

FORM ONE MATHEMATICS UPDATED TUTORIAL



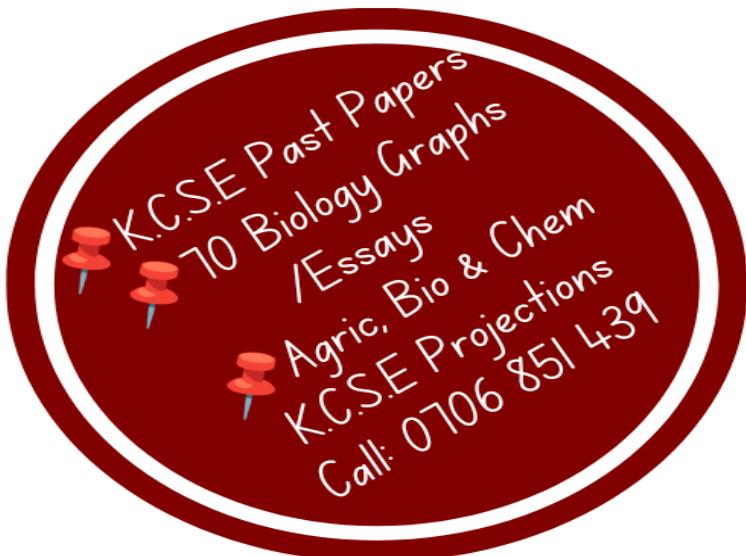
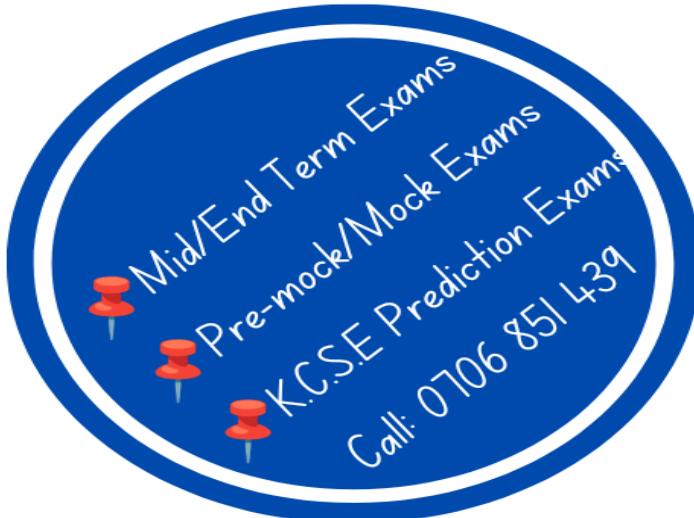
FORM ONE MATHEMATICS UPDATED NOTES

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MATHEMATICS FORM 1 TUTORIAL

CHAPTER ONE

NATURAL NUMBERS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Identify, read and write natural numbers in symbols and words;
- b.) Round off numbers to the nearest tens, hundreds, thousands, millions and billions;
- c.) Classify natural numbers as even, odd or prime;
- d.) Solve word problems involving natural numbers.

Content

- a.) Place values of numbers
- b.) Rounding off numbers to the nearest tens, hundreds, thousands, millions and billions
- c.) Odd numbers
- d.) Even numbers
- e.) Prime numbers
- f.) Word problems involving natural numbers

Introduction

Place value

A digit have a different value in a number because of its position in a number. The position of a digit in a number is called its **place value**.

Total value

This is the product of the digit and its place value.

Example

Number	Hundred Millions	Ten Millions	Millions	Hundred Thousands	Ten Thousands	Thousands	Hundred	Tens	ones
345,678,901	3	4	5	6	7	8	9	0	1
769,301,854	7	6	9	3	0	1	8	5	4
902,350,409	9	0	2	3	5	0	4	0	9

A place value chart can be used to identify both place value and total value of a digit in a number. The place value chart is also used in writing numbers in words.

Example

- ✓ Three hundred and forty five million, six hundred and seventy eight thousand, nine hundred and one.
- ✓ Seven hundred and sixty nine million, Three hundred and one thousand, eight hundred and fifty four.

Billions

A billion is one thousands million, written as 1, 000, 000,000. There are ten places in a billion.

Example

What is the place value and total value of the digits below?

- a.) 47,397,263,402 (place value 7 and 8).
- b.) 389,410 ,000,245 (place 3 and 9)

Solution

- a.) The place value for 6 is ten thousands. Its total value is 60,000.
- b.) The place value of 3 is hundred billions. Its total value is 300,000,000,000.

Rounding off

When rounding off to the nearest ten, the ones digit determines the ten i.e. if the ones digit is 1, 2, 3, or 4 the nearest ten is the ten number being considered. If the ones digit is 5 or more the nearest ten is the next ten or rounded up.

Thus 641 to the nearest ten is 640, 3189 to the nearest is 3190.

When rounding off to the nearest 100, then the last two digits or numbers end with 1 to 49 round off downwards. Number ending with 50 to 99 are rounded up.

Thus 641 to the nearest hundred is 600, 3189 is 3200.

Example

Rounding off each of the following numbers to the nearest number indicated in the bracket:

- a.) 473,678 (100)
- b.) 524,239 (1000)
- c.) 2,499 (10)

Solution

- a.) 473,678 is 473,700 to the nearest 100.
- b.) 524,239 is 524,000 to the nearest 1000
- c.) 2,499 is 2500 to the nearest 10.

Operations on whole Numbers

Addition

Example

Find out:

- a.) $98 + 6734 + 348$
- b.) $6349 + 259 + 7954$

Solution

Arrange the numbers in vertical forms

$$\begin{array}{r} 98 \\ 6734 \\ + \underline{348} \\ \hline 7180 \end{array}$$

$$\begin{array}{r} 6349 \\ 259 \\ + \underline{79542} \\ \hline \end{array}$$

$$\underline{86150}$$

Subtracting

Example

Find: $73469 - 8971$

Solution

$$\begin{array}{r} 73469 \\ - \underline{8971} \\ \hline 64498 \end{array}$$

Multiplication

The product is the result of two or more numbers.

Example

Work out: 469×63

Solution

$$\begin{array}{r} 469 \\ \times 63 \\ \hline 1407 \rightarrow 469 \times 3 = 1407 \\ + \underline{28140} \rightarrow 469 \times 60 = 28140 \\ \hline \underline{29547} \end{array}$$

Division

When a number is divided by the result is called the quotient. The number being divided is the dividend and the number dividing is the divisor.

Example

Find: $6493 \div 14$

Solution

We get 463 and 11 is the remainder

Note:

$$6493 = (463 \times 14) + 11$$

In general, dividend = quotient \times division + remainder.

Operation	Words
Addition	sum plus added more than increased by
Subtraction	difference minus subtracted from less than decreased by reduced by deducted from
Multiplication	product of multiply times twice thrice
Division	quotient of divided by
Equal	equal to result is is

Word problem

In working the word problems, the information given must be read and understood well before attempting the question.

The problem should be broken down into steps and identify each other operations required.

Example

Otego had 3469 bags of maize, each weighing 90 kg. He sold 2654 of them.

- How many kilogram of maize was he left with?
- If he added 468 more bags of maize, how many bags did he end up with?

Solution

- One bag weighs 90 kg.

3469 bags weigh $3469 \times 90 = 312,210$ kg

2654 bags weigh $2654 \times 90 = 238,860$ kg

Amount of maize left = $312,210 - 238,860 = 73,350$ kg.

- Number of bags = $815 + 468 = 1283$

Even Number

A number which can be divided by 2 without a remainder E.g. 0,2,4,6 0 or 8

3600, 7800, 806, 78346

Odd Number

Any number that when divided by 2 gives a remainder. E.g. 471,123, 1197,7129. The numbers ends with the following digits 1, 3, 5,7 or 9.

Prime Number

A prime number is a number that has only two factors one and the number itself.

For example, 2, 3, 5, 7, 11, 13, 17 and 19.

Note:

- 1 is not a prime number.
- 2 is the only even number which is a prime number.

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- Write 27707807 in words
- All prime numbers less than ten are arranged in descending order to form a number
 - Write down the number formed
 - What is the total value of the second digit?
 - Write the number formed in words.

CHAPTER TWO

FACTORS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Express composite numbers in factor form;
- b.) Express composite numbers as product of prime factors;
- c.) Express factors in power form.

Content

- a.) Factors of composite numbers.
- b.) Prime factors.
- c.) Factors in power form
- d.)

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CHAPTER THREE

DIVISIBILITY

Specific Objectives

By the end of the topic the learner should be able to:

The learner should be able to test the divisibility of numbers by 2, 3, 4, 5, 6, 8, 9, 10 and 11.

Content

Divisibility test of numbers by 2, 3, 4, 5, 6, 8, 9, 10 and 11

Introduction

Divisibility test makes computation on numbers easier. The following is a table for divisibility test.

Divisibility Tests	Example
A number is divisible by 2 if the last digit is 0, 2, 4, 6 or 8.	168 is divisible by 2 since the last digit is 8.
A number is divisible by 3 if the sum of the digits is divisible by 3.	168 is divisible by 3 since the sum of the digits is 15 ($1+6+8=15$), and 15 is divisible by 3.
A number is divisible by 4 if the number formed by the last two digits is divisible by 4.	316 is divisible by 4 since 16 is divisible by 4.
A number is divisible by 5 if the last digit is either 0 or 5.	195 is divisible by 5 since the last digit is 5.
A number is divisible by 6 if it is divisible by 2 AND it is divisible by 3.	168 is divisible by 6 since it is divisible by 2 AND it is divisible by 3.
A number is divisible by 8 if the number formed by the last three digits is divisible by 8.	7,120 is divisible by 8 since 120 is divisible by 8.
A number is divisible by 9 if the sum of the digits is divisible by 9.	549 is divisible by 9 since the sum of the digits is 18 ($5+4+9=18$), and 18 is divisible by 9.
A number is divisible by 10 if the last digit is 0.	1,470 is divisible by 10 since the last digit is 0.
A number is divisible by 11 if the sum of its digits in the odd positions like 1 st , 3 rd , 5 th , 7 th Positions, and the sum of its digits in the even position like 2 nd , 4 th , 6 th , 8 th positions are equal or differ by 11, or by a multiple of 11	8,260,439 sum of 8 + 6 + 4 + 9 = 27: $2 + 0 + 3 = 5$; $27 - 5 = 22$ which is a multiple of 11

End of topic

Did you understand everything?

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Past KCSE Questions on the topic

CHAPTER FOUR

GREATEST COMMON DIVISOR

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Find the GCD/HCF of a set of numbers.
- b.) Apply GCD to real life situations.

Content

- a.) GCD of a set of numbers
- b.) Application of GCD/HCF to real life situations

Introduction

A Greatest Common Divisor is the largest number that is a factor of two or more numbers.

When looking for the Greatest Common Factor, you are only looking for the COMMON factors contained in both numbers. To find the G.C.D of two or more numbers, you first list the factors of the given numbers, identify common factors and state the greatest among them.

The G.C.D can also be obtained by first expressing each number as a product of its prime factors. The factors which are common are determined and their product obtained.

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CHAPTER FIVE

LEAST COMMON MULTIPLE

Specific Objectives

By the end of the topic the learner should be able to:

- a.) List multiples of numbers.
- b.) Find the L CM of a set of numbers.
- c.) Apply knowledge of L CM in real life situations.

Content

- a.) Multiples of a number
- b.) L CM of a set of numbers
- c.) Application of L CM in real life situations.

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CHAPTER SIX

INTGERS

Specific Objectives

By the end of the topic the learner should be able to:

- Define integers
- Identify integers on a number line
- Perform the four basic operations on integers using the number line.
- Work out combined operations on integers in the correct order
- Apply knowledge of integers to real life situations.

Content

- Integers
- The number line
- Operation on integers
- Order of operations
- Application to real life situations

Introduction

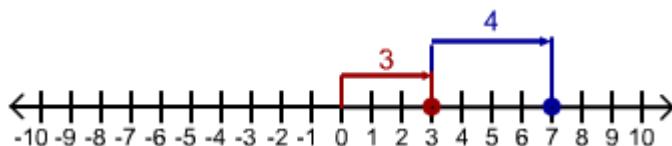
The Number Line

Integers are whole numbers, negative whole numbers and zero. Integers are always represented on the number line at equal intervals which are equal to one unit.

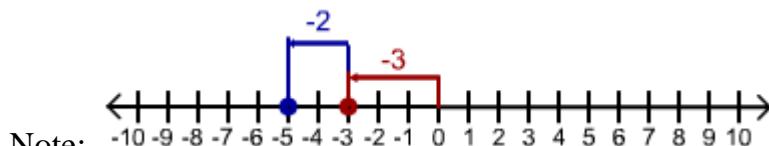
Operations on Integers

Addition of Integers

Addition of integers can be represented on a number line .For example, to add +3 to 0 , we begin at 0 and move 3 units to the right as shown below in red to get +3, Also to add + 4 to +3 we move 4 units to the right as shown in blue to get +7.



To add -3 to zero we move 3 units to the left as shown in red below to get -3 while to add -2 to -3 we move 2 steps to the left as shown in blue to get -5.

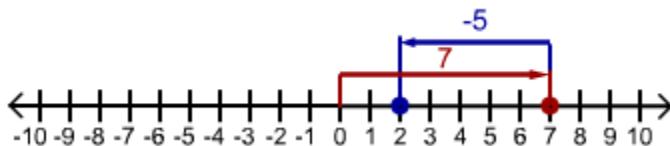


Note;

When adding positive numbers we move to the right.

When dealing with negative we move to the left.

Subtraction of integers.



Example

$$(+7) - (0) = (+7)$$

To subtract +7 from 0 ,we find a number n which when added to get 0 we get +7 and in this case n = +7 as shown above in red.

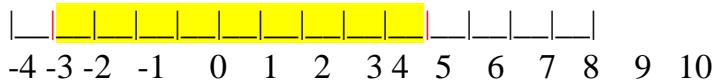
Example

$$(+2) - (+7) = (-5)$$

Start at +7 and move to +2. 5 steps will be made towards the left. The answer is therefore -5.

Example

$$-3 - (+6) = -9$$



We start at +6 and moves to -3. 9 steps to the left, the answer is -9.

Note:

- ✓ In general positives signs can be ignored when writing positive numbers i.e. +2 can be written as 2 but negative signs cannot be ignored when writing negative numbers -4 can only be written as -4.

$$4 - (+3) = 4 - 3$$

$$= 1$$

$$-3 - (+6) = 3 - 6$$

$$= -3$$

- ✓ Positive integers are also referred to as natural numbers. The result of subtracting the negative of a number is the same as adding that number.

$$2 - (-4) = 2 + 4$$

$$= 6$$

$$(-5) - (-1) = -5 + 2$$

$$= -3$$

- ✓ In mathematics it is assumed that that the number with no sign before it has appositive sign.

Multiplication

In general

- (a negative number) x (appositive number) = (a negative number)
- (a positive number) x (a negative number) = (a negative number)
- (a negative number) x (a negative number) = (a positive number)

Examples

$$-6 \times 5 = -30$$

$$7 \times -4 = -28$$

$$-3 \times -3 = 9$$

$$-2 \times -9 = 18$$

Division

Division is the inverse of multiplication. In general

- i.) (a positive number) \div (a positive number) = (a positive number)
- ii.) (a positive number) \div (a negative number) = (a negative number)
- iii.) (a negative number) \div (a negative number) = (a positive number)
- iv.) (a negative number) \div (a positive number) = (a negative number)

Note;

For multiplication and division of integer:

- ✓ Two like signs gives positive sign.
- ✓ Two unlike signs gives negative sign
- ✓ Multiplication by zero is always zero and division by zero is always zero.

Order of operations

BODMAS is always used to show as the order of operations.

B – Bracket first.

O – Of is second.

D – Division is third.

M – Multiplication is fourth.

A – Addition is fifth.

S – Subtraction is considered last.

Example

$$6 \times 3 - 4 \div 2 + 5 + (2 - 1) =$$

Solution

Use **BODMAS**

$(2 - 1) = 1$ we solve brackets first

$(4 \div 2) = 2$ we then solve division

$(6 \times 3) = 18$ next is multiplication

Bring them together

$18 - 2 + 5 + 1 = 22$ we solve addition first and lastly subtraction

$18 + 6 - 2 = 22$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) The sum of two numbers exceeds their product by one. Their difference is equal to their product less five. Find the two numbers. (3mks)

2.) $3x - 1 > -4$

$2x + 1 \leq 7$

3.) Evaluate $\frac{-12 \div (-3) \times 4 - (-15)}{-5 \times 6 \div 2 + (-5)}$

4.) Without using a calculator/mathematical tables, evaluate leaving your answer as a simple fraction

$\frac{(-4)(-2) + (-12) \div (+3)}{-9 - (15)}$ + $\frac{-20 + (+4) + -6}{46 - (8+2)-3}$

5.) Evaluate $\frac{-8 \div 2 + 12 \times 9 - 4 \times 6}{56 \div 7 \times 2}$

6.) Evaluate without using mathematical tables or the calculator

$\frac{1.9 \times 0.032}{20 \times 0.0038}$

CHAPTER SEVEN

FRACTIONS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Identify proper and improper fractions and mixed number.
- b.) Convert mixed numbers to improper fractions and vice versa.
- c.) Compare fractions;
- d.) Perform the four basic operations on fractions.
- e.) Carry out combined operations on fractions in the correct order.
- f.) Apply the knowledge of fractions to real life situations.

