

Exploiting macauff cross-matches with two new Rubin software packages: birnam and banquo

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University of Exeter

LSST@Europe6 – In-Kind Contributions, 17/Sep/24



Science and
Technology
Facilities Council



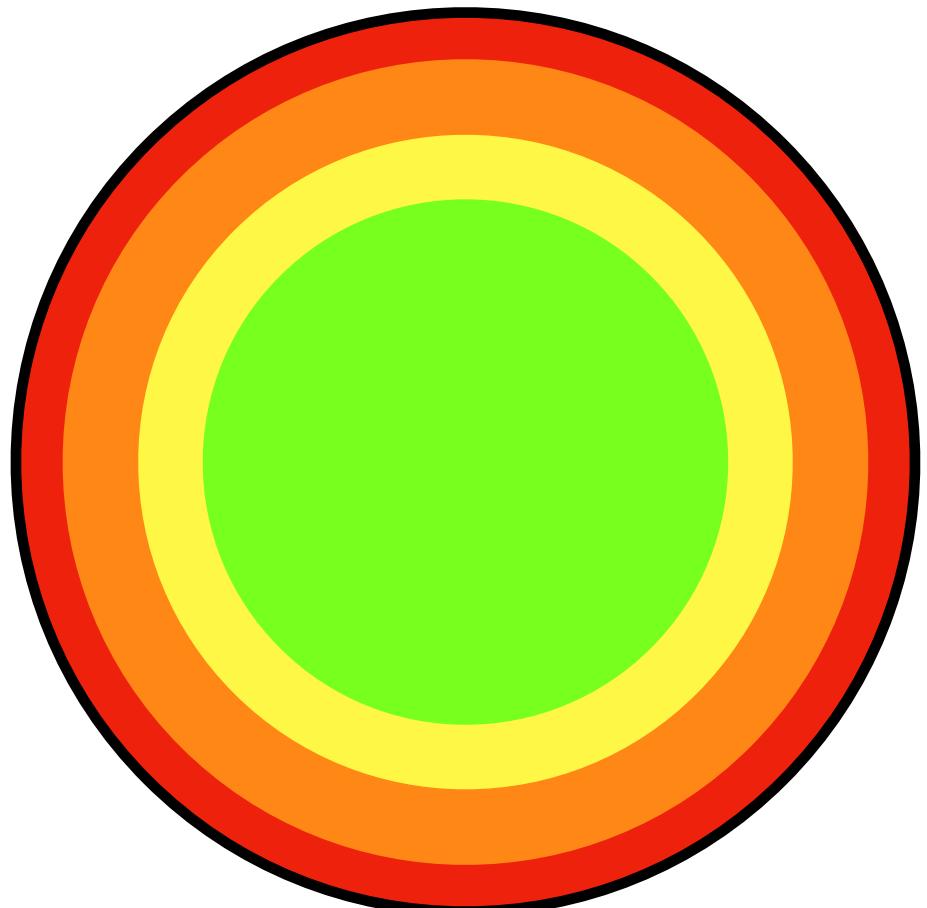
University
of Exeter



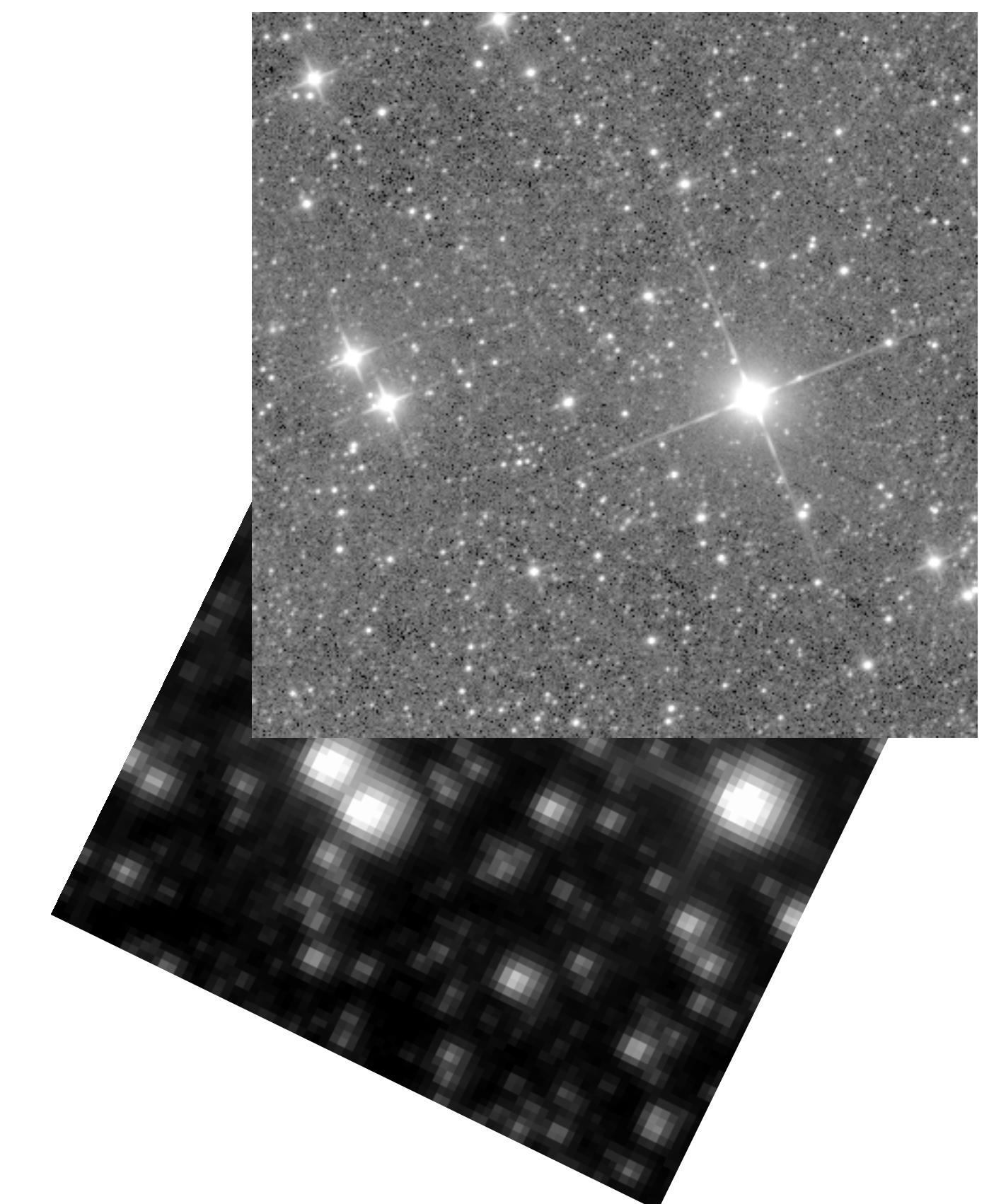
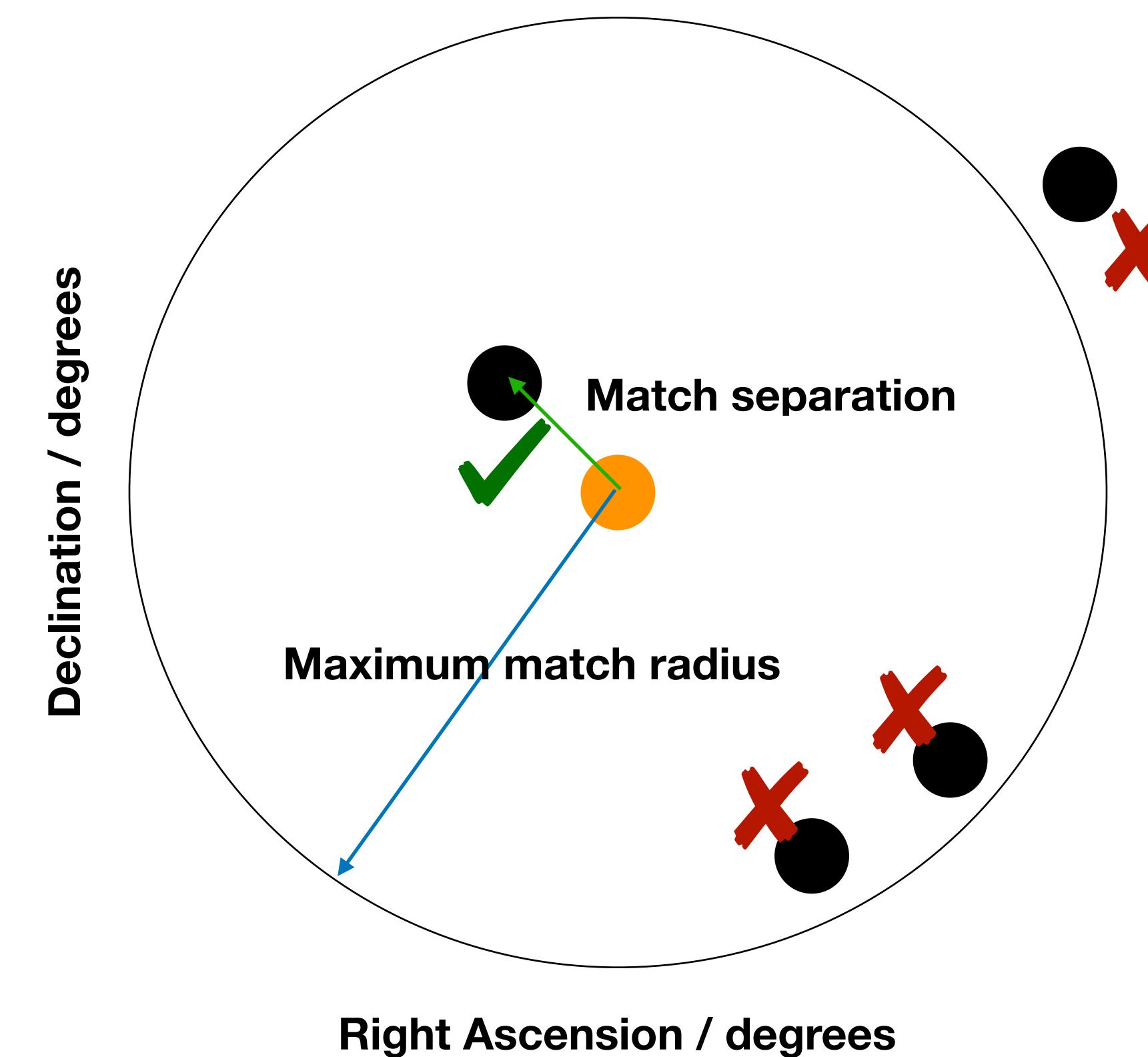
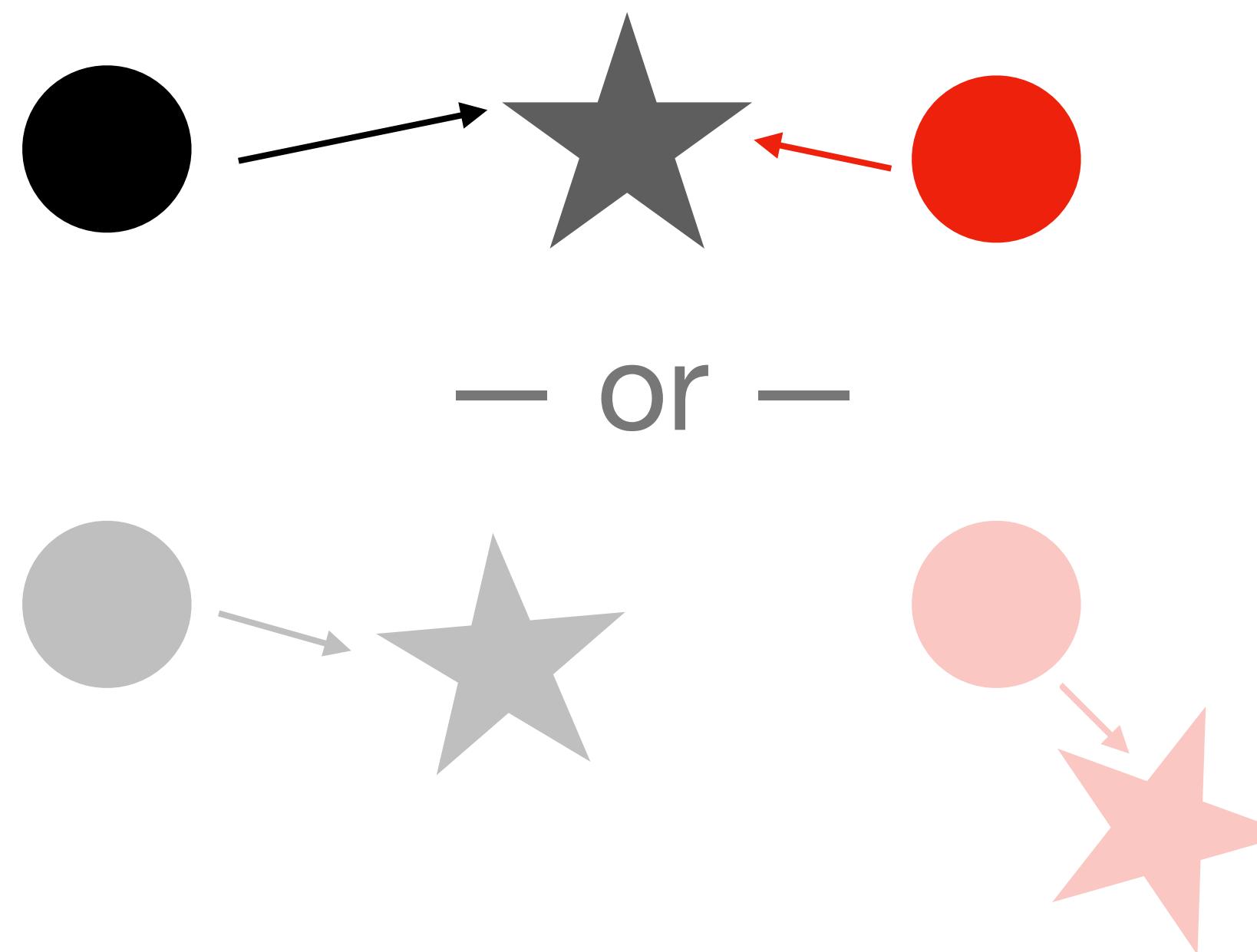
@Onoddil @pm.me
.github.io [@onoddil.com](https://www.onoddil.com)

