CS221 Assignment: Scheduling

Hassan Fahmy

April 2019

Problem 0

(a) If we consider a CSP with m variables and n constraints we would have variables that correspond to the light switches: $X_1, X_2, ... X_m \in \{0, 1\}$ such that $X_i = 1$ if the button i is pressed and zero if it is unpressed.

The constraints: $t_1, t_2, ... t_m$ such that $t_i = mod_2(\sum_{j=0}^n ([i \in T_j]X_j))$.

- (b) (I) There are two consistent assignments: 1,0,1 and 0,1,0.
 - (II) We get 9 calls to backtrack() The stack frame will look as follows:

```
 \begin{split} & [x=\{\}\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \\ & [x=\{X1:0\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \\ & [x=\{X1:0, \ X3:0\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\},\{0,1\}\}] \ --> \ ret \ (0,1,0) \\ & [x=\{X1:0, \ X3:1\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \\ & [x=\{X1:1\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \\ & [x=\{X1:1, \ X3:0\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \\ & [x=\{X1:1, \ X3:1\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \\ & [x=\{X1:1, \ X3:1\}, \ w=1, \ \{\{0,1\},\{0,1\},\{0,1\}\}] \ --> \ ret \ (1,0,1) \end{split}
```

(III) With AC-3 we get 7 calls to backtrack:

```
[x={}, w=1, {{0,1},{0,1},{0,1}}]
    [x={X1:0}, w=1, {{0,1},{1},{0}}]
        [x={X1:0, X3:0}, w=1, {{0,1},{1},{0}}]
        [x={X1:0, X3:0, X2:1}, w=1, {{0,1},{1},{0}}] --> ret (0,1,0)
    [x={X1:1}, w=1, {{0,1},{0},{1}}]
        [x={X1:1, X3:1}, w=1, {{0,1},{0},{1}}]
        [x={X1:1, X3:1}, w=1, {{0,1},{0},{1}}]
        [x={X1:1, X3:1}, X2:0}, w=1, {{0,1},{0},{1}}] --> ret (1,0,1)
```

Problem 2

(a) We will introduce an auxiliary variable A as a tuple with two entries. We will then enforce three binary constraints $[A[0] = X_1]$, $[A[1] = A[0] + X_2]$ and $[A[1] + X_3 \le K]$ thus we will have $A[1] = X_1 + X_2$ and we will be enforcing that $(X_1 + X_2) + X_3 \le K$

Problem 2

- (a)
- (b)
- (c) This is the content of the file I submitted as a schedule:

```
minUnits 4
maxUnits 16
register Aut2019
register Win2020
register Spr2020
taken CS107
taken CS103
taken CS109
taken CS161
taken CS221
taken CS229A
taken MATH52
taken CS106B
taken PHYSICS43
taken PHYSICS41
taken MATH51
request CS110 weight 2
request CS181 weight 2
request CS154 weight 2
request MATH104 weight 2
request ECON1 weight 1.5
request MATH53 weight 1.5
```

This is what I got as an optimal schedule

```
Quarter Units Course
Aut2019 5 MATH53
Win2020 4 CS154
Spr2020 4 CS110
Spr2020 4 CS181
Spr2020 3 MATH104
Spr2020 5 ECON1
```

Of course in real life that is not a great schedule because it does not balance the workload between the quarters but it fits everything according to the constraints.