Content

- a.) Fractions
- b.) Proper, improper fractions and mixed numbers.
- c.) Conversion of improper fractions to mixed numbers and vice versa.
- d.) Comparing fractions.
- e.) Operations on fractions.
- f.) Order of operations on fractions
- g.) Word problems involving fractions in real life situations.

Introduction

A fraction is written in the form $\frac{a}{b}$ where a and b are numbers and b is not equal to 0. The upper number is called the numerator and the lower number is the denominator.

$$\begin{array}{c} a \rightarrow \text{numerator} \\ \hline b \rightarrow \text{denominator} \end{array}$$

Proper fraction

In proper fraction the numerator is smaller than the denominator. E.g.

$$\frac{2}{3}, \frac{1}{4}$$

Improper fraction

The numerator is bigger than or equal to denominator. E.g.

$$\frac{7}{3}, \frac{15}{6}, \frac{9}{2}$$

Mixed fraction

An improper fraction written as the sum of an integer and a proper fraction. For example

$$\begin{aligned} \frac{7}{3} &= 2 + \frac{1}{3} \\ &= 2\frac{1}{3} \end{aligned}$$

Changing a Mixed Number to an Improper Fraction

Mixed number - $4 \frac{2}{3}$ (contains a whole number and a fraction)

Improper fraction - $\frac{14}{3}$ (numerator is larger than denominator)

Step 1 – Multiply the denominator and the whole number

Step 2 – Add this answer to the numerator; this becomes the new numerator

Step 3 – Carry the original denominator over

Example

$$3 \frac{1}{8} = 3 \times 8 + 1 = 25$$

$$= \frac{25}{8}$$

Example

$$4 \frac{4}{9} = 4 \times 9 + 4 = 40$$

$$= \frac{40}{9}$$

Changing an Improper Fraction to a Mixed Number

Step 1 – Divide the numerator by the denominator

Step 2 – The answer from step 1 becomes the whole number

Step 3 – The remainder becomes the new numerator

Step 4 – The original denominator carries over

Example

$$\frac{47}{5} = \overline{47 \div 5} \quad \text{or}$$

$$\begin{array}{r} 5 \overline{)47} \\ 45 \\ \hline 2 \end{array}$$

Example

$$\frac{9}{2} = 2 \overline{)9} = 2 \overline{)9}^{\frac{4}{9}} = 4 \frac{1}{2}$$
$$\begin{array}{r} 8 \\ \hline 1 \end{array}$$

Comparing Fractions

When comparing fractions, they are first converted into their equivalent forms using the same denominator.

Equivalent Fractions

To get the equivalent fractions, we multiply or divide the numerator and denominator of a given fraction by the same number. When the fraction has no factor in common other than 1, the fraction is said to be in its simplest form.

Example

Arrange the following fractions in ascending order (from the smallest to the biggest):

1/2 1/4 5/6 2/3

Step 1: Change all the fractions to the same denominator.

Step 2: In this case we will use 12 because 2, 4, 6, and 3 all go into i.e. We get 12 by finding the L.C.M of the denominators. To get the equivalent fractions divide the denominator by the L.C.M and then multiply both the numerator and denominator by the answer,

For 1/2 we divide 12 ÷ 2 = 6, then multiply both the numerator and denominator by 6 as shown below.

$$\begin{array}{cccc} \underline{1} & \underline{1} & \underline{5} & \underline{2} \\ \times 6 & \times 3 & \times 2 & \times 4 \\ \underline{2} & \underline{4} & \underline{6} & \underline{3} \\ \times 6 & \times 3 & \times 2 & \times 4 \end{array}$$

Step 3: The fractions will now be:

6/12 3/12 10/12 8/12

Step 4: Now put your fractions in order (smallest to biggest.)

3/12 6/12 8/12 10/12

Step 5: Change back, keeping them in order.

1/4 1/2 2/3 5/6

You can also use percentages to compare fractions as shown below.

INCOMPLETE NOTES

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Example

Arrange the following in descending order (from the biggest)

5/12 7/3 11/5 9/4

Solution

$$\frac{5}{12} \times 100 = 41.67\%$$

$$\frac{7}{3} \times 100 = 233.3\%$$

$$\frac{11}{5} \times 100 = 220\%$$

$$\frac{9}{4} \times 100 = 225\%$$

7/3, 9/4, 11/5, 5/12

Operation on Fractions

Addition and Subtraction

The numerators of fractions whose denominators are equal can be added or subtracted directly.

Example

$$2/7 + 3/7 = 5/7$$

$$6/8 - 5/8 = 1/8$$

When adding or subtracting numbers with different denominators like:

$$5/4 + 3/6 = ?$$

$$2/5 - 2/7 = ?$$

Step 1– Find a common denominator (a number that both denominators will go into or L.C.M)

Step 2– Divide the denominator of each fraction by the common denominator or L.C.M and then multiply the answers by the numerator of each fraction

Step 3– Add or subtract the numerators as indicated by the operation sign

Step 4 – Change the answer to lowest terms

Example

$$\frac{1}{2} + \frac{7}{8} = \text{Common denominator is 8 because both 2 and 8 will go into 8}$$

$$\frac{1}{2} + \frac{7}{8} = \frac{4+7}{8}$$

$$\frac{11}{8} \text{ Which simplifies to } 1\frac{3}{8}$$

Example

$$4\frac{3}{5} - \frac{1}{4} = \text{Common denominator is 20 because both 4 and 5 will go into 20}$$

$$\begin{array}{rcl} 4\frac{3}{5} & = & 4\frac{12}{20} \\ - \frac{1}{4} & = & \frac{5}{20} \\ \hline \end{array}$$

$$4\frac{7}{20}$$

Or

$$4\frac{3}{5} - \frac{1}{4} = 4\frac{\frac{12-5}{20}}{20} = 4\frac{7}{20}$$

Mixed numbers can be added or subtracted easily by first expressing them as improper fractions.

Examples

$$5\frac{2}{3} + 1\frac{4}{5}$$

Solution

$$5\frac{2}{3} + 1\frac{4}{5} = 5 + \frac{2}{3} + 1 + \frac{4}{5}$$

$$= (5 + 1) + \frac{2}{3} + \frac{4}{5}$$

$$= 6 + \frac{10 + 12}{15}$$

CHAPTER EIGHT

DECIMALS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Convert fractions into decimals and vice versa
- b.) Identify recurring decimals
- c.) Convert recurring decimals into fractions
- d.) Round off a decimal number to the required number of decimal places
- e.) Write numbers in standard form
- f.) Perform the four basic operations on decimals
- g.) Carry our operations in the correct order
- h.) Apply the knowledge of decimals to real life situations.

Content

- a.) Fractions and decimals
- b.) Recurring decimals
- c.) Recurring decimals and fractions
- d.) Decimal places
- e.) Standard form
- f.) Operations on decimals
- g.) Order of operations
- h.) Real life problems involving decimals.

Introduction

A fraction whose denominator can be written as the power of 10 is called a decimal fraction or a decimal.
E.g. $\frac{1}{10}$, $\frac{1}{100}$, $\frac{50}{1000}$.

A decimal is always written as follows $\frac{1}{10}$ is written as 0.1 while $\frac{5}{100}$ is written as 0.05. The dot is called the decimal point.

Numbers after the decimal points are read as single digits e.g. 5.875 is read as five point eight seven five.
A decimal fraction such 8.3 means $8 + \frac{3}{10}$. A decimal fraction which represents the sum of a whole number and a proper fraction is called a mixed fraction.

Place value chart

	Hundred Thousands	Ten Thousands	Thousands	Hundreds	Tens	Ones	Decimal Point	Tenths	Hundredths	Thousands Tenths	Ten Thousands Tenths
10,000	1,000	100	10	101	.001	.0001	.00001

Decimal to Fractions

To convert a number from fraction form to decimal form, simply divide the numerator (the top number) by the denominator (the bottom number) of the fraction.

Example:

5/8

$$\begin{array}{r} .625 \\ 8 \overline{) 5.000} \\ \leftarrow \text{Add as many zeros as needed.} \end{array}$$

$$\begin{array}{r} 48 \\ 20 \\ 16 \\ 40 \\ 40 \\ 0 \end{array}$$

Converting a decimal to a fraction

To change a decimal to a fraction, determine the place value of the last number in the decimal. This becomes the denominator. The decimal number becomes the numerator. Then reduce your answer.

Example:

.625 - the 5 is in the thousandths column, therefore,

$$.625 = \frac{625}{1000} = \text{reduces to } \frac{5}{8}$$

Note:

Your denominator will have the same number of zeros as there are decimal digits in the decimal number you started with - .625 has three decimal digits so the denominator will have three zero.

Recurring Decimals

These are decimal fractions in which a digit or a group of digits repeat continuously without ending.

$$\begin{aligned} \frac{1}{3} &= 0.333333 \\ \frac{5}{11} &= 0.4545454545 \end{aligned}$$

We cannot write all the numbers, we therefore place a dot above a digit that is recurring. If more than one digit recurs in a pattern, we place a dot above the first and the last digit in the pattern.

E.g.

0.3333.....is written as $0.\dot{3}$

0.4545.....is written as $0.4\dot{5}$

0.324324.....is written as $0.\dot{3}2\dot{4}$

Any division whose divisor has prime factors other than 2 or 5 forms a recurring decimal or non-terminating decimal.

Example

Express each as a fraction

- a.) $0.\dot{6}$
- b.) $0.7\dot{3}$
- c.) $0.1\dot{5}$

Solution

a.) Let $r = 0.66666 \text{ ----- (I)}$

$$10r = 6.6666 \text{ ----- (II)}$$

Subtracting I from II

$$9r = 6$$

$$\begin{aligned} r &= \frac{6}{9} \\ &= \frac{2}{3} \end{aligned}$$

b.) Let $r = 0.73333 \text{ ----- (I)}$

$$10r = 7.33333 \text{ ----- (II)}$$

$$100r = 73.33333 \text{ ----- (III)}$$

Subtracting (II) from (III)

$$90r = 66$$

$$\begin{aligned} r &= \frac{66}{90} \\ &= \frac{11}{15} \end{aligned}$$

c.) Let $r = 0.151515 \text{ ----- (I)}$

$$100r = 15.1515 \text{ ----- (II)}$$

$$99r = 15$$

$$\begin{aligned} r &= \frac{15}{99} \\ &= \frac{5}{33} \end{aligned}$$

Decimal places

When the process of carrying out division goes over and over again without ending we may round off the digits to any number of required digits to the right of decimal points which are called decimal places.

Example

Round 2.832 to the nearest hundredth.

Solution

Step 1 – Determine the place to which the number is to be rounded is.

2.832

Step 2 – If the digit to the right of the number to be rounded is less than 5, replace it and all the digits to the right of it by zeros. If the digit to the right of the underlined number is 5 or higher, increase the underlined number by 1 and replace all numbers to the right by zeros. If the zeros are decimal digits, you may eliminate them.

2.832 = 2.830 = 2.83

Example

Round 43.5648 to the nearest thousandth.

Solution

43.5648 = 43.5650 = 43.565

Example

Round 5,897,000 to the nearest hundred thousand.

Solution

5,897,000 = 5,900,000

Standard Form

A number is said to be in standard form if it is expressed in form $A \times 10^n$, Where $1 < A < 10$ and n is an integer.

Example

Write the following numbers in standard form.

- a.) 36 b.) 576 c.) 0.052

Solution

- a.) $36/10 \times 10 = 3.6 \times 10^1$
b.) $576/100 \times 100 = 5.76 \times 10^2$
c.) $0.052 = 0.052 \times 100/100$

$$5.2 \times \frac{1}{100}$$

$$5.2 \times \left(\frac{1}{100}\right)^2$$

$$5.2 \times 10^{-2}$$

Operation on Decimals

Addition and Subtraction

The key point with addition and subtraction is to line up the decimal points!

Example

$$\begin{array}{r} 2.64 + 11.2 = 2.64 \\ + \underline{11.20} \rightarrow \text{in this case, it helps to write 11.2 as 11.20} \\ \hline 13.84 \end{array}$$

Example

$$\begin{array}{r} 14.73 - 12.155 = 14.730 \rightarrow \text{again adding this 0 helps} \\ - \underline{\quad\quad\quad 12.155} \\ \hline 2.575 \end{array}$$

Example

$$\begin{array}{r} 127.5 + 0.127 = 327.500 \\ + \underline{0.127} \\ \hline 327.627 \end{array}$$

Multiplication

When multiplying decimals, do the sum as if the decimal points were not there, and then calculate how many numbers were to the right of the decimal point in both the original numbers - next, place the decimal point in your answer so that there are this number of digits to the right of your decimal point?

Example

$$2.1 \times 1.2.$$

Calculate $21 \times 12 = 252$. There is one number to the right of the decimal in each of the original numbers, making a total of two. We therefore place our decimal so that there are two digits to the right of the decimal point in our answer.

Hence $2.1 \times 1.2 = 2.52$.

Always look at your answer to see if it is sensible. $2 \times 1 = 2$, so our answer should be close to 2 rather than 20 or 0.2 which could be the answers obtained by putting the decimal in the wrong place.

Example

$$1.4 \times 6$$

Calculate $14 \times 6 = 84$. There is one digit to the right of the decimal in our original numbers so our answer is 8.4

Check $1 \times 6 = 6$ so our answer should be closer to 6 than 60 or 0.6

Division

When dividing decimals, the first step is to write your numbers as a fraction. Note that the symbol / is used to denote division in these notes.

$$\text{Hence } 2.14 / 1.2 = \underline{2.14}$$

$$1.2$$

Next, move the decimal point to the right until both numbers are no longer decimals. Do this the same number of places on the top and bottom, putting in zeros as required.

$$\text{Hence } \frac{2.14}{1.2} \text{ becomes } \frac{214}{120}$$

This can then be calculated as a normal division.

Always check your answer from the original to make sure that things haven't gone wrong along the way. You would expect $2.14/1.2$ to be somewhere between 1 and 2. In fact, the answer is 1.78.

If this method seems strange, try using a calculator to calculate $2.14/1.2$, $21.4/12$, $214/120$ and $2140/1200$. The answer should always be the same.

Example

$$4.36 / 0.14 = \underline{4.36} = \underline{436} = 31.14$$

$$1.14 \qquad \qquad \qquad 14$$

Example

$$27.93 / 1.2 = \underline{27.93} = \underline{2793} = 23.28$$

$$1.2 \qquad \qquad \qquad 120$$

Rounding Up

Some decimal numbers go on forever! To simplify their use, we decide on a cutoff point and “round” them up or down.

If we want to round 2.734216 to two decimal places, we look at the number in the third place after the decimal, in this case, 4. If the number is 0, 1, 2, 3 or 4, we leave the last figure before the cut off as it is. If the number is 5, 6, 7, 8 or 9 we “round up” the last figure before the cut off by one. 2.734216 therefore becomes 2.73 when rounded to 2 decimal places.

If we are rounding to 2 decimal places, we leave 2 numbers to the right of the decimal.
If we are rounding to 2 significant figures, we leave two numbers, whether they are decimals or not.

Example

$$243.7684 = 243.77 \text{ (2 decimal places)} \\ = 240 \text{ (2 significant figures)}$$

$$1973.285 = 1973.29 \text{ (2 decimal places)}$$

$$= 2000 \text{ (2 significant figures)}$$

$$2.4689 = 2.47 \text{ (2 decimal places)}$$

$$= 2.5 \text{ (2 significant figures)}$$

$$0.99879 = 1.00 \text{ (2 decimal places)}$$

$$= 1.0 \text{ (2 significant figures)}$$

Order of operation

The same rules on operations is always the same even for decimals.

Examples

Evaluate

$$0.02 + 3.5 \times 2.6 - 0.1 (6.2 - 3.4)$$

Solution

$$0.02 + 3.5 \times 2.6 - 0.1 \times 2.8 = 0.02 + 0.91 - 0.28$$

$$= 8.84$$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- Without using logarithm tables or a calculator evaluate.

$$\underline{384.16 \times 0.0625}$$

$$96.04$$

- Evaluate without using mathematical table

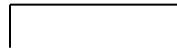
$$\left(\sqrt{\frac{1000}{200}} \right) 0.0128$$

- 3.) Express the numbers 1470 and 7056, each as a product of its prime factors.