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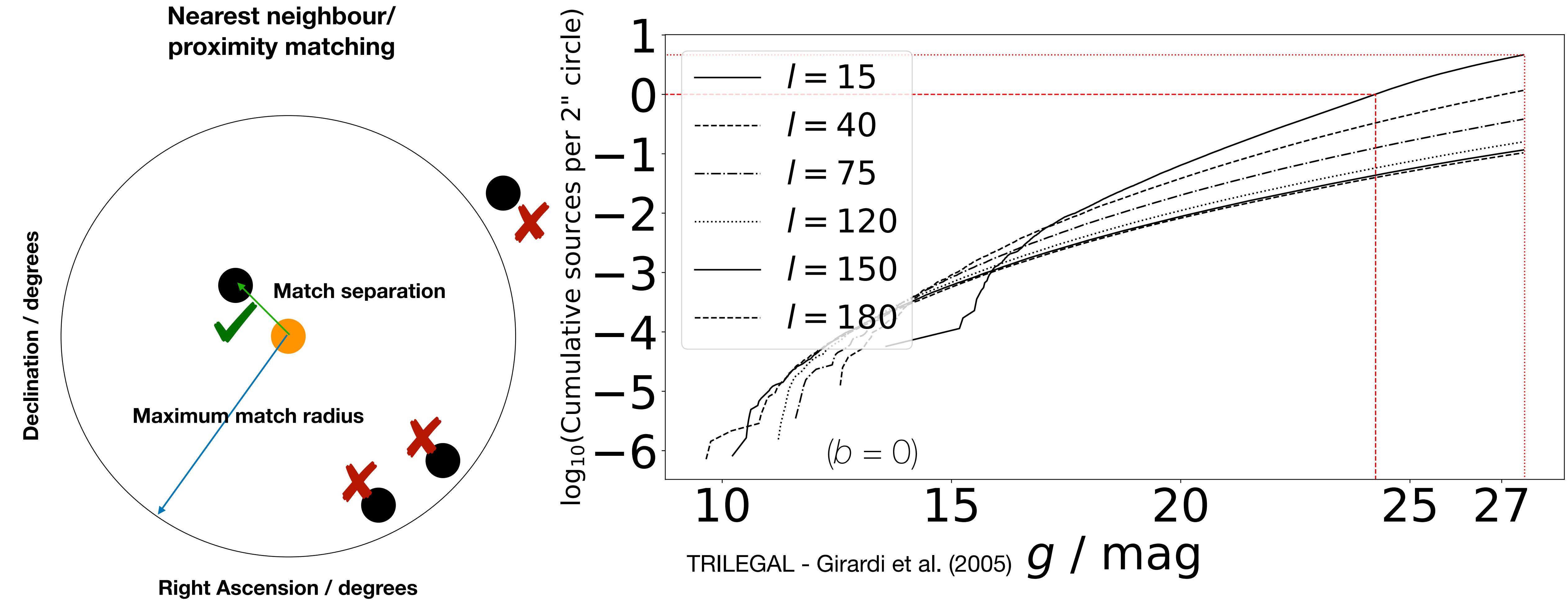
Cross-Match Science, Methodology, Background



