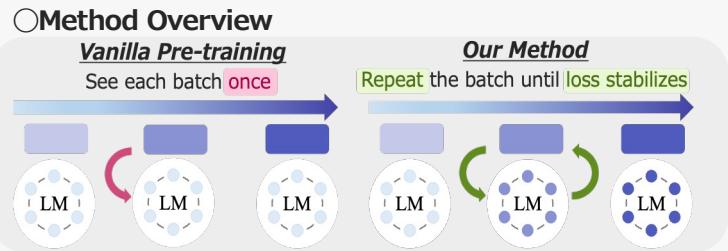


Overview

Concept: What if a LM could gradually accumulate knowledge through repetitions within limited contexts – like children?

Method :

Learn each batch repeatedly with regularization to reduce forgetting



Method: Batch-wise Convergent Pre-training

Step1 → Get \mathcal{L}_{CE} for batch x_t

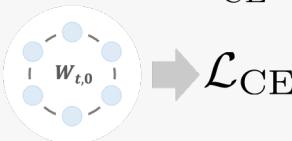
Let's Say:

x_t : Target Batch

$W_{t,0}$: Learnable Params^{*1}

α : Adaptive learning strength^{*2}

Caluculate \mathcal{L}_{CE}



*1. Start with $W_{t,0} = W_{t-1,n}$
• Update iteratively to $W_{t,k}$

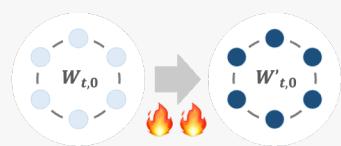
*2. Start with $\alpha = 1$
• α grows when $\mathcal{L}_{CE} > \mathcal{L}_{CE_{goal}}$

Step2 → Parameter Update with α

- ① How far from $\mathcal{L}_{CE_{goal}}$ ② Accelerate with α'^{*4}

$$\alpha' \leftarrow f(\mathcal{L}_{CE}, \alpha)^{*3}$$

Boost learning for this batch! 🔥🔥



*3. What is $f(\mathcal{L}_{CE}, \alpha)$?
 $\alpha' \leftarrow \alpha + \eta(\mathcal{L}_{CE} - \mathcal{L}_{CE_{goal}})$
• η is learning rate for α update

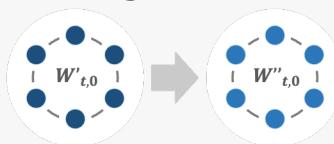
*4. Use AdamW
 $W' \leftarrow \text{AdamW}(\alpha' \mathcal{L}_{CE})$

Step3 → Pull back W' toward $W_{t,0}$

① Regularization term

② Regularize W'^{*6}

$$\nabla R = \frac{C}{p} \|W' - W_{t,0}\|_p^p$$



*5. C controls the regularization strength
• L_1 when $p = 1$, L_2 when $p = 2$

*6. Regularization
 $W'' = W' - \nabla R$

Step4 → Convergence Check

Has the model learned x_t sufficiently?

→ Check α' , Not \mathcal{L}_{CE}

Check List

- Is α decreasing continuously?
- $\alpha < \text{threshold}$?

✓ Next Batch x_{t+1}

$$W_{t+1,0} \leftarrow W_{t,0}$$

✗ Repeat Batch x_t

$$W_{t,1} \leftarrow W_{t,0}$$

Experiments / Analysis

Comparison with Official Baselines

Setup:

- We compare our model with **GPT-2**, **GPT-BERT**
- Model size is 117M, Qwen2.5 architecture
- A curriculum based on our original difficulty score

Result: No significant improvement

Model	BLiMP↑	BLiMP-S↑	WUG-ADJ↑	Text-Avg.↑
GPT-BERT	80.5	73.0	41.2	70.9
GPT-2	74.9	63.3	50.2	54.7
Ours($p=1$)	49.2	50.4	57.5	32.8
Ours($p=2$)	52.2	50.2	57.1	32.5

Next TODO : Isolated batch learning breaks the distributional assumption
→ Batch Design? or Architecture Design?

Training Orders & Repetition Strategies

Setup:

- Random**: 10 epochs with the random data
- Curriculum**: 10 epochs with the curriculum data
- Curriculum-Repeat**: the curriculum data + repeat each batch 10 times in a row
- Our Proposed Method**

Result: Comparable but not better

Analysis:

Our Proposed Method performs slightly better in Text-Avg, by only 2 points

Random performed best on BLiMP

Curriculum performed best on WUG-ADJ

Curriculum-Repeat performed best on Entity