Hence evaluate: $\frac{1470^2}{7056}$

Leaving the answer in prime factor form

- 4.) Without using mathematical tables or calculators, evaluate



$$\frac{\sqrt[3]{675 \times 135}}{\sqrt{2025}}$$

- 5.) Evaluate without using mathematical tables or the calculator

$$\frac{0.0625 \times 2.56}{0.25 \times 0.08}$$

CHAPTER NINE

SQUARE AND SQuRE ROOTS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Find squares of numbers by multiplication
- b.) Find squares from tables
- c.) Find square root by factor method
- d.) Find square root from tables.

Content

- a.) Squares by multiplication
- b.) Squares from tables
- c.) Square roots by factorization
- d.) Square roots from tables.

Introduction

Squares

The square of a number is simply the umber multiplied by itself once. For example the square of 15 is 225. That is $15 \times 15 = 225$.

Square from tables

The squares of numbers can be read directly from table of squares. This tables give only approximate values of the squares to 4 figures. The squares of numbers from 1.000 to 9.999 can be read directly from the tables.

The use of tables is illustrated below

Example

Find the square of:

- a.) 4.25
- b.) 42.5
- c.) 0.425

Tables

- a.) To read the square of 4.25, look for 4.2 down the column headed x. Move to the right along this row, up to where it intersects with the column headed 5. The number in this position is the square of 4.25
So $4.25^2 = 18.06$ to 4 figures
- b.) The square of 4.25 lies between 40^2 and 50^2 between 1600 and 2500.

$$\begin{aligned}
 42.5^2 &= (4.25 \times 10^1)^2 \\
 &= 4.25^2 \times 10^2 \\
 &= 18.06 \times 100 \\
 &= 1806
 \end{aligned}$$

c.) $0.425^2 = (4.25 \times \frac{1}{10})^2$

$$\begin{aligned}
 &= 4.25^2 \times (\frac{1}{10})^2 \\
 &= 18.06 \times 1/100 \\
 &= 0.1806
 \end{aligned}$$

The square tables have extra columns labeled 1 to 9 to the right of the thick line. The numbers under these columns are called mean differences. To find 3.162, read 3.16 to get 9.986. Then read the number in the position where the row containing 9.986 intersects with the differences column headed 2. The difference is 13 and this should be added to the last digits of 9.986

$$\begin{array}{r}
 9.986 \\
 + \quad 13 \\
 \hline
 9.999
 \end{array}$$

56.129 has 5 significant figures and in order to use 4 figures tables, we must first round it off to four figures.

$$\begin{aligned}
 56.129 &= 56.13 \text{ to 4 figures} \\
 56.13^2 &= (5.613 \times 10^1)^2 \\
 &= 31.50 \times 10^2 \\
 &= 3150
 \end{aligned}$$

Square Roots

Square roots are the opposite of squares. For example $5 \times 5 = 25$, we say that 5 is a square root of 25. Any positive number has two square roots, one positive and the other negative. The symbol for the square root of a number is $\sqrt{}$.

A number whose square root is an integer is called a perfect square. For example 1, 4, 9, 25 and 36 are perfect squares.

Square roots by Factorization.

The square root of a number can also be obtained using factorization method.

Example

Find the square root of 81 by factorization method.

Solution

$$\begin{aligned}\sqrt{81} &= \sqrt{3 \times 3 \times 3 \times 3} \quad (\text{Find the prime factor of 81}) \\ &= (3 \times 3) (3 \times 3) \quad (\text{Group the prime factors into two identical numbers}) \\ &= 3 \times 3 \quad (\text{Out of the two identical prime factors, choose one and find their product}) \\ &= 9\end{aligned}$$

Note:

Pair the prime factors into two identical numbers. For every pair, pick only one number then obtain the product.

Example

Find $\sqrt{1764}$ by factorization.

Solution

$$\begin{aligned}\sqrt{1764} &= \sqrt{2 \times 2 \times 3 \times 3 \times 7 \times 7} \\ &= 2 \times 3 \times 7 \\ &= 42\end{aligned}$$

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CHAPTER TEN

ALGEBRAIC EXPRESSION

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Use letters to represent numbers
- b.) Write statements in algebraic form
- c.) Simplify algebraic expressions
- d.) Factorize an algebraic expressions by grouping
- e.) Remove brackets from algebraic expressions
- f.) Evaluate algebraic expressions by substituting numerical values
- g.) Apply algebra in real life situations.

Content

- a.) Letters for numbers
- b.) Algebraic fractions
- c.) Simplification of algebraic expressions
- d.) Factorization by grouping
- e.) Removal of brackets
- f.) Substitution and evaluation
- g.) Problem solving in real life situations.

Introduction

An algebraic expression is a mathematical expression that consists of variables, numbers and operations. The value of this expression can change. Clarify the definitions and have students take notes on their graphic organizer.

Note:

- **Algebraic Expression**—contains at least one variable, one number and one operation. An example of an algebraic expression is $n + 9$.
- **Variable**—a letter that is used in place of a number. Sometimes, the variable will be given a value. This value will replace the variable in order to solve the equation. Other times, the variable is not assigned a value and the student is to solve the equation to determine the value of the variable.
- **Constant**—a number that stands by itself. The 9 in our previous vocabulary is an example of a constant.
- **Coefficient**—a number in front of and attached to a variable. For example, in the expression $5x + 3$, the 5 is the coefficient.
- **Term**—each part of an expression that is separated by an operation. For instance, in our earlier example $n + 9$, the terms are n and 7.

Examples

Write each phrase as an algebraic expression.

Nine increased by a number $r \rightarrow 9 + r$

Fourteen decreased by a number $x \rightarrow 14 - x$

Six less than a number $t \rightarrow t - 6$

The product of 5 and a number $n \rightarrow 5 \times n$ or $5n$

Thirty-two divided by a number $y \rightarrow 32 \div x$ or $\frac{32}{x}$

Example

An electrician charges sh 450 per hour and spends sh 200 a day on gasoline. Write an algebraic expression to represent his earnings for one day.

Solution: Let x represent the number of hours the electrician works in one day. The electrician's earnings can be represented by the following algebraic expression:

Solution

$$450x - 200$$

Simplification of Algebraic Expressions

Note:

Basic steps to follow when simplify an algebraic expression:

- ✓ Remove parentheses by multiplying factors.
- ✓ Use exponent rules to remove parentheses in terms with exponents.
- ✓ Combine like terms by adding coefficients.
- ✓ Combine the constants.

Like and unlike terms

Like terms have the same variable /letters raised to the same power i.e. $3b + 2b = 5b$ or $a + 5a = 6a$ and they can be simplified further into $5b$ and $6a$ respectively (a^2 and $3a^2$ are also like terms). While unlike terms have different variables i.e. $3b + 2c$ or $4b + 2x$ and they cannot be simplified further.

Example

$$3a + 12b + 4a - 2b = 7a + 10b \quad (\text{collect the like terms})$$

$$2x - 5y + 3x - 7y + 3w = 5x - 12y + 3w$$

Example

$$\text{Simplify: } 2x - 6y - 4x + 5z - y$$

Solution

$$\begin{aligned} 2x - 6y - 4x + 5z - y &= 2x - 4x - 6y - y + 5z \\ &= (2x - 4x) - (6y + y) + 5z \\ &= -2x - 7y + 5z \end{aligned}$$

Note:

$$-6y - y = -(6y + y)$$

Example

$$\text{Simplify: } \frac{1}{2}a - \frac{1}{3}b + \frac{1}{4}a$$

Solution

The L.C.M of 2, 3 and 4 is 12.

$$\text{Therefore } \frac{1}{2}a - \frac{1}{3}b + \frac{1}{4}a = \frac{6a - 4b + 3a}{12}$$

$$\begin{aligned} &= \frac{6a + 3a - 4b}{12} \\ &= \frac{9a - 4b}{12} \end{aligned}$$

Example

$$\text{Simplify: } \frac{a+b}{2} - \frac{2a-b}{3}$$

Solution

$$\begin{aligned} \frac{a+b}{2} - \frac{2a-b}{3} &= \frac{3(a+b) - 2(2a-b)}{6} \\ &= \frac{3a + 3b - 4a + 2b}{6} \\ &= \frac{6}{6} \\ &= \frac{-a + 5b}{6} \end{aligned}$$

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CHAPTER ELEVEN

RATES, RATIO, PROPORTION AND PERCENTAGE

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Define rates
- b.) Solve problems involving rates
- c.) Define ratio
- d.) Compare two or more quantities using ratios
- e.) Change quantities in a given ratio
- f.) Compare two or more ratios
- g.) Represent and interpret proportional parts
- h.) Recognize direct and inverse proportions
- i.) Solve problems involving direct and inverse proportions
- j.) Convert fractions and decimals to percentages and vice-versa
- k.) Calculate percentage change in a given quantity
- l.) Apply rates, ratios, percentages to real life situations and proportion.

Content

- a.) Rates
- b.) Solving problems involving rates
- c.) Ratio
- d.) Comparing quantities using ratio
- e.) Increase and decrease in a given ratio
- f.) Comparing ratios
- g.) Proportion: direct and inverse
- h.) Solve problems on direct and inverse proportions
- i.) Fractions and decimals as percentages
- j.) Percentage increase and decrease
- k.) Application of rates, ratios, percentages and proportion to real life situations.

Introduction

Rates

A rate is a measure of quantity, and comparing one quantity with another of different kind.

Example

If a car takes two hours to travel a distance of 160 km. then we will say that it is travelling at an average rate of 80 km per hour. If two kilograms of maize meal is sold for sh. 38.00, then we say that maize meal is selling at the rate of sh.19.00 per kilogram.

Example

What is the rate of consumption per day if twelve bags of beans are consumed in 120 days?

Solution.

Rate of consumption = number of bags/number of days

$$= \frac{12}{120}$$

=1/10 bags per day

Example

A laborer's wage is sh.240 per eight hours working day. What is the rate of payment per hour?

Solution

Rate = amount of money paid/number of hours

$$= \frac{240}{8}$$

=sh.30 per hour

Ratio

A ratio is a way of comparing two similar quantities. For example, if alias is 10 years old and his brother basher is 14 years old. Then alias age is 10/14 of Bashir's age, and their ages are said to be in the ratio of 10 to 14. Written, 10:14.

Alias age: Bashir's age =10:14

Bashir's age: alias age =14:10

In stating a ratio, the units must be the same. If on a map 2cm rep 5km on the actual ground, then the ratio of map distance to map distance is 2cm: 5x1 00 000cm, which is 2:500 000.

A ratio is expressed in its simplest form in the same way as a fraction,

E.g. $10/14 = 5/7$, hence 10:14= 5:7.

Similarly, $2:500\ 000 = 1: 250\ 000$,

A proportion is a comparison of two or more ratios. If, example, a, b and c are three numbers such that a: b: c=2:3:5, then a, b, c are said to be proportional to 2, 3, 5 and the relationship should be interpreted to mean $a/2 = b/3=c/5$.

Similarly, we can say that a: b =2:3, b: c=3:5 a: c=2:5

Example 3

If a: b = 3: 4 and b: c = 5: 7 find a: c

Solution

a: b =3 : 4.....(i)

b: c=5 : 7.....(ii)

Consider the right hand side;

Multiply (i) by 5 and (ii) by 4 to get, a: b=15: 20 and b: c=20: 28

Thus, a: b: c = 15: 20: 28 and a: c=15: 28

Increase and decrease in a given ratio

To increase or decrease a quantity in a given ratio, we express the ratio as a fraction and multiply it by the quantity.

Example

Increase 20 in the ratio 4: 5

Solution

New value = $\frac{5}{4} \times 20$

$$= 5 \times 5$$

$$= 25$$

Example

Decrease 45 in the ratio 7:9

Solution

New value = $\frac{7}{9} \times 45$

$$= 7 \times 5$$

$$= 35$$

Example

The price of a pen is adjusted in the ratio 6:5. If the original price was sh.50. What is the new price?

Solution

New price: old price = 6:5

New price /old price = $\frac{6}{5}$

New price = $\frac{6}{5} \times 50$

$$= \text{sh. } 60$$

Note:

When a ratio expresses a change in a quantity an increase or decrease , it is usually put in the form of new value: old value

Comparing ratios

In order to compare ratios, they have to be expressed as fractions first, ie., $a:b = a/b$. the resultant fraction can then be compared.

Example

Which ratio is greater, 2: 3 or 4: 5?

Solution $2:3 = \frac{2}{3}$, $4:5 = \frac{4}{5}$

$$\frac{2}{3} = \frac{10}{15}, \frac{4}{5} = \frac{12}{15} = \frac{4}{5} > \frac{2}{3}$$

Thus, $4: 5 > 2: 3$

Distributing a quantity in a given ratio

If a quantity is to be divided in the ratio a: b: c, the fraction of the quantity represented by:

(i) A will be $\frac{a}{a+b+c}$

(ii) B will be $\frac{b}{a+b+c}$

(iii) C will be $\frac{c}{a+b+c}$

Example

A 72-hactare farm is to be shared among three sons in the ratio 2:3:4. What will be the sizes in hectares of the three shares?

Solution

Total number of parts is $2+3+4=9$

The she shares are: $2/9 \times 72\text{ha} = 16\text{ha}$

$3/9 \times 72\text{ha} = 24\text{ha}$

$4/9 \times 72\text{ha} = 36\text{ha}$

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CHAPTER TWELVE

LENGTH

Specific Objectives

By the end of the topic the learner should be able to:

- a.) State the units of measuring length
- b.) Convert units of length from one form to another
- c.) Express numbers to required number of significant figures
- d.) Find the perimeter of a plane figure and circumference of a circle.

Content

- a.) Units of length (mm, cm, m, km)
- b.) Conversion of units of length from one form to another
- c.) Significant figures
- d.) Perimeter
- e.) Circumference (include length of arcs)

Introduction

Length is the distance between two points. The SI unit of length is metres. Conversion of units of length.

1 kilometer (km) = 1000metres

1 hectometer (hm) = 100metres

1 decameter (Dm) = 10 metres

1 decimeter (dm) = 1/10 metres

1 centimeter (cm) = 1/100 metres

1 millimeter (mm) = 1/1000 metres

The following prefixes are often used when referring to length:

Mega – 1 000 000

Kilo – 1 000

Hecto – 100

Deca -10

Deci-1/10

Centi-1/100

Milli-1/1000

Micro-1/1 000 000

Significant figures

The accuracy with which we state or write a measurement may depend on its relative size. It would be unrealistic to state the distance between towns A and B as 158.27 km. a more reasonable figure is 158 km. 158.27km is the distance expressed to 5 significant figures and 158 km to 3 significant figures.

Example

Express each of the following numbers to 5, 4, 3, 2, and 1 significant figures:

- (a) 906 315
- (b) 0.08564
- (c) 40.0089
- (d) 156 000

Solution

	number	5 s.f.	4s.f	3s.f	2s.f	1 s.f.
(a)	906 315	906 320	906 300	906 000	910 000	900 000
(b)	0.085641	0.085641	0.08564	0.0856	0.085	0.09
(c)	40.0089	40.009	40.01	40.0	40	40
(d)	156 000	156 000	156 000	156 000	160 000	200 000

The above example show how we would round off a measurement to a given number of significant figures

Zero may not be a significant. For example:

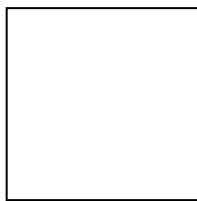
- (i) 0.085 - zero is not significant therefore, 0.085 is a two- significant figure.
- (ii) 2.30 – zero is significant. Therefore 2.30 is a three-significant figure.
- (iii) 5 000 –zero may or may not be significant figure. Therefore, 5 000 to three significant figure is 5 00 (zero after 5 is significant). To one significant figure is 5 000. Zero after 5 is not significant.
- (iv) 31.805 Or 305 – zero is significant, therefore 31.805 is five significant figure. 305 is three significant figure.

Perimeter

The perimeter of a plane is the total length of its boundaries. Perimeter is a length and is therefore expressed in the same units as length.

Square shapes

5cm



Its perimeter is $5+5+5+5= 2(5+5)$

$$=2(10)$$

$$=20\text{cm}$$

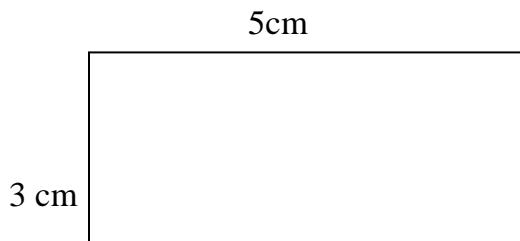
Hence

$$5 \times 4 = 20$$

So perimeter of a square = Sides x 4

Rectangular shapes

Figure 12.2 is a rectangle of length 5cm and breadth 3cm.