“Simple” Cross-Matching



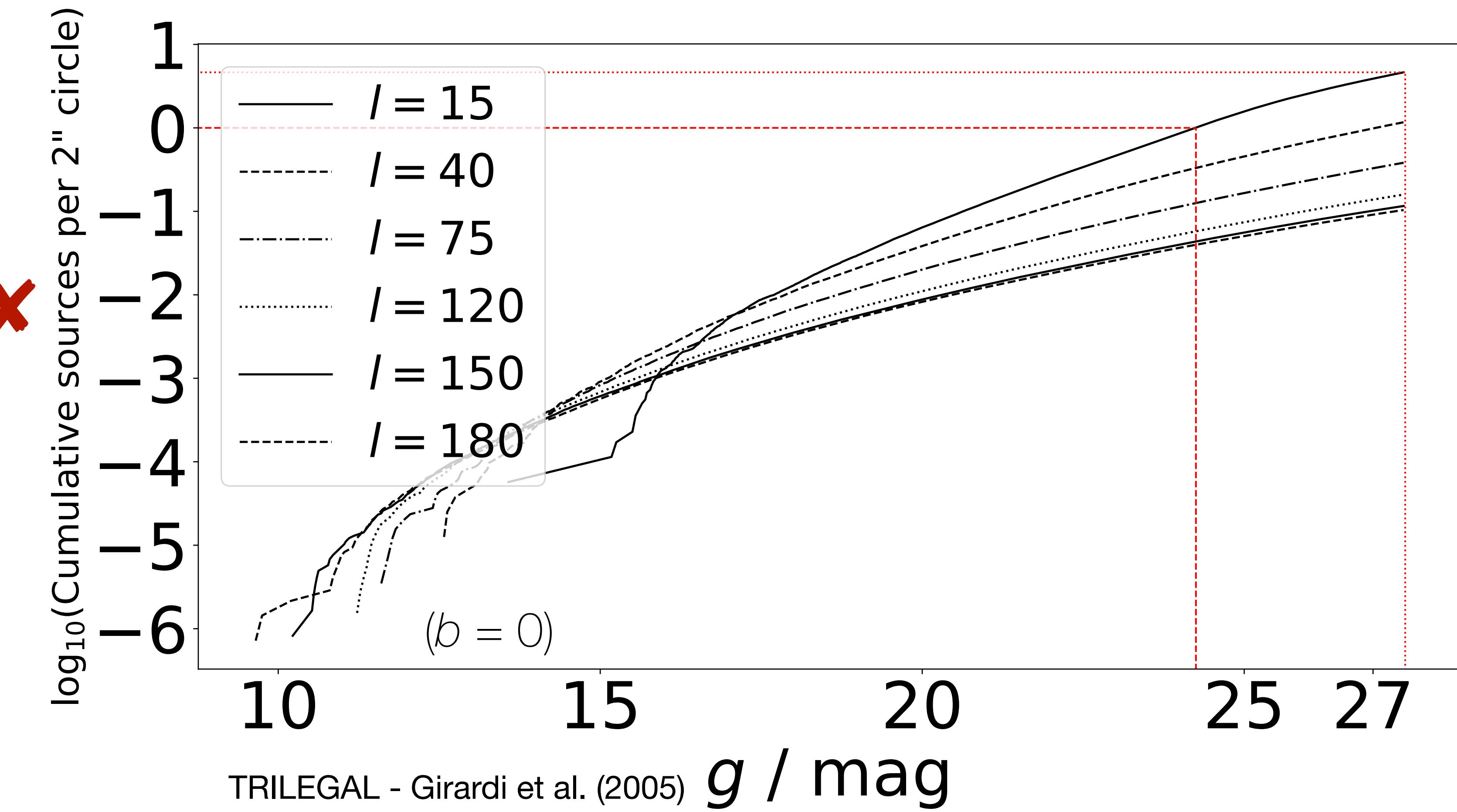
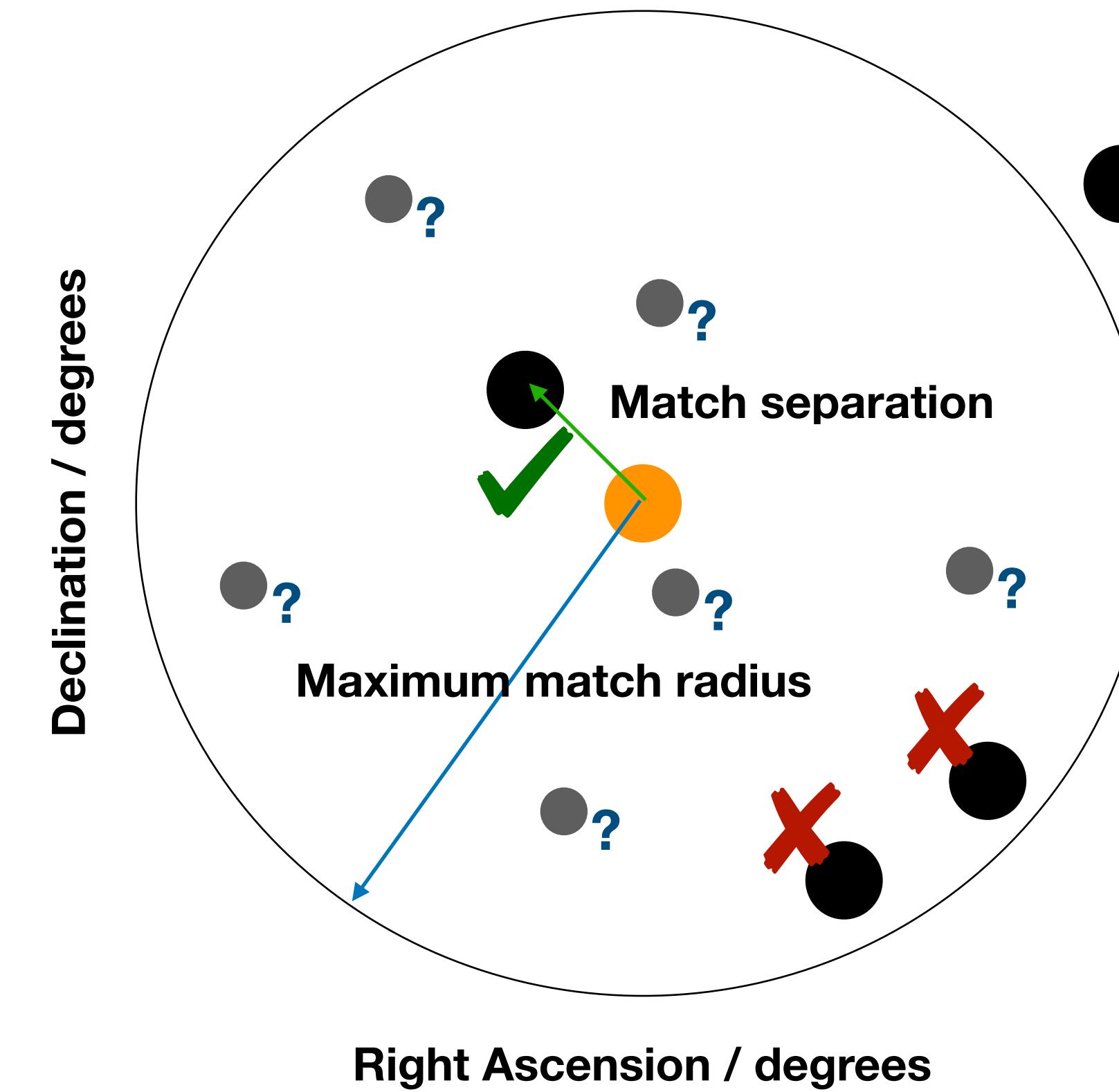
The Problem With LSST



