should change some values of matrix to satisfy the
        condition */
    3.6.4 shytangyuan+ 链表
 1 #include <cstdio>
 2 #include <cstdlib>
 3 #include <cstring>
 4 #include <ctime>
 5 #include <cmath>
 6 #include <iostream>
 7
   #include <algorithm>
 8
9
   using namespace std;
10
   const int oo = 1 \ll 30;
11
    \textbf{int} \ \ ans \ , \ \ first \ [501] \ , \ \ l \ , \ \ where \ [250001] \ , \ \ next \ [250001] \ , \ \ value \ [250001] \ , \ \ n \ , \ m \ , \ L \ [501] \ , \ R
        [501], v[501];
   bool bx[501], by[501];
13
14
15
    inline void makelist(int x, int y, int z){
16
         where [++1] = y;
17
         value[1] = z;
         next[l] = first[x];
18
         first[x] = 1;
19
20
    }
21
22
    bool find(int now){
23
         bx[now] = true;
24
         for (int x = first[now]; x; x = next[x])
25
              if (!by[where[x]] \&\& L[now] + R[where[x]] = value[x])
```

```
26
27
                 by [where [x]] = true;
28
                 if (!v[where[x]] || find(v[where[x]]))
29
30
                    v[where[x]] = now;
31
                    return(true);
32
33
34
        return(false);
35
   }
36
37
   inline void km(){
        memset(L, 0, sizeof(L));
38
        memset(R, 0, sizeof(R));
39
40
        for (int i = 1; i \le n; i++)
41
             for (int x = first[i]; x; x = next[x])
42
                  L[i] = max(L[i], value[x]);
43
44
        memset(v, 0, sizeof(v));
45
        for (int i = 1; i \le \min(n, m); i++)
46
             for (;;)
47
             {
48
                  memset(bx, false, sizeof(bx));
                  memset(by, false, sizeof(by));
49
                  if (find(i)) break;
50
51
                  int Min = oo;
                  \quad \mathbf{for} \ (\mathbf{int} \ \mathbf{j} \ = \ 1; \ \mathbf{j} \ <= \ \mathbf{n}; \ \mathbf{j} +\!\!\!\!+)
52
53
                       if (bx[j])
                          for (int x = first[j]; x; x = next[x])
54
55
                               if (!by[where[x]])
                                   Min = min(Min, L[j] + R[where[x]] - value[x]);
56
                  for (int j = 1; j \le n; j++) if (bx[j]) L[j] -= Min;
57
                  for (int j = 1; j \le m; j++) if (by[j]) R[j] += Min;
58
59
60
        for (int i = 1; i \le n; i++)
             for (int x = first[i]; x; x = next[x])
61
                  if (v[where[x]] == i) ans += value[x];
62
63
         printf("%d\n", abs(ans));
64
   }
65
66
   int main(){
        scanf("%d%d", &m, &m);
67
        memset(first, 0, sizeof(first)); l = 0;
for (int i = 1; i \le n; i++)
68
69
70
             for (int j = 1; j \ll m; j++)
71
72
                  int x;
                  scanf("%d", &x);
73
74
                  makelist(i, j, -x);
```

3.7. HOPCROFT 83

3.7 Hopcroft

```
1 #include <cstdio>
 2 #include <cstring>
 3 #define maxn 50005
 4 #define maxm 150005
 5 \quad \textbf{int} \ \text{cx} \left[ \left[ \text{maxn} \right], \text{cy} \left[ \text{maxn} \right], \text{mk} \left[ \text{maxn} \right], \text{q} \left[ \text{maxn} \right], \text{src} \left[ \text{maxn} \right], \text{pre} \left[ \text{maxn} \right];
   int head [maxn], vtx [maxm], next [maxm], tot, n,m;
 7
     inline void Add(int a,int b)
 8
 9
           vtx[tot]=b;
           next[tot]=head[a];
10
11
           head[a] = tot++;
12
13
    inline int Maxmatch()
14
     {
15
           memset(mk, -1, sizeof(mk));
16
           memset(cx, -1, sizeof(cx));
           memset(cy, -1, sizeof(cy));
17
           for (int p=1, fl=1,h, tail; fl;++p)
18
19
20
                 f l = 0:
21
                 h=t a i l = 0;
22
                 for (int i=0; i< n; ++i)
23
                       if (cx[i]==-1)
                             q[++tail]=i, pre [i]=-1, src [i]=i;
24
                 for (h=1;h<=tail;++h)
25
26
27
                       int u=q[h];
                       if (cx[src[u]]!=-1) continue;
28
29
                       for (int pp=head[u], v=vtx[pp]; pp; pp=next[pp], v=vtx[pp])
30
                             if (mk[v]!=p)
31
                             {
32
                                   mk[v]=p;
                                   q[++tail]=cy[v];
33
                                   if (cy[v]>=0)
34
35
                                   {
36
                                         pre[cy[v]] = u;
37
                                         \operatorname{src}\left[\operatorname{cy}\left[\mathbf{v}\right]\right] = \operatorname{src}\left[\mathbf{u}\right];
38
                                         continue;
```

```
39
40
                                  int d, e, t;
41
                                          -t\,ail\,\,,\,f\,l\,{=}\,1,d\!\!=\!\!u\,,\,e\!\!=\!\!v\,;d\,!\!\!=\!-1;t\!\!=\!\!cx\,[\,d\,]\,\,,\,cx\,[\,d\,]\!\!=\!\!e\,,\,cy\,[\,e\,]\!\!=\!\!d\,,\,e\!\!=\!\!t\,\,,d\!\!=\!\!pre\,[\,
42
                                             d]);
43
                                  break;
44
                            }
45
                 }
46
47
           int res = 0;
48
           for (int i=0; i< n; ++i)
                 res+=(cx[i]!=-1);
49
50
           return res;
51
52
    int main()
53
    {
           freopen ("4206. in", "r", stdin);
54
55
           freopen ("4206. out", "w", stdout);
56
           int P;
           scanf("%d%d%d",&n,&m,&P);
57
58
           tot=2;
           for (int i=0; i< P; ++i)
59
60
61
                int a,b;
                scanf ("%d%d",&a,&b);
62
63
                --a;--b;
64
                Add(a,b);
65
           printf("%d\n", Maxmatch());
66
67
           return 0;
68
    }
```

3.8 一般图最大匹配

```
#include <cstdio>
  #include <cstdlib>
  #include <cstring>
4 #include <iostream>
5 #include <algorithm>
6
   using namespace std;
   const int N=250;
8
   int n;//点数(1->n)
   int head;
10
   int tail;
   int Start;
11
   int Finish;
   int match [N]; //表示哪个点匹配了哪个点
   int Father [N]; //增广路的 Father
   int Base [N]; //该点属于哪朵花
```

3.8. 一般图最大匹配 85

```
int Q[N];
16
17
   bool mark [N];
   bool mat [N] [N]; //邻接矩阵
18
   bool InBlossom[N];
19
   bool in_Queue[N];
20
21
22
   void BlossomContract(int x,int y){
23
        memset(mark,0, sizeof(mark));
24
        memset(InBlossom, 0, sizeof(InBlossom));
25
   #define pre Father[match[i]]
26
        int lca,i;
27
        for (i=x; i; i=pre) { i=Base[i]; mark[i]=true; }
28
        for (i=y;i;i=pre) {i=Base[i]; if (mark[i]) {lca=i; break;} }//寻找 lca一定要注
            意, i=Base [i]
29
        for (i=x; Base[i]!=lca; i=pre) {
30
             if (Base[pre]!=lca) Father[pre]=match[i];//对于树中的父边是匹配边的点,向后
                跳BFSFather
            InBlossom [Base [i]] = true;
31
32
            InBlossom [Base [match [i]]] = true;
33
34
        for (i=y; Base[i]!=lca; i=pre) {
35
             if (Base[pre]!=lca) Father[pre]=match[i];//同理
36
            InBlossom [Base [i]] = true;
37
            InBlossom [Base [match [i]]] = true;
38
   #undef pre
39
        \mathbf{if} (Base [x]!=lca) Father [x]=y; //注意不能从这个奇环的关键点跳回来 lca
40
        if (Base[y]!=lca) Father[y]=x;
41
        for (i=1; i \le n; i++)
42
             if (InBlossom [Base[i]]) {
43
44
                 Base [i] = lca;
                 if (!in_Queue[i]) {
45
                     Q[++tail]=i;
46
47
                     \operatorname{in}_{\operatorname{Queue}}[i] = \mathbf{true}; //要注意如果本来连向树中父结点的边是非匹配边的点,可能是没有入
                         队的BFS
48
                 }
49
            }
   }
50
51
52
   void Change(){
53
        int x, y, z;
        z=Finish;
54
        while (z) {
55
56
            y=Father[z];
57
            x=match [y];
58
            match[y]=z;
59
            match[z]=y;
60
            z=x;
```

61

```
62
    }
63
64
    void FindAugmentPath(){
         memset(Father, 0, sizeof(Father));
65
         memset(in_Queue,0, sizeof(in_Queue));
66
67
         for (int i=1; i \le n; i++) Base [i]=i;
68
         head=0; tail=1;
69
        Q[1] = Start;
        in_Queue [Start]=1;
70
         while (head!=tail) {
71
72
             int x=Q++head;
73
             for (int y=1;y<=n;y++)
                  \mathbf{if} (mat[x][y] & Base[x]!=Base[y] & match[x]!=y) {//无意义的边
74
                      if ( Start==y || (match[y] && Father[match[y]]))//精髓地用表示该点是
75
                          否Father
76
                          BlossomContract(x,y);
77
                      else if (!Father[y]) {
                          Father [y]=x;
78
79
                          if (match[y]){
                               Q[++tail]=match[y];
80
81
                               in_Queue[match[y]] = true;
82
                          }
                          else{
83
                               Finish=y;
84
85
                               Change();
86
                               return;
87
                          }
                      }
88
89
                 }
90
         }
    }
91
92
93
    void Edmonds(){
94
         memset(match, 0, sizeof(match));
         for (Start=1;Start \le n;Start++)
95
             if (match [Start] == 0)
96
97
                 FindAugmentPath();
98
    }
99
100
    void output(){
101
         memset(mark,0, sizeof(mark));
         int cnt=0;//一般图最大匹配 最大点数
102
         for (int i=1; i<=n; i++)
103
104
             if (match[i]) cnt++;
         printf("%d\n",cnt);
105
106
         for (int i=1; i<=n; i++)
107
             if (!mark[i] && match[i]) {
108
                 mark[i]=true;//和imatch[i匹配]
109
                 mark[match[i]] = true;
```

3.9. 无向图最小割 87

```
110
                   printf("%d_{\square}%d n", i, match[i]);
111
              }
112
    }
113
114 int main(){
115
         int x,y;
116
         scanf("%d",&n);
117
         memset(mat, 0, sizeof(mat));
         while (scanf("%d%d",&x,&y)!=EOF)
118
              mat[x][y] = mat[y][x] = 1;
119
120
         Edmonds();
121
         output();
122
         return 0;
   }
123
```

3.9 无向图最小割

```
1 const int V = 100;
 2 #define typec int
 3 const typec inf = 0x3f3f3f; // max of res
   const typec maxw = 1000; // maximum edge weight
    typec g[V][V], w[V]; //g[i]/[j] = g[j]/[i]
    \mathbf{int} \ a[V], \ v[V], \ na[V];
 7
    typec mincut(int n) {
 8
         int i, j, pv, zj;
         typec best = \max * n * n;
 9
10
         for (i = 0; i < n; i++) v[i] = i; // vertex: 0 ~ n-1
         while (n > 1) {
11
              \mbox{for } (a [v [0]] = 1, \ i = 1; \ i < n; \ i++) \ \{
12
13
                   a[v[i]] = 0; na[i - 1] = i;
14
                   w[i] = g[v[0]][v[i]];
15
              for (pv = v[0], i = 1; i < n; i++) {
16
17
                    for (zj = -1, j = 1; j < n; j++)
                         if (!a[v[j]] && (zj < 0 || w[j] > w[zj]))
18
19
                              zj = j;
                    a[v[zj]] = 1;
20
21
                    if (i = n - 1) {
                         {\bf if} \ (\, b\, e\, s\, t \, > \, w\, [\, z\, j\, ]\,) \ b\, e\, s\, t \, = \, w\, [\, z\, j\, ]\,;
22
23
                         for (i = 0; i < n; i++)
                              g[v[i]][pv] = g[pv][v[i]] +=
24
25
                                   g[v[zj]][v[i]];
26
                         v[zj] = v[--n];
27
                         break;
                    }
28
29
                   pv = v[zj];
30
                    \  \  \, \textbf{for}\  \  \, (\,\, j \,\, = \,\, 1\,; \  \  \, j \,\, < \,\, n\,; \  \  \, j \,+\!+)
                         if (!a[v[j]])
31
32
                             w[j] += g[v[zj]][v[j]];
```

```
33
             }
34
35
        return best;
36
   }
37
38
   int main()
39
   {
40
        return 0;
41
            最小树形图 (ElogE + V^2)
   const int N = 1111;
 1
   const int M = 11111111;
   {\bf int}\ n,\ m,\ a\,,\ b\,,\ c\,,\ x\,[N]\,,\ y\,[N]\,,\ z\,[N]\,,
 4
        edgeCnt, firstEdge[N], from[M], length[M], nextEdge[M],
        inEdge [N], key [M], delta [M], depth [M], child [M] [2],
5
6
        parent [N], choosen [N], degree [N], queue [N];
 7
   void pass (int x) {
8
        if (delta[x] != 0) {
9
             key[child[x][0]] += delta[x];
             delta[child[x][0]] += delta[x];
10
             key[child[x][1]] += delta[x];
11
12
             delta[child[x][1]] += delta[x];
13
             delta[x] = 0;
14
        }
   }
15
   int merge (int x, int y) {
16
        if (x = 0 \text{ or } y = 0) {
17
             return x ^ y;
18
19
        \mathbf{if} (\ker[x] > \ker[y])  {
20
21
             swap(x, y);
22
23
        pass(x);
         \operatorname{child}[x][1] = \operatorname{merge}(\operatorname{child}[x][1], y);
24
25
         if (depth[child[x][0]] < depth[child[x][1]]) 
26
             swap(child[x][0], child[x][1]);
27
28
        depth[x] = depth[child[x][1]] + 1;
29
        return x;
30
   }
31
   void addEdge (int u, int v, int w) {
32
        from[++ edgeCnt] = u;
33
        length[edgeCnt] = w;
34
        nextEdge[edgeCnt] = firstEdge[v];
35
        firstEdge[v] = edgeCnt;
        key[edgeCnt] = w;
36
```

37

delta[edgeCnt] = 0;

```
38
         depth[edgeCnt] = 0;
39
         child [edgeCnt][0] = child [edgeCnt][1] = 0;
40
         inEdge[v] = merge(inEdge[v], edgeCnt);
41
   }
42
   void deleteMin (int &r) {
43
         pass(r);
44
         r = merge(child[r][0], child[r][1]);
45
    int findRoot (int u) {
46
         if (parent[u] != u) {
47
48
             parent [u] = findRoot (parent [u]);
49
50
         return parent[u];
    }
51
    void clear () {
52
53
         edgeCnt = 0;
54
         depth[0] = -1;
55
         memset(inEdge, 0, sizeof(inEdge));
56
         memset(firstEdge, 0, sizeof(firstEdge));
57
    int solve (int root) {
58
59
         int result = 0;
         \  \  \, \textbf{for} \  \, (\, \textbf{int} \  \, \textbf{i} \, = \, 0\,; \  \, \textbf{i} \, < \, \textbf{n}\,; \, +\!\!\!\!+ \, \textbf{i}\,) \  \, \{\,
60
             parent[i] = i;
61
62
         while (true) {
63
             memset(degree, 0, sizeof(degree));
64
65
             for (int i = 0; i < n; +++ i) {
                  if (i == root or parent[i] != i) {
66
67
                       continue;
68
                  while (findRoot(from[inEdge[i]]) == findRoot(i)) {
69
70
                       deleteMin(inEdge[i]);
                  }
71
72
                  choosen[i] = inEdge[i];
                  degree [findRoot (from [choosen [i]])] += 1;
73
74
             int head = 0, tail = 0;
75
76
             for (int i = 0; i < n; ++ i) {
                  if (i != root and parent[i] == i and degree[i] == 0) {
77
78
                       queue [tail ++] = i;
79
                  }
80
             }
             while (head < tail) {
81
                  if (-- degree [findRoot (from [choosen [queue [head]]])] == 0) {
82
83
                       queue [tail ++] = findRoot (from [choosen [queue [head]]]);
84
85
                  head += 1;
86
             }
```