Its perimeter is $5+3+5+3 = 2(5+3)\text{cm}$

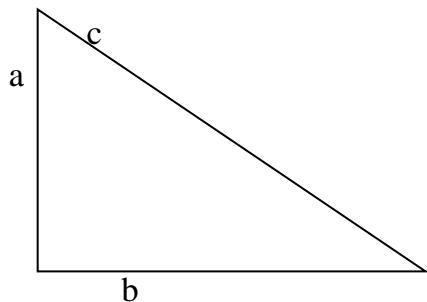
$$=2 \times 8$$

$$= 16\text{cm}$$

Hence perimeter of a rectangle $p=2(L+W)$

Triangular shapes

To find the perimeter of a triangle add all the three sides.



Perimeter = $(a + b + c)$ units, where a , b and c are the lengths of the sides of the triangle.

The circle

The circumference of a circle = $2 \pi r$ or πD

Example

(a) Find the circumference of a circle of a radius 7cm.

(b) The circumference of a bicycle wheel is 140 cm. find its radius.

Solution

(a) $C = \pi d$

$$= 22/7 \times 7$$

$$= 44 \text{ cm}$$

$$(b) C = \pi d$$

$$= 2\pi r$$

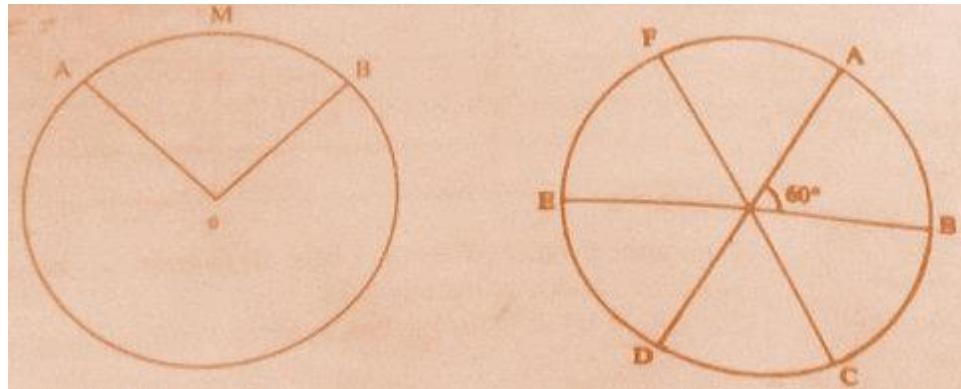
$$= 2 \times 22/7 \times r$$

$$= 140 \div 44/7$$

$$= 22.27 \text{ cm}$$

Length of an arc

An arc of a circle is part of its circumference. Figure 12.10 (a) shows two arcs AMB and ANB. Arc AMB, which is less than half the circumference of the circle, is called the minor arc, while arc ANB, which is greater than half of the circumference is called the major arc. An arc which is half the circumference of the circle is called a semicircle.



Example

An arc of a circle subtends an angle 60 at the centre of the circle. Find the length of the arc if the radius of the circle is 42 cm. ($\pi = 22/7$).

Solution

The length, l , of the arc is given by:

$$L = \theta/360 \times 2\pi r.$$

$$\theta = 60, r = 42 \text{ cm}$$

$$\text{Therefore, } l = 60/360 \times 2 \times 22/7 \times 42$$

$$= 44 \text{ cm}$$

Example

The length of an arc of a circle is 62.8 cm. find the radius of the circle if the arc subtends an angle 144 at the centre, (take $\pi = 3.142$).

Solution

$$L = \theta/360 \times 2\pi r = 62.8 \text{ and } \theta = 144$$

$$\text{Therefore, } \frac{144}{360} \times 2 \times 3.142 \times r = 62.8$$

$$R = 62.8 \times \frac{360}{144} \times 2 \times 3.142$$

$$= 24.98 \text{ cm}$$

Example

Find the angle subtended at the centre of a circle by an arc of length 11cm if the radius of the circle is 21cm.

Solution

$$L = \theta/360 \times 2 \times \pi r = 11 \text{ cm} \text{ and } r = 21 \text{ cm}$$

$$L = \theta/360 \times 2 \times 22/7 \times 21 = 11$$

$$\text{Thus, } \theta = 11 \times 360 \times 7 / 2 \times 22 \times 21$$

$$= 30^\circ$$

End of topic

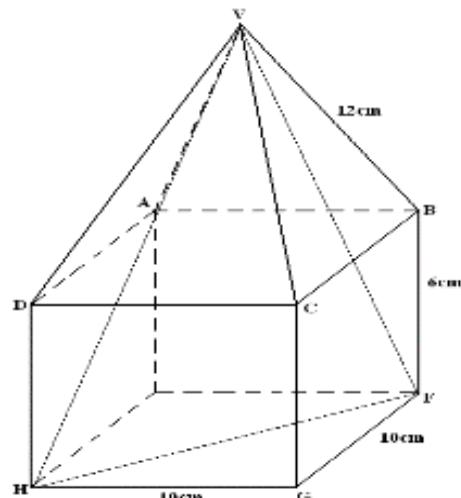
Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) Two coils which are made by winding copper wire of different gauges and length have the same mass. The first coil is made by winding 270 metres of wire with cross sectional diameter 2.8mm while the second coil is made by winding a certain length of wire with cross-sectional diameter 2.1mm. Find the length of wire in the second coil .

2. The figure below represents a model of a hut with HG = GF = 10cm and FB = 6cm. The four slanting edges of the roof are each 12cm long.



Calculate

Length DF.

Angle VHF

The length of the projection of line VH on the plane EFGH.

The height of the model hut.

The length VH.

The angle DF makes with the plane ABCD.

3.

A square floor is fitted with rectangular tiles of perimeters 220 cm. each row (tile length wise) carries 20 less tiles than each column (tiles breadth wise). If the length of the floor is 9.6 m.

Calculate:

a. The dimensions of the tiles

b. The number of tiles needed

c. The cost of fitting the tiles, if tiles are sold in dozens at sh. 1500 per dozen and the labour cost is sh. 3000

CHAPTER THIRTEEN

AREA

Specific Objectives

By the end of the topic the learner should be able to:

- a.) State units of area
- b.) Convert units of area from one form to another
- c.) Calculate the area of a regular plane figure including circles
- d.) Estimate the area of irregular plane figures by counting squares
- e.) Calculate the surface area of cubes, cuboids and cylinders.

Content

- a.) Units of area (cm² , m² , km² , Ares, ha)
- b.) Conversion of units of area
- c.) Area of regular plane figures
- d.) Area of irregular plane shapes
- e.) Surface area of cubes, cuboids and cylinders

Introduction

Units of Areas

The area of a plane shape is the amount of the surface enclosed within its boundaries. It is normally measured in square units. For example, a square of sides 5 cm has an area of

$$5 \times 5 = 25 \text{ cm}^2$$

A square of sides 1m has an area of 1m, while a square of side 1km has an area of 1km

Conversion of units of area

$$1 \text{ m}^2 = 1 \text{ m} \times 1 \text{ m}$$

$$= 100 \text{ cm} \times 100 \text{ cm}$$

$$= 10\,000 \text{ cm}^2$$

$$1 \text{ km}^2 = 1 \text{ km} \times 1 \text{ km}$$

$$= 1\,000 \text{ m} \times 1\,000 \text{ m}$$

$$= 1\,000\,000 \text{ m}^2$$

$$1 \text{ are} = 10 \text{ m} \times 10 \text{ m}$$

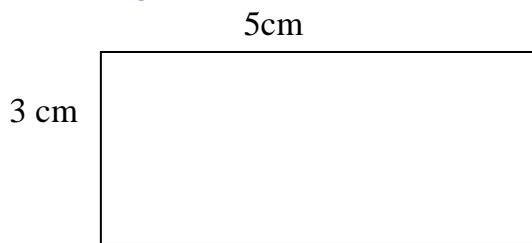
$$= 100 \text{ m}^2$$

$$1 \text{ hectare (ha)} = 100 \text{ Ares}$$

$$= 10\,000 \text{ m}^2$$

Area of a regular plane figures

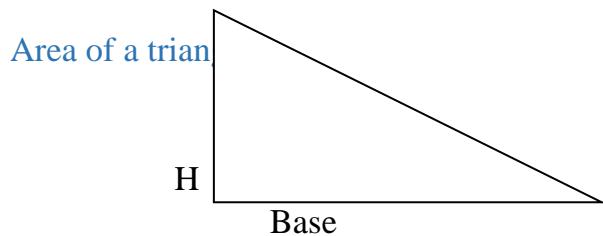
Areas of rectangle



$$\text{Area, } A = 5 \times 3 \text{ cm}$$

$$= 15 \text{ cm}^2$$

Hence, the area of the rectangle, $A = L \times W$ square units, where l is the length and b breadth.



Area of a triangle

$$A = \frac{1}{2}bh \text{ square units}$$

Area of parallelogram

$$\text{Area} = \frac{1}{2}bh + \frac{1}{2}bh$$

$$= bh \text{ square units}$$

Note:

This formulae is also used for a rhombus

Area of a trapezium

The figure below shows a trapezium in which the parallel sides are a units and b units, long. The perpendicular distance between the two parallel sides is h units.

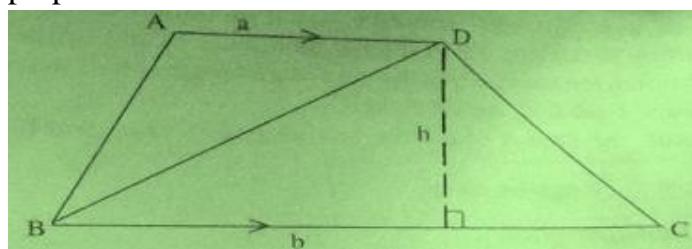
$$\text{Area of a triangle } ABD = \frac{1}{2} ah \text{ square units}$$

$$\text{Area of triangle } DBC = \frac{1}{2} bh \text{ square units}$$

$$\text{Therefore area of trapezium } ABCD = \frac{1}{2} ah + \frac{1}{2} bh$$

$$= \frac{1}{2}h(a + b) \text{ square units.}$$

Thus, the area of a trapezium is given by a half the sum of the length of parallel sides multiplied by the perpendicular distance between them.



$$\text{That is, area of trapezium } = \frac{1}{2}(a + b)h$$

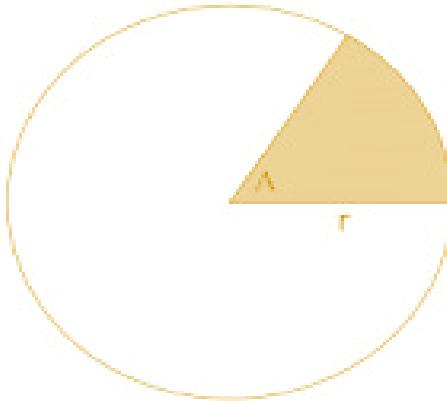
Area of a circle

The area A of a circle of radius r is given by: $A = \pi r^2$

The area of a sector

A sector is a region bounded by two radii and an arc.

Suppose we want to find the area of the shaded part in the figure below



The area of the whole circle is πr^2

The whole circle subtends 360° at the centre.

Therefore, 360° corresponds to πr^2

1° corresponds to $1/360 \times \pi r^2$

60° corresponds to $60/360 \times \pi r^2$

Hence, the area of a sector subtending an angle θ at the centre of the circle is given by

$$A = \frac{\theta}{360^\circ} \times \pi r^2$$

Example

Find the area of the sector of a circle of radius 3cm if the angle subtended at the centre is 140° (take $\pi=22/7$)

Solution

Area A of a sector is given by

$$A = \frac{\theta}{360^\circ} \times \pi r^2$$

Here, $r = 3$ cm and $\theta = 140^\circ$

$$\begin{aligned} \text{Therefore, } A &= \frac{140}{360^\circ} \times \frac{22}{7} \times 3 \times 3 \\ &= 11 \text{ cm}^2 \end{aligned}$$

Example

The area of a sector of a circle is 38.5 cm². Find the radius of the circle if the angle subtended at the centre is 90° (Take $\pi=22/7$)

Solution

From the formula $a = \theta/360 \times \pi r^2$, we get $90/360 \times 22/7 \times r^2 = 38.5$

$$\text{Therefore, } r^2 = \frac{38.5 \times 360 \times 7}{90 \times 22}$$

Thus, $r = 7$

Example

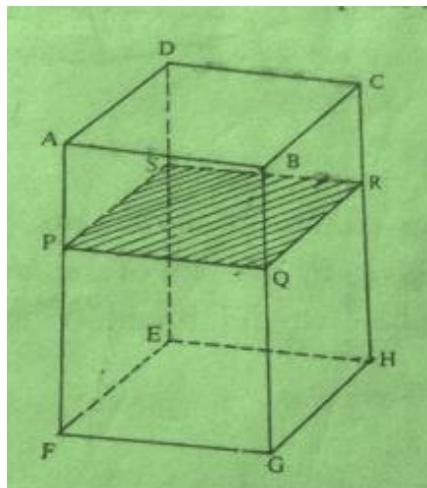
The area of a circle radius 63 cm is 4158 cm^2 . Calculate the angle subtended at the centre of the circle.
(Take $\pi = 22/7$)

Using $a = \theta/360 \times \pi r^2$,

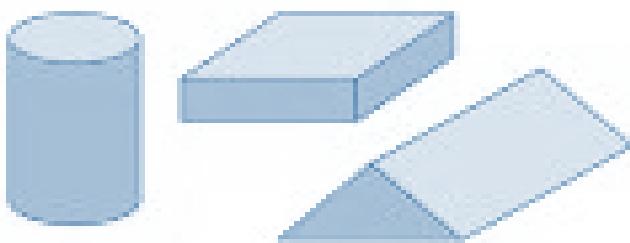
$$\Theta = \frac{4158 \times 7 \times 360}{22 \times 63 \times 63}$$
$$= 120^\circ$$

Surface area of solids

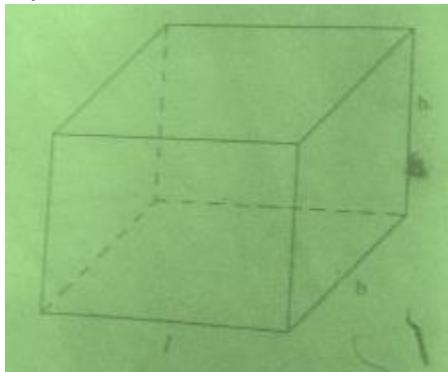
Consider a cuboid ABCDEFGH shown in the figure below. If the cuboid is cut through a plane parallel to the ends, the cut surface has the same shape and size as the end faces. PQRS is a plane. The plane is called the cross-section of the cuboid



A solid with uniform cross-section is called a prism. The following are some of the prisms. The following are some of the prisms.



The surface area of a prism is given by the sum of the area of the surfaces.



The figure below shows a cuboid of length l , breath b and height h . its area is given by;

$$A = 2lb + 2bh + 2hl$$

$$= 2(lb + bh + hl)$$

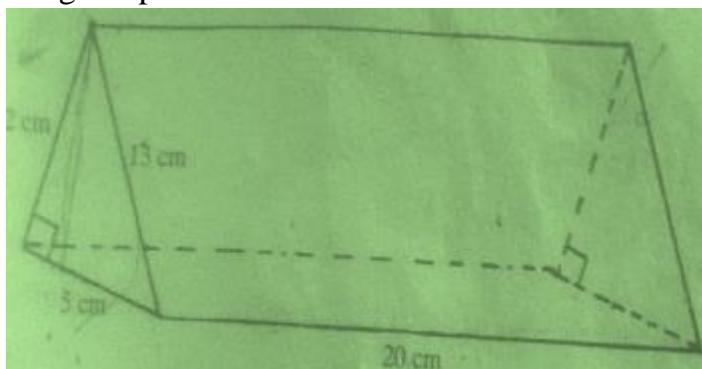
For a cube offside 2cm;

$$A = 2(3 \times 2^2)$$

$$= 24 \text{ cm}^2$$

Example

Find the surface area of a triangular prism shown below.



$$\text{Area of the triangular surfaces} = \frac{1}{2} \times 5 \times 12 \times 2 \text{ cm}^2$$

$$= 60 \text{ cm}^2$$

$$\text{Area of the rectangular surfaces} = 20 \times 13 + 5 \times 20 + 12 \times 20$$

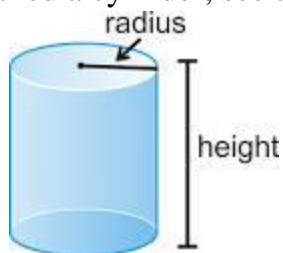
$$= 260 + 100 + 240 = 600 \text{ cm}^2$$

$$\text{Therefore, the total surface area} = (60 + 600) \text{ cm}^2$$

$$= 660 \text{ cm}^2$$

Cylinder

A prism with a circular cross-section is called a cylinder, see the figure below.