The Problem With LSST

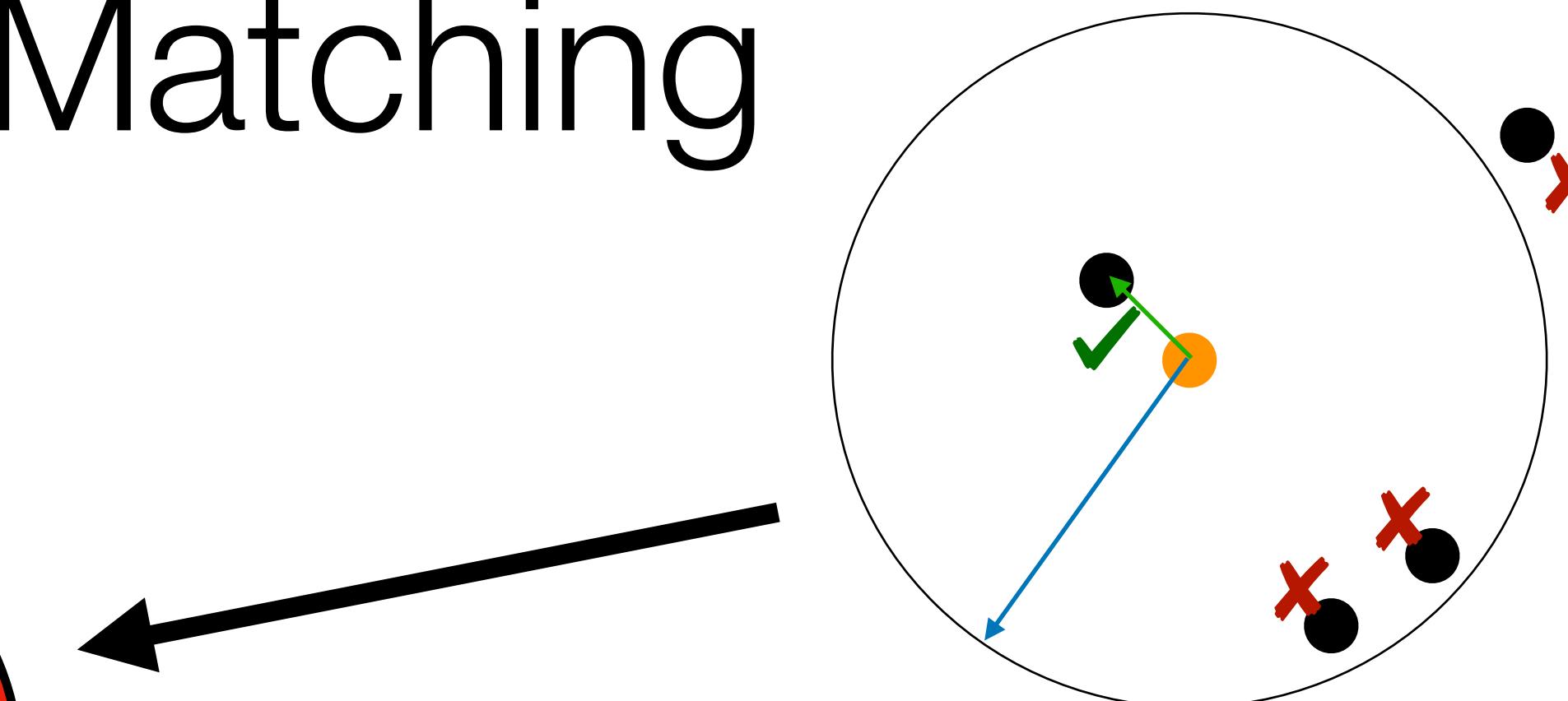
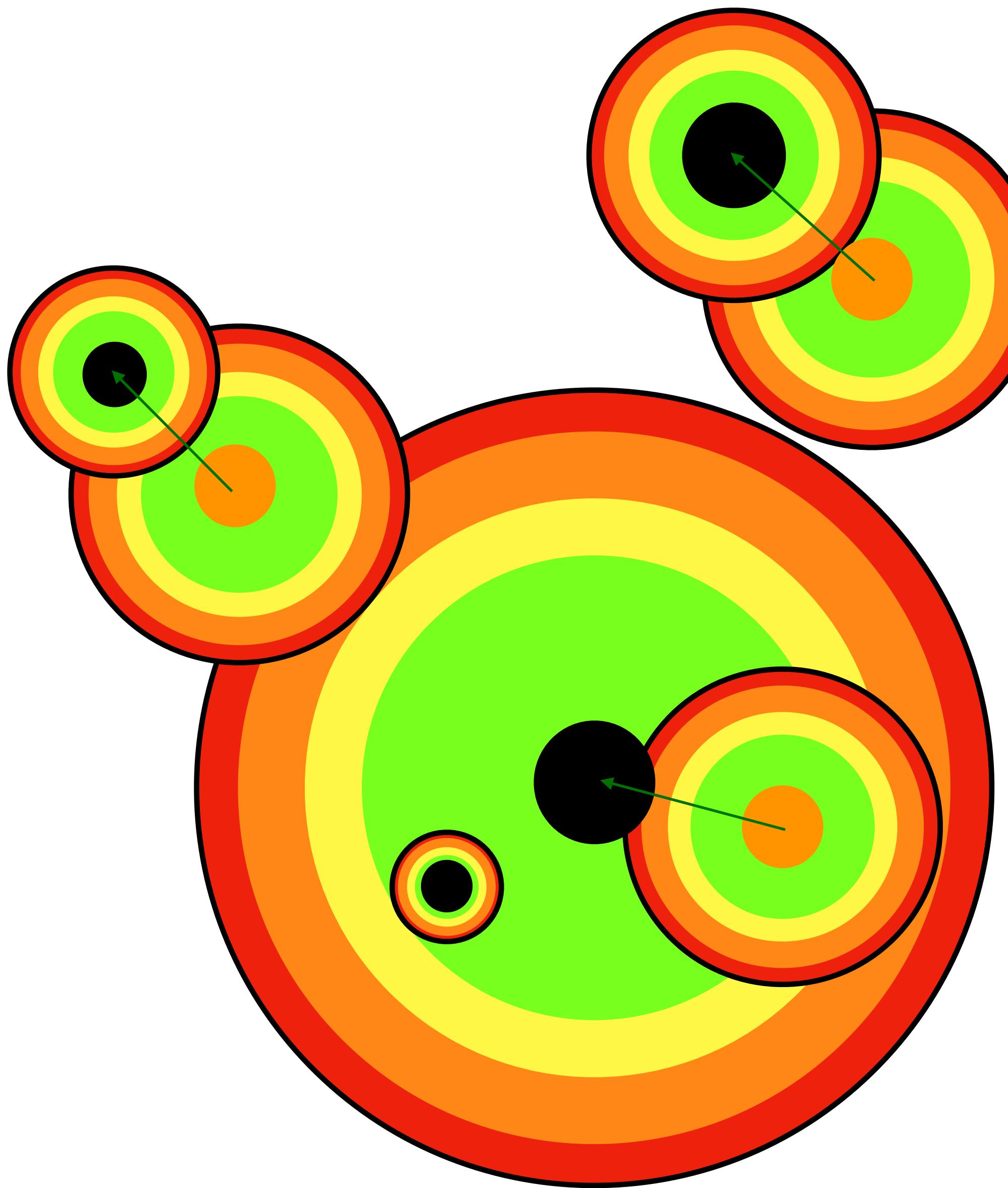
(It's still a few randomly placed objects in every match radius at high Galactic latitudes)

Nearest neighbour/
proximity matching



Nearest-neighbour matching *will not* work in the era of Rubin!

Probabilistic Cross-Matching



Probability of two sources having their on-sky separation given the hypothesis they are counterparts

$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$

Probability of sources having their brightnesses given they are unrelated to one another (“field stars”)