```
87
             bool found = false;
88
             for (int i = 0; i < n; ++ i) {
89
                  if (i != root and parent[i] == i and degree[i] > 0) {
90
                       found = true;
91
                       int j = i, temp = 0;
92
                      do{
93
                           j = findRoot(from[choosen[j]]);
94
                           parent[j] = i;
95
                           deleteMin(inEdge[j]);
96
                           result += key[choosen[j]];
97
                           key[inEdge[j]] -= key[choosen[j]];
                           delta [inEdge [j]] -= key [choosen [j]];
98
                           temp = merge(temp, inEdge[j]);
99
                       } while (j != i);
100
                       inEdge[i] = temp;
101
                  }
102
103
             }
104
             if (not found) {
                  break;
105
106
             }
107
         for (int i = 0; i < n; ++ i) {
108
109
              if (i != root and parent[i] == i) {
                  result += key[choosen[i]];
110
              }
111
112
113
         return result;
114
            最小树形图 (V^3)
    3.11
    const int maxn=1100;
 1
    int n,m, g[maxn][maxn], used[maxn], pass[maxn], eg[maxn], more, queue[maxn];
    void combine (int id , int &sum ) {
         \mathbf{int} \ \mathtt{tot} = 0 \ , \ \mathtt{from} \ , \ \mathtt{i} \ , \ \mathtt{j} \ , \ \mathtt{k} \ ;
 4
         for ( ; id!=0 && !pass[ id ] ; id=eg[id] ) {
 5
 6
              queue [tot++]=id; pass [id]=1;
 7
         for ( from=0; from<tot && queue[from]!=id ; from++);</pre>
 8
 9
         i f
10
              ( from=tot ) return ;
11
         more = 1;
         for (i=from ; i< tot ; i++) {
12
13
             sum+=g[eg[queue[i]]][queue[i]];
14
              if ( i!=from ) {
15
                  used [queue [ i ]] = 1;
16
                  for (j = 1; j \le n; j++) if (!used[j])
```

if (g[queue[i]][j]<g[id][j]) g[id][j]=g[queue[i]][j] ;

17

18

}

3.11. 最小树形图 (V^3)

91

```
19
       for ( i=1; i<=n ; i++) if ( !used[i] && i!=id ) {
20
21
           for (j=from ; j< tot ; j++){}
22
               k=queue[j];
23
               if (g[i][id]>g[i][k]-g[eg[k]][k])g[i][id]=g[i][k]-g[eg[k]][k];
24
25
26
27
   int mdst( int root ) { // return the total length of MDST
28
       int i , j , k , sum = 0 ;
       memset ( used , 0 , sizeof ( used ) ) ;
29
       for (more = 1; more ;)
30
31
           more = 0;
           memset (eg, 0, sizeof(eg));
32
33
           34
               for (j=1, k=0; j \le n; j ++) if (!used[j] \&\& i!=j)
35
                   if ( k==0 || g[j][i] < g[k][i] ) k=j;
36
               eg[i] = k;
37
           }
38
           memset(pass,0, sizeof(pass));
           for (i=1; i \le n; i++) if (!used[i] \&\& !pass[i] \&\& i!= root) combine
39
40
               ( i , sum ) ;
41
42
       for ( i =1; i <=n ; i ++) if ( !used[i] && i!= root ) sum+=g[eg[i]][i];
43
       return sum ;
44
   int main(){
45
       freopen("input.txt","r",stdin);
46
       freopen("output.txt", "w", stdout);
47
48
       int i,j,k,test,cases;
49
       cases=0;
50
       scanf("%d",&test);
51
       while (test){
52
           test --:
           //if (n==0) break;
53
           scanf("%d%d",&n,&m);
54
55
56
           memset(g,60,sizeof(g));
57
           foru(i,1,n)
58
               foru (j,1,n) g [i] [j]=1000001;
59
           foru(i,1,m) {
               scanf ("%d%d",&j,&k);
60
61
               j++;k++;
               scanf("%d",&g[j][k]);
62
           }
63
64
           cases++;
           printf("Case_#%d:_", cases);
65
66
           k=mdst(1);
           if (k>1000000) printf("Possums!\n");
67
```

Chapter 4

数据结构

4.1 KD 树

4.1.1 tEJtM+ **高维**

```
1 #include < cstring >
2 #include < cstdio >
3 #include<algorithm>
4 #include < cmath >
5 using namespace std;
  int nkd = 0, n, d, m;
   template<typename T> struct vector
8
9
       T a [2];
10
       T \& operator [] (int x) {return a[x];}
11
       const T & operator [] (int x) const {return a[x];}
12
   };
13 struct kd
14
   {
      kd * s[2];
15
      {f int} i;
16
17
      vector < int > x;
      vector<int> find();
18
19
   } kdpool[222222], *root;
   vector < int > u, v, vec[111111];
21
   long long dis(const vector<int> & a, const vector<int> & b)
22
23
      long long rtn = 0;
      24
25
      return rtn;
26
27
   void bize(int le, int ri, int index, int i)
28
       if(ri <= le) return;</pre>
29
30
      if(ri == le + 1)
```

```
31
       {
32
            if(vec[le][i] > vec[ri][i]) swap(vec[le], vec[ri]);
33
            return;
34
35
       int l = le, r = ri, x = vec[le + rand() \% (ri - le + 1)][i];
36
       for (;;)
37
38
            \mathbf{while}\,(\,\mathrm{vec}\,[\,l\,\,]\,[\,\,\mathrm{i}\,\,]\ <\ \mathrm{x}\,)\ l++;
39
            while (vec [r][i] > x) r--;
40
            if(l < r)
41
42
                 swap (vec [1], vec [r]);
43
                 1++; r--;
44
            if(l >= r) break;
45
46
47
       int posi = le;
48
       while (posi \leq ri and vec [posi][i] \leq x) posi++;
49
       if(index \le posi - 1) bize(le, posi - 1, index, i);
       if(index >= posi) bize(posi, ri, index, i);
50
51
    kd * build(int le, int ri, int i)
52
53
    {
       if(le > ri) return 0;
54
       kd * p = \&kdpool[++nkd];
55
       {\tt bize(le\,,\ ri\,,\ (le\,+\,ri\,)\ /\ 2\,,\ i\,)}\,;
56
       p->x = vec[(le + ri) / 2];
57
58
       p\rightarrow i = i;
59
       if(le != ri)
60
       {
            p->s[0] = build(le, (le + ri) / 2 - 1, (i + 1) % d);
61
62
            p \rightarrow s[1] = build((le + ri) / 2 + 1, ri, (i + 1) % d);
63
       else p->s[0] = p->s[1] = 0;
64
       return p;
65
    }
    vector <int> kd:: find()
66
67
       vector < int > rtn(x), tmp;
68
69
       double l; int go = v[i] > x[i];
70
       if (s [go])
71
       {
72
            tmp = s[go] -> find();
73
            if(dis(tmp, v) < dis(rtn, v)) rtn = tmp;
74
75
       l = sqrt(dis(rtn, v));
76
       \mathbf{if}(v[i] - 1 < x[i]) and x[i] < v[i] + 1 and s[go ^ 1])
77
            tmp = s [go ^1] -> find();
78
79
            if(dis(tmp, v) < dis(rtn, v)) rtn = tmp;
```

4.1. KD 树 95

```
80
81
        return rtn;
 82
    }
 83 int main()
 84
        scanf("%d%d", &n, &d);
 85
 86
        for(int i = 1; i \le n; i++)
87
             for (int j = 0; j < d; j++)
 88
                 scanf("%d", &vec[i][j]);
 89
 90
        }
        root = build(1, n, 0);
91
        scanf("%d", &m);
 92
 93
        for (int i = 1; i \le m; i++)
94
             \mbox{ for } (\mbox{ int } \mbox{ j } = \mbox{ 0}; \mbox{ j } < \mbox{ d}; \mbox{ j++})
95
                 scanf("%d", &v[j]);
96
97
             u = root \rightarrow find();
98
             for(int j = 0; j < d; j++)
99
                 printf("%d%c", u[j], j == d - 1?' \n': '_{\sqcup}');
100
101
102
103
        return 0;
104
    4.1.2 Logic_IU
    读入 N 个点,输出距离每个点的最近点。
    const int MAX_N = 100000 + 10;
    const int MAX_NODE = 200000 + 10;
 3
    const LL INF = 20000000000000000020LL;
 4
 5 int N;
 6
    struct Point
 7
 8
    {
 9
         int x, y, id;
 10
    };
 11
 12 LL dis (const Point &a, const Point &b)
 14
         return 1LL * (a.x - b.x) * (a.x - b.x) + 1LL * (a.y - b.y) * (a.y - b.y);
 15
 16
    struct Node
 17
 18
 19
         Point p;
20
         int maxX, minX, maxY, minY;
21
         int 1, r, d;
```

```
22
         Node *ch[2];
23
    };
24
25 LL ret;
26
    LL ans [MAX_N];
27
    Node *root;
    Point p[MAX_N], queryPoint;
28
29
    Node \ *totNode \ , \ nodePool \ [MAX\_NODE] \ ;
30
   int cmpx(const Point &a, const Point &b)
31
32
    {
33
         return a.x < b.x;
34
    int cmpy(const Point &a, const Point &b)
35
36
    {
37
         return a.y < b.y;
38
    }
39
40
    Node* newNode(int 1, int r, Point p, int deep)
41
42
         Node *t = totNode ++;
         t->1 = 1; t->r = r;
43
44
         t->p = p; t->d = deep;
45
         t \rightarrow maxX = t \rightarrow minX = p.x;
46
         t\rightarrow maxY = t\rightarrow minY = p.y;
47
         return t;
48
    }
49
    void updateInfo(Node *t, Node *p)
50
51
    {
52
          t \rightarrow maxX = max(t \rightarrow maxX, p \rightarrow maxX);
         t\rightarrow maxY = max(t\rightarrow maxY, p\rightarrow maxY);
53
54
         t \rightarrow minX = min(t \rightarrow minX, p \rightarrow minX);
55
          t \rightarrow minY = min(t \rightarrow minY, p \rightarrow minY);
56
    }
57
    Node* build(int 1, int r, int deep)
58
59
60
          if (l == r) return NULL;
61
          if (\text{deep } \& 1) \text{ sort}(p+1, p+r, \text{cmpx});
62
          else sort (p + 1, p + r, cmpy);
63
         int mid = (l + r) \gg 1;
64
         Node *t = \text{newNode}(1, r, p[\text{mid}], \text{deep & } 1);
65
          if (l + 1 == r) return t;
         t -\!\!>\!\! ch \, [\, 0\, ] \ = \ build \, (\, l \; , \ mid \, , \ deep \; + \; 1) \; ;
66
67
         t \rightarrow ch[1] = build(mid + 1, r, deep + 1);
68
          if (t->ch[0]) updateInfo(t, t->ch[0]);
69
          if (t->ch[1]) updateInfo(t, t->ch[1]);
70
          return t;
```

4.1. KD 树 97

```
71
    }
72
73
    void updateAns(Point p)
74
         ret = min(ret, dis(p, queryPoint));
75
76
    }
77
78 LL calc(Node *t, LL d)
79
    {
80
         LL tmp;
81
         if (d) {
82
             if (queryPoint.x >= t->minX && queryPoint.x <= t->maxX) tmp = 0;
83
             else tmp = min(abs(queryPoint.x - t->maxX), abs(queryPoint.x - t->minX));
84
              if (queryPoint.y >= t->minY && queryPoint.y <= t->maxY) tmp = 0;
85
86
             else tmp = min(abs(queryPoint.y - t->maxY), abs(queryPoint.y - t->minY));
87
88
         return tmp * tmp;
    }
89
90
    void query(Node *t)
91
92
93
         if (t == NULL) return;
         if (t->p.id != queryPoint.id) updateAns(t->p);
94
95
         if (t->l + 1 == t->r) return;
         LL dl = t - sch[0] ? calc(t - sch[0], t - sd) : INF;
96
         LL dr = t->ch[1] ? calc(t->ch[1], t->d) : INF;
97
98
         if (dl < dr) 
99
             query(t->ch[0]);
100
              if (ret > dr) query (t->ch[1]);
101
         } else {
102
             query(t->ch[1]);
103
             if (ret > dl) query (t->ch[0]);
104
         }
105
    }
106
107
    void solve()
108
         \operatorname{scanf}\left(\,\text{``'}\!\text{''d''}\;,\;\;\&\!N\right)\;;
109
110
         for(int i = 0; i < N; ++ i)
             scanf("%d%d", &p[i].x, &p[i].y);
111
112
             p[i].id = i;
113
         totNode = nodePool;
114
         root = build(0, N, 1);
115
116
         for(int i = 0; i < N; ++ i) {
117
118
             queryPoint = p[i];
119
             ret = INF;
```

```
120
             query(root);
121
             ans[p[i].id] = ret;
122
123
         for (int i = 0; i < N; ++ i)
             printf("%I64d\n", ans[i]);
124
125
    }
126
127
    int main()
128
         int T; scanf("%d", \&T);
129
130
         for( ; T --; )
             solve();
131
132
         return 0;
133
    }
```

4.2 后缀自动机

4.2.1 tEJtM+LCA **非递归** Tarjan

```
1 #include < cstdio >
2 #include < cstring >
3 #include<ctime>
, Q, siz[2000022];
  int ans [1000011], x, y;
  struct recq
6
7
8
      int v, p;
9
  } q[2000022];
10
  bool f[2000022];
  char c;
11
12
  struct recmap
13
14
      int y, next, i;
  15
  void build(int x, int y)
16
17
  {
18
      map[++1] \cdot y = y;
19
      map[l].next = idx[x];
20
      idx[x] = 1;
21
  }
  void build(int x, int y, int z)
22
23
24
      map1[++11] \cdot y = y;
25
      map1[11].i = z;
26
      map1[ll].next = iddx[x];
27
      iddx[x] = 11;
28
  }
```

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```
29 int getr(int x)
30 {
31
         int p = x, p1, p2;
32
         \mathbf{while}(\operatorname{rela}[p]!=p) \ p = \operatorname{rela}[p];
33
         p1 = p; p = x;
34
         while (rela[p]!=p) \{p2 = rela[p]; rela[p] = p1; p = p2; \}
35
         return p1;
36 }
37 struct recsam
38 {
39
         int 1, v;
         recsam * go[26], *p;
40
    } *leaf, *root, polsam[2000022];
41
    recsam * newrecsam(int _l)
42
43
   {
44
         recsam * p = \&polsam[++np];
45
         p->1 = _1; p->v = np; p->p=0;
46
         memset(p->go, 0, sizeof(p->go));
47
         return p;
48
   }
   recsam * newrecsam (recsam & x)
49
50
51
         recsam * p = \&polsam[++np];
52
         *p=x;
53
         p->v = np;
54
         return p;
55
56
   int main()
57
         \operatorname{scanf}("%d n", \&n);
58
         root = newrecsam(0); leaf = root;
59
60
         memset(siz, 0, sizeof(siz));
61
         for(int i = 1; i \le n; i++)
62
              scanf("%c", &c); c = 'a';
63
              recsam * np = newrecsam(i);
64
              nod[i] = np->v; siz[np->v] = 1;
65
66
              recsam * p = leaf;
67
              \mbox{ for } (\,;p \ \mbox{ and } \ p\!\! -\!\! >\!\! go\,[\,c\,] \ =\! \ 0\,;p\!\! =\!\! p\!\! -\!\! >\!\! p)\,p\!\! -\!\! >\!\! go\,[\,c\,] \ = \ np\,;
68
              if(!p) np->p = root;
              else
69
70
71
                   recsam * q;
72
                   if((q=p->go[c])->l == p->l+1) np->p = q;
73
                   else
74
                   {
75
                        recsam * nq = newrecsam(*q);
76
                        nq -> l = p -> l + 1;
77
                        nq->p = q->p;
```

```
78
                                                                  q->p = np->p = nq;
  79
                                                                   \begin{tabular}{ll} \beg
                                                      }
  80
  81
                                         }
  82
                                         leaf = np;
  83
  84
                           1 = 0; memset(idx, 0, sizeof(idx));
  85
                           for(int i = 1; i \le np; i++) if(polsam[i].p)build(polsam[i].p->v, polsam[i].v);
                           scanf("%d", &Q);
  86
                           11 = 0; memset(iddx, 0, sizeof(iddx));
  87
  88
                           for (int i = 1; i \le Q; i++)
  89
                                        {\rm scanf}\,(\,\text{``'}\!\text{d}\!\text{''}\!\text{d}''\,,\ \&\!x\,,\ \&\!y\,)\,;
  90
                                         build(nod[x], nod[y], i);
  91
                                         build \, (nod \, [\, y\,] \, , \, nod \, [\, x\,] \, , \, i\,) \, ;
  92
  93
                           }
  94
                           q[cl=1].v = 1;
  95
                           q[cl=1].p = idx[1];
  96
                           memset(f, false, sizeof(f));
  97
                           for(int i = 1; i <= np; i++) rela[i] = i;
                           while (cl)
  98
  99
100
                                        v = q[cl].v;
101
                                        q[cl].p = map[p=q[cl].p].next;
102
                                        if (p)
103
                                         {
                                                     q[++cl] . v = map[p]. y;
104
                                                     q\,[\,\,c\,l\,\,]\,\,.\,\,p\,\,=\,\,i\,d\,x\,\,[\,\,q\,[\,\,c\,l\,\,]\,\,.\,\,v\,\,]\,\,;
105
                                         }else
106
107
                                         {
108
                                                      f[v] = true;
                                                      for(int p = iddx[v]; p; p = map1[p].next)
109
110
                                                                    if(f[map1[p].y] = true) ans [map1[p].i] = getr(map1[p].y);
111
                                                      \operatorname{siz} [q[\operatorname{cl}-1].v] += \operatorname{siz} [v];
112
                                                      rela[getr(v)] = getr(q[cl-1].v);
113
                                        }
114
115
116
                           for (int i = 1; i \le Q; i++) printf ("%d\n", ans [i]!=1? siz [ans [i]]:0);
117
                           return 0;
118 }
             4.2.2 Logic_IU
             struct State
     1
     2
     3
                           int val;
     4
                           State *suf, *go[26];
             } *root, *last;
```