If you roll a piece of paper around the curved surface of a cylinder and open it out, you will get a rectangle whose breath is the circumference and length is the height of the cylinder. The ends are two circles. The surface area S of a cylinder with base and height h is therefore given by;

$$S=2\pi rh + 2\pi r^2$$

Example

Find the surface area of a cylinder whose radius is 7.7 cm and height 12 cm.

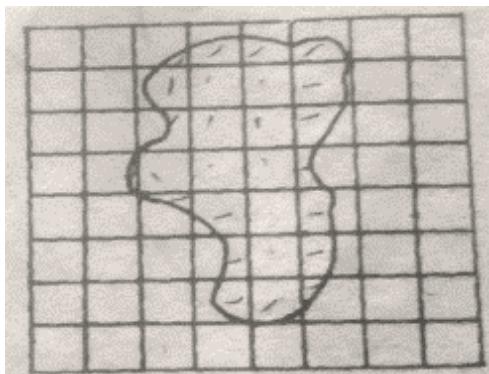
Solution

$$\begin{aligned} S &= 2 \pi (7.7) \times 12 + 2 \pi (7.7) \text{ cm}^2 \\ &= 2 \pi (7.7) \times 12 + (7.7) \text{ cm}^2 \\ &= 2 \times 7.7 \pi (12 + 7.7) \text{ cm}^2 \\ &= 2 \times 7.7 \times \pi (19.7) \text{ cm}^2 \\ &= 15.4\pi (19.7) \text{ cm}^2 \\ &= 953.48 \text{ cm}^2 \end{aligned}$$

Area of irregular shapes

The area of irregular shape cannot be found accurately, but it can be estimated. As follows;

- (i) Draw a grid of unit squares on the figure or copy the figure on such a grid, see the figure below



- (ii) Count all the unit squares fully enclosed within the figure.
(iii) Count all partially enclosed unit squares and divide the total by two, i.e., treat each one of them as half of a unit square.
(iv) The sum of the numbers in (ii) and (iii) gives an estimate of the areas of the figure.

From the figure, the number of full squares is 9

Number of partial squares = 18

Total number of squares = $9 + 18/2$

=18

Approximate area = 18 sq. units.

End of topic

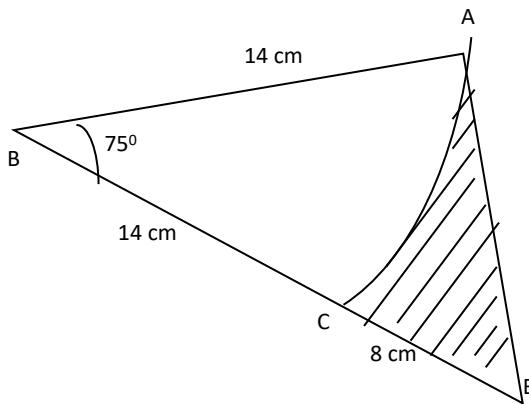
Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

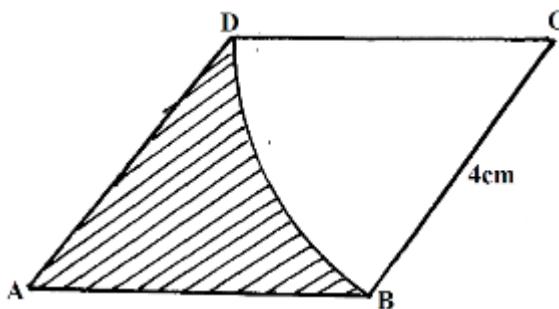
- 1.) Calculate the area of the shaded region below, given that AC is an arc of a circle centre B.

$AB=BC=14\text{cm}$ $CD=8\text{cm}$ and angle $ABD = 75^\circ$ (4 mks)

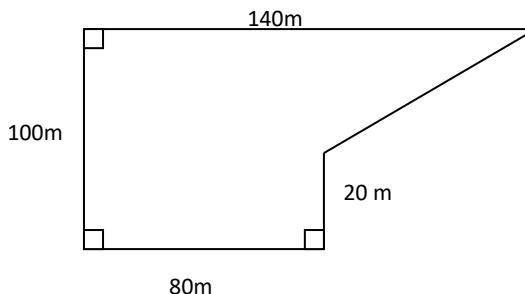


- 2.) The scale of a map is 1:50000. A lake on the map is 6.16cm^2 . find the actual area of the lake in hectares. (3mks)

- 3.) The figure below is a rhombus ABCD of sides 4cm. BD is an arc of circle centre C. Given that $\angle ABC = 138^\circ$. Find the area of shaded region. (3mks)

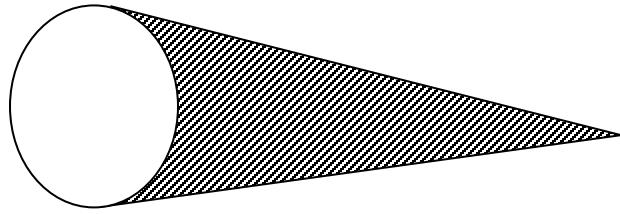


- 4.) The figure below shows the shape of Kamau's farm with dimensions shown in meters



Find the area of Kamau's farm in hectares (3mks)

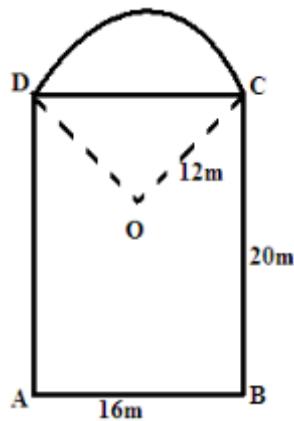
- 5.) In the figure below AB and AC are tangents to the circle centre O at B and C respectively, the angle $AOC = 60^\circ$



Calculate

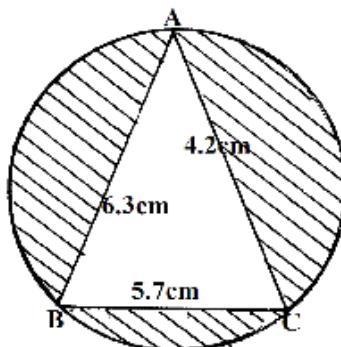
- (a) The length of AC

- 6.) The figure below shows the floor of a hall. A part of this floor is in the shape of a rectangle of length 20m and width 16m and the rest is a segment of a circle of radius 12m. Use the figure to find:-

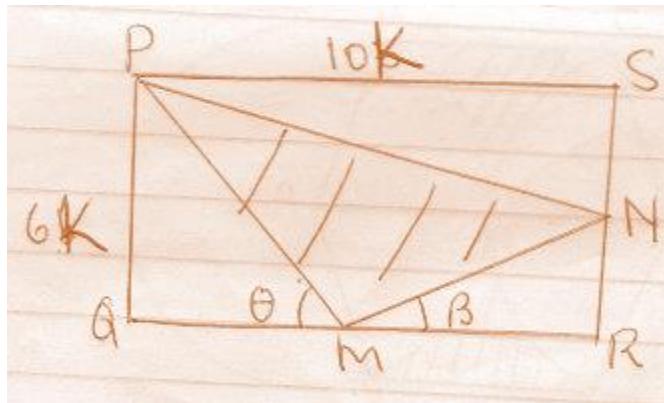


- (a) The size of angle COD (2mks)
 (b) The area of figure DABCO (4mks)
 (c) Area of sector ODC (2mks)
 (d) Area of the floor of the house. (2mks)

- 7.) The circle below whose area is 18.05cm^2 circumscribes a triangle ABC where $AB = 6.3\text{cm}$, $BC = 5.7\text{cm}$ and $AC = 4.8\text{cm}$. Find the area of the shaded part

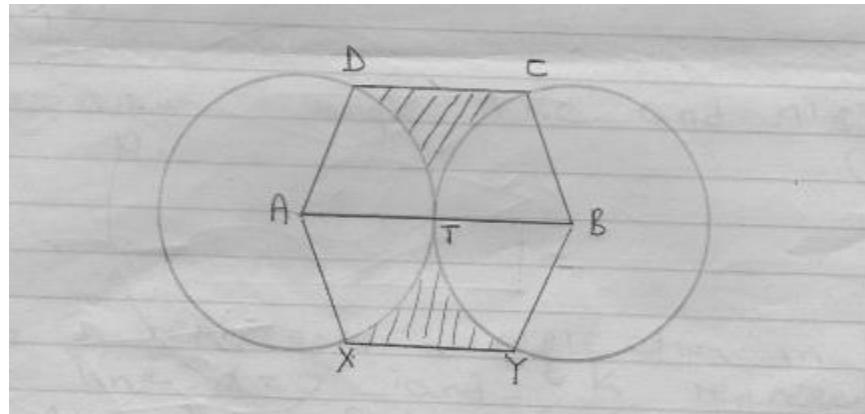


- 8.) In the figure below, PQRS is a rectangle in which $PS = 10k$ cm and $PQ = 6k$ cm. M and N are midpoints of QR and RS respectively



- a) Find the area of the shaded region (4 marks)
 b) Given that the area of the triangle MNR = 30 cm^2 . find the dimensions of the rectangle(2 marks)
 c) Calculate the sizes of angles θ and β giving your answer to 2 decimal places (4 marks)

- 9.) The figure below shows two circles each of radius 10.5 cm with centres A and B. the circles touch each other at T



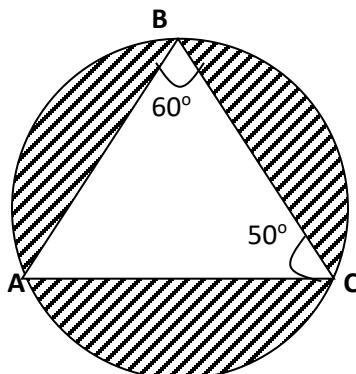
Given that angle XAD = angle YBC = 160° and lines XY, ATB and DC are parallel, calculate the area of:

- d) The minor sector AXTD (2 marks)
 e) Figure AXYBCD (6marks)
 f) The shaded region (2 marks)

- 10.) The floor of a room is in the shape of a rectangle 10.5 m long by 6 m wide. Square tiles of length 30 cm are to be fitted onto the floor.
 (a) Calculate the number of tiles needed for the floor.
 (b) A dealer wishes to buy enough tiles for fifteen such rooms. The tiles are packed in cartons each containing 20 tiles. The cost of each carton is Kshs. 800. Calculate

- (i) the total cost of the tiles.
(ii) If in addition, the dealer spends Kshs. 2,000 and Kshs. 600 on transport and subsistence respectively, at what price should he sell each carton in order to make a profit of 12.5% (Give your answer to the nearest Kshs.)

- 11.) The figure below is a circle of radius 5cm. Points **A**, **B** and **C** are the vertices of the triangle ABC in which $\angle ABC = 60^\circ$ and $\angle ACB=50^\circ$ which is in the circle. Calculate the area of ΔABC)



- 12.) Mr.Wanyama has a plot that is in a triangular form. The plot measures 170m, 190m and 210m, but the altitudes of the plot as well as the angles are not known. Find the area of the plot in hectares
- 13.) Three sirens wail at intervals of thirty minutes, fifty minutes and thirty five minutes. If they wail together at 7.18a.m on Monday, what time and day will they next wail together?
- 14.) A farmer decides to put two-thirds of his farm under crops. Of this, he put a quarter under maize and four-fifths of the remainder under beans. The rest is planted with carrots. If 0.9acres are under carrots, find the total area of the farm

CHAPTER FOURTEEN

VOLUME AND CAPACITY

Specific Objectives

By the end of the topic the learner should be able to:

- a.) State units of volume
- b.) Convert units of volume from one form to another
- c.) Calculate volume of cubes, cuboids and cylinders
- d.) State units of capacity
- e.) Convert units of capacity from one form to another
- f.) Relate volume to capacity
- g.) Solve problems involving volume and capacity.

Content

- a.) Units of volume
- b.) Conversion of units of volume
- c.) Volume of cubes, cuboids and cylinders
- d.) Units of capacity
- e.) Conversion of units of capacity
- f.) Relationship between volume and capacity
- g.) Solving problems involving volume and capacity

Introduction

Volume is the amount of space occupied by a solid object. The unit of volume is cubic units.
A cube of edge 1 cm has a volume of $1 \text{ cm} \times 1 \text{ cm} \times 1 \text{ cm} = 1 \text{ cm}^3$.

Conversion of units of volume

A cube of side 1 m has a volume of 1 m^3

But $1 \text{ m} = 100 \text{ cm}$

$1 \text{ m} \times 1 \text{ m} \times 1 \text{ m} = 100 \text{ cm} \times 100 \text{ cm} \times 100 \text{ cm}$

Thus, $1 \text{ m} = (0.01 \times 0.01 \times 0.01) \text{ m}^3$

$= 0.000001 \text{ m}^3$

$= 1 \times 10^{-6} \text{ m}^3$

A cube side 1 cm has a volume of 1 cm^3 .

But $1 \text{ cm} = 10 \text{ mm}$

$1 \text{ cm} \times 1 \text{ cm} \times 1 \text{ cm} = 10 \text{ mm} \times 10 \text{ mm} \times 10 \text{ mm}$

Thus, $1 \text{ cm}^3 = 1000 \text{ mm}^3$

Volume of cubes, cuboids and cylinders

Cube

A cube is a solid having six plane square faces in which the angle between two adjacent faces is a right-angle.

Volume of a cube= area of base x height

$$=l^2 \times l$$

$$=l^3$$

Cuboid

A cuboid is a solid with six faces which are not necessarily square.

Volume of a cuboid = length x width x height

$$=a \text{ sq. units} \times h$$

$$=ah \text{ cubic units.}$$

Cylinder

This is a solid with a circular base.

Volume of a cylinder = area of base x height

$$=\pi r^2 \times h$$

$$=\pi r^2 h \text{ cubic units}$$

Example

Find the volume of a cuboid of length 5 cm, breadth 3 cm and height 4 cm.

Solution

$$\text{Area of its base} = 5 \times 4 \text{ cm}^2$$

$$\text{Volume} = 5 \times 4 \times 3 \text{ cm}^3$$

$$= 60 \text{ cm}^3$$

Example

Find the volume of a solid whose cross-section is a right-angled triangle of base 4 cm, height 5 cm and length 12 cm.

Solution

$$\text{Area of cross-section} = 1/2 \times 4 \times 5$$

$$= 10 \text{ cm}^2$$

$$\text{Therefore volume} = 10 \times 12$$

$$= 120 \text{ cm}^3$$

Example

Find the volume of a cylinder with radius 1.4 m and height 13 m.

Solution

$$\text{Area of cross-section} = 22/7 \times 1.4 \times 1.4$$

$$= 6.16 \text{ m}^2$$

$$\text{Volume} = 6.16 \times 13$$

$$= 80.08 \text{ m}^3$$

In general, volume v of a cylinder of radius r and length l given by $v = \pi r^2 l$

Capacity

Capacity is the ability of a container to hold fluids. The SI unit of capacity is litre (l)

Conversion of units to capacity

1 centiliter (cl) = 10 millilitre (ml)

1 decilitre (dl) = 10 centilitre (cl)

1 litre (l) = 10 decilitres (dl)

1 Decalitre (Dl) = 10 litres (l)

1 hectolitre (Hl) = 10 decalitre (Dl)

1 kilolitre (kl) = 10 hectolitres (Hl)

1 kilolitre (kl) = 1000 litres (l)

1 litre (l) = 1000 millilitres (ml)

Relationship between volume and capacity

A cubed of an edge 10 cm holds 1 litre of liquid.

1 litre = 10 cm x 10cm x 10cm

= 1 000 cm^3

1 m^3 = 10⁶ cm^3

1 m^3 = 10³ litres.

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) All the water is poured into a cylindrical container of circular radius 12cm. If the cylinder has height 45cm, calculate the surface area of the cylinder which is not in contact with water.

2.) The British government hired two planes to airlift football fans to South Africa for the World cup tournament. Each plane took 10 $\frac{1}{2}$ hours to reach the destination.

