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22002809

CS 202 Section 1

HW4

Question 1

a) Insert 2

(2)

Insert 20

(2 20)

Insert 6

(6)
(2) (20)

Insert 16

(6)
(2) (16 20)

Insert 10

(6 16)
(2) (10) (20)

Delete 2

(16)
(6 10) (20)

Insert 12

(10 16)
(6) (12) (20)

Insert 14

(10 16)
(6) (12 14) (20)

Insert 8

(10 16)
(6 8) (12 14) (20)

Delete 16

(10 14)
(6 8) (12) (20)

Insert 18

(10 14)
(6 8) (12) (18 20)

Insert 3

(10)
(6) (14)
(3) (8) (12) (18 20)

Delete 6

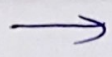
(10 14)
(3 8) (12) (18 20)

Delete 14

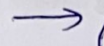
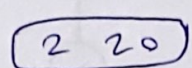
(10 18)
(3 8) (12) (20)

b)

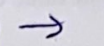
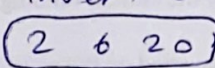
Insert 2



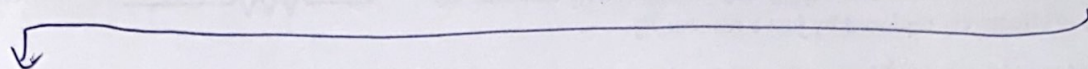
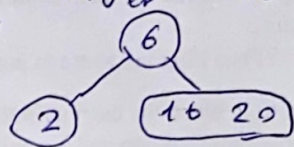
Insert 20



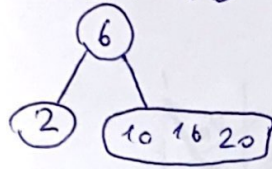
Insert 6



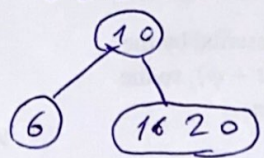
Insert 16



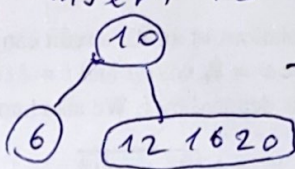
Insert 10



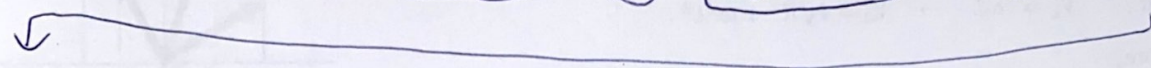
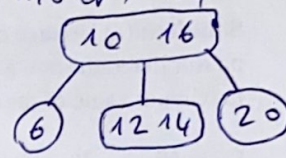
Delete 2



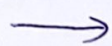
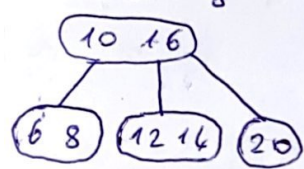
Insert 12



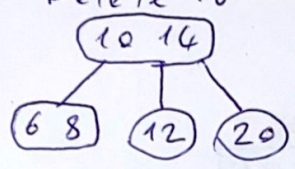
Insert 14



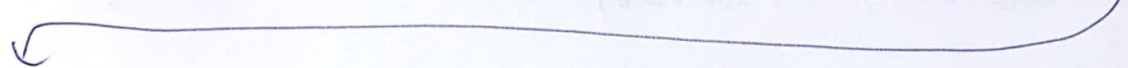
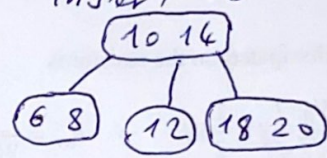
Insert 8



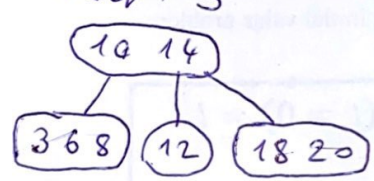
Delete 16



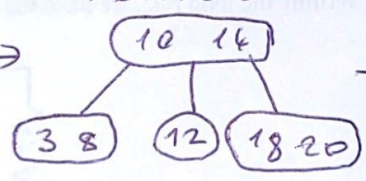
Insert 18



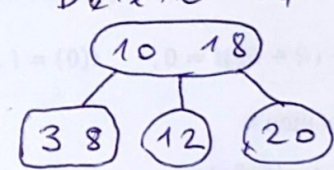
Insert 3



Delete 6



Delete 14



Question 2

a)

26		54		17	69	45	58	32	60			64
0	1	2	3	4	5	6	7	8	9	10	11	12

$$45 \bmod 13 = 6$$

$$64 \bmod 13 = 12$$

$$54 \bmod 13 = 2$$

$$17 \bmod 13 = 4$$

$$69 \bmod 13 = 4 \rightarrow 4 + 1 = 5$$

$$58 \bmod 13 = 6 \rightarrow 6 + 1 \rightarrow 6 + 2 = 8$$

$$60 \bmod 13 = 8 \rightarrow 8 + 1 = 9$$

$$26 \bmod 13 = 0$$

Average number of probes for successful search = $\frac{1}{2} \left(1 + \frac{1}{1 - \frac{9}{13}} \right) = 2.125$

Unsuccessful search = $\frac{1}{2} \left(1 + \frac{1}{1 - \left(\frac{9}{13} \right)^2} \right) = 5.78$

b)

26		54		17	69	45	58	60		32		64
0	1	2	3	4	5	6	7	8	9	10	11	12

$$45 \bmod 13 = 6$$

$$64 \bmod 13 = 12$$

$$54 \bmod 13 = 2$$

$$17 \bmod 13 = 4$$

$$69 \bmod 13 = 4 \rightarrow 4 + 1^2 = 5$$

$$58 \bmod 13 = 6 \rightarrow 6 + 1^2 = 7$$

$$32 \bmod 13 = 6 \rightarrow 6 + 1^2 \rightarrow 6 + 2^2 = 10$$

$$60 \bmod 13 = 8$$

$$26 \bmod 13 = 0$$

Average number of probes for successful search = $\frac{-\ln \left(1 - \frac{9}{13} \right)}{9/13} = 1.7$

unsuccessful search = $\frac{1}{1 - \frac{9}{13}} = 3.25$

c) 0 → 26

1

2 → 54

3

4 → 17 → 69

5

6 → 45 → 58 → 32

7

8 → 60

9

10

11

12 → 64

Average number of probes for

$$\text{Successful search} = 1 + \frac{9/13}{2} = \underline{1.34}$$

$$\text{Unsuccessful search} = \frac{9}{13} = \underline{0.69}$$

Question 3

For this part, I implemented a weighted undirected graph. In the graph, I have an array of linked lists every one of which stores the airport number and the duration of the flight from the corresponding airport.

Insert Operation

I add new nodes at the start of each list so it takes $O(1)$ time to insert. I do the insertion twice (for each direction) and show information about new flight. There is no worst case for the operation.

List operation

List operation grows linearly depending on the number of flights from the airport. Algorithm goes through all nodes in the list so it takes $O(N)$ time. Worst case is when all the flights are from that specific airport. Then we would have iterations as the number of all flights.

Shortest path operation

I created parallel arrays to store the distance, visited vertices and resulting strings. Time complexity of the algorithm is $O(N^2)$ because we check for new paths for each unvisited vertex.

Minimize costs operation

For this operation I used a min heap to store the flights starting from the first. To find the minimum spanning tree, I added the flight with least duration to the new graph. Heap operation takes $O(\log N)$ time and since I do it for all vertices worst case time complexity is $O(N \log N)$.