4.3. SPLAY 树

```
7
      State statePool [MAX_N], *curState;
 8
      void extend(int w)
 9
10
               State *p = last, *np = curState ++;
11
               np \rightarrow val = p \rightarrow val + 1;
12
               \mathbf{for} \left( \hspace{0.2cm} ; \hspace{0.2cm} p \hspace{0.2cm} \& \& \hspace{0.2cm} ! \hspace{0.2cm} p \hspace{-0.2cm} -\hspace{-0.2cm} > \hspace{-0.2cm} \mathrm{go} \left[ w \right]; \hspace{0.2cm} p \hspace{0.2cm} = \hspace{0.2cm} p \hspace{-0.2cm} -\hspace{-0.2cm} > \hspace{-0.2cm} \mathrm{suf} \hspace{0.2cm} \right)
13
14
                      p\rightarrow go[w] = np;
               if (! p)
15
16
                      np \rightarrow suf = root;
17
               else {
                       State *q = p - so[w];
18
                       if (q\rightarrow val = p\rightarrow val + 1)
19
20
                              np \rightarrow suf = q;
                       else {
21
22
                               State *nq = curState ++;
23
                              nq \rightarrow val = p \rightarrow val + 1;
24
                              memcpy(nq->go, q->go, sizeof q->go);
25
                              nq \rightarrow suf = q \rightarrow suf;
26
                              q \rightarrow suf = np \rightarrow suf = nq;
27
                               for( ; p \&\& p->go[w] == q; p = p->suf)
28
                                      p \rightarrow go[w] = nq;
29
                      }
30
31
               last = np;
32
      }
```

4.3 Splay 树

4.3.1 Logic_IU

注意初始化内存池和 null 节点,以及根据需要修改 update 和 relax,区间必须是 1-based

```
const int MAX_NODE = 50000 + 10;
   const int INF = 20000000000;
3
   struct Node *null;
4
5
6
    struct Node
7
    {
8
        int rev , add;
9
        int val, maxv, size;
10
        Node *ch[2], *p;
11
        void set(Node *t, int _d) {
12
             ch[\underline{d}] = t;
13
14
             t \rightarrow p = this;
15
16
        int dir() {
17
             return this == p->ch[1];
```

```
18
19
         void update() {
20
              \max v = \max(\max(\operatorname{ch}[0] - > \max v, \operatorname{ch}[1] - > \max v), \operatorname{val});
21
               size = ch[0] -> size + ch[1] -> size + 1;
22
         void relax() {
23
24
               if (add) {
25
                    ch[0] - > appAdd(add);
26
                    ch[1] - > appAdd(add);
27
                    add = 0;
28
29
               if (rev) {
                    ch[0] - > appRev();
30
                    ch[1] -> appRev();
31
32
                    rev = false;
33
               }
34
         }
35
         void appAdd(int x) {
36
               if (this == null) return;
37
              add += x;
               val += x;
38
39
              \max y += x;
40
41
         void appRev() {
               if (this == null) return;
42
               rev = true;
43
44
              swap(ch[0], ch[1]);
45
         }
    };
46
47
    Node nodePool[MAX_NODE], *curNode;
48
49
50
    Node *newNode(int val = 0)
51
    {
52
         Node *t = curNode ++;
53
         t->maxv = t->val = val;
54
         t\rightarrow rev = t\rightarrow add = 0;
55
         t \rightarrow size = 1;
56
         t \rightarrow ch[0] = t \rightarrow ch[1] = t \rightarrow p = null;
57
         return t;
58
    }
59
60
    struct Splay
61
    {
         Node *root;
62
63
         Splay() {
64
               root = newNode();
65
66
               root \rightarrow set (newNode(), 0);
```

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```
67
               root -> update();
 68
          }
 69
 70
          Splay(int *a, int N) \{ //sequence is 1-based
 71
               root = build(a, 0, N + 1);
 72
 73
 74
          Node* build(int *a, int l, int r) {
 75
               if (l > r) return null;
 76
               int mid = 1 + r \gg 1;
 77
               Node *t = \text{newNode}(a[\text{mid}]);
 78
               t \rightarrow set(build(a, l, mid - 1), 0);
 79
               t\rightarrow set(build(a, mid + 1, r), 1);
 80
               t->update();
 81
               return t;
 82
          }
 83
 84
          void rot(Node *t)
 85
 86
               Node *p = t \rightarrow p; int d = t \rightarrow dir();
               p->relax(); t->relax();
 87
               if (p = root) root = t;
 88
 89
               p\rightarrow set(t\rightarrow ch[! d], d);
90
               p->p->set(t, p->dir());
91
               t \rightarrow set(p, ! d);
92
               p->update();
93
94
 95
          void splay(Node *t, Node *f = null)
 96
               for (t->relax(); t->p != f; ) {
97
98
                    if (t\rightarrow p\rightarrow p = f) rot(t);
                    else t \rightarrow dir() = t \rightarrow p \rightarrow dir()? (rot(t \rightarrow p), rot(t)): (rot(t), rot(t));
99
100
101
               t->update();
102
          }
103
104
          Node* getKth(int k) {
105
               Node *t = root;
106
               int tmp;
107
               for ( ; ; ) {
                    t->relax();
108
                    tmp = t - size + 1;
109
                    if (tmp == k) return t;
110
                    if (tmp < k) {
111
                         k = tmp;
112
113
                         t = t - > ch[1];
114
                    } else
115
                         t = t \rightarrow ch[0];
```

```
116
               }
117
118
          //make\ range[l,r]\ root \rightarrow ch[1] - ch[0]
119
          //make\ range[x+1,x]\ to\ add\ something\ after\ position\ x
120
          void getRng(int 1, int r) {
121
122
               r += 2;
               Node *p = getKth(l);
123
               Node *q = getKth(r);
124
125
               splay(p); splay(q, p);
          }
126
127
128
          void addRng(int 1, int r, int x) {
               {\tt getRng}\,(\,l\ ,\ r\,)\,;
129
130
               root \rightarrow ch[1] \rightarrow ch[0] \rightarrow appAdd(x);
131
          }
132
133
          void revRng(int 1, int r) {
134
               getRng(l, r);
               root - > ch[1] - > ch[0] - > appRev();
135
136
          }
137
138
          int maxvRng(int 1, int r) {
139
               getRng(l, r);
               return root ->ch [1] ->ch [0] ->maxv;
140
          }
141
142
     };
143
     void initNull()
144
145
    {
146
          curNode = nodePool;
          null = curNode ++;
147
148
          \text{null} \rightarrow \text{size} = 0;
149
          null \rightarrow maxv = -INF;
150
    }
     4.3.2 shytangyuan
  1 #include <cstdio>
  2 #include <cstdlib>
  3 #include <cstring>
  4 #include <ctime>
  5
  6
    using namespace std;
 7
 8
     struct {
```

int L,R, father, key, size;

9

} f[100001];

4.3. SPLAY 树

```
int root, n,Q;
11
12
13
   inline void zig(int now){
        int x=f[now]. father, y=f[x]. father;
14
        if (y)
15
16
           if (f[y].L=x) f[y].L=now;
17
           else f[y].R=now;
18
        f [now].father=y;
19
        f[x]. father=now;
20
        f[x].L=f[now].R;
21
        f[f[x].L].father=x;
        f [now].R=x;
22
23
        f[x].size=f[f[x].L].size+f[f[x].R].size+1;
24
        f [now]. size=f [f [now].L]. size+f [f [now].R]. size+1;
   }
25
26
27
   inline void zag(int now){
28
        int x=f[now]. father, y=f[x]. father;
29
        if (y)
30
           if (f[y].L=x) f[y].L=now;
31
           else f [y]. R=now;
32
        f[now]. father=y;
33
        f[x]. father=now;
34
        f[x].R=f[now].L;
35
        f[f[x].R].father=x;
36
        f [now]. L=x;
37
        f[x].size=f[f[x].L].size+f[f[x].R].size+1;
38
        f [now]. size=f [f [now].L]. size+f [f [now].R]. size+1;
39
   }
40
   inline void splay(int now){
41
42
        int x=f[now].father,y=f[x].father;
43
        while (x)
44
45
               if (!y)
                   if (f[x].L = now) zig(now);
46
47
                   else zag(now);
48
               else if (f[y].L=x)
49
                        if (f[x].L=now) zig(x), zig(now);
50
                        else zag(now), zig(now);
51
                    else if (f[x].L=now) zig(now), zag(now);
52
                    else zag(x), zag(now);
53
               x=f[now]. father; y=f[x]. father;
54
55
        root=now;
56
57
58
   inline void insert (int now, int k) {
59
        if (!root)
```

```
60
         {
61
            root=k;
62
            return;
63
         if (f[k]. key \le f[now]. key)
64
             if (!f[now].L) f[now].L=k, f[k].father=now, splay(k);
65
66
             else insert (f [now].L,k);
67
         else if (!f[now].R) f[now].R=k,f[k].father=now,splay(k);
              else insert (f [now].R,k);
68
    }
69
70
    inline void del(int now){
71
72
         splay (now);
         int LL=f [now].L,RR=f [now].R;
73
74
         f[now]. L=f[now]. R=f[now]. key=f[now]. father=f[now]. size=0;
75
         f[LL]. father=f[RR]. father=0;
76
         if (!LL && !RR) root=0;
77
         else if (!LL) root=RR;
78
         else if (!RR) root=LL;
79
         else
80
81
             root=RR;
82
             while (f[RR].L) RR=f[RR].L;
83
             f[RR].L=LL;
             f[LL].father=RR;
84
85
             splay(LL);
         }
86
87
    }
88
89
    int findkth(int now,int k){
         if (k=f[f[now].L].size+1) return(now);
90
91
92
    int main(){
         scanf("%d",&n);
93
94
         root = 0;
         for (int i=1;i<=n;i++)
95
             scanf("%d",&f[i].key),f[i].size=1,insert(root,i);
96
97
         scanf("%d",&Q);
98
         for (;Q--;)
99
100
             int type;
101
             scanf("%d",&type);
             if (type==1)
102
103
104
                  int x,y;
105
                  scanf("%d%d",&x,&y);
106
                  del(x);
107
                  f[x]. key=y; f[x]. size=1;
108
                  insert (root, x);
```

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```
109 }
110 else
111 {
112 int x;
113 scanf("%d",&x);
114 printf("%d\n",f[findkth(root,x)].key);
115 }
116 }
117 }
```

4.4 动态树

根据需求修改 Node 中的 relax 和 update 函数,修改 access,以及 Node 的构造函数,注意初始化内存池和 null 节点

```
struct Node
1
2
3
        Node *ch[2], *p;
4
        int isroot;
5
        bool dir();
6
        void set(Node*, bool);
7
        void update();
        void relax();
8
   } *null;
9
10
   void rot(Node *t)
11
12
13
        Node *p = t - p; bool d = t - dir();
14
        p->relax(); t->relax();
        p->set(t->ch[! d], d);
15
        if (p\rightarrow isroot) t\rightarrow p = p\rightarrow p, swap(p\rightarrow isroot, t\rightarrow isroot);
16
17
        else p->p->set(t, p->dir());
18
        t \rightarrow set(p, ! d);
19
        p->update();
   }
20
21
   void Splay(Node *t)
22
23
   {
24
        for (t->relax(); ! t->isroot; ) {
25
             if (t\rightarrow p\rightarrow isroot) rot(t);
             26
27
28
        t->update();
29
   }
30
   void Access(Node *t)
31
32
33
        for(Node *s = null; t != null; s = t, t = t -> p) 
34
            Splay(t);
35
             t\rightarrow ch[1]->isroot = true;
36
            s \rightarrow isroot = false;
```

```
37
              t \rightarrow ch[1] = s;
38
              t->update();
39
40
    }
    bool Node::dir()
41
42
43
         return this = p->ch[1];
44
    void Node::set(Node *t, bool _d)
45
46
    {
47
         ch[\underline{d}] = t; t \rightarrow p = this;
48
    void Node::Update()
49
50
    {
51
52
   }
53
   void Node::Relax()
54
55
         if (this == Null) return;
56
57
```

二叉堆 4.5

双射堆, ind[v] 表示标号为 v 的节点在堆中的位置

```
const int MAX_V = 100000 + 10;
2
   struct Heap
3
4
        int tot;
5
       int a [MAX\_V], h [MAX\_V], ind [MAX\_V];
6
       void exchange(int i, int j) {
7
            swap(h[i], h[j]);
8
            swap(ind[h[i]], ind[h[j]]);
9
10
        inline int val(int x) {
11
            return a[h[x]];
12
13
       void fixUp(int x) {
            if (x / 2 &  val(x / 2) < val(x))
14
15
                exchange(x, x / 2), fixUp(x / 2);
16
17
       void fixDown(int x) {
            int p = x * 2; if (p > tot) return;
18
            if (p < tot && val(p + 1) > val(p)) ++ p;
19
20
            if (val(p) > val(x))
21
                exchange(p, x), fixDown(p);
22
       void Update(int i, int x) {
23
```

4.6. 左偏树 109

```
24
            a[i] = x;
25
            fixUp(ind[i]);
26
            fixDown(ind[i]);
27
28
        int top() {
29
            return h[1];
30
31
        void pop() {
32
            exchange(1, tot);
33
            -- tot;
34
            fixDown(1);
35
36
        void insert(int i, int x) {
            ++ tot;
37
38
            h[tot] = i;
39
            ind[i] = tot;
40
            a[i] = x;
41
            fixUp(tot);
42
        }
   } H;
43
```

4.6 左偏树

没写 delete 操作,注意初始化内存池和 null 节点

```
struct Node
 2
 3
         int dis, val;
         Node *ch[2];
 4
 5
    } *null;
 6
 7
    Node* merge(Node *u, Node *v)
 8
    {
 9
          if (u == null) return v;
         if (v == null) return u;
10
         if (u\rightarrow val < v\rightarrow val) swap(u, v);
11
12
         u \rightarrow ch[1] = merge(u \rightarrow ch[1], v);
13
          if (u->ch[1]->dis > u->ch[0]->dis)
14
              swap(u->ch[1], u->ch[0]);
15
         u \rightarrow dis = u \rightarrow ch[1] \rightarrow dis + 1;
16
         return u;
17
    }
18
19
    Node* newNode(int w)
20
21
         Node *t = totNode ++;
22
         t \rightarrow ch[0] = t \rightarrow ch[1] = null;
23
         t -> val = w; t -> dis = 0;
24
         return t;
```

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25 }

4.7 Treap

```
包含 build, insert 和 erase , 执行时注意初始化内存池和 null 节点
```

```
struct Node *null;
 2
3
    struct Node
 4
 5
         int key, val, size;
 6
         Node *ch[2];
 7
         Node() {
              key = INT MAX;
 8
9
              val = size = 0;
10
         Node(int _val) {
11
12
              size = 1;
              val = val;
13
              key = bigRand();
14
              \operatorname{ch}[0] = \operatorname{ch}[1] = \operatorname{null};
15
16
17
         int bigRand() {
              return rand() * RAND_MAX + rand();
18
19
20
         void update() {
21
              \mbox{size} \; = \; \mbox{ch}[0] - \! > \! \mbox{size} \; + \; \mbox{ch}[1] - \! > \! \mbox{size} \; + \; 1;
22
23
    };
24
25
    struct Treap
26
    {
         Node *root;
27
28
         Treap() {
29
              root = null;
30
         void rot(Node *&t, int d) {
31
              Node *p = t->ch [d]; t->ch [d] = p->ch [! d]; p->ch [! d] = t;
32
33
              34
              t = p;
         }
35
36
         {f void} insert (Node *&t, int x) {
37
              if (t = null) {
38
39
                   t = new Node(x);
40
                   return;
41
42
              int dir = x >= t -> val;
43
              insert(t->ch[dir], x);
```

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```
44
             if (t->ch[dir]->key < t->key)
45
                  rot(t, dir);
46
             else
47
                 t->update();
        }
48
49
50
        void erase(Node *&t, int x) {
51
             if (t = null)
                 return;
52
             if (t\rightarrow val == x)  {
53
54
                  int dir = t->ch[1]->key < t->ch[0]->key;
                  if (t->ch[dir] = null) {
55
56
                      delete t;
57
                      t = null;
                      \mathbf{return}\,;
58
59
                  }
60
                  rot(t, dir);
61
                  erase(t->ch[! dir], x);
62
                 t->update();
63
                 return;
64
             bool dir = x > t -> val;
65
66
             erase(t->ch[dir], x);
67
             t->update();
68
69
70
        void insert(int x) {
71
             insert(root, x);
72
73
74
        void erase(int x) {
75
             erase(root, x);
76
77
   };
```

4.8 线段树

包含建树和区间操作样例,没有写具体操作