Boeng 747 has carrying capacity of 300 people and consumes fuel at 120 litres per minute. It makes 5 trips at full capacity. Boeng 740 has carrying capacity of 140 people and consumes fuel at 200 litres per minute. It makes 8 trips at full capacity. If the government sponsored the fans one way at the cost of 800 dollars per fan, calculate:

(a) The total number of fans airlifted to South Africa. (2mks)

(b) The total cost of fuel used if one litre costs 0.3 dollars. (4mks)

- (c) The total collection in dollars made by each plane. (2mks)
- (d) The net profit made by each plane. (2mks)
- 3.)** A rectangular water tank measures 2.6m by 4.8m at the base and has water to a height of 3.2m. Find the volume of water in litres that is in the tank
- 4.)** Three litres of water (density 1g/cm^3) is added to twelve litres of alcohol (density 0.8g/cm^3). What is the density of the mixture?
- 5.)** A rectangular tank whose internal dimensions are 2.2m by 1.4m by 1.7m is three fifth full of milk.
- (a) Calculate the volume of milk in litres
- (b) The milk is packed in small packets in the shape of a right pyramid with an equilateral base triangle of sides 10cm. The vertical height of each packet is 13.6cm. Full packets obtained are sold at shs.30 per packet. Calculate:
- (i) The volume in cm^3 of each packet to the nearest whole number
- (ii) The number of full packets of milk
- (iii) The amount of money realized from the sale of milk
- 6.)** An 890kg culvert is made of a hollow cylindrical material with outer radius of 76cm and an inner radius of 64cm. It crosses a road of width 3m, determine the density of the material used in its construction in Kg/m^3 correct to 1 decimal place.

CHAPTER FIFTEEN

MASS WEIGHT AND DENSITY

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Define mass
- b.) State units of mass
- c.) Convert units of mass from one form to another
- d.) Define weight
- e.) State units of weight
- f.) Distinguish mass and weight
- g.) Relate volume, mass and density.

Content

- a.) Mass and units of mass
- b.) Weight and units of weight
- c.) Density
- d.) Problem solving involving real life experiences on mass, volume, density and weight.

INCOMPLETE NOTES

**This Forms a Sample
From The Original Notes**

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For F1-F4 All Subjects Complete Notes

CHAPTER TEN

TIME

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Convert units of time from one form to another
- b.) Relate the 12 hour and 24 hour clock systems
- c.) Read and interpret travel time-tables
- d.) Solve problems involving travel time tables.

Content

- a.) Units of time
- b.) 12 hour and 24 hour clock systems
- c.) Travel time-tables
- d.) Problems involving travel time tables

Introduction

Units of time

1 week = 7 days

1 day = 24 hours

1 hour = 60 minutes

1 minutes = 60 seconds

Example

How many hours are there in one week?

Solution

1 week = 7 days

1 day = 24 hours

1 week = (7×24) hours

=168 hours

Example

Convert 3h 45 min into minutes

Solution

1 h = 60 min

$3 \text{ h} = (3 \times 60) \text{ min}$

$3\text{h } 45\text{min} = ((60 \times 3) + 45) \text{ min}$

$= (180 + 45) \text{ min}$

=225 min

Example

Express 4h 15 min in sec

Solution

$$1 \text{ hour} = 60 \text{ min}$$

$$1 \text{ min} = 60 \text{ sec}$$

$$4\text{h } 15 \text{ min} = (4 \times 60 + 15) \text{ min}$$

$$= 240 + 15 \text{ min}$$

$$= 255 \text{ min}$$

$$= 255 \times 60 \text{ sec}$$

$$= 15300 \text{ sec.}$$

The 12 and the 24 hour systems

In the 12 hour system, time is counted from midnight. The time from midnight to midday is written as am . while that from midday to midnight is written as pm.

In the 24 hour system, time is counted from midnight and expressed in hours.

Travel time table

Travel timetables shows the expected arrival and departure time for vehicles. Ships, aeroplanes, trains.

Example

The table below shows a timetable for a public service vehicle plying between two towns A and D via towns B and C.

Town	Arrival time	Departure time
A		8.20 A.M
B	10.40 P.M	11.00 A.M
C	2.30 P.M	2.50 P.M
D	4.00 P.M	

- What time does the vehicle leave town A?
- At what time does it arrive in town D?
- How long does it take to travel from town A to D.
- What time does the vehicle takes to travel from town C to D?

Solution

(a) 8.20 A.M

(b) 4.00 P.M

(c) Arrival time in town D was 4.00 p.m. its departure from town A was 8.20 a.m.

$$\text{Time taken} = (12.00 - 8.20 + 4 \text{ h})$$

$$= 3 \text{ h } 40 \text{ min } + 4 \text{ h}$$

$$= 7 \text{ h } 40 \text{ min}$$

(d) The vehicle arrived in town D at 4.00 p.m. it departed from town C at 2.50 p.m.

$$\text{Time taken} = 4.00 - 2.50$$

$$= 1 \text{ h } 10 \text{ min}$$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) A van travelled from Kitale to Kisumu a distance of 160km. The average speed of the van for the first 100km was 40km/h and the remaining part of the journey its average speed was 30km/h. Calculate the average speed for the whole journey. (3 mks)
- 2.) A watch which loses a half-minute every hour was set to read the correct time at 0545h on Monday. Determine the time, in the 12 hour system, the watch will show on the following Friday at 1945h.
- 3.) The timetable below shows the departure and arrival time for a bus plying between two towns **M** and **R**, 300km apart 0710982617

Town	Arrival	Departure
M		0830h
N	1000h	1020h
P	1310h	1340h
Q	1510h	1520h
R	1600h	

(a) How long does the bus take to travel from town **M** to **R**?

(b) What is the average speed for the whole journey?

CHAPTER SEVENTEEN

LINEAR EQUATIONS

Specific Objectives

By the end of the topic the learner should be able to:

- solve linear equations in one unknown
- solve simultaneous linear equations by substitution and elimination
- Linear equations in one and two unknowns.

Content

- Linear equations in one unknown
- Simultaneous linear equations
- Linear equations in one and two unknowns from given real life situations

Introduction

Linear equations are straight line equations involving one or two unknowns. In this chapter, we will deal with the formation and solving of such equations consider the following cases.

Example

Solve for the unknowns in each of the following equations

$$3x + 4 = 10$$

$$\frac{x}{3} - 2 = 4$$

$$\frac{p+5}{3} = \frac{5}{4}$$

Solution

$$3x + 4 = 10$$

$$3x + 4 - 4 = 10 - 4 \quad (\text{to make } x \text{ the subject subtract 4 on both sides})$$

$$3x = 6$$

$$X = 2$$

$$\frac{x}{3} - 2 = 4$$

$$\frac{x}{3} - 2 + 2 = 4 + 2$$

$$\frac{x}{3} = 6$$

$$X = 18$$

$$\frac{p+5}{3} = \frac{5}{4}$$

$$3 \times \left(\frac{p+5}{3}\right) = \frac{5}{4} \times 3$$

$$P + 5 = \frac{5}{4} x 3$$

$$4(p + 5) = \frac{5}{4} x 4$$

$$4p + 20 = 15$$

$$4p = -5$$

$$P = \frac{-5}{4}$$

$$= -1 \frac{1}{4}$$

Solving an equation with fractions or decimals, there is an option of clearing the fractions or decimals in order to create a simpler equation involving whole numbers.

1. To clear fractions, multiply both sides of the equation (distributing to all terms) by the LCD of all the fractions.
2. To clear decimals, multiply both sides of the equation (distributing to all terms) by the lowest power of 10 that will make all decimals whole numbers.

INCOMPLETE NOTES

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By the end of the topic the learner should be able to:

- a.) State the currencies of different countries
- b.) Convert currency from one form into another given the exchange rates
- c.) Calculate profit and loss
- d.) Express profit and loss as percentages
- e.) Calculate discount and commission
- f.) Express discount and commission as percentage.

Content

- a.) Currency
- b.) Current currency exchange rates
- c.) Currency conversion
- d.) Profit and loss
- e.) Percentage profit and loss
- f.) Discounts and commissions
- g.) Percentage discounts and commissions

Introduction

In commercial arithmetic we deal with calculations involving business transaction. The medium of any business transactions is usually called the currency. The Kenya currency consist of a basic unit called a shilling. 100 cents are equivalent to one Kenyan shillings, while a Kenyan pound is equivalent to twenty Kenya shillings.

Currency Exchange Rates

The Kenyan currency cannot be used for business transactions in other countries. To facilitate international trade, many currencies have been given different values relative to another. These are known as exchange rates.

The table below shows the exchange rates of major international currencies at the close of business on a certain day in the year 2015. The buying and selling column represents the rates at which banks buy and sell these currencies.

Note

The rates are not always fixed and they keep on changing. When changing the Kenyan currency to foreign currency, the bank sells to you. Therefore, we use the selling column rate. Conversely when changing foreign currency to Kenyan Currency, the bank buys from you, so we use the buying column rate.

Currency	Buying	Selling
DOLLAR	102.1472	102.3324
STG POUND	154.0278	154.3617
EURO	109.6072	109.8522
SA RAND	7.3332	7.3486
KES / USHS	33.0785	33.2363
KES / TSHS	20.9123	21.0481
KES / RWF	7.2313	7.3423
AE DIRHAM	27.8073	27.8653
CAN \$	77.6018	77.7661
JAPANESE YEN	84.0234	84.1964
SAUDI RIYAL	27.2284	27.2959
CHINESE YUAN	16.0778	16.1082
AUSTRALIAN \$	71.8606	72.0420

Example

Convert each of the following currencies to its stated equivalent

- a.) Us \$305 to Ksh
- b.) 530 Dirham to euro

Solution

a.) The bank buys Us 1 at Ksh 102.1472

Therefore US \$ 305 = Ksh (102.1472×305)

= Ksh 31,154.896

= Ksh 31,154.00 (To the nearest shillings)

The bank buys 1 Dirham at Ksh 27.8073

Therefore 530 Dirham = Ksh (27.8073×530)

= Ksh 11,557.00 (To the nearest shillings)

The bank sells 1 Euro at 109.8522

Therefore 530 Dirham = $11,557 / 109.8522$

= 105.170 Euros

Example

During a certain month, the exchange rates in a bank were as follows;

	Buying (Ksh.)	Selling (Ksh.)
1 US \$	91.65	91.80
1 Euro	103.75	103.93

A tourist left Kenya to the United States with Ksh.1 000,000. On the airport he exchanged all the money to dollars and spent 190 dollars on air ticket. While in US he spent 4500 dollars for upkeep and proceeded to Europe. While in Europe he spent a total of 2000 Euros. How many Euros did he remain with? (3marks)

Solution

$$\frac{1\ 000\ 000}{91.80} = 10,893.25$$

$$10,893.25 - (190 + 4500) = 6203.25$$

$$6203.25 \times 91.65 = 568,278.86$$

$$\frac{568,527.86}{103.93} = 5,470.30$$

$$5470.30 - 2000 = 3,470.30$$

Profit and Loss

The difference between the cost price and the selling price is either profit or loss. If the selling price is greater than the cost price, the difference is a profit and if the selling price is less than the total cost price, the difference is a loss.

Note

Selling price - cost price = profit

$$\text{Percentage profit} = \frac{\text{Profit}}{\text{Cost price}} \times 100$$

Cost price - selling price = loss

$$\text{Percentage loss} = \frac{\text{Profit}}{\text{Cost price}} \times 100$$

Example

Ollie bought a cow at sh 18000 and sold it at sh 21000. What percentage profit did he make?

Solution

Selling price = sh 21000

Cost price = sh 18000

Profit = sh (21000 - 18,000)

= sh 3000

$$\text{Percentage profit} = \frac{3000}{18000} \times 100$$

$$= 16 \frac{2}{3} \%$$

Example

Johnny bought a dress at 3500 and later sold it at sh. 2800. what percentage loss did he incur?

Cost price = sh 3500

Selling price = sh 2800

Loss = sh (3500 - 2800)

= Sh 700

$$\text{Percentage loss} = \frac{700}{3500} \times 100 = 20\%$$

Discount

A shopkeeper may decide to sell an article at reduced price. The difference between the marked price and the reduced price is referred to as the discount. The discount is usually expressed as a percentage of the actual price.

Example

The price of an article is marked at sh 120. A discount is allowed and the article sold at sh 96. Calculate the percentage discount.

Solution

Actual price = sh 120.00

Reduced price = sh 96.00

Discount = sh $(120.00 - 96.00)$

=sh 24

Percentage discount = $24/120 \times 100$

= sh 20%

Commission

A commission is an agreed rate of payment, usually expressed as a percentage, to an agent for his services.

Example

Mr. Neasa, a salesman in a soap industry, sold 250 pieces of toilet soap at sh 45.00 and 215 packets of detergent at sh 75.00 per packet. If he got a 5% commission on the sales, how much money did he get as commission?

Solution

Sales for the toilet soap was $250 \times 45 =$ sh 11250

Sales for the detergent was $215 \times 75 =$ sh 16125

Commission = $\frac{5}{100} (11250 + 16125)$

$$\frac{5}{100} \times 27375 = \text{sh} 1368$$

Example

A salesman earns a basic salary of sh. 9,000 per month. In addition he is also paid a commission of 5% for sales above sh. 15,000. In a certain month he sold goods worth sh. 120,000 at a discount of 2½%. Calculate his total earnings that month. {3 marks}

Solution

sales sh. 120,000

$$\text{net after discount } \frac{97.5}{100} \times 120,000 = 117,000$$

$$\text{sales above sh. } 15,000 = 117,000 - 15,000$$

$$= \text{kshs. } 102,000$$

$$\text{commission } \frac{5}{100} \times 102,000 = 5,100$$

$$\text{total earnings} = 9,000 + 5,100$$

$$= \text{kshs } 14,100$$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1. The cash prize of a television set is Kshs 25000. A customer paid a deposit of Kshs 3750. He repaid the amount owing in 24 equal monthly installments. If he was charged simple interest at the rate of 40% p.a how much was each installment?
2. Mr Ngeny borrowed Kshs 560,000 from a bank to buy a piece of land. He was required to repay the loan with simple interest for a period of 48 months. The repayment amounted to Kshs 21,000 per month.

Calculate

- (a) The interest paid to the bank
 - (b) The rate per annum of the simple interest
3. A car dealer charges 5% commission for selling a car. He received a commission of Kshs 17,500 for selling car. How much money did the owner receive from the sale of his car?
 4. A company saleslady sold goods worth Kshs 240,000 from this sale she earned a commission of Kshs 4,000
 - (a) Calculate the rate of commission
 - (b) If she sold good whose total marked price was Kshs 360,000 and allowed a discount of 2% calculate the amount of commission she received.
 5. A business woman bought two bags of maize at the same price per bag. She discovered that one bag was of high quality and the other of low quality. On the high quality bag she made a profit by selling at Kshs 1,040, whereas on the low quality bag she made a loss by selling at Kshs 880. If the profit was three times the loss, calculate the buying price per bag.
 6. A salesman gets a commission of 2. 4 % on sales up to Kshs 100,000. He gets an additional commission of 1.5% on sales above this. Calculate the commission he gets on sales worth Kshs 280,000.
 7. Three people Koris, Wangare and Hassan contributed money to start a business. Korir contributed a quarter of the total amount and Wangare two fifths of the remainder. Hassan's contribution was one and a half times that of Koris. They borrowed the rest of the money from the bank which was Kshs 60,000 less than Hassan's contribution. Find the total amount required to start the business.

8. A Kenyan tourist left Germany for Kenya through Switzerland. While in Switzerland he bought a watch worth 52 deutsche Marks. Find the value of the watch in:

- (a) Swiss Francs.
- (b) Kenya Shillings

Use the exchange rates below:

- 1 Swiss Franc = 1.28 Deutsche Marks.
- 1 Swiss Franc = 45.21 Kenya Shillings

9. A salesman earns a basic salary of Kshs. 9000 per month
In addition he is also paid a commission of 5% for sales above Kshs 15000
In a certain month he sold goods worth Kshs. 120, 000 at a discount of $2\frac{1}{2}\%$. Calculate his total earnings that month

10. In this question, mathematical table should not be used

A Kenyan bank buys and sells foreign currencies as shown below

Buying (In Kenya shillings)	Selling In Kenya Shillings
1 Hong Kong dollar	9.74
1 South African rand	12.03

A tourists arrived in Kenya with 105 000 Hong Kong dollars and changed the whole amount to Kenyan shillings. While in Kenya, she pent Kshs 403 897 and changed the balance to South African rand before leaving for South Africa. Calculate the amount, in South African rand that she received.

11. A Kenyan businessman bought goods from Japan worth 2, 950 000 Japanese yen. On arrival in Kenya custom duty of 20% was charged on the value of the goods.

If the exchange rates were as follows

1 US dollar = 118 Japanese Yen

1 US dollar = 76 Kenya shillings

Calculate the duty paid in Kenya shillings

12. Two businessmen jointly bought a minibus which could ferry 25 paying passengers when full. The fare between two towns A and B was Kshs. 80 per passenger for one way. The minibus made three round trips between the two towns daily. The cost of fuel was Kshs 1500 per day. The driver and the conductor were paid daily allowances of Kshs 200 and Kshs 150 respectively.

A further Kshs 4000 per day was set aside for maintenance.

(a) One day the minibus was full on every trip.

(i) How much money was collected from the passengers that day?

(ii) How much was the net profit?