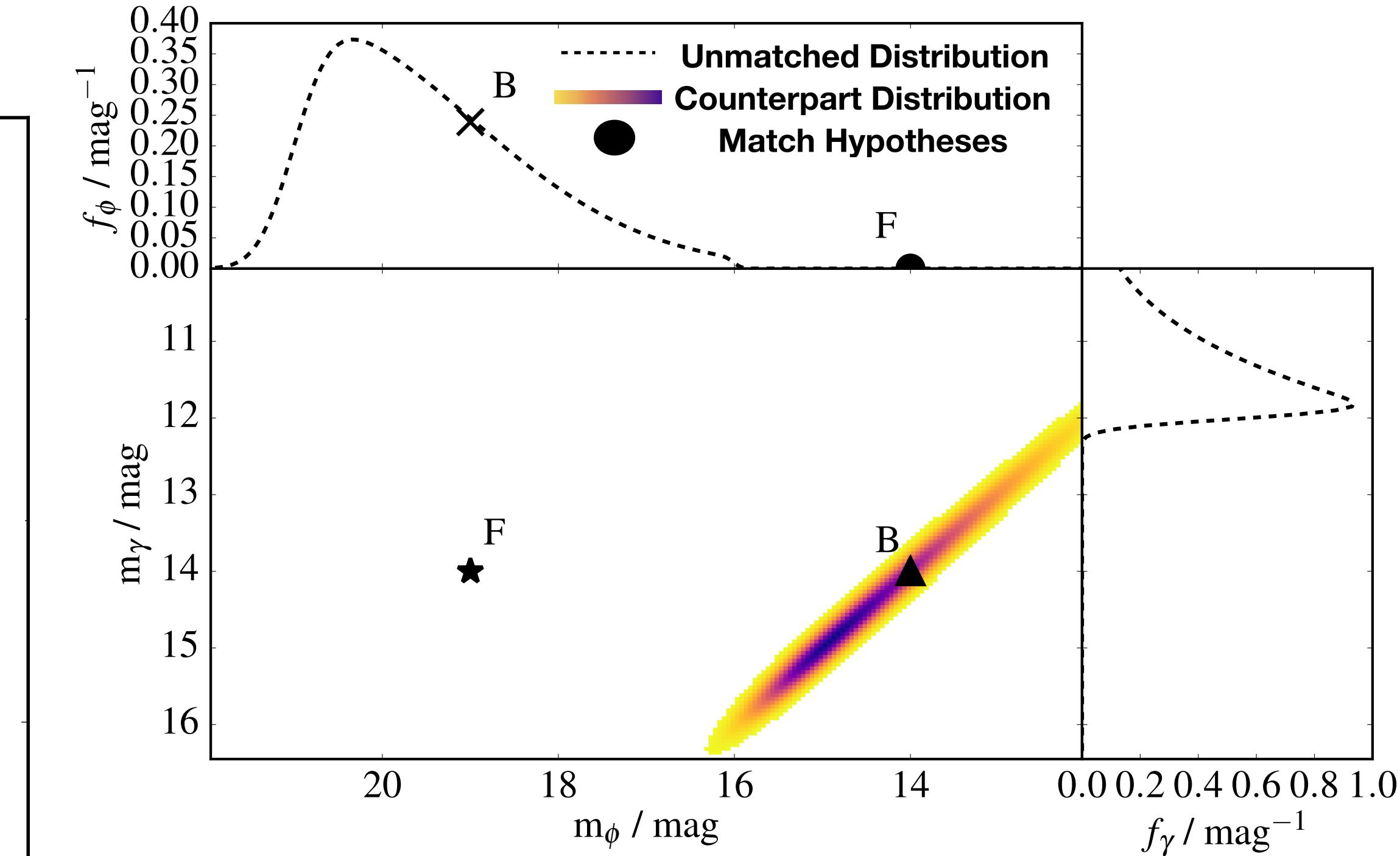
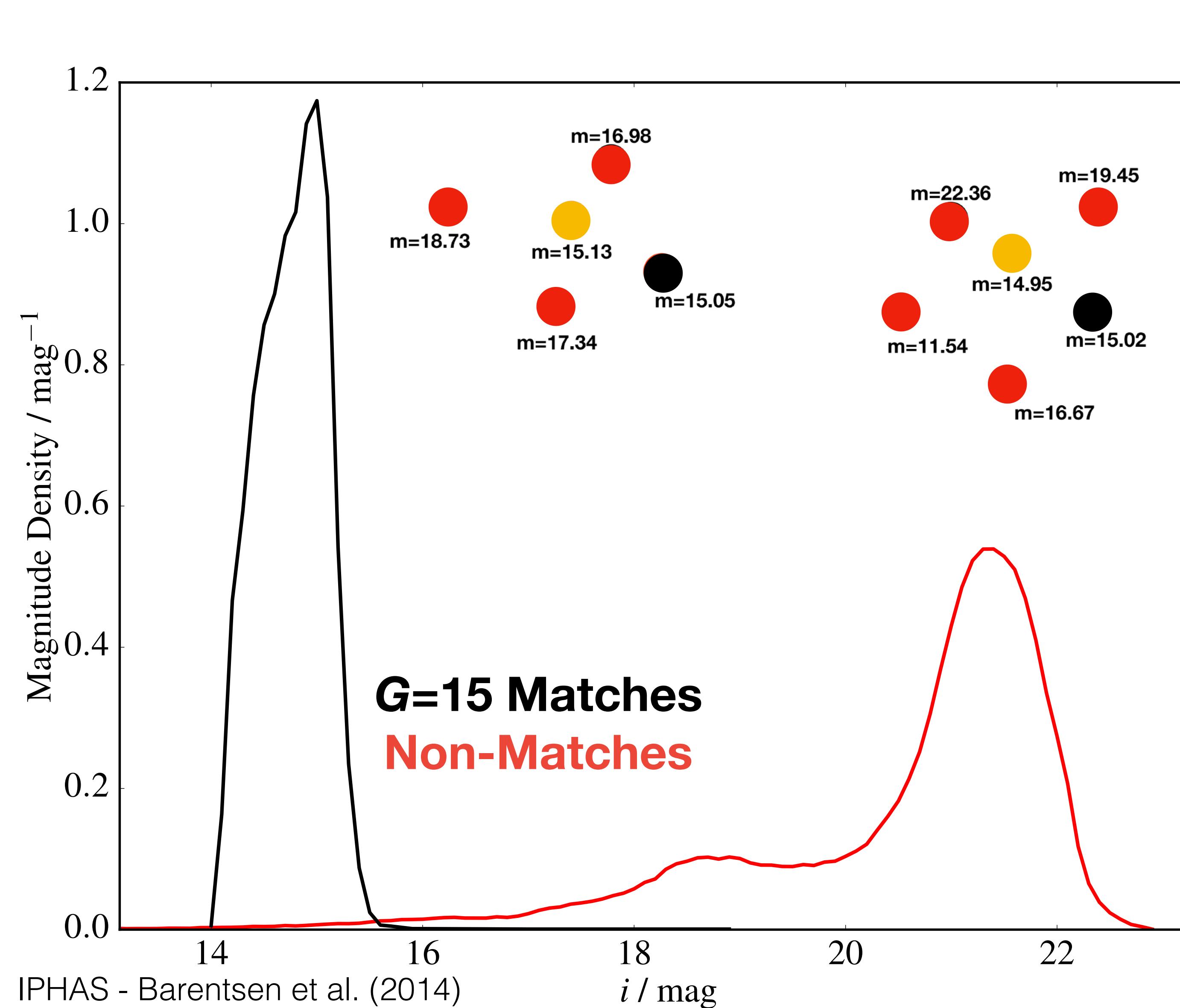
Probability of sources having their brightnesses given they are counterparts

Wilson & Naylor (2018a)

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Photometry: Rejecting False Positives