```
struct Tree
1
2
  {
3
      int 1, r;
      Tree *ch[2];
4
      Tree() {}
5
      6
7
8
         if (1 + 1 = r)
9
             return;
10
         int mid = 1 + r \gg 1;
```

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```
11
            ch[0] = new Tree(1, mid, sqn);
12
            ch[1] = new Tree(mid, r, sqn);
        }
13
14
15
        void insert(int p, int x) {
16
            if (p < l \mid | p >= r)
17
                return;
18
            //some operations
19
            if (1 + 1 == r)
20
                return;
21
            ch[0] -> insert(p, x);
22
            ch[1] -> insert(p, x);
23
        }
24
25
        int query(int l, int r, int x) {
26
            if (_r <= l || _l >= r)
                return 0;
27
28
            if (_l <= l && _r >= r)
29
                // return information in [l, r)
            //merge\ ch[0]->query(\_l,\ \_r,\ x), ch[1]->query(\_l,\ \_r,\ x) and return
30
        }
31
32
   };
```

4.9 轻重链剖分

包含 BFS 剖分过程,线段树部分视题目而定

```
struct Tree()
1
2
3
4
   };
5
   int father [MAX_N] , size [MAX_N] , depth [MAX_N];
7
   int bfsOrd [MAX_N], pathId [MAX_N], ordInPath [MAX_N], sqn [MAX_N];
   Tree *root [MAX_N];
8
9
10
   void doBfs(int s)
11
   {
        int *que = bfsOrd;
12
13
        int qh = 0, qt = 0;
        father[s] = -1; depth[s] = 0;
14
15
16
        for(que[qt ++] = s; qh < qt;)
            int u = que[qh ++];
17
18
            foreach (iter, adj[u]) {
19
                int v = *iter;
20
                if (v = father[u])
21
                     continue;
22
                father[v] = u;
```

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```
23
                 depth[v] = depth[u] + 1;
24
                 que[qt ++] = v;
25
             }
26
        }
27
   }
28
29 void doSplit()
30
31
        for (int i = N - 1; i >= 0; — i) {
32
             int u = bfsOrd[i];
33
             size[u] = 1;
             for each(iter, adj[u]) {
34
                 int v = *iter;
35
36
                  if (v = father[u])
                      continue;
37
38
                  size[u] += size[v];
39
             }
40
        }
41
42
        memset(pathId, -1, sizeof pathId);
        for(int i = 0; i < N; ++ i)
43
             int top = bfsOrd[i];
44
45
             if (pathId[top] != -1)
46
                 continue;
47
48
             int cnt = 0;
49
             for (int u = top; u != -1;) {
50
                 \operatorname{sqn}[\operatorname{cnt}] = \operatorname{val}[u];
                 ordInPath[u] = cnt;
51
52
                 pathId[u] = top;
53
                 ++ cnt;
54
                 int next = -1;
55
56
                  for each(iter, adj[u]) {
                      int v = *iter;
57
                      if (v = father[u])
58
59
                           continue;
60
                      if (next < 0 \mid | size[next] < size[v])
61
                           next = v;
62
                 }
63
                 u = next;
64
             }
65
66
             root[top] = new Tree(0, cnt, sqn);
67
68
69
70 void prepare()
71
   {
```

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```
72 doBfs(0);
73 doSplit();
74 }
```

4.10 KMP

```
vector < int > KMP()
1
2
    {
3
          vector<int> ans;
          nxt[0] = -1;
 4
          nxt[1] = 0;
 5
 6
          for(int i = 2; i \le m; i++)
 7
 8
               nxt[i] = nxt[i - 1];
9
               while (nxt[i] >= 0 \text{ and } st[i] != st[nxt[i] + 1])
10
                     nxt[i] = nxt[nxt[i]];
11
               nxt[i]++;
12
          for (int i = 1, p = 1; i \le n; i++)
13
14
15
               \mathbf{while}(p \ \mathbf{and} \ \mathbf{str1}[i] \ != \ \mathbf{st}[p])
16
                     p = nxt[p-1] + 1;
17
               p++;
               {\bf i}\,{\bf f}\,(p\,=\!\!=m\,+\,1)\ p\,=\,nxt\,[m]\,\,+\,1\,,\ ans\,.\,push\_back\,(\,i\,\,-\,m)\,;
18
19
20
          {f return} \ {f ans} \; ;
21
    }
```

4.11 **扩展** KMP

```
传入字符串 s 和长度 N , \operatorname{next}[i] = \operatorname{LCP}(s, s[i..N-1])
   void z(char *s, int *next, int N)
1
2
   {
3
        int j = 0, k = 1;
        while (j + 1 < N \&\& s[j] = s[j + 1]) ++ j;
4
5
        next[0] = N - 1; next[1] = j;
6
        for(int i = 2; i < N; ++ i)
7
             int far = k + next[k] - 1, L = next[i - k];
8
             if (L < far - i + 1) next[i] = L;
9
             else {
                 j = \max(0, far - i + 1);
10
11
                 while (i + j < N \&\& s[j] = s[i + j]) ++ j;
12
                 next[i] = j; k = i;
13
             }
14
        }
15
   }
```

4.12. MANACHER 115

4.12 Manacher

```
void manacher (char str[], int len[], int n) {
1
2
       len[0] = 1;
       for (int i = 1, j = 0; i < (n << 1) - 1; ++ i) {
3
4
            int p = i \gg 1,
            q = i - p
5
            r = ((j + 1) >> 1) + len[j] - 1;
6
            len[i] = r < q? 0: min(r - q + 1, len[(j << 1) - i]);
7
8
            while (p - len[i] > -1 and q + len[i] < n and str[p - len[i]] = str[q + len[i]]
               i ] ] ) {
                len[i] += 1;
9
10
            if (q + len[i] - 1 > r) {
11
12
                j = i;
13
            }
14
       }
15
```

4.13 AC 自动机

4.13.1 Logic_IU

包含建 trie 和构造自动机的过程

```
1
2 struct acNode
3
4
         int id;
         acNode *ch[26], *fail;
    } *totNode, *root, nodePool[MAX_V];
6
7
   acNode* newNode()
8
9
    {
10
         acNode *now = totNode ++;
         now->id = 0; now->fail = 0;
11
         memset(now->ch, 0, sizeof now->ch);
12
13
         return now;
14
    }
15
   void acInsert(char *c, int id)
16
17
18
         acNode *cur = root;
         while (*c) {
19
              int p = *c - 'A'; //change the index
20
21
              if (! \operatorname{cur} - \operatorname{ch}[p]) \operatorname{cur} - \operatorname{ch}[p] = \operatorname{newNode}();
22
              cur = cur - > ch[p];
23
              ++ c;
24
25
         cur \rightarrow id = id;
```

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```
26
    }
27
28
    void getFail()
29
30
          acNode *cur;
          queue<acNode*> Q;
31
32
          for(int i = 0; i < 26; ++ i)
33
                if (root->ch[i]) {
34
                      root \rightarrow ch[i] \rightarrow fail = root;
35
                      Q. push (root ->ch [i]);
36
                else root \rightarrow ch[i] = root;
37
          while (! Q. empty()) {
                cur = Q. front(); Q. pop();
38
39
                for(int i = 0; i < 26; ++ i)
                      if (cur->ch[i]) {
40
41
                           \operatorname{cur} - \operatorname{ch}[i] - \operatorname{fail} = \operatorname{cur} - \operatorname{fail} - \operatorname{ch}[i];
42
                           Q. push ( cur->ch [ i ] );
43
                      } else cur->ch[i] = cur->fail->ch[i];
44
          }
45
    }
```

4.13.2 shytangyuan

```
1 #include <cstdio>
   #include <cstdlib>
   #include <cstring>
   #include <ctime>
5
6
   using namespace std;
7
   int a[100001][27], fail [100001], last [100001], c[100001], l, father [100001], type [100001];
8
9
   char can [1001];
10
   inline void maketrie(){
11
12
        memset(a, 0, sizeof(a));
13
        memset(type,0,sizeof(type));
14
        memset(last,0,sizeof(last));
15
        int = strlen(can), now=0;
16
        1 = 0;
17
        for (int i=0; i< n; i++)
18
            if (!a[now][can[i]-'A']) a[now][can[i]-'A']=++1, type[1]=can[i]-'A', father[1]=
19
20
            now=a [now] [can[i]-'A'];
21
22
        last [now] = 1;
23
   }
24
```

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```
25
    inline void makefail(){
26
         memset (fail, 255, sizeof (fail));
27
         fail[0] = 0;
28
         int k=0;
29
         for (int i=0; i <=25; i++)
30
             if (a [0] [i]) fail [a [0] [i]]=0, c[++k]=a [0] [i];
31
         for (int l=1; l<=k; l++)
32
              int m=c[1];
33
              if (fail [m] = -1)
34
35
36
                  int p=father[m];
                  while (p && !a[fail[p]][type[m]]) p=fail[p];
37
38
                  fail [m]=a [ fail [p]] [ type [m]];
39
                  last[m]+=last[fail[m]];
40
41
              for (int i=0; i <=25; i++)
42
                   if (a [m] [ i ]) c[++k]=a [m] [ i ];
43
         }
44
45
46
    int main(){
         scanf("%s", can);
47
48
         maketrie();
         makefail();
49
50
   }
    4.14
             后缀数组
    4.14.1 Logic IU
    对于串 a 求 SA, 长度为 N, M 为元素值范围, height[i]=LCP(suf[rank[i]],suf[rank[i]-1])
   const int MAX_N = 1000000 + 10;
 1
   int rank [MAX_N] , height [MAX_N] ;
 3
 4
    int cmp(int *x, int a, int b, int d)
 5
 6
    {
         return x[a] = x[b] \&\& x[a + d] = x[b + d];
 7
 8
 9
10
   void doubling (int *a, int N, int M)
11
12
         static int sRank [MAX_N], tmpA [MAX_N], tmpB [MAX_N];
         int *x = tmpA, *y = tmpB;
13
         for(int i = 0; i < M; ++ i) sRank[i] = 0;
14
15
         for (int i = 0; i < N; ++ i) ++ sRank[x[i] = a[i]];
16
         for (int i = 1; i < M; ++ i) sRank[i] += sRank[i - 1];
         \label{eq:for_int} \mbox{for} \, (\, \mbox{int} \  \, i \, = \, N \, - \, 1 \, ; \  \, i \, > = \, 0 \, ; \, \, - - \, \, i \, ) \  \, sa[-- \, \, sRank \, [\, x \, [\, i \, \, ] \, ] \, ] \, \, = \, i \, ;
17
```

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```
18
19
        for (int d = 1, p = 0; p < N; M = p, d <<= 1) {
20
            p = 0; for (int i = N - d; i < N; ++ i) y[p ++] = i;
            for(int i = 0; i < N; ++ i)
21
22
                if (sa[i] >= d) y[p ++] = sa[i] - d;
            for (int i = 0; i < M; ++ i) sRank[i] = 0;
23
24
            for(int i = 0; i < N; ++ i) ++ sRank[x[i]];
25
            for(int i = 1; i < M; ++ i) sRank[i] += sRank[i - 1];
            for (int i = N - 1; i \ge 0; — i) sa[— sRank [x[y[i]]]] = y[i];
26
27
            swap(x, y); x[sa[0]] = 0; p = 1;
28
            for (int i = 1; i < N; ++ i)
                x[sa[i]] = cmp(y, sa[i], sa[i-1], d) ? p - 1 : p ++;
29
30
        }
31
   }
32
33
   void calcHeight()
34
35
        for (int i = 0; i < N; ++ i) rank [sa[i]] = i;
36
       int cur = 0;
37
        for(int i = 0; i < N; ++ i)
            if (rank[i]) {
38
                if (cur) cur --;
39
40
                for( ; a[i + cur] = a[sa[rank[i] - 1] + cur]; ++ cur);
                height [rank [i]] = cur;
41
42
            }
43
   }
   4.14.2 shytangyuan
1 #include <cstdio>
2 #include <cstdlib>
   #include <cstring>
   #include <ctime>
5
6
   using namespace std;
   int test, n, SA[100001], c[100001], Rank[100001], tmp[100001], H[100001], f[100001];
8
9
   char can [50001];
10
11
   int main(){
       //freopen("1. txt", "r", stdin);
12
        //freopen ("2. txt", "w", stdout);
13
       scanf("%d",&test);
14
        for (test; test; test --)
15
16
                 scanf ( "%s\n",&can );
17
```

18

19

n=strlen(can);

memset(f, 0, sizeof(f));

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```
20
                                     for (int i=1; i \le n; i++) f[i]=int (can[i-1]);
21
                                     memset(c, 0, sizeof(c));
22
                                     for (int i=1; i \le n; i++) c[f[i]]++;
23
                                     for (int i=1; i <=1000; i++) c[i]+=c[i-1];
                                     for (int i=n; i; i--) SA[c[f[i]]--]=i;
24
25
                                     Rank[SA[1]] = 1;
26
                                     for (int i=2; i \le n; i++)
27
                                            if (f[SA[i]] == f[SA[i-1]]) Rank [SA[i]] = Rank [SA[i-1]];
28
                                            else \operatorname{Rank}[\operatorname{SA}[i]] = \operatorname{Rank}[\operatorname{SA}[i-1]] + 1;
                                     for (int L=1;L<=n;L+=L)
29
30
31
                                              if (Rank[SA[n]]==n) break;
                                              memset(c, 0, sizeof(c));
32
33
                                              for (int i=1; i \le n; i++) c[Rank[L+i]]++;
                                              for (int i=1; i \le n; i++) c[i]+=c[i-1];
34
35
                                              for (int i=n; i; i--) tmp[c[Rank[L+i]]--]=i;
36
                                              memset(c, 0, sizeof(c));
37
                                              for (int i=1;i<=n;i++) c[Rank[i]]++;
38
                                              for (int i=1; i \le n; i++) c[i]+=c[i-1];
39
                                              for (int i=n; i; i--) SA[c[Rank[tmp[i]]]--]=tmp[i];
40
                                              tmp[SA[1]] = 1;
41
                                              for (int i=2; i \le n; i++)
42
                                                      if \quad ((Rank [SA[i]] = Rank [SA[i-1]]) \&\& (Rank [SA[i] + L] = Rank [SA[i-1] + L] 
                                                            ]))
                                                             \operatorname{tmp}[\operatorname{SA}[i]] = \operatorname{tmp}[\operatorname{SA}[i-1]];
43
44
                                                     else \text{tmp}[SA[i]] = \text{tmp}[SA[i-1]] + 1;
                                              for (int i=1;i<=n;i++) Rank[i]=tmp[i];
45
46
                 int p=0;
47
48
                 for (int i=1;i<=n;i++)
49
                          int j=SA[Rank[i]-1];
50
51
                         p - = 1;
                          if (p<0) p=0;
52
                          while ((f[i+p]==f[j+p])) p++;
53
                         H[i]=p;
54
55
56
                 int ans=0;
57
                 for (int i=1;i<=n;i++)
                          ans+=n-SA[i]+1-H[i];
58
59
                 printf("%d\n", ans);
60
61
       4.14.3 DC3
      //DC3 待排序的字符串放在r 数组中从,r到 /0/r/n长度为-1/,n且最大值小于,omm
       //约定除r/n外所有的-1/r/i都大于0, r/n。-1/=0
      //函数结束后结果放在,sa数组中从,sa到,sa1,sa1,sa2,sa2,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3,sa3
 4 //必须开长度乘r3
```

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```
5 #define maxn 10000
6 #define F(x) ((x)/3+((x)\%3==1?0:tb))
7 #define G(x) ((x) < tb?(x)*3+1:((x)-tb)*3+2)
8 int wa[maxn], wb[maxn], wv[maxn], wss[maxn];
   int s [maxn*3], sa [maxn*3];
   int c0(int *r,int a,int b)
10
11
12
         return r[a] == r[b] \&\&r[a+1] == r[b+1] \&\&r[a+2] == r[b+2];
13
    }
   int c12(int k, int *r, int a, int b)
14
   {
15
16
         if(k==2) return r[a] < r[b] | | | r[a] = = r[b] \&\&c12(1,r,a+1,b+1);
         else return r[a] < r[b] | | | r[a] == r[b] \& \& wv[a+1] < wv[b+1];
17
18
    void sort(int *r,int *a,int *b,int n,int m)
19
20
   {
21
         int i;
22
         for (i=0; i < n; i++) wv [i]=r[a[i]];
23
         for (i=0; i \le m; i++) wss [i]=0;
24
         for (i=0; i < n; i++) wss [wv[i]]++;
25
         for (i=1; i \le m; i++) wss [i]+=wss [i-1];
26
         for (i=n-1; i \ge 0; i--) b[--wss[wv[i]]] = a[i];
27
28
   void dc3(int *r,int *sa,int n,int m)
29
    {
         int i, j, *rn=r+n, *san=sa+n, ta=0, tb=(n+1)/3, tbc=0,p;
30
31
         r[n]=r[n+1]=0;
32
         for (i = 0; i < n; i++)
33
              if(i\%3!=0) wa[tbc++]=i;
34
         sort(r+2,wa,wb,tbc,m);
35
         sort(r+1,wb,wa,tbc,m);
36
         sort (r, wa, wb, tbc, m);
37
         for(p=1,rn[F(wb[0])]=0, i=1; i < tbc; i++)
38
              rn[F(wb[i])] = c0(r, wb[i-1], wb[i])?p-1:p++;
39
         if (p<tbc) dc3(rn, san, tbc, p);
40
         else for (i=0; i < tbc; i++) san[rn[i]]=i;
41
         for (i=0; i < tbc; i++)
42
              if(san[i] < tb) wb[ta++]=san[i]*3;
43
         if(n\%3==1) wb[ta++]=n-1;
44
         sort (r, wb, wa, ta, m);
45
         for (i = 0; i < tbc; i++)
              wv[wb[i]=G(san[i])]=i;
46
47
         for (i=0, j=0, p=0; i < ta \&\& j < tbc; p++)
              sa[p]=c12(wb[j]\%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
48
49
         for (; i < ta; p++) sa [p]=wa[i++];
         \label{eq:formula} \mbox{for} \; (\, ; \, j\! <\! t \, b \, c \; ; \, p\! +\! +) \; \; sa \; [\, p]\! =\! wb \, [\, j \, +\! +] \; ;
50
51
    }
52
    int main(){
53
         int n, m=0;
```

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```
\begin{array}{lll} 54 & scanf\left(\text{``%d'',\&n}\right); \\ 55 & \textbf{for (int } i=0; i< n; i++) \ scanf\left(\text{``%d'',\&s[i]}\right), s[i]++, m=max(s[i]+1, m); \\ 56 & printf\left(\text{``%d\n'',m}\right); \\ 57 & s[n++]=0; \\ 58 & dc3\left(s, sa, n, m\right); \\ 59 & \textbf{for (int } i=0; i< n; i++) \ printf\left(\text{``%d\_'', sa[i]}\right); printf\left(\text{``\n''}\right); \\ 60 & \end{array}
```