(b) On another day, the minibus was 80% on the average for the three round trips. How much did each business get if the days profit was shared in the ratio 2:3?

13. A traveler had sterling pounds 918 with which he bought Kenya shillings at the rate of Kshs 84 per sterling pound. He did not spend the money as intended. Later, he used the Kenyan shillings to buy sterling pound at the rate of Kshs. 85 per sterling pound. Calculate the amount of money in sterling pounds lost in the whole transaction.

14. A commercial bank buys and sells Japanese Yen in Kenya shillings at the rates shown below

Buying 0.5024

Selling 0.5446

A Japanese tourist at the end of his tour of Kenya was left with Kshs. 30000 which he converted to Japanese Yen through the commercial bank. How many Japanese Yen did he get?

15. In the month of January, an insurance salesman earned Kshs. 6750 which was commission of 4.5% of the premiums paid to the company.
(a) Calculate the premium paid to the company.
(b) In February the rate of commission was reduced by $66\frac{2}{3}\%$ and the premiums reduced by 10% calculate the amount earned by the salesman in the month of February
16. Akinyi, Bundi, Cura and Diba invested some money in a business in the ratio of 7:9:10:14 respectively. The business realized a profit of Kshs 46800. They shared 12% of the profit equally and the remainder in the ratio of their contributions. Calculate the total amount of money received by Diba.
17. A telephone bill includes Kshs 4320 for a local calls Kshs 3260 for trunk calls and rental charge Kshs 2080. A value added tax (V.A.T) is then charged at 15%, Find the total bill.
18. During a certain period. The exchange rates were as follows
1 sterling pound = Kshs 102.0
1 sterling pound = 1.7 us dollar
1 U.S dollar = Kshs 60.6
A school management intended to import textbooks worth Kshs 500,000 from UK. It changed the money to sterling pounds. Later the management found out that the books the sterling pounds to dollars. Unfortunately a financial crisis arose and the money had to be converted to Kenya shillings. Calculate the total amount of money the management ended up with.
19. A fruiterer bought 144 pineapples at Kshs 100 for every six pineapples. She sold some of them at Kshs 72 for every three and the rest at Kshs 60 for every two.
If she made a 65% profit, calculate the number of pineapples sold at Kshs 72 for every three.

CHAPTER TEN

COORDINATES AND GRAPHS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Draw and label the complete Cartesian plane
- b.) Locate and plot points on the Cartesian plane
- c.) Choose and use appropriate scale for a given data
- d.) Make a table of values for a given linear relation
- e.) Use values to draw a linear graph
- f.) Solve simultaneous linear equations graphically
- g.) Draw, read and interpret graphs.

Content

- a.) Cartesian plane
- b.) Cartesian co-ordinate
- c.) Points on the Cartesian plane
- d.) Choice of appropriate scale
- e.) Table of values for a given linear relation
- f.) Linear graphs
- g.) Graphical solutions of simultaneous linear equations
- h.) Interpretation of graphs.

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CHAPTER TWENTY

ANGLES AND PLANE FIGURES

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Name and identify types of angles
- b.) Solve problems involving angles on a straight line
- c.) Solve problems involving angles at a point
- d.) Solve problems involving angles on a transversal cutting parallel lines
- e.) State angle properties of polygons
- f.) Solve problems involving angle properties of polygons
- g.) Apply the knowledge of angle properties to real life situations.

Content

- a.) Types of angles
- b.) Angles on a straight line
- c.) Angles at a point
- d.) Angles on a transversal (corresponding, alternate and allied angles)
- e.) Angle properties of polygons
- f.) Application to real life situations.

Introduction

A flat surface such as the top of a table is called a plane. The intersection of any two straight lines is a point.

Representation of points and lines on a plane

A point is represented on a plane by a mark labelled by a capital letter. Through any two given points on a plane, only one straight line can be drawn.

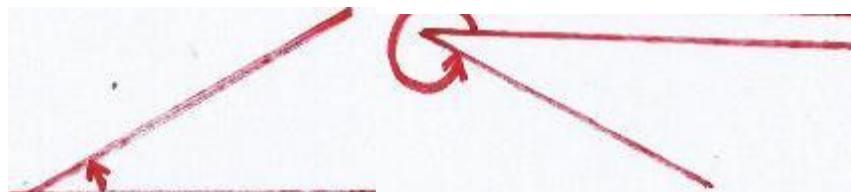


The line passes through points A and B and hence can be labelled line AB.

Types of Angles

When two lines meet, they form an angle at a point. The point where the angle is formed is called the vertex of the angle. The symbol \angle is used to denote an angle.

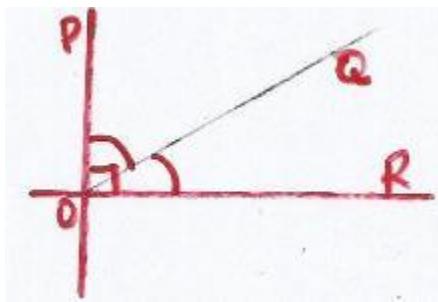
Acute angle.



Reflex angle.



Obtuse angle



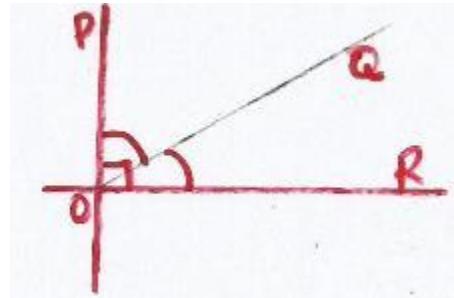
Right angle

To obtain the size of a reflex angle which cannot be read directly from a protractor ,the corresponding acute or obtuse angle is subtracted from 360° .If any two angles X and Y are such that:

i.) Angle X + angle Y = 90° , the angles are said to be complementary angles. Each angle is then said to be the complement of the other.

ii.) Angle X + angle Y = 180° , the angles are said to be supplementary angles. Each angle is then said to be the supplement of the other.

In the figure below $\angle POQ$ and $\angle ROQ$ are a pair of complementary angles.

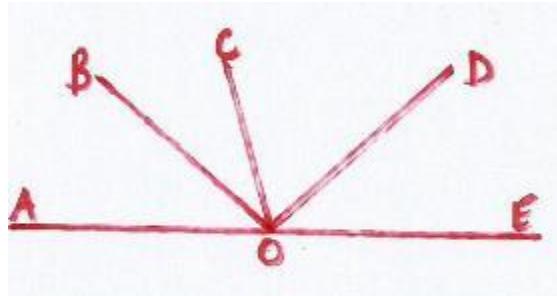


In the figure below $\angle DOF$ and $\angle FOE$ are a pair of supplementary angles.



Angles on a straight line.

The below shows a number of angles with a common vertex O. AOE is a straight line.



Two angles on either side of a straight line and having a common vertex are referred to as **adjacent angles**.

In the figure above:

$\angle AOB$ is adjacent to $\angle BOC$

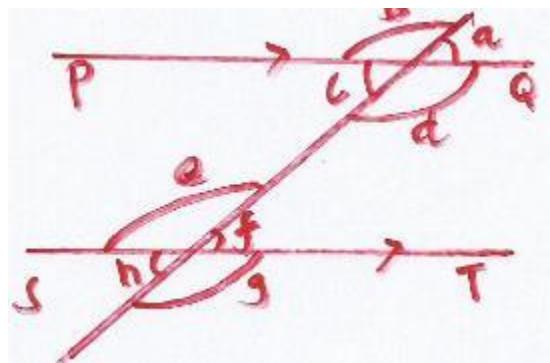
$\angle BOC$ is adjacent to $\angle COD$

$\angle COD$ is adjacent to $\angle DOE$

Angles on a straight line add up to 180° .

Angles at a point

Two intersecting straight lines form four angles having a common vertex. The angles which are on opposite sides of the vertex are called vertically opposite angles. Consider the following:



In the figure above $\angle COB$ and $\angle AOC$ are adjacent angles on a straight line. We can now show that $a = c$ as follows:

$$a + b = 180^\circ \text{ (Angles on a straight line)}$$

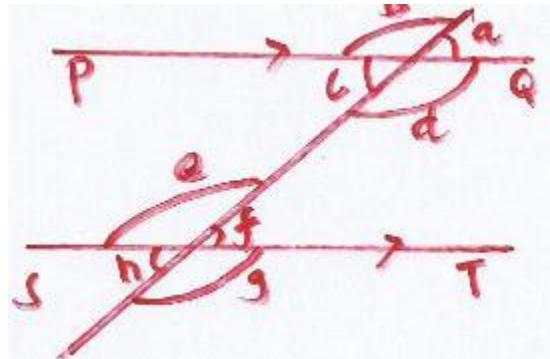
$$c + d = 180^\circ \text{ (Angles on a straight line)}$$

$$\text{So, } a + b + c + d = 180^\circ + 180^\circ = 360^\circ$$

This shows that angles at a point add up to 360°

Angles on a transversal

A transversal is a line that cuts across two parallel lines.



In the above figure PQ and ST are parallel lines and RU cuts through them. RU is a transversal.

Name:

- i.) Corresponding angles are Angles b and e, c and h, a and f, d and g.
- ii.) Alternate angles a and c, f and h, b and d, e and g.
- iii.) Co-interior or allied angles are f and d, c and e.

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CHAPTER TWENTY ONE

GEOMETRIC CONSTRUCTIONS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Use a ruler and compasses only to:
 - ✓ construct a perpendicular bisector of a line
 - ✓ construct an angle bisector
 - ✓ construct a perpendicular to a line from a given point
 - ✓ construct a perpendicular to a line through a given point on the line
 - ✓ construct angles whose values are multiples of $7\frac{1}{2}^\circ$
 - ✓ construct parallel lines
 - ✓ divide a line proportionally
- b.) Use a ruler and a set square to construct parallel lines, divide a line proportionally, and to construct perpendicular lines
- c.) Construct a regular polygon using ruler and compasses only, and ruler, compasses and protractor
- d.) Construct irregular polygons using a ruler, compasses and protractor.

Content

- a.) Construction of lines and angles using a ruler and compasses only
- b.) Construction of perpendicular and parallel lines using a ruler and a set square only
- c.) Proportional division of a line
- d.) Construction of regular polygons (up to a hexagon)
- e.) Construction of irregular polygons (up to a hexagon).

Introduction

Construction Instruments

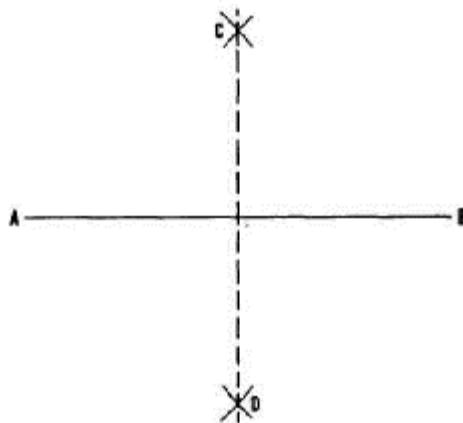
The following minimum set of instruments is required in order to construct good quality drawings:

- Two set squares.
- A protractor.
- A 15cm or 150 mm ruler
- Compass
- Protractor
- Divider
- An eraser/rubber
- Two pencils - a 2H and an HB, together with some sharpening device – Razor blade or shaper.

Construction of Perpendicular Lines

Perpendicular lines

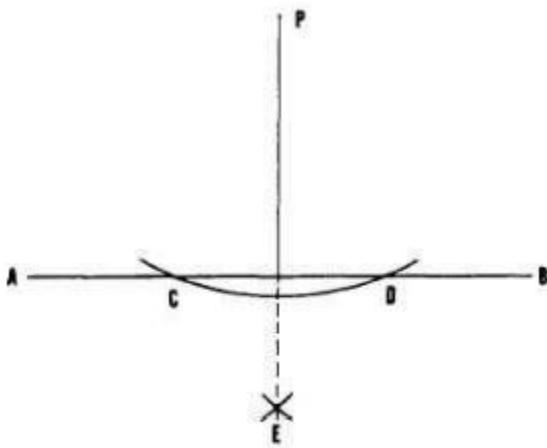
The figure below shows PQ as a perpendicular bisector of a given line AB.



To obtain the perpendicular bisector PQ

- ✓ With A and B as centre, and using the same radius, draw arcs on either side of AB to intersect at P and Q.
- ✓ Join P to Q.

The figure below shows PE, a perpendicular from a point P to a given line AB.



To construct a perpendicular line from a point

- ✓ To drop a perpendicular line from point P to AB.
- ✓ Set the compass point at P and strike an arc intersecting AB at C and D.
- ✓ With C and D as centres and any radius larger than one-half of CD,
- ✓ Strike arcs intersecting at E.
- ✓ A line from P through E is perpendicular to AB.

To construct a perpendicular line from a point

- ✓ Using P as centre and any convenient radius, draw arcs to intersect the lines at A and B.
- ✓ Using A as centre and a radius whose measure is greater than AP, draw an arc above the line.
- ✓ Using B as the centre and the same radius, draw an arc to intersect the one in (ii) at point Q.
- ✓ Using a ruler, draw PQ.

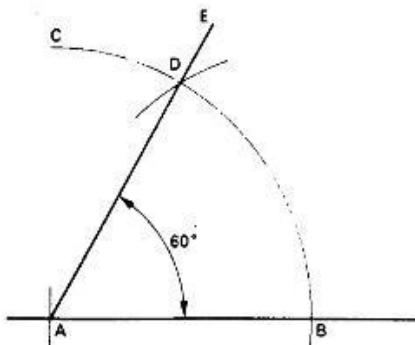
FIGUR 21.4

Construction of perpendicular lines using a set square.

Two edges of a set square are perpendicular. They can be used to draw perpendicular lines. When one of the edges is put along a line, a line drawn along the other one is perpendicular to the given line.

To construct a perpendicular from a point p to a line

- ✓ Place a ruler along the line.
- ✓ Place one of the edges of a set square which form a right angle along the ruler.
- ✓ Slide the set square along the ruler until the other edge reaches p.



- ✓ Hold the set square firmly and draw the line through P to meet the line perpendicularly.

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CHAPTER TWENTY TWO

SCALE DRAWING

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Interpret a given scale
- b.) Choose and use an appropriate scale
- c.) Draw suitable sketches from given information
- d.) State the bearing of one point from another
- e.) Locate a point using bearing and distance
- f.) Determine angles of elevation and depression
- g.) Solve problems involving bearings elevations and scale drawing
- h.) Apply scale drawing in simple surveying.

Content

- a.) Types of scales
- b.) Choice of scales
- c.) Sketching from given information and scale drawing
- d.) Bearings
- e.) Bearings, distance and locating points
- f.) Angles of elevation and depression
- g.) Problems involving bearings, scale drawing, angles of elevation and depression
- h.) Simple surveying techniques.

Introduction

The scale

The ratio of the distance on a map to the actual distance on the ground is called the scale of the map. The ratio can be in statement form e.g. 50 cm represents 50,000 cm or as a representative fraction (R.F), 1: 5,000,000 is written as $\frac{1}{5,000,000}$.

Example

The scale of a map is given in a statement as 1 cm represents 4 km. convert this to a representative fraction (R.F).

Solution

One cm represents $4 \times 100,000$ cm. 1 cm represents 400,000

Therefore, the ratio is 1: 400,000 and the R.F is $\frac{1}{400,000}$

Example

The scale of a map is given as 1:250,000. Write this as a statement.

Solution

1:250,000 means 1 cm on the map represents 250,000 cm on the ground. Therefore, 1 cm represents $\frac{250,000}{100,000}$ km.

I.e. 1 cm represents 2.5 km.

Scale Diagram

When using scale, one should be careful in choosing the right scale, so that the drawing fits on the paper without much details being left.

Bearing and Distances

Direction is always found using a compass point.



A compass has eight points as shown above. The four main points of the compass are North, South, East, and West. The other points are secondary points and they include North East (NE), South East (SE), South West (SW) and North West (NW). Each angle formed at the centre of the compass is 45° the angle between N and E is 90° .

Compass Bearing

When the direction of a place from another is given in degrees and in terms of four main points of a compass. E.g. $N45^\circ W$, then the direction is said to be given in compass bearing. Compass bearing is measured either clockwise or anticlockwise from North or south and the angle is acute.

True bearing

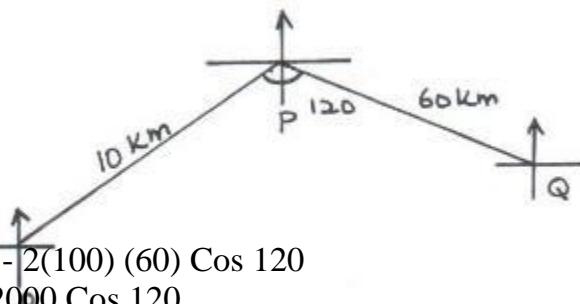
North East direction, written as $N45^\circ E$ can be given in three figures as 045° measured clockwise from True North. This three-figure bearing is called the **true bearing**.