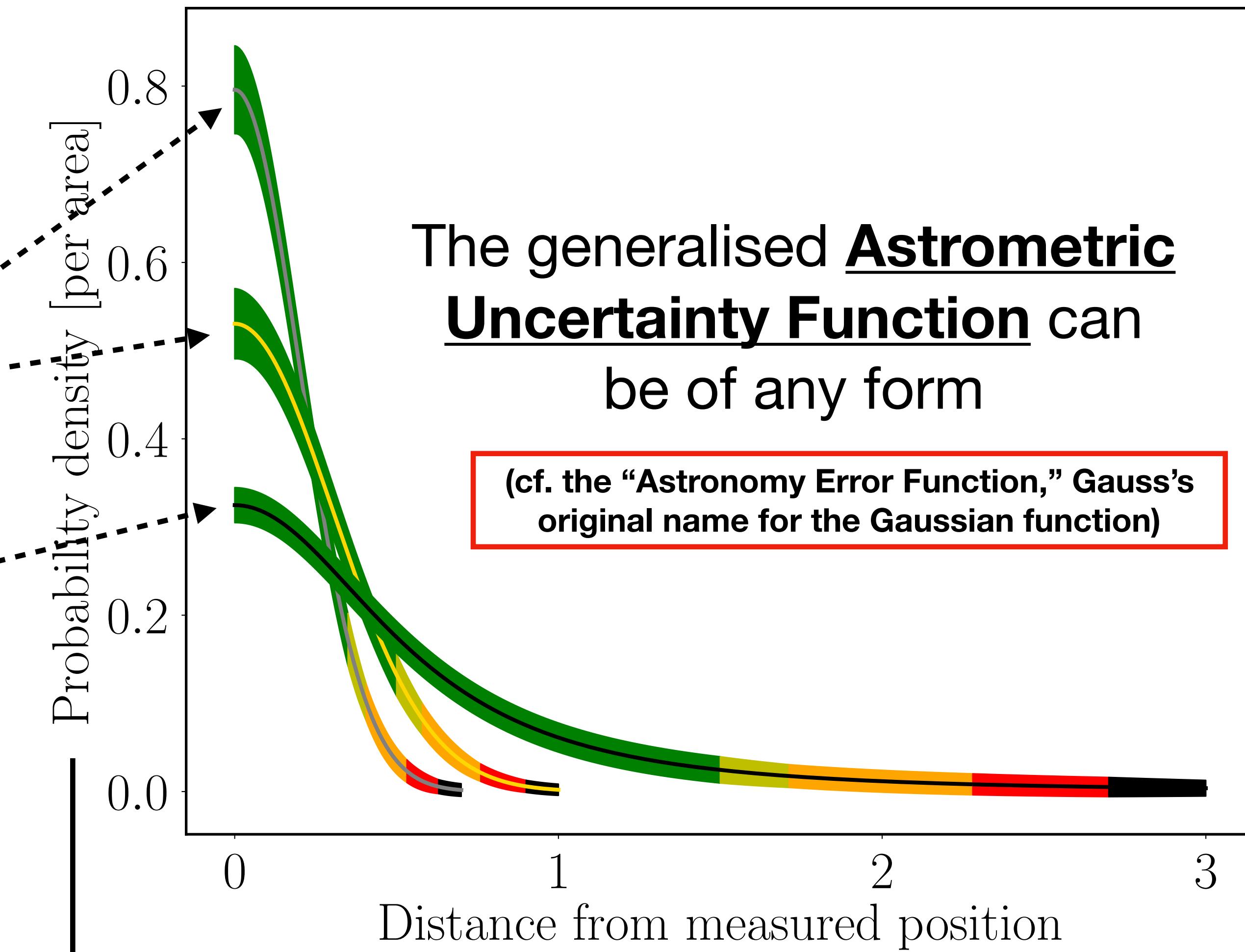
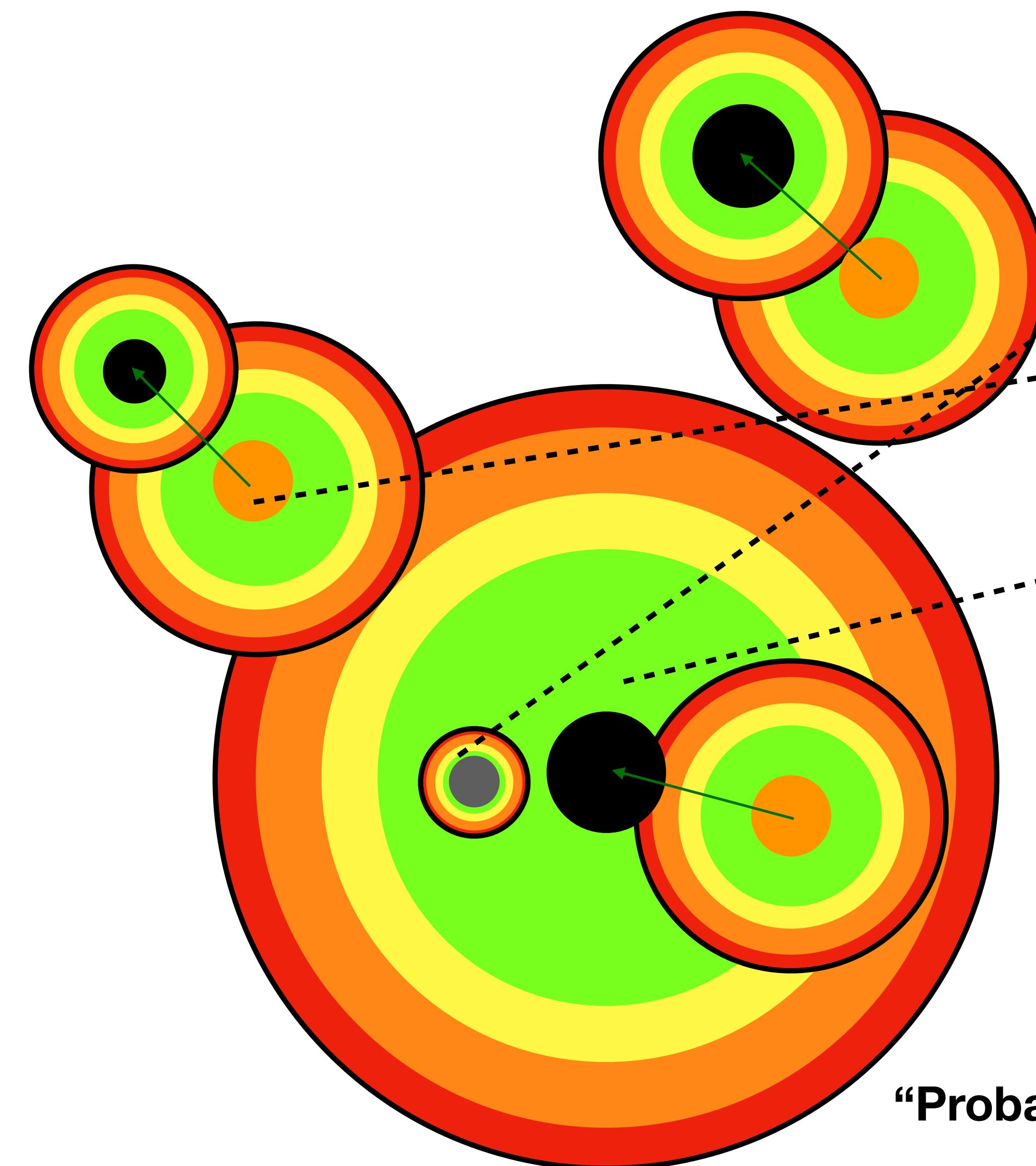
$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$