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Chapter 5

杂

5.1 m²logn **求线性递推第** n 项

```
// given first m a[i] and coef c[i] (0-based),
   // calc a[n] mod p in <math>O(m^*m^*log(n)).
   // a[n] = sum(c[m-i]*a[n-i]), i = 1...m
   // i.e. a[m] = sum(c[i]*a[i]), i = 0...m-1
   int linear_recurrence(LL n, int m, int a[], int c[], int p) {
5
        LL \ v[M] = \{1 \% p\}, \ u[M < 1], \ msk = !!n;
6
7
        for(LL \ i = n; \ i > 1; \ i >>= 1) \ msk <<= 1;
8
        for (LL x = 0; msk; msk >>= 1, x <<= 1) {
9
             fill_n(u, m << 1, 0);
10
             int b = !!(n \& msk); x = b;
             if(x < m) u[x] = 1 \% p;
11
             else {
12
                  for(int i = 0; i < m; ++i)
13
14
                      for(int j = 0, t = i+b; j < m; ++j, ++t)
                           u\,[\,\,t\,\,] \ = \ (\,u\,[\,\,t\,\,] + v\,[\,\,i\,\,] \,^*\,v\,[\,\,j\,\,]\,)\ \%\ p\,;
15
16
                  for (int i = (m < 1) - 1; i >= m; --- i)
                      for (int j = 0, t = i-m; j < m; ++j, ++t)
17
18
                           u[t] = (u[t]+c[j]*u[i]) \% p;
19
20
             copy(u, u+m, v);
21
22
        int an = 0;
        for (int i = 0; i < m; ++i) an = (an+v[i]*a[i]) % p;
23
24
        return an;
25
```

5.2 FFT

- 1 #include < cstdio >
- 2 #include < cmath >
- 3 #include < cstring >

```
4 #include<algorithm>
    using namespace std;
    double pi = 2 * acos(0.0);
 7 const int pw2lim = 65536;
    {f struct} recmap
 8
 9
10
           int y, next;
11
    } map[100011];
12
    struct recq
13
           \quad \textbf{int} \quad p \,, \quad v \,; \quad
14
    } st[50011];
15
    int idx[50001], ii[5000000], li1, n, K, x, y, z, ans[50001], l, l2, ele, siz[50001],
16
    \begin{array}{c} q[50001]\,,\ cl\,,\ dis\,[50001]\,,\ fa\,[50001];\\ \textbf{int}\ L,\ go[2\ ^*\ pw2lim]\,,\ d,\ nrec\,,\ rec\,[50001]\,,\ v\,,\ p\,; \end{array}
17
18
    bool f [50001], isprime [50001];
    int mnpw2(int x)
19
20
    {
21
           int rtn = 1;
22
          \mathbf{while}(\mathbf{x})
23
24
                x >>= 1;
25
                rtn \ll 1;
26
27
          return rtn;
28
    }
29
    struct vector
30
    {
           int siz , *a;
31
32
           int & operator [] (int x)
33
34
                return a[x];
35
           }
36
           vector()
37
                a = ii + li1;
38
39
40
     };
41
    struct C
42
    {
43
           double real, imag;
44
          C(const double & _real, const double & _imag) : real(_real), imag(_imag){}
45
46
          C(\mathbf{const}\ \mathbf{double}\ \&\ x)\{\mathrm{real}\ =\ x;\ \mathrm{imag}\ =\ 0;\}
           void print(char c)
47
48
           {
                 \texttt{printf}\left(\,\text{``}(\%f\,, \, | \%f\,)\%c\,\text{''}\,, \text{ real}\,, \text{ imag}\,, \text{ c}\,\right)\,;
49
           }
50
```

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```
} a[pw2lim], b[pw2lim], res1[pw2lim], res2[pw2lim], res[pw2lim], tmp[pw2lim], unit[
51
       pw2lim], temp;
   const C operator * (const C & a, const C & b)
52
53
        return C(a.real * b.real - a.imag * b.imag, a.real * b.imag + a.imag * b.real);
54
55
  }
56
   const C operator + (const C & a, const C & b)
57
        return C(a.real + b.real, a.imag + b.imag);
58
59
  }
  const C operator - (const C & a, const C & b)
60
61
        return C(a.real - b.real, a.imag - b.imag);
62
63
   void build(int x, int y)
64
65
66
        map[++1] \cdot y = y;
67
       map[1].next = idx[x];
        idx[x] = 1;
68
69
   void dft(C * sour, C * dest)
70
71
72
        for (int i = 0; i < L; i++) tmp[go[i + L]] = sour[i];
73
        for (int l = 1; l < L; l <<= 1)
74
            12 = 1 << 1;
75
76
            ele = pw2lim / l2;
77
            for (int i = 0; i < L; i += 12)
                for(int j = 0; j < 1; j++)
78
79
                    temp = tmp[i + l + j] * unit[ele * j];
80
81
                    tmp[i + l + j] = tmp[i + j] - temp;
82
                    tmp[i + j] = tmp[i + j] + temp;
83
                }
84
        for (int i = 0; i < L; i++) dest[i] = tmp[i];
85
86
87
   void fft (vector p1, vector p2)
88
89
       L = mnpw2(p1.siz + p2.siz - 1);
90
        for (int i = 0; i < p1. siz; i++) a[i] = p1[i];
        for (int i = p1. siz; i < L; i++) a[i] = 0;
91
        for (int i = 0; i < p2.siz; i++) b[i] = p2[i];
92
        for (int i = p2. siz; i < L; i++) b[i] = 0;
93
94
        dft(a, res1);
95
        dft(b, res2);
96
        for (int i = 0; i < L; i++) res [i] = res1[i] * res2[i];
        dft(res, res1);
97
```

```
98
          for (int i = 1; i \le nrec and rec[i] < p1.siz + p2.siz - 1; <math>i++) ans [i] += (int) (
               res1[L - rec[i]].real / L + 0.5);
99
          //ans[i](0 \le i \le L) = res1[(L - i) \% L].
100
     }
     vector dvcq(int v)
101
102
103
          if(siz[v] == 2)
104
105
               vector vec;
106
               vec.siz = 2;
107
               vec[0] = 0;
               vec[1] = 1;
108
               li1 += vec.siz;
109
110
               return vec;
111
112
          \mathbf{int} \ u\!\!=\!\!v\,, \ sum\!=\!1;
113
          for (int p=idx [v]; p;)
114
115
               if(siz[y=map[p].y] > siz[u]/2)
116
                    siz[y] += siz[u] -= siz[y];
117
118
                    u = y;
119
                    p = idx[y];
120
               else p = map[p].next;
121
122
          int bak, biz;
123
          vector p1, p2;
124
          for(int p = idx[u]; p; p = map[p].next)
125
126
               sum += siz [map[p].y];
127
               if(sum >= siz[u]/2)
128
129
                    biz = siz[u];
130
                    bak = idx[u];
                    i\, d\, x\, [\, u\, ] \,\, = \, map\, [\, p\, ]\, .\,\, n\, e\, x\, t\; ;
131
                    siz[u] = sum - 1;
132
                    p1 = dvcq(u);
133
134
                    idx[u] = bak;
135
                    bak = map[p].next;
                    map[p].next = 0;
136
137
                    siz[u] = sum;
                    p2 = dvcq(u);
138
                    \operatorname{siz} \left[\, u\,\right] \;=\; \operatorname{biz} \;;
139
140
                    map[p].next = bak;
141
                    break;
142
               }
143
144
          fft (p1, p2);
145
          vector vec;
```

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```
146
           fa[v] = 0;
147
           q[cl=1] = v;
148
           dis[v] = 0;
           vec[0] = 0;
149
150
           vec.siz = 0;
151
           for(int op = 1; op \ll cl; op++)
152
                 for(int p = idx[u = q[op]], y; p; p = map[p].next)
153
                       if ((y=map[p].y) != fa[u])
154
                            vec[dis[y] = dis[fa[q[++c1] = y] = u] + 1] ++;
155
156
                            vec.siz = max(vec.siz, dis[y]);
157
158
           vec.siz++;
159
           li1 += vec.siz;
160
           return vec;
161
162
     int main()
163
      {
164
           go[1] = 0;
           for(int i = 2; i \le pw2lim; i \le 1)
165
166
                 for (int j = 0; j < i / 2; j++)
167
168
                      go[i + j] = go[i / 2 + j] * 2;
169
170
                 for (int j = i / 2; j < i; j++)
171
172
                      go[i + j] = go[j] * 2 + 1;
173
174
175
           }
176
           unit[0] = 1;
           unit [32768] = -1;
177
178
           unit [16384] = C(0, 1);
179
           for (int i = 8192; i >= 1; i /= 2)
180
                 unit[i] = C((unit[0].real + unit[i * 2].real) / 2, (unit[0].imag + unit[i *
181
                      2].imag) / 2);
                 \mathbf{double} \ \operatorname{len} \ = \ \operatorname{sqrt} \big( \, \operatorname{unit} \, [\, \operatorname{i} \, ] \, . \, \operatorname{imag} \ * \ \operatorname{unit} \, [\, \operatorname{i} \, ] \, . \, \operatorname{imag} \ + \ \operatorname{unit} \, [\, \operatorname{i} \, ] \, . \, \operatorname{real} \ * \ \operatorname{unit} \, [\, \operatorname{i} \, ] \, . \, \operatorname{real} \big) \, ;
182
183
                 unit[i].imag *= 1/len; unit[i].real *= 1/len;
184
           for (int i = 1; i \le 65536; i++)
185
186
                 if(i - (i & -i))
187
188
                       unit [i] = C(1, 0);
189
190
                       for (int x = i; x; x = x \& -x)
191
                            unit[i] = unit[i] * unit[x & -x];
192
193
```

```
194
          } //求单位复根
195
196
          memset(isprime, true, sizeof(isprime));
          nrec = 0; rec[0] = 0x7fffffff;
197
          for (int i = 2; i \le 50000; i++)
198
199
               if(isprime[i]) rec[++nrec] = i;
200
201
               for(int j = 1; j \le nrec and i * rec[j] \le 50000 and i % rec[j - 1]; j++)
202
                    isprime[i * rec[j]] = false;
203
          scanf("%d", &n);
204
205
          memset(idx, 0, sizeof(idx));
206
          1 = 1;
          for(int i = 1; i < n; i++)
207
208
209
               scanf("%d%d", &x, &y);
210
               build(x, y);
211
               build (y, x);
212
          }
213
          memset(siz, 0, sizeof(siz));
          memset(f, true, sizeof(f));
214
          f[1] = false;
215
          st[cl = 1].v = 1;
216
          st[1].p = idx[1];
217
218
          while (cl)
219
          {
220
               v = st[cl].v;
221
               st[cl].p = map[p = st[cl].p].next;
222
               if(p)
223
               {
                    if (f [map[p].y])
224
225
226
                         st[++cl] \cdot v = map[p] \cdot y;
227
                         st[cl].p = idx[map[p].y];
228
                         f[map[p].y] = false;
229
                    }
               }else
230
231
232
                    siz[v]++;
233
                    siz[st[cl - 1].v] += siz[v];
234
                    cl --;
235
               }
236
237
          li1 = 0;
238
          memset(ans, 0, sizeof(ans));
239
          dvcq(1);
240
          long long tot = 0;
          for (int i = 1; i \le \operatorname{nrec}; i++) tot += \operatorname{ans}[i];
241
242
          \operatorname{printf}(\text{"%lf} \setminus \text{n"}, (\operatorname{double}) \operatorname{tot} / ((\operatorname{long long}) \text{n *} (\text{n} - 1) / 2));
```

5.3. 中国剩余定理 129

5.3 中国剩余定理

包括扩展欧几里得, 求逆元, 和保证除数互质条件下的 CRT

```
1 LL x, y;
2
  void exGcd(LL a, LL b)
3
       if (b == 0) {
4
          x = 1;
5
          y = 0;
6
7
          return;
8
9
       \operatorname{exGcd}(b, a \% b);
10
       LL k = y;
       y = x - a / b * y;
11
12
       x = k;
   }
13
14
15 LL inversion (LL a, LL b)
16
17
       exGcd(a, b);
       return (x \% b + b) \% b;
18
   }
19
20
21 LL CRT(vector<LL> m, vector<LL> a)
22
23
       int N = m. size();
24
       LL M = 1, ret = 0;
25
       for(int i = 0; i < N; ++ i)
26
          M *= m[i];
27
       28
29
30
31
       return ret;
32
  }
```

5.4 Pollard's Rho+Miller-Rabbin

```
大数分解和素性判断
```

```
1 typedef long long LL;
2
3 LL modMul(LL a, LL b, LL P)
```

```
{
4
 5
        LL ret = 0;
6
         for( ; a; a >>= 1) {
7
              if (a & 1) {
 8
                  ret += b;
9
                  if (ret >= P) ret -= P;
10
11
             b <<= 1;
12
              if (b \gg P) b = P;
13
14
        return ret;
15
    }
16
    LL modPow(LL a, LL u, LL P)
17
18
   {
19
        LL ret = 1;
20
         \mathbf{for}( ; u; u \gg 1, a = \operatorname{modMul}(a, a, P))
21
              if (u \& 1) ret = modMul(ret, a, P);
22
         return ret;
23
    }
24
25
    int millerRabin (LL N)
26
27
         if (N = 2) return true;
        LL \ t \ = \ 0 \ , \ u \ = \ N \ - \ 1 \ , \ x \ , \ y \ , \ a \ ;
28
29
         for( ; ! (u \& 1); ++ t, u >>= 1) ;
30
         for (int k = 0; k < 10; ++ k) {
             a = rand() \% (N - 2) + 2;
31
32
             x = \text{modPow}(a, u, N);
33
             for (int i = 0; i < t; ++ i, x = y) {
                  y \ = \ \mathrm{modMul}(\,x\,,\ x\,,\ N)\;;
34
35
                  if (y = 1 \&\& x > 1 \&\& x < N - 1) return false;
36
37
              if (x != 1) return false;
38
39
         return true;
40
    }
41
42 LL gcd(LL a, LL b)
43
         return ! b ? a : gcd(b, a % b);
44
45
    }
46
47
    LL pollardRho(LL N)
48
49
        LL i = 1, x = rand() \% N;
50
        LL y = x, k = 2, d = 1;
51
52
             d = \gcd(x - y + N, N);
```

```
53
            if (d != 1 && d != N) return d;
54
            if (++ i == k) y = x, k <<= 1;
55
            x = (modMul(x, x, N) - 1 + N) \% N;
        } while (y != x);
56
57
        return N;
58
   }
59
60
   void getFactor(LL N)
61
   {
62
        if (N < 2) return;
63
        if (millerRabin(N)) {
64
            //do some operations
65
            return;
66
        LL x = pollardRho(N);
67
68
        getFactor(x);
69
        getFactor(N / x);
70
   }
```