The true bearings due north is given as 000° . Due south East as 135° and due North West as 315° .

Example

From town P, a town Q is 60km away on a bearing South 80° east. A third town R is 100km from P on the bearing South 40° west. A cyclist travelling at 20km/h leaves P for Q. He stays at Q for one hour and then continues to R. He stays at R for $1\frac{1}{2}$ hrs. and then returns directly to P.

(a) Calculate the distance of Q from R.



$$P^2 = 100^2 + 60^2 - 2(100)(60) \cos 120$$

$$P^2 = 13600 - 12000 \cos 120$$

$$P^2 = 19600$$

$$P = 140 \text{ km}$$

(b) Calculate the bearing of R from Q.

$$\frac{140}{\sin 120} = \frac{100}{\sin Q} \text{ M1}$$

$$\sin Q = \frac{100 \sin 120}{140} \text{ M1}$$

$$= 38.2^\circ \quad \text{A1}$$

$$\text{Bearing } 270 - 38.2 = 241.8$$

B1

(c) What is the time taken for the whole round trip?

$$\text{Time from P to R} = \frac{60}{20} = 3 \text{ hrs}$$

$$\text{Time from Q to R} = \frac{140}{20} = 7 \text{ hrs}$$

$$\text{From R to P} = \frac{100}{20} = 5 \text{ hrs}$$

$$\begin{aligned} \text{Taken travelling} &= 3 + 7 + 5 \\ &= 15 \text{ hrs} \end{aligned}$$

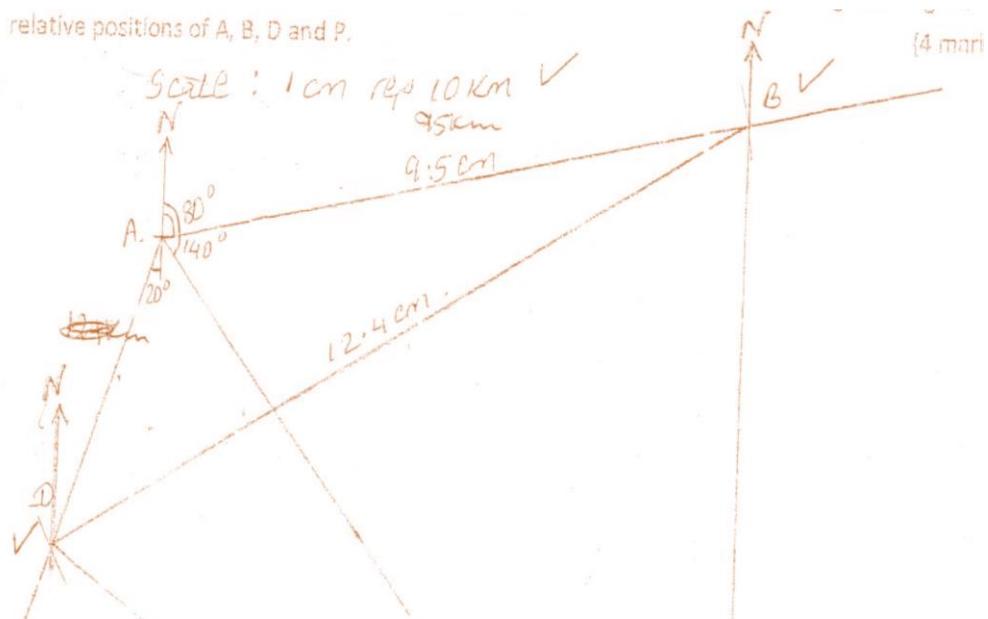
M1 ✓

B1 for all three correct

Example

A port B is on a bearing of 080° from a port A and a distance of 95 km. A Submarine is stationed at a port D, which is on a bearing of 200° from A, and a distance of 124 km from B. A ship leaves B and moves directly Southwards to an Island P, which is on a bearing of 140° from A. The Submarine at D on realizing that the ship was heading to the Island P, decides to head straight for the Island to intercept the ship. Using a scale of 1 cm to represent 10 km, make a scale drawing showing the relative positions of A, B, D and P. {4 marks}

relative positions of A, B, D and P.



Hence find:

b) The distance from A to D.

{2 marks}

$$4.6 \pm 0.1 \times 10 = 46 \text{ KM} \pm 1 \text{ KM}$$

c) The bearing of the Submarine from the ship when the ship was setting off from B. {1 mark}

$$240^\circ \pm 1^\circ \text{ OR } S 60^\circ W \pm 2^\circ$$

d) The bearing of the Island P from D.

{1 mark}

$$122^\circ \pm \text{ OR } S 58^\circ E \pm 1^\circ$$

e) The distance the Submarine had to cover to reach the Island

$$P127 \pm 0.1 \times 10 =$$

$127 \pm 1 \text{ KM}$ {2 marks}

INCOMPLETE NOTES

This Forms a Sample
From The Original Notes

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For F1-F4 All Subjects Complete Notes

CHAPTER TWENTY THREE

COMMON SOLIDS

Specific Objectives

By the end of the topic the learner should be able to:

- Identify and sketch common solids
- Identify vertices, edges and faces of common solids
- State the geometric properties of common solids
- Draw nets of solids accurately
- Make models of solids from nets
- Calculate surface area of solids from nets

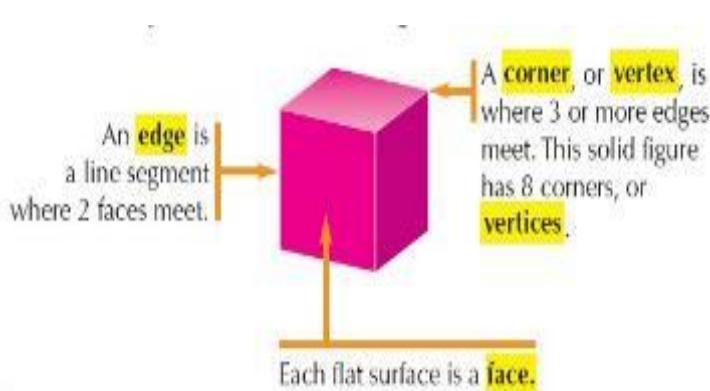
Content

- Common solids (cubes, cuboids, pyramids, prisms, cones, spheres, cylinders etc)
- Vertices, edges and faces of common solids.
- Geometric properties of common solids.
- Nets of solids.
- Models of solids from nets.
- Surface area of solids from nets (include cubes, cuboids, cones, pyramids prisms)

Introduction

A solid is an object which occupies space and has a definite or fixed shape. Solids are either regular or irregular.

Shape	Characteristics	Real Life Examples
Sphere	no faces, edges or corners; completely round	  
Cylinder	2 circular bases connected by a curved surface	  
Cube	6 square faces, 12 edges and 8 corners; all sides equal	  
Cone	round base with a curved surface that forms a point	  
Rectangular Prism	6 faces with opposite faces being equal, 12 edges and 8 corners	 
Pyramid	square base and 4 triangular faces, 8 edges and 5 corners	 



Note:

- ✓ Intersections of faces are called edges.
- ✓ The point where three or more edges meet is called a vertex.

Sketching solids

To draw a reasonable sketch of a solid on a plan paper, the following ideas are helpful:

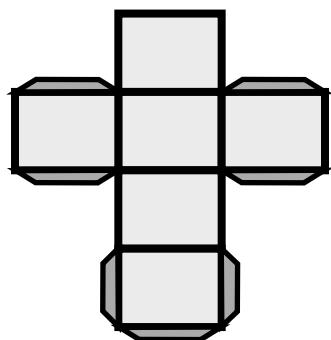
Use of isometric projections

In this method the following points should be obtained:

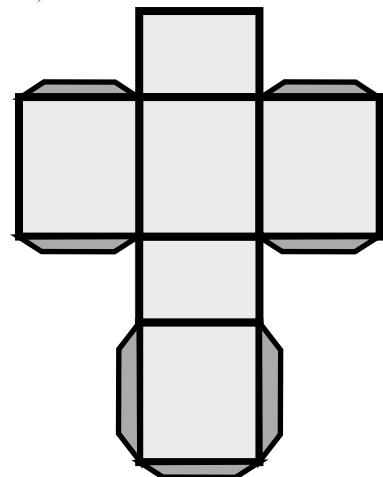
- ✓ Each edge should be drawn to the correct length.
- ✓ All rectangular faces must be drawn as parallelograms.
- ✓ Horizontal and vertical edges must be drawn accurately to scale.
- ✓ The base edges are drawn at an angle 30° with the horizontal lines.
- ✓ Parallel lines are drawn parallel.

Examples

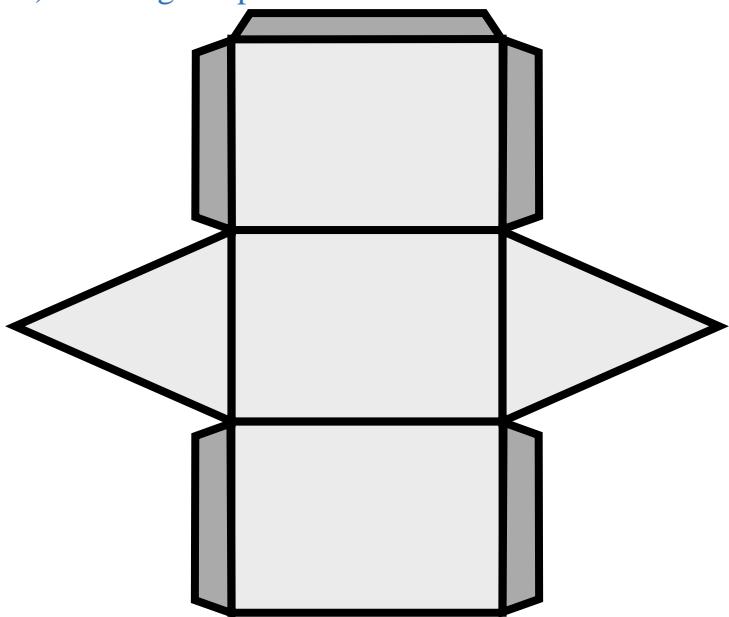
a.) Cube net



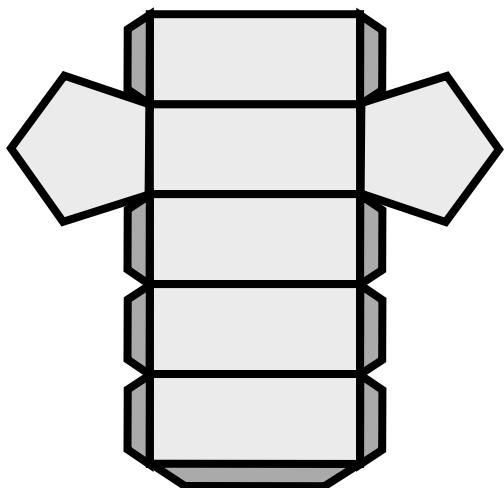
b.) Cuboid net



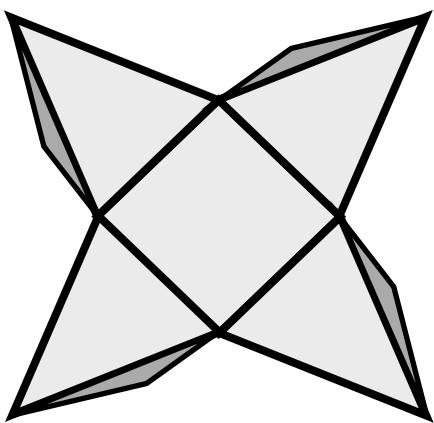
c.) Triangular prism net



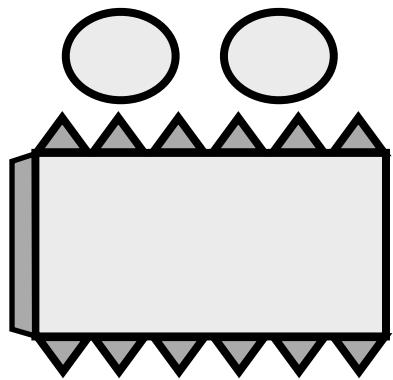
d.) Pentagonal prism



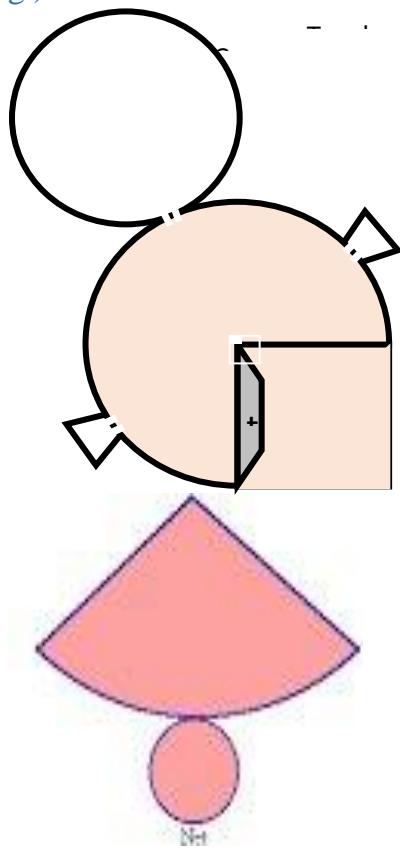
e.) Square base pyramid



f.) Cylinder net

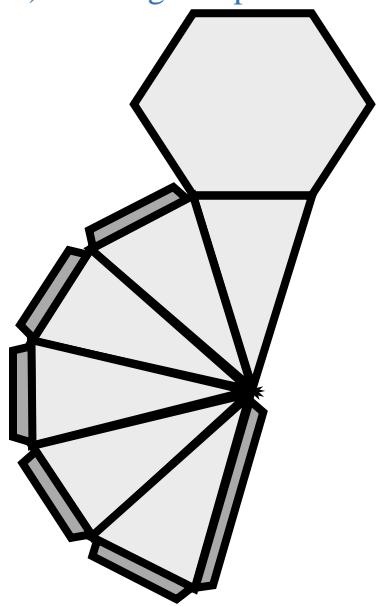


g.) Cone net

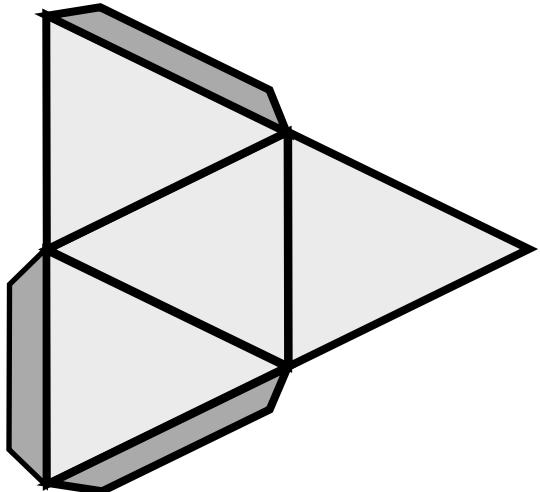


Cone net

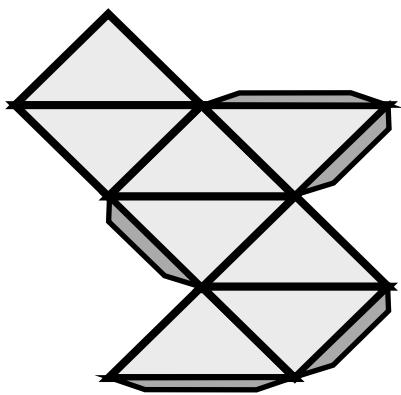
h.) Hexagonal prism



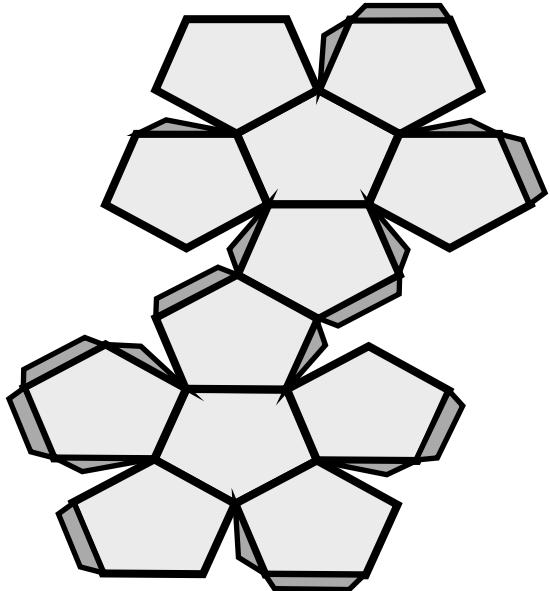
i.) Tetrahedron



j.) Octahedron



k.) Dodecagon



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