## Tribhuvan University Institute of Science and Technology 2075



Bachelor Level / First Year/ First Semester/ Science
Computer Science and Information Technology (MTH. 112)
(Mathematics I)
(NEW COURSE)

Full Marks: 80 Pass Marks: 32

Time: 3 hours.

Candidates are required to give their answers in their own words as for as practicable. The figures in the margin indicate full marks.

## Attempt any three questions:

 $(3 \times 10 = 30)$ 

- 1. (a) A function is defined by f(x) = |x|, calculate f(-3), f(4), and sketch the graph. (5)
  - (b) Prove that the  $\lim_{x\to 2} \frac{|x-2|}{x-2}$  does not exist. (5)
- 2. (a) Find the domain and sketch the graph of the function  $f(x) = x^2 6x$ . (5)
  - (b) Estimate the area between the curve  $y = x^2$  and the lines y = 1 and y = 2. (5)
- 3. (a) Find the Maclaurin series for  $\cos x$  and prove that it represents  $\cos x$  for all x. (4)
  - (b) Define initial value problem. Solve that initial value problem of y' + 2y = 3, y(0) = 1. (4)
  - (c) Find the volume of a sphere of radius a. (2)
- 4. (a) If  $f(x, y) = \frac{y}{x'}$  does  $\lim_{(x, y) \to (0, 0)} f(x, y)$  exist? Justify. (5)
  - (b) Calculate  $\iint_R f(x, y) dA$  for  $f(x, y) = 100 6x^2y$  and  $R: 0 \le x \le 2, -1 \le y \le 1$ . (5)

## Attempt any ten questions:

 $(10 \times 5 = 50)$ 

5. If 
$$f(x) = \sqrt{2-x}$$
 and  $g(x) = \sqrt{x}$ , find fog and fof. (5)

- 6. Define continuity on an interval. Show that the function  $f(x) = 1 \sqrt{1 x^2}$  is continuous on the interval [-1, 1].
- 7. Verify Mean value theorem of  $f(x) = x^3 3x + 2$  for [-1, 2]. (5)
- 8. Starting with  $x_1 = 2$ , fine the third approximation  $x_3$  to the root of the equation  $x^3 2x 5 = 0$ . (5)
- 9. Evaluate  $\int_0^\infty x^3 \sqrt{1-x^4} dx$ . (5)
- 10. Find the volume of the resulting solid which in enclosed by the curve y = x and  $y = x^2$  is rotated about the x sxis.
- 11. Find the solution of y'' + 4y' + 4 = 0 (5)

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- 12. Determine whether the series  $\sum_{n=1}^{\infty} \frac{n^2}{5n^2 + 4}$  converges or diverges. (5)
- 13. If  $\mathbf{a} = (4, 0, 3)$  and  $\mathbf{b} = (-2, 1, 5)$  find  $|\mathbf{a}|$ , the vector  $\mathbf{a} \mathbf{b}$  and  $2\mathbf{a} + 5\mathbf{b}$ . (1+2+2)
- 14. Find  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$  if z is defined as a function of x and y by the equation  $x^3 + y^3 + z^3 + 6xyz = 1$ .
- 15. Find the extreme values of the function  $f(x, y) = x^2 + 2y^2$  on the circle  $x^2 + y^2 = 1$  (5)