5.5 **素数判定** (long long **内确定性算法**)

```
int strong_pseudo_primetest(long long n,int base) {
1
2
        long long n2=n-1, res;
3
        int s; s=0;
4
        while (n2\%2==0) n2>>=1,s++;
        res=powmod(base, n2, n);
5
6
        if((res == 1) | | (res == n-1)) return 1;
7
8
        while (s > = 0) {
9
            res=mulmod(res,res,n);
10
            if(res=n-1) return 1;
11
12
13
        return 0; // n is not a strong pseudo prime
14
   int isprime(long long n) {
15
        if (n<2) return 0;
16
17
        if (n<4) return 1;
18
        if(strong_pseudo_primetest(n,2)==0) return 0;
19
        if (strong pseudo primetest (n,3) == 0) return 0;
20
        if(n<1373653LL) return 1;
21
        if(strong_pseudo_primetest(n,5)==0) return 0;
22
        if (n<25326001LL) return 1;
        if(strong_pseudo_primetest(n,7)==0) return 0;
23
24
        if(n==3215031751LL) return 0;
25
        if (n<2500000000LL) return 1;
26
        if (strong_pseudo_primetest(n,11)==0) return 0;
27
        if (n<2152302898747LL) return 1;
```

```
28
         if(strong_pseudo_primetest(n,13)==0) return 0;
29
         if (n<3474749660383LL) return 1;
30
         if (strong_pseudo_primetest(n,17)==0) return 0;
31
         if (n<341550071728321LL) return 1;
32
         if(strong_pseudo_primetest(n,19)==0) return 0;
33
         if(strong_pseudo_primetest(n,23)==0) return 0;
34
         if(strong_pseudo_primetest(n,29)==0) return 0;
35
         if(strong_pseudo_primetest(n,31)==0) return 0;
36
         if (strong pseudo primetest (n,37)==0) return 0;
37
         return 1;
38
   }
           求前 P 个数的逆元
   void solve (int m) {
2
         int inv[m];
3
        inv[1] = 1;
         for (int i = 2; i < m; ++ i) {
 4
             inv \left[ \; i \; \right] \; = \; \left( \; \left( \; \mathbf{long} \; \; \mathbf{long} \; \right) \left( m \; - \; m \; / \; \; i \; \right) \; \; * \; \; inv \left[ m \; \% \; \; i \; \right] \right) \; \% \; m;
 5
 6
         }
 7
   }
          广义离散对数 (不需要互质)
   void extendedGcd (int a, int b, long long &x, long long y) {
1
2
        if (b) {
3
             extendedGcd(b, a % b, y, x);
             y = a / b * x;
 4
 5
         } else {}
 6
             x = a;
7
             y = 0;
8
         }
9
10
    int inverse (int a, int m) {
        long long x, y;
11
12
         extendedGcd(a, m, x, y);
13
        return (x \% m + m) \% m;
14
    // a \hat{x} = b \pmod{m}
15
   int solve (int a, int b, int m) {
16
17
        int tmp = 1 \% m, c;
        map < int, int > s;
18
19
         if (tmp == b) {
20
             return 0;
21
         for (int i = 1; i \le 50; ++ i) {
22
23
             tmp = ((long long)tmp * a) \% m;
```

24

25

if (tmp = b)

return i;

5.8. N 次剩余 133

```
26
27
28
        int x_0 = 0, d = 1 \% m;
29
        while (true) {
            tmp = gcd(a, m);
30
31
            if (tmp == 1) {
32
                break;
33
            x = 0 + +;
34
            d = ((long long)d * (a / tmp)) % m;
35
36
            if (b % tmp) {
37
                return -1;
38
39
            b /= tmp;
40
            m /= tmp;
41
        \dot{b} = ((long long)b * inverse(d, m)) \% m;
42
43
        c = int(ceil(sqrt(m)));
44
        s.clear();
45
        tmp = b;
        int tmpInv = intverse(a, m);
46
        for (int i = 0; i != c; ++ i) {
47
48
            if (s.find(tmp) = s.end()) 
49
                s[tmp] = i;
50
            tmp = ((long long)tmp * tmpInv) % m;
51
        }
52
53
        tmp = 1;
        for (int i = 0; i != c; ++ i) {
54
            tmp = ((long long)tmp * a) % m;
55
56
57
        int ans = 1;
58
        for (int i = 0; i != c; ++ i) {
59
            if (s.find(ans) != s.end()) 
                return x_0 + i * c + s. find (ans) -> second;
60
61
            ans = ((long long) ans * tmp) \% m;
62
63
64
        return -1;
65
   5.8
          n 次剩余
1 const int LimitSave=100000;
   long long P,K,A;
3
   vector<long long>ans;
4
   struct tp{
        long long expo, res;
```

data[LimitSave + 100];

```
7
    long long _mod(long long a, long long mo) {
8
         a=a\%mo;
9
         if (a<0) a+=mo;
10
         return a;
11
    long long powers (long long a , long long K , long long modular) {
12
13
         long long res;
14
         res=1;
15
         while (K!=0) {
              if (K & 1) res= mod(res*a, modular);
16
17
             K=K>>1:
              a=\mod(a*a, \mod a);
18
19
20
         return res;
21
    }
22
    long long get_originroot(long long p) {
23
         long long primes [100];
24
         long long tot , i , tp , j ;
25
         i=2; tp=P-1; tot=0;
26
         while (i * i \le P-1) {
27
              if (_mod(tp,i)==0) {
28
                   tot++;
29
                   primes[tot]=i;
30
                   while (\mod(tp, i) == 0) tp/=i;
31
32
              i++;
33
34
         if (tp!=1) \{tot++; primes[tot]=tp;\}
35
         i = 2;
36
         bool ok;
37
         while (1) {
38
              ok=true;
39
              foru(j,1,tot) {
40
                   \mathbf{if} \ (\operatorname{powers}\left(\mathbf{i} \ , \ (P-1)/\operatorname{primes}\left[ \ \mathbf{j} \ \right] \ , \ P\right) = = 1) \ \{
41
                        150
42
                        ok = false;
43
                        break;
44
                   }
45
46
              if (ok) break;
47
              i++;
48
         }
49
         return i;
50
51
    bool
    euclid_extend(long long A ,long long B ,long long C ,long long &x, long
52
    long &y, long long
53
54
   &gcdnum) {
55
         long long t;
```

5.8. N 次剩余 135

```
56
         if (A==0) {
57
             gcdnum = B;
58
             if \pmod{C , B} ==0) \{
                 x=0; y=C/B;
59
                 return true;
60
61
62
             else return false;
63
         else if (euclid_extend(_mod(B , A) , A , C , y , t , gcdnum)) {
64
             x = t - int(B / A) * y;
65
66
             return true;
67
68
         else return false;
69
    long long Division (long long A, long long B, long long modular) {
70
         long long gcdnum, K, Y;
71
72
         euclid_extend(modular, B,A,K,Y,gcdnum);
73
        Y=_mod(Y, modular);
74
         if (Y<0) Y+=modular;
75
         return Y;
76
    bool Binary_Search(long long key, long long &position) {
77
78
         long long start, stop;
79
         start=1; stop=LimitSave;
         bool flag=true;
80
81
         while (start <= stop) {
82
             position = (start + stop)/2;
83
             if (data[position].res=key) return true;
84
             else
                  if (data[position].res<key) start=position+1;</pre>
85
86
                 else stop=position -1;
87
88
         return false;
89
90
    bool compareab (const tp &a, const tp &b) {
91
         return a.res<br/>b.res;
92
93
    long long get_log(long long root, long long A, long long modular) {
94
         long long i,j,times,XD,XT,position;
         if (modular-1<LimitSave) {</pre>
95
96
             long long now=1;
             foru(i,0,modular-1) {
97
98
                 if (now=A) {
                      return i;
99
100
                 now=_mod(now * root , modular);
101
102
             }
103
104
         data[1].expo=0; data[1].res=1;
```

```
105
         foru(i,1,LimitSave-1) {
106
              data[i+1].expo=i;
              data[i+1].res=_mod(data[i].res*root, modular);
107
108
         }
         sort (data+1,data+LimitSave+1,compareab);
109
110
         times=powers (root, LimitSave, modular);
111
         j = 0;
112
         XD=1;
         while (1) {
113
             XT=Division (A, XD, modular);
114
115
             if (Binary_Search(XT, position)) {
116
                  return j+data[position].expo;
117
118
             j=j+LimitSave;
             XD=\mod(XD*times, modular);
119
120
         }
121
    }
122
    void work_ans() {
123
         ans.clear();
124
         if (A==0) {
125
              ans.push_back(0);
126
             return;
127
128
         long long root, logs, delta, deltapower, now, gcdnum, i, x, y;
         root=get_originroot(P);
129
130
         logs=get\_log(root,A,P);
         if (euclid\_extend(K,P-1,logs,x,y,gcdnum))  {
131
132
              delta = (P-1)/gcdnum;
             x = \mod(x, delta);
133
134
              if (x<0) x+=delta;
             now=powers(root, x, P);
135
              deltapower=powers (root, delta, P);
136
137
             while (x < P-1) {
                  ans.push_back(now);
138
139
                  now=_mod(now*deltapower,P);
140
                  x=x+delta;
              }
141
142
143
         if (ans.size()>1)
             sort(ans.begin(),ans.end());
144
145
    }
146
    int main(){
         int i, j, k, test, cases=0;
147
         scanf("%d",&test);
148
149
         prepare();
         while (test) {
150
151
              test --;
             cin>>P>>K>>A;
152
153
             A=A\% P;
```

5.9. 二次剩余

```
a*x^2+b*x+c==0 \pmod{P}求
2
3
        0..P-1 的根
4
5 #include <cstdio>
6 #include <cstdlib>
7 #include <ctime>
8 #define sqr(x) ((x)*(x))
9 int pDiv2,P,a,b,c,Pb,d;
10 inline int calc(int x,int Time)
11
        if (!Time) return 1;
12
13
        int tmp=calc(x, Time/2);
        tmp=(long long)tmp*tmp%P;
14
        if (Time&1) tmp=(long long)tmp*x%P;
15
16
        return tmp;
17
   inline int rev(int x)
18
19
        if (!x) return 0;
20
21
        return calc (x,P-2);
22
23
   inline void Compute()
24
   {
25
        while (1)
26
27
            b=rand()\%(P-2)+2;
28
            if (calc(b,pDiv2)+1==P) return;
29
30
   }
31
   int main()
32
33
        srand (time (0)^312314);
34
        int T;
        for (scanf("%d",&T);T;--T)
35
36
            scanf("%d%d%d%d",&a,&b,&c,&P);
37
            if (P==2)
38
39
```

```
40
                  int cnt = 0;
41
                  for (int i=0; i<2;++i)
42
                      if ((a*i*i+b*i+c)\%P==0) ++cnt;
                  printf("%d", cnt);
43
44
                  for (int i=0; i<2;++i)
                      if ((a*i*i+b*i+c)\%P==0) printf("\d",i);
45
46
                  puts("");
47
             }else
48
                  int delta=(long long)b*rev(a)*rev(2)%P;
49
50
                 a=(long long)c*rev(a)%P-sqr((long long)delta)%P;
51
                 a\%=P; a+=P; a\%=P;
                 a=P-a; a\%=P;
52
53
                  pDiv2=P/2;
54
                  if (calc(a,pDiv2)+1==P) puts("0");
55
                  else
56
                  {
57
                      int t=0,h=pDiv2;
58
                      while (!(h\%2)) ++t, h/=2;
59
                      int root=calc(a, h/2);
                      if (t>0)
60
61
                      {
62
                           Compute();
63
                           Pb=calc(b,h);
64
65
                      for (int i=1; i <= t; ++i)
66
67
                           d = (long long) root *root *a%P;
                           for (int j=1; j <=t-i;++j)
68
69
                                d = (long long) d*d\%P;
70
                           if (d+1==P)
                                root=(long long) root*Pb%P;
71
72
                           Pb=(long long)Pb*Pb%P;
73
                      }
74
                      root=(long long)a*root%P;
75
                      int root1=P-root;
76
                      root-=delta;
77
                      root%=P;
78
                      if (root < 0) root += P;
79
                      root1-=delta;
80
                      root1%=P;
81
                      if (root1 < 0) root1 += P;
82
                      if (root>root1)
83
                      {
84
                           t=root; root=root1; root1=t;
85
                      if (root = root1) printf("1 | %d \ ", root);
86
                      else printf("2 \lfloor \%d \rfloor \%d \backslash n", root, root1);
87
88
                  }
```

```
89 }
90 }
91 return 0;
92 }
```

5.10 长方体表面两点最短距离

返回最短距离的平方

```
1 #include < cstdio >
 2 #include<iostream>
   #include<algorithm>
 5 using namespace std;
 6
7
   int r;
   void turn(int i, int j, int x, int y, int z, int x0, int y0, int L, int W, int H)
9
10
         if (z == 0) {
             int R = x * x + y * y;
11
12
             if (R < r) r = R;
13
         } else {
14
             if (i >= 0 \&\& i < 2)
                  turn(i + 1, j, x0 + L + z, y, x0 + L - x, x0 + L, y0, H, W, L);
15
16
             if (j >= 0 \&\& j < 2)
                  turn(i, j + 1, x, y0 + W + z, y0 + W - y, x0, y0 + W, L, H, W);
17
             if (i \leq 0 && i > -2)
18
                  turn(i - 1, j, x0 - z, y, x - x0, x0 - H, y0, H, W, L);
19
20
             if (j \le 0 \&\& j > -2)
21
                  turn(i, j - 1, x, y0 - z, y - y0, x0, y0 - H, L, H, W);
22
         }
23
   }
24
25
   int main()
26
    {
27
         {\bf int}\ L\,,\ H,\ W,\ x1\,,\ y1\,,\ z1\,,\ x2\,,\ y2\,,\ z2\,;
28
         cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
29
         if (z1 != 0 && z1 != H) {
30
             if (y1 == 0 | | y1 == W)
31
                  \operatorname{swap}(y1, z1), \operatorname{swap}(y2, z2), \operatorname{swap}(W, H);
32
             else
33
                  \operatorname{swap}(x1, z1), \operatorname{swap}(x2, z2), \operatorname{swap}(L, H);
34
         if (z1 = H) z1 = 0, z2 = H - z2;
35
36
         r = 0 \times 3 fffffff;
37
         turn(0, 0, x2 - x1, y2 - y1, z2, -x1, -y1, L, W, H);
38
         cout << r << endl;
39
         return 0;
40 }
```

5.11 字符串的最小表示

5.11.1 Logic_IU

```
传入字符串 \mathrm{s} , 返回 \mathrm{i} , 表示以 \mathrm{i} 开始的循环串字典序最小,但不保证 \mathrm{i} 在同样字典序最小的循环串里起始位置最小
```

```
int minCycle(char *a)
1
2
   {
3
        int n = strlen(a);
 4
         for(int i = 0; i < n; ++ i) {
5
             a[i + n] = a[i];
6
7
        a[n + n] = 0;
8
        int i = 0, j = 1, k = 0;
9
        do {
             for (k = 0; a[i + k] = a[j + k]; ++ k);
10
             if (a[i + k] > a[j + k]) i = i + k + 1;
11
12
             \mathbf{else} \ \mathbf{j} = \mathbf{j} + \mathbf{k} + 1;
13
             j += i == j;
14
             if (i > j) swap(i, j);
         \} while (j < n);
15
16
         return i;
17
   }
```

5.11.2 tEJtM

```
1
   struct cyc_string
2
3
        int n, offset;
4
        char str [max_length];
5
        char & operator [] (int x)
6
        \{return str[((offset + x) \% n)]; \}
7
        cyc\_string() \{ offset = 0; \}
8
   };
9
   void minimum_circular_representation(cyc_string & a)
10
   {
        int i = 0, j = 1, dlt = 0, n = a.n;
11
12
        while (i < n \text{ and } j < n \text{ and } dlt < n)
13
14
          if(a[i + dlt] = a[j + dlt]) dlt++;
15
16
             if(a[i + dlt] > a[j + dlt]) i += dlt + 1; else j += dlt + 1;
17
18
             dlt = 0;
19
20
        }
21
        a.offset = min(i, j);
22
23
   int main()
```

5.12. 牛顿迭代开根号

```
24 {return 0;}
```

5.12 牛顿迭代开根号

速度慢,精度有保证

```
typedef unsigned long long ull;
2
   ull sqrtll(ull n)
3
   {
4
        if (n == 0) return 0;
        ull x = 1 \text{ ull} << ((63 - \_builtin\_clzll(n)) >> 1);
5
6
        ull xx = -1;
7
        for( ; ; ) {
            ull nx = (x + n / x) >> 1;
8
9
            if (nx = xx)
10
                return min(x, nx);
11
            xx = x;
12
            x = nx;
13
        }
14
```

5.13 求某年某月某日星期几

```
int whatday(int d, int m, int y)
2
  {
3
       int ans;
        if (m = 1 | | m = 2)  {
4
5
           m += 12; y --;
6
7
        if ((y < 1752) \mid | (y = 1752 \&\& m < 9) \mid | (y = 1752 \&\& m = 9 \&\& d < 3))
           ans = (d + 2 * m + 3 * (m + 1) / 5 + y + y / 4 + 5) \% 7;
8
9
       else ans = (d + 2 * m + 3 * (m + 1) / 5 + y + y / 4 - y / 100 + y / 400) % 7;
10
       return ans;
11
```

5.14 A*

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #include <ctime>
5
6 using namespace std;
7
8 struct {
9 int pos,tot;
10 } w[2000001];
11
```

