



Computer Science

## 34<sup>th</sup> Annual High School Programming Contest

Sponsored by **transfinder**

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### Gold Problem #7: Postage Stamps

Background Information: Suppose you can purchase a total of  $n$  postage stamps, but can only have them in two distinct integer denominations,  $a_1$  and  $a_2$ . What is the highest postage amount,  $h$ , such that you can represent every positive integer amount 1 through  $h$  using a total of at most  $n$  stamps of denominations  $a_1$  and  $a_2$ ? Well, it definitely depends on which values you choose for  $a_1$  and  $a_2$ !

Your program will take as input the value  $n$ , and it will output the highest number  $h$ , such that the optimal choices for stamp values  $a_1$  and  $a_2$  will produce combinations of at most  $n$  stamps that add up to all integers on the interval  $[1, h]$ . You will also output the stamp values  $a_1$  and  $a_2$ , where  $a_1 < a_2$ , which can be used to produce those postage values on the interval  $[1, h]$ .

### Programming Problem:

Input: The maximum number of stamps that can be used,  $n \leq 75$ .

Output: The highest number,  $h$ , such that each total of stamp values  $[1, h]$  can be produced. The stamp values  $a_1$  and  $a_2$ , both integers are also outputted on the next line.

Example 1:    Input:        1  
                 Output:     2  
                              1 2

Example 2:    Input:        3  
                 Output:     7  
                              1 3

Example 3:    Input:        5  
                 Output:    14  
                              1 4

Example 4:    Input:        7  
                 Output:    23  
                              1 5