```
12
   const int inf=120234234;
   int n,m,1,len, first [5001], c [2000001], dist [5001], where [2000001], next [2000001], v [2000001],
        f [5001], lenn [5001];
   bool b[5001];
14
15
   inline void makelist(int x, int y, int z){
16
17
        where [++1]=y;
18
        v[1]=z;
19
        next[l] = first[x];
20
         first[x]=1;
21
   }
22
23
   inline void spfa(){
24
        memset(b, false, sizeof(false));
25
        memset(f, 127, sizeof(f));
26
        f[n] = 0;
27
        c[1] = n;
28
        for (int k=1, l=1; l \le k; l++)
29
30
                   int m=c[1];
31
                   b[m] = false;
                   for (int x=first[m]; x; x=next[x])
32
33
                        \mathbf{if} (f[m]+v[x]<f[where[x]])
34
                             f[where[x]] = f[m] + v[x];
35
36
                             if (!b[where[x]])
37
38
                                 b[where[x]] = true;
39
                                 c[++k] = where[x];
40
41
                        }
42
         }
   }
43
44
45
   inline void insect(int re,int uu){
        w[++len].pos=re;
46
        w[len].tot=uu;
47
48
        int now=len;
49
        while (now!=1)
50
           if (w[now]. tot+f[w[now]. pos] < w[now >> 1]. tot+f[w[now >> 1]. pos])
51
             {
52
                 int k=w[now].tot;
53
                w[now]. tot=w[now>>1]. tot;
                w[\text{now}>>1].\text{tot}=k;
54
                k=w[now].pos;
55
56
                w[now].pos=w[now>>1].pos;
57
                w[now >> 1].pos=k;
58
                now=now>>1;
59
             }
```

 $5.14. A^*$

```
60
            else break;
61
 62
    inline void delete1(){
63
         w[1].pos=w[len].pos;
64
         w[1]. tot=w[len]. tot;
65
 66
         w[len].pos=inf;
 67
         w[len].tot=inf;
 68
         len --;
 69
         int now=1;
 70
         while ((\text{now} << 1) <= \text{len})
            if ((now<<1)==len)
 71
 72
             if (w[now <<1].tot+f[w[now <<1].pos]< w[now].tot+f[w[now].pos])
 73
 74
                  int k=w[now].tot;
 75
                 w[now]. tot=w[now<<1]. tot;
                 w[now << 1].tot=k;
 76
 77
                 k=w[now].pos;
 78
                 w[now].pos=w[now<<1].pos;
 79
                 w[now <<1].pos=k;
 80
                 now=now << 1;
 81
 82
            else break;
 83
            else
            if ((w[now <<1].tot+f[w[now <<1].pos]< w[(now <<1)+1].tot+f[w[(now <<1)+1].pos]))
 84
            if (w[now <<1].tot+f[w[now <<1].pos]< w[now].tot+f[w[now].pos])
 85
 86
 87
                  int k=w[now].tot;
                 w[now]. tot=w[now<<1]. tot;
 88
                 w[now < <1]. tot=k;
 89
                 k=w[now].pos;
 90
                 w[now].pos=w[now<<1].pos;
91
92
                 w[now < <1].pos=k;
 93
                 now=now << 1;
 94
            }
 95
            else break;
 96
 97
            if (w[(now << 1) + 1]. tot + f[w[(now << 1) + 1]. pos] < w[now]. tot + f[w[now]. pos])
98
            {
99
                  int k=w[now].tot;
                 w[now]. to t=w[(now << 1) + 1]. to t;
100
101
                 w[(now << 1) + 1]. tot=k;
102
                 k=w[now].pos;
                 w[now]. pos=w[(now<<1)+1]. pos;
103
                 w[(now << 1) + 1]. pos = k;
104
105
                 now = (now << 1) + 1;
106
107
            else break;
108
```

```
109
110
     inline void spfa_ans(){
          memset(dist, 127, sizeof(dist));
111
          memset(lenn,0, sizeof(lenn));
112
          memset(w, 127, sizeof(w));
113
114
          c[1]=1;
115
          len=1;
116
          w[1].pos=1;
          w[1]. tot = 0;
117
           for (int k=1, l=1; l <= k;)
118
119
             {
                      int = w[1].pos, flow=w[1].tot;
120
                      delete1();
121
                      dist[m] = inf;
122
123
                      lenn[m]++;
                      \mathbf{if} \hspace{0.1cm} (\hspace{0.1em} \mathtt{lenn}\hspace{0.1em} [m] \hspace{-0.1em} > \hspace{-0.1em} 1000)
124
125
126
                          printf("%d\n",-1);
127
                          return;
128
                      if ((m=n)&&(lenn[m]==2))
129
130
131
                                printf("%d\n",flow);
132
                               return;
133
                      for (int x=first[m]; x; x=next[x])
134
135
                                    dist[where[x]] = flow+v[x];
136
137
                                    insect(where[x], dist[where[x]]);
138
139
             }
140
     }
141
142
     int main(){
           scanf("%d%d",&n,&m);
143
144
           1 = 0;
           for (int i = 1; i < m; i + +)
145
146
                      \mathbf{int}\ x\,,y\,,z\,;
147
148
                      scanf("%d%d%d",&x,&y,&z);
                      makelist(x,y,z);
149
                      makelist(y,x,z);
150
151
152
           spfa();
153
           spfa_ans();
154
     }
```

5.15 Dancing Links

5.15. DANCING LINKS

```
1 #include < stdio.h>
2 #include<stdlib.h>
3 #include < string.h>
4 #include<time.h>
5 #define maxn 105
   #define N maxn*maxn
   int = [maxn][maxn], [N], r[N], d[N], u[N], c[N], s[maxn], head[maxn], n, m, ans;
   inline int getid (int x, int y) {return (x-1)*n+y;}
9
   void remove(int x){
10
        1[r[x]] = 1[x]; r[1[x]] = r[x];
11
        for (int i=d[x]; i!=x; i=d[i])
12
             for (int j=r[i]; j!=i; j=r[j]) {
                  \dot{u}[d[j]] = \dot{u}[j]; d[u[j]] = d[j];
13
14
                  --s [ c [ j ] ];
15
             }
16
    }
17
    void resume(int x){
18
        for (int i=u[x]; i!=x; i=u[i])
19
             for (int j=l[i]; j!=i; j=l[j]) {
                  u[d[j]] = j; d[u[j]] = j;
20
21
                  ++s [c [j]];
22
23
        l[r[x]] = x; r[l[x]] = x;
24
25
   void dfs(int t){
26
         if (t>=ans) return;
27
         if (!r[0]) {
28
             if (t < ans) ans = t;
29
             return;
30
31
        int x=0, min=1 << 30;
32
        for (int i=r[0]; i; i=r[i])
33
             if (s[i] < min) min = s[i], x=i;
34
        remove(x);
35
        for (int i=d[x]; i!=x; i=d[i]) {
             for (int j=r[i]; j!=i; j=r[j]) remove(c[j]);
36
37
             dfs(t+1);
38
             for (int j=l[i]; j!=i; j=l[j]) resume(c[j]);
39
40
        resume(x);
41
42
   int main()
43
    {
        //freopen("1.in","r", stdin);
//freopen("1.out","w", stdout);
44
45
46
        memset(a, 0, sizeof(a));
        scanf("%d%d",&m,&n);
47
48
        for (int i=1; i \le n; ++i)
49
             int x, y; scanf("%d",&x);
```

```
50
             for (int j=1; j <=x; ++j)
51
                  scanf("%d",&y); a[i][y]=1;
52
53
        }
54
        for (int i=1; i \le m; ++i) head[i]=n*m+i; head[0]=0;
        for (int i=1; i \le m; ++i) r [head[i]] = head[i+1];
55
56
        for (int i=1; i \le m; ++i) l [head[i]] = head[i-1];
57
        r [head [0]] = head [1]; l [head [1]] = head [0];
        l [head [0]] = head [m]; r [head [m]] = head [0];
58
        for (int i=1; i<=n;++i) {
59
60
             int pre=0, first=0;
61
             for (int j=1; j<=m;++j) if (a[i][j]) {
62
                  if (pre) | [getid(i,j)] = getid(i,pre), r [getid(i,pre)] = getid(i,j);
                  pre=j; if (! first) first=j;
63
64
65
             if (first){
66
                  l [ getid (i, first )] = getid (i, pre); r [ getid (i, pre )] = getid (i, first );
67
             }
68
69
        for (int j=1; j<=m;++j){
70
             int pre=0, first=0;
71
             for (int i=1; i<=n;++i) if (a[i][j]) {
72
                  if (pre)u[getid(i,j)] = getid(pre,j), d[getid(pre,j)] = getid(i,j);
                  pre=i; if (! first) first=i;
73
74
             if (pre){
75
                 u[getid(first,j)]=head[j];d[head[j]]=getid(first,j);
76
77
                  u[head[j]] = getid(pre, j);d[getid(pre, j)] = head[j];
78
             }
79
        for (int i=1; i \le n; ++i)
80
81
             for (int j=1;j<=m;++j) if (a[i][j])c[getid(i,j)]=head[j];
82
        memset(s, 0, sizeof(s));
83
        for (int i=1; i \le n; ++i)
84
             for (int j=1;j<=m;++j)if (a[i][j])++s[j];
85
        ans=1 << 30;
        dfs(0);
86
87
        if (ans==1<<30) printf ("-1\n");
88
        else printf("%d\n", ans);
        system("pause"); for (;;);
89
90
        return 0;
91
   }
```

5.16 弦图判定

```
1 #include <cstdio>
2 #include <cstdlib>
3 #include <cstring>
4 #include <ctime>
```

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```
5 #include <cmath>
6 #include <iostream>
7 #include <algorithm>
8
9
  using namespace std;
10
11
   int n, m, first [1001], l, next [2000001], where [2000001], f[1001], a[1001], c[1001], L
       [1001], R[1001],
   v[1001], idx[1001], pos[1001];
12
   bool b[1001][1001];
14
15
   int read(){
16
        char ch;
        for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
17
18
        int cnt = 0;
        for (; ch >= '0' \&\& ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
19
20
        return(cnt);
21
   }
22
23
   inline void makelist(int x, int y){
        where [++1] = y;
24
        next[l] = first[x];
25
26
        first[x] = 1;
27
   }
28
29
   bool cmp(const int &x, const int &y){
        return(idx[x] < idx[y]);
30
31
   }
32
33
   int main(){
       //freopen("1015.in", "r", stdin);
34
35
       // freopen("1015.out", "w", stdout);
36
       for (;;)
37
        {
38
            n = read(); m = read();
            if (!n && !m) return 0;
39
            memset(first, 0, sizeof(first)); l = 0;
40
41
            memset(b, false, sizeof(b));
42
            for (int i = 1; i \le m; i++)
43
44
                int x = read(), y = read();
                if (x != y \&\& !b[x][y])
45
46
47
                   b[x][y] = true; b[y][x] = true;
48
                   makelist(x, y); makelist(y, x);
49
50
            }
            memset(f, 0, sizeof(f));
51
52
            memset(L, 0, sizeof(L));
```

```
53
            memset(R, 255, sizeof(R));
54
            L[0] = 1; R[0] = n;
55
            for (int i = 1; i \le n; i++) c[i] = i, pos[i] = i;
            memset(idx, 0, sizeof(idx));
56
            memset(v, 0, sizeof(v));
57
58
            for (int i = n; i; ---i)
59
60
                int now = c[i];
61
                R[f[now]] - -;
                if (R[f[now]] < L[f[now]]) R[f[now]] = -1;
62
63
                idx [now] = i; v[i] = now;
                for (int x = first[now]; x; x = next[x])
64
                    if (!idx [where [x]])
65
66
                        swap(c[pos[where[x]]], c[R[f[where[x]]]);
67
                        pos[c[pos[where[x]]]] = pos[where[x]];
68
69
                        pos[where[x]] = R[f[where[x]]];
70
                       L[f[where[x]] + 1] = R[f[where[x]]] - -;
71
                        if (R[f[where[x]]] < L[f[where[x]]]) R[f[where[x]]] = -1;
                        if (R[f[where[x]] + 1] = -1)
72
                            R[f[where[x]] + 1] = L[f[where[x]] + 1];
73
74
                       ++f[where[x]];
75
                    }
76
77
            bool ok = true;
78
            for (int i = 1; i \le n \&\& ok; i++)
79
80
                int cnt = 0;
                for (int x = first[v[i]]; x; x = next[x])
81
82
                     if (idx[where[x]] > i) c[++cnt] = where[x];
83
                sort(c + 1, c + cnt + 1, cmp);
84
                bool can = true;
85
                for (int j = 2; j <= cnt; j++)
86
                     if (!b[c[1]][c[j]])
87
                         ok = false;
88
89
                         break;
90
91
92
            if (ok) printf("Perfect\n");
93
            else printf("Imperfect\n");
94
            printf("\n");
95
        }
96
   }
```

5.17 弦图求团数

```
1 #include <cstdio>
2 #include <cstdlib>
```

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```
3 #include <cstring>
4 #include <ctime>
5 #include <cmath>
6 #include <iostream>
7 #include <algorithm>
9 using namespace std;
10
   int n, m, first [100001], next [2000001], where [2000001], 1, L[100001], R[100001], c
       [100001], f[100001],
   pos[100001], idx[100001], v[100001], ans;
12
13
   inline void makelist(int x, int y){
14
15
        where[++1] = y;
16
        next[l] = first[x];
17
        first[x] = 1;
18
   }
19
20
   int read(){
21
        char ch;
22
        for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
23
        int cnt = 0;
        for (; ch >= '0' && ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
24
25
        return(cnt);
26
   }
27
28
   int main(){
        freopen("1006.in", "r", stdin);
freopen("1006.out", "w", stdout);
29
30
31
        memset(first, 0, sizeof(first)); 1 = 0;
32
        n = read(); m = read();
33
        for (int i = 1; i \le m; i++)
34
35
            int x, y;
36
            x = read(); y = read();
37
            makelist(x, y); makelist(y, x);
38
39
        memset(L, 0, sizeof(L));
40
        memset(R, 255, sizeof(R));
        memset(f, 0, sizeof(f));
41
42
        memset(idx, 0, sizeof(idx));
        for (int i = 1; i \le n; i++) c[i] = i, pos[i] = i;
43
       L[0] = 1; R[0] = n; ans = 0;
44
        for (int i = n; i; ---i)
45
46
        {
47
            int now = c[i], cnt = 1;
48
            idx[now] = i; v[i] = now;
            if (--R[f[now]] < L[f[now]]) R[f[now]] = -1;
49
50
            for (int x = first [now]; x; x = next [x])
```

```
51
                if (!idx[where[x]])
52
53
                    swap(c[pos[where[x]]], c[R[f[where[x]]]);
                    pos[c[pos[where[x]]]] = pos[where[x]];
54
                    pos[where[x]] = R[f[where[x]]];
55
                    L[f[where[x]] + 1] = R[f[where[x]]] - -;
56
57
                    if (R[f[where[x]]] < L[f[where[x]]]) R[f[where[x]]] = -1;
58
                    if (R[f[where[x]] + 1] = -1) R[f[where[x]] + 1] = L[f[where[x]] +
                        1];
                    ++f[where[x]];
59
60
                }
61
                else ++cnt;
62
            ans = max(ans, cnt);
63
64
        printf("%d\n", ans);
65
   }
```

5.18 有根树的同构

```
//http://acm.sdut.edu.cn/judgeonline/showproblem?problem_id=1861
   #include <cstdio>
   #include <cstdlib>
   #include <cstring>
5
   #include <ctime>
6
7
   using namespace std;
8
   const int mm=1051697,p=4773737;
9
   int m,n, first [101], where [10001], next [10001], l, hash [10001], size [10001], pos [10001];
10
11
   long long f [10001], rt [10001];
12
   bool in [10001];
13
14
15
   inline void makelist(int x, int y){
16
        where [++1]=y;
        next[l] = first[x];
17
        first[x]=1;
18
19
   }
20
21
22
   inline void hashwork(int now){
23
        int a[1001], v[1001], tot=0;
24
        size [now] = 1;
25
        for (int x=first[now]; x; x=next[x])
26
27
            hashwork (where [x]);
28
            a[++tot] = f[where[x]];
29
            v[tot] = size[where[x]];
30
             size [now] += size [where [x]];
```

5.18. 有根树的同构 151

```
31
32
         a[++tot] = size [now];
33
         v[tot]=1;
34
         int len = 0;
         {\bf for}\ ({\bf int}\ i\!=\!1; i\!<\!\!=\!tot\ ; i\!+\!\!+\!\!)
35
36
             for (int j=i+1; j \le tot; j++)
37
                 if (a[j]<a[i])
38
39
                     int u=a[i]; a[i]=a[j]; a[j]=u;
                     u\!\!=\!\!v\,[\;i\;]\;;\,v\,[\;i\;]\!=\!v\,[\;j\;]\;;\,v\,[\;j\;]\!=\!u\;;
40
41
         f[now] = 1;
42
         for (int i=1; i <= tot; i++)
43
44
45
                     f[now] = ((f[now]*a[i])\%p*rt[len])\%p;
46
                     len+=v[i];
47
             }
48
    }
49
50
    int main(){
         //freopen("1. txt", "r", stdin);
51
         //freopen ("2. txt", "w", stdout);
52
53
         scanf("%d%d",&n,&m);
54
         rt[0] = 1;
         for (int i=1; i <=100; i++)
55
56
              rt[i] = (rt[i-1]*mm)\%p;
         for (int i=1;i<=n;i++)
57
58
59
              memset(first,0,sizeof(first));
60
              memset(in, false, sizeof(in));
61
              l=0:
62
              for (int j=1; j < m; j++)
63
64
                    int x, y;
                    scanf("%d%d",&x,&y);
65
66
                    makelist(x,y);
                    in[y] = true;
67
68
69
              int root=0;
70
              for (int j=1; j < m; j++)
71
              if (!in[j])
72
73
                    root=j;
74
                   break;
75
76
              memset(size,0,sizeof(size));
77
              memset(f, 0, sizeof(f));
              hashwork (root);
78
79
              hash[i] = f[root];
```

```
80
81
         for (int i=1; i \le n; i++) pos[i]=i;
82
         memset(in, false, sizeof(in));
         for (int i=1;i<=n;i++)
83
          if (!in[i])
84
85
86
                         printf("%d",i);
87
                        for (int j=i+1; j \le n; j++)
88
                        if (hash [j]==hash [i])
89
90
                              in [j] = true;
91
                              printf("=%d",j);
92
                         printf("\n");
93
94
          }
95
             极大团搜索算法
    5.19
    Int g[][] 为图的邻接矩阵。
    MC(V) 表示点集 V 的最大团
    令 Si=vi, vi+1, ..., vn, mc[i] 表示 MC(Si)
    倒着算 mc[i], 那么显然 MC(V)=mc[1]
    此外有 mc[i]=mc[i+1] or mc[i]=mc[i+1]+1
1
    void init(){
2
         \mathbf{int} \quad i \ , \quad j \ ;
3
         for (i=1; i<=n; ++i) for (j=1; j<=n; ++j) scanf("%d", &g[i][j]);
 4
5
    void dfs(int size){
6
         \mathbf{int} \ i \ , \ j \ , \ k \, ;
7
         if (len[size]==0) {
 8
              if (size > ans) {
9
                   ans=size; found=true;
10
11
              return;
12
          \begin{tabular}{ll} \textbf{for} & $(k=0; \ k< len [ size ] \&\& ! found; ++k) \ \end{tabular} 
13
              if (size+len[size]-k \le ans) break;
14
15
              i=list[size][k];
16
              if (size+mc[i] <= ans) break;
17
              for (j=k+1, len[size+1]=0; j<len[size]; ++j)
                    \begin{tabular}{ll} \bf if & (g[i][list[size][j]]) & list[size+1][len[size+1]++]=list[size][j]; \\ \end{tabular} 
18
19
              dfs(size+1);
         }
20
```

21 }

22

23

24

void work(){

int i, j;

mc[n]=ans=1;

5.20. 极大团的计数 153

```
25
        for (i=n-1; i; ---i) {
26
             found=false;
27
             len[1] = 0;
             for (j=i+1; j \le n; ++j) if (g[i][j]) list [1][len[1]++]=j;
28
29
             dfs(1);
30
             mc[i]=ans;
31
32
   }
33
   void print(){
34
        printf("%d\n", ans);
35
   }
```

5.20 极大团的计数

Bool g[][] 为图的邻接矩阵, 图点的标号由 1 至 n。

```
void dfs(int size){
2
        int i, j, k, t, cnt, best = 0;
3
        bool bb;
        if (ne[size] = ce[size]) {
4
5
            if (ce[size]==0) ++ans;
6
            return;
7
        for (t=0, i=1; i\le ne[size]; ++i) {
8
9
            for (cnt=0, j=ne[size]+1; j=ce[size]; ++j)
                if (!g[list[size][i]][list[size][j]]) ++cnt;
10
            if (t==0 || cnt<best) t=i, best=cnt;
11
12
13
        if (t && best \leq =0) return;
14
        for (k=ne[size]+1; k \le ce[size]; ++k) {
15
            if (t>0){
                for (i=k; i<=ce[size]; ++i) if (!g[list[size][t]][list[size][i]])
16
17
                swap(list[size][k], list[size][i]);
18
19
            i=list[size][k];
20
21
            ne[size+1]=ce[size+1]=0;
22
            for (j=1; j<k; ++j) if (g[i][list[size][j]])
23
                list [size+1][++ne[size+1]] = list [size][j];
24
            for (ce[size+1]=ne[size+1], j=k+1; j \le ce[size]; ++j)
25
                 if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
            dfs(size+1);
26
27
            ++ne[size];
28
            --best;
29
            for (j=k+1, cnt=0; j \le ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;
30
            if (t==0 || cnt<best) t=k, best=cnt;
            if (t && best <=0) break;
31
32
        }
```

```
33
   }
34
   int work(){
35
        int i;
36
        ne[0] = 0; ce[0] = 0;
37
        for (i=1; i \le n; ++i) list[0][++ce[0]]=i;
38
39
        dfs(0);
40
        return 0;
41
   }
```

5.21 多项式求根 (求导二分)

```
const double error=1e-12;
    const double infi=1e+12;
3
    double a [10], x [10];
 4
    int n;
    int sign(double x) {
6
         return (x \leftarrow error)?(-1):(x > error);
7
    double f (double a [], int n, double x) {
8
9
         double tmp=1, sum=0;
10
          \  \, \textbf{for} \  \, (\, \mathbf{int} \  \  \, i \! = \! 0; i \! < \! \! = \! \! n \, ; \, i \! + \! \! + \! ) \  \, \{ \,
11
              sum=sum+a[i]*tmp;
12
              tmp=tmp*x;
13
14
         return sum;
15
16
    double binary (double 1, double r, double a[], int n) {
17
         int sl=sign(f(a,n,1)), sr=sign(f(a,n,r));
18
         if (sl==0) return l;
         if (sr==0) return r;
19
         if (sl*sr>0) return infi;
20
21
         while (r-l>error) {
              double mid=(l+r)/2;
22
23
              int ss=sign(f(a,n,mid));
24
              if (ss==0) return mid;
25
              if (ss*sl>0) l=mid; else r=mid;
26
         }
27
         return 1;
28
    }
29
    void solve(int n,double a[],double x[],int &nx) {
30
         if (n==1) {
31
              x[1] = -a[0]/a[1];
              nx=1;
32
33
              return;
34
         double da [10], dx [10];
35
36
         int ndx;
```

```
37
        for (int i=n; i>=1;i--) da[i-1]=a[i]*i;
38
        solve (n-1, da, dx, ndx);
39
        nx=0;
40
        if (ndx==0) {
             double tmp=binary(-infi,infi,a,n);
41
42
             if (tmp < infi) x[++nx] = tmp;
43
             return;
44
        double tmp;
45
        tmp=binary(-infi, dx[1], a, n);
46
47
        if (tmp < infi) x[++nx] = tmp;
        for (int i=1; i \le ndx-1; i++) {
48
             tmp=binary(dx[i],dx[i+1],a,n);
49
             if (tmp < infi) x[++nx] = tmp;
50
51
52
        tmp=binary(dx[ndx],infi,a,n);
53
        if (tmp < infi) x[++nx] = tmp;
54
   int main() {
55
        scanf("%d",&n);
56
        for (int i=n; i>=0;i--) scanf("%lf",&a[i]);
57
58
        int nx:
59
        solve (n, a, x, nx);
        for (int i=1;i<=nx;i++) printf("%0.61f\n",x[i]);
60
        return 0;
61
62
```

5.22 有多少个点在多边形内

```
//中的标号必须逆时针给出。一开始要旋转坐标rn保证同一个,值上只有一个点。正向减点x
  //反向加点。num[i][j]=num[j][i严格在这根线下方的点。]= on[i][j]=on[j][i严格]=
  //在线段上的点包括两个端点。若有回边的话注意计算,的方法onit不要多算了线段上的点。,
  int ans = 0, z, onit = 0, lows = 0;
4
5
  rep(z,t)
      i=rn[z]; j=rn[z+1]; onit+=on[i][j]-1;
6
7
      if (a[j].x>a[i].x) {ans-=num[i][j]; lows+=on[i][j]-1;}
8
      else ans+=num[i][j];
9
  //ans-lows+1 is inside. 只会多算一次正向上的点除去最左和最右的点()。只算了除开最左边的点Lows但会
10
     多算最右边的点所以要再加上,,1.
  printf("%d\n",ans-lows+1+ onit);
```

5.23 斜线下格点统计

```
1 LL solve(LL n, LL a, LL b, LL m){
2    //计算for (int i=0;i<n;++i) s+=floor((a+b*i)/m)
3    //n,m,a,b>0
4    //printf("%lld %lld %lld %lld \n", n, a, b, m);
5    if(b == 0){
```

```
return n * (a / m);
6
7
        if(a >= m)
8
            return n * (a / m) + solve(n, a % m, b, m);
9
10
11
        if(b >= m)
            return (n - 1) * n / 2 * (b / m) + solve(n, a, b % m, m);
12
13
       LL q = (a + b * n) / m;
14
       return solve (q, (a + b * n) \% m, m, b);
15
16
   }
```

5.24 杂知识

牛顿迭代

x1=x0-func(x0)/func1(x0); 进行牛顿迭代计算 我们要求 f(x)=0 的解。func(x) 为原方程,func1 为原方程的导数方程

图同构 Hash

$$F_t(i) = (F_{t-1}(i) * A + \sum_{i \to j} (F_{t-1}(j) * B) + \sum_{j \to i} (F_{t-1}(j) * C) + D * (i == a)) \mod P$$

枚举点 a, 迭代 K 次后求得的 $F_k(a)$ 就是 a 点所对应的 hash 值。 其中 K、A、B、C、D、P 为 hash 参数, 可自选。

圆上有整点的充要条件

设正整数 n 的质因数分解为 $n=\Pi p_i^{a_i}$,则 $x^2+y^2=n$ 有整数解的充要条件是 n 中不存在形如 $p_i \mod 4=3$ 且指数 a_i 为奇数的质因数 p_i

Pick 定理

简单多边形,不自交。(严格在多边形内部的整点数 *2 + 在边上的整点数 -2)/2 =面积

图定理

定理 1: 最小覆盖数 = 最大匹配数 定理 2: 最大独立集 S 与最小覆盖集 T 互补。 算法:

- 1. 做最大匹配,没有匹配的空闲点 $\in S$
- 2. 如果 $u \in S$ 那么 u 的临点必然属于 T
- 3. 如果一对匹配的点中有一个属于 T 那么另外一个属于 S
- 4. 还不能确定的,把左子图的放入 S, 右子图放入 T 算法结束

梅森素数

p 是素数且 2^p-1 的是素数,n 不超过 258 的全部梅森素数终于确定! 是:n=2,3,5,7,13,17,19,31,61,89,107,127

上下界网络流

有上下界网络流, 求可行流部分, 增广的流量不是实际流量。若要求实际流量应该强算一遍源点出去的流量。 求最小下届网络流:

方法一: 加 t-s 的无穷大流, 求可行流, 然后把边反向后 (减去下届网络流), 在残留网络中从汇到源做最大流。

方法二: 在求可行流的时候, 不加从汇到源的无穷大边, 得到最大流 X, 加上从汇到源无穷大边后, 再求最大流得到 Y。 那么 Y 即是答案最小下界网络流。

原因: 感觉上是在第一遍已经把内部都消耗光了, 第二遍是必须的流量。

平面图定理

平面图一定存在一个度小于等于 5 的点,且可以四染色 (欧拉公式) 设 G 是连通的平面图,n,m,r 分别是其顶点数、边数和面数,n-m+r=2 极大平面图 $m \leq 3n-6$

Fibonacci 相关结论

 $\gcd(F[n],F[m])=F[\gcd(n,m)]$ Fibonacci 质数 (和前面所有的 Fibonacci 数互质), 下标为质数或 4定理: 如果 a 是 b 的倍数, 那么 F[a] 是 F[b] 的倍数。

二次剩余

```
p 为奇素数, 若 (a,p)=1, a 为 p 的二次剩余必要充分条件为 a^{(p-1)/2} \mod p = 1.(否则为 p-1) p 为奇素数, x^b=a \pmod p, a 为 p 的 b 次剩余的必要充分条件为若 a^{(p-1)/(p-1,b)} \mod p = 1.
```

5.25 Language Reference

5.25.1 C++ Tips

- 1. 开栈的命令 #pragma comment(linker, "/STACK:16777216"), 交 C++
- 2. ios::sync with stdio(false);
- 3. %o 八进制 %x 十六进制

5.25.2 Java Reference

```
1 import java.io.*;
2 import java.math.*;
3 import java.util.*;
4
5 public class Main {
6 final static int MOD = (int)1e9 + 7;
```

```
7
8
        public void run() {
9
            try {
10
                int n = reader.nextInt();
                String[] map = new String[n];
11
                for (int i = 0; i < n; ++ i) {
12
13
                    map[i] = reader.next();
14
                writer.println(10 \% MOD);
15
16
            } catch (IOException ex) {
17
18
            writer.close();
19
        }
20
21
        InputReader reader;
22
        PrintWriter writer;
23
24
        Main() {
25
            reader = new InputReader();
26
            writer = new PrintWriter(System.out);
27
28
        public static void main(String[] args) {
29
30
            new Main().run();
31
32
33
        void debug(Object...os) {
34
            System.err.println(Arrays.deepToString(os));
35
36
   }
37
   class InputReader {
38
39
        BufferedReader reader;
40
        StringTokenizer tokenizer;
41
42
        InputReader() {
            reader = new BufferedReader (new InputStreamReader (System.in));
43
44
            tokenizer = new StringTokenizer("");
45
        }
46
47
        String next() throws IOException {
            while (!tokenizer.hasMoreTokens()) {
48
49
                tokenizer = new StringTokenizer(reader.readLine());
50
51
            return tokenizer.nextToken();
52
        }
53
54
        Integer nextInt() throws IOException {
55
            return Integer.parseInt(next());
```

```
56
57
58
    import java.util.*;
59
    import java.math.*;
60
    import java.io.*;
62
63
    public class Main {
64
65
         Scanner cin;
66
67
         void solve() {
             BigInteger a, b, c;
68
69
             a = cin.nextBigInteger();
70
             b = cin.nextBigInteger();
             c = a.add(b);
71
             System.out.println(a + " \bot \bot \bot " + b + " \bot = \bot" + c);
72
73
         }
74
75
        void run() {
             cin = new Scanner(new BufferedInputStream(System.in));
76
77
             int tmp = cin.nextInt();
78
             int testcase = 0;
79
             while(cin.hasNextBigInteger()) {
                 ++ testcase;
80
81
                 if (testcase > 1)
                      System.out.println();
82
                 System.out.println("Case_" + testcase + ":");
83
84
                 solve();
85
             }
86
87
88
         public static void main(String[] args) {
89
             new Main().run();
90
91
    }
    //Arrays
92
93 int a[]=new int [10];
94 Arrays. fill(a,0);
95 Arrays.sort(a);
   //String
96
97 String s;
98 s.charAt(int i);
   s.compareTo(String b);
100 s.compareToIgnoreCase();
101 s.contains(String b);
102 s.length();
103 s.substring(int l, int len);
104 //BigInteger
```

```
105 BigInteger a;
106 a.abs();
107 a.add(b);
108 a. bitLength();
109 a.subtract(b);
110 a. divide (b);
111
    a.remainder(b);
112 a.divideAndRemainder(b);
113 a.modPow(b,c); //a^b \mod c;
114 a.pow(int);
115 a. multiply (b);
116 a.compareTo(b);
117 a.gcd(b);
118
    a.intValue();
119 a.longValue();
120 a. isProbablePrime (int certainty); //(1 - 1/2^{certainty}).
121 a.nextProbablePrime();
122 a. shiftLeft(int);
123 a. valueOf();
124
    //BigDecimal
    static int ROUND CEILING, ROUND DOWN, ROUND FLOOR,
125
                ROUND HALF DOWN, ROUND HALF EVEN, ROUND HALF UP, ROUND UP;
126
127
    a.divide(BigDecimal b, int scale, int round_mode);
128 a. double Value ();
129 a.movePointLeft(int i);
130 a.pow(int);
131 a.setScale(int scale,int round_mode);
132 a. strip Trailing Zeros ();
    //StringBuilder
133
    StringBuilder sb=new StringBuilder();
134
135 sb.append(elem);
136 out.println(sb);
137
    //StringTokenizer
    StringTokenizer st=new StringTokenizer(in.readLine());
138
    st.countTokens();
139
140 st.hasMoreTokens();
    st.nextToken();
141
142
    //Vector
143 a.add(elem);
144 a.add(index, elem);
145 a.clear();
146 a. elementAt (index);
147 a. isEmpty();
    a.remove(index);
148
149
    a. set (index, elem);
150 a. size();
151
    //Queue
152
    a.add(elem);
    a. peek (); //front
```

5.26. VIMRC 161

```
\begin{array}{ll} 154 & \text{a.poll();//pop} \\ 155 & //Integer & Double & Long \end{array}
```

5.26 vimrc

```
1 set nu ai ci si mouse=a ts=4 sts=4 sw=4
2
3 nmap <C-A> ggVG
4 vmap <C-C> "+y
5
6 nmap<F3>__: __vs__%<.in__<CR>
7 nmap<F8>__: __!./%<__%<.in__<CR>
8 nmap<F9>__: __make__%<__<CR>
9
10 nmap<F4>__: __! gedit__%_<CR>
11 nmap<F5>__: __!./%<__<CR>
12 nmap<F6>__: __! java__%<__<_%_<CR>
13 nmap<F10>__: _!! javac__%_<CR>
```