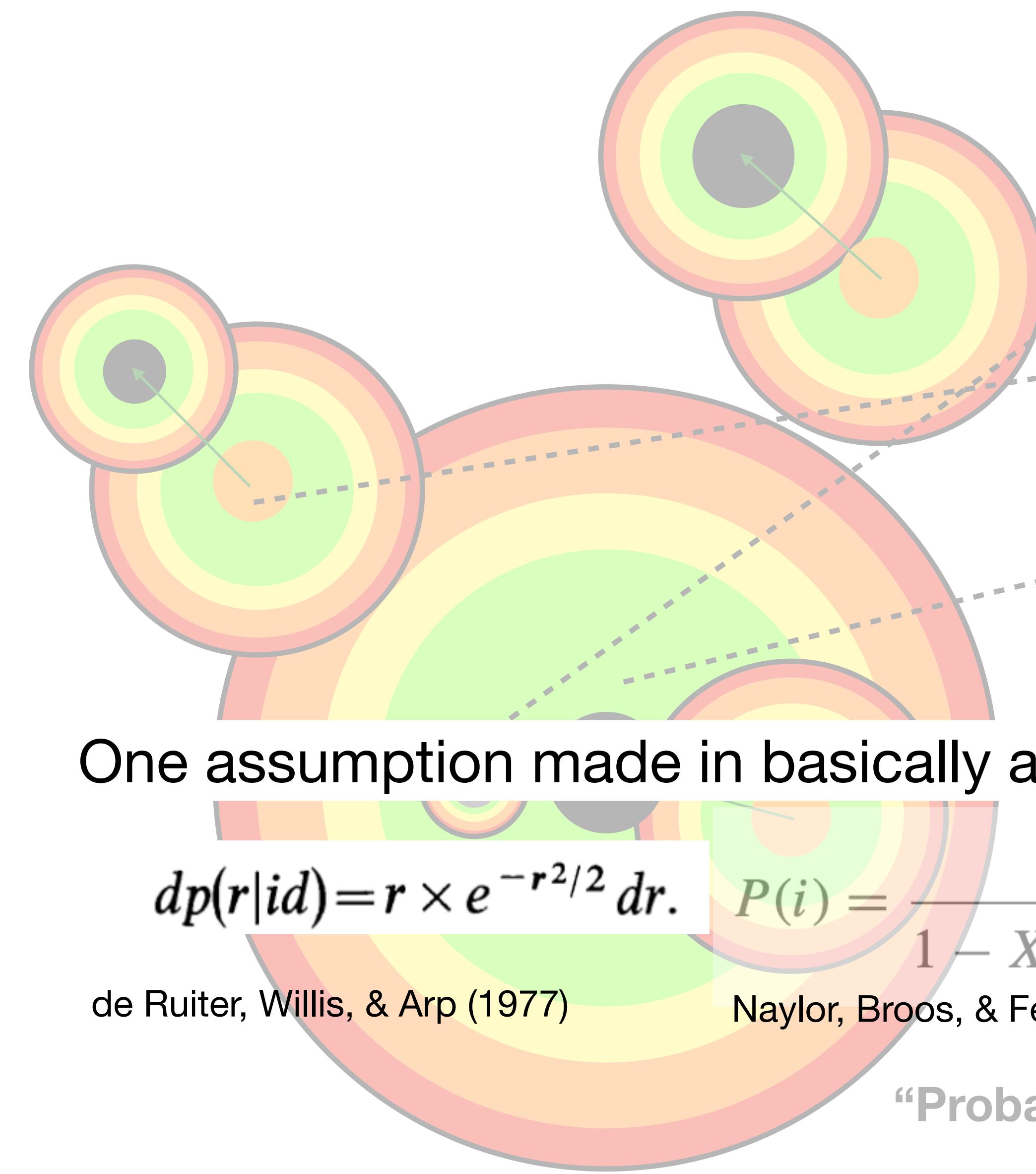
Wilson & Naylor (2018a)

The photometry-based likelihoods (c and f) allow us to mitigate high false positive rate in crowded fields, but now we need the position-based likelihood G

Probabilistic Cross-Matching: the AUF



Probabilistic Cross-Matching: the AUF



One assumption made in basically all literature: positional errors of sources are Gaussian!

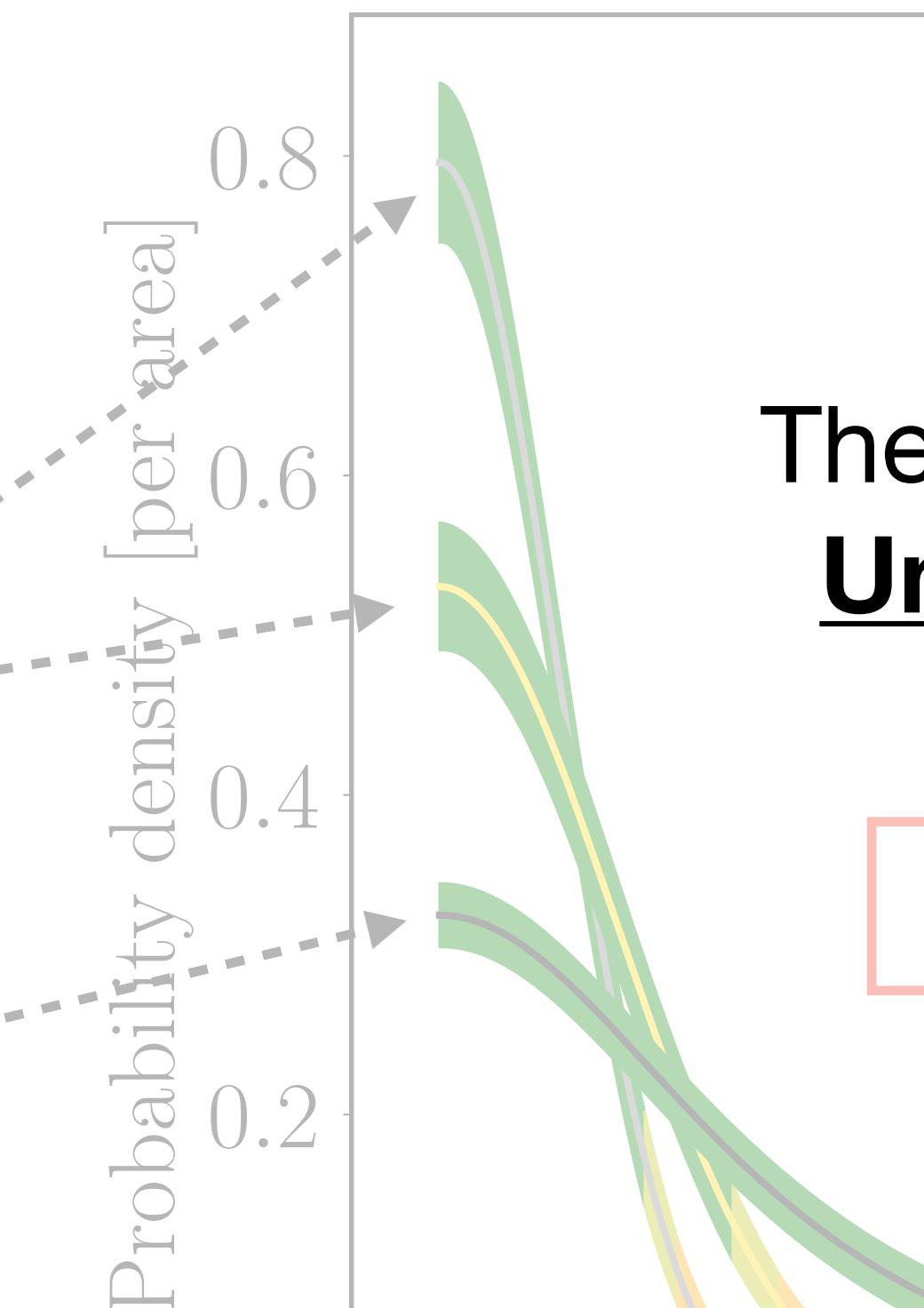
$$dp(r|id) = r \times e^{-r^2/2} dr.$$

de Ruiter, Willis, & Arp (1977)

$$P(i) = \frac{\frac{Xc(m_i) g(\Delta x_i, \Delta y_i)}{Nf(m_i)}}{1 - X + \sum_j \frac{Xc(m_j) g(\Delta x_j, \Delta y_j)}{Nf(m_j)}}$$

Naylor, Broos, & Feigelson (2013)

“Probability of True Position being this far from the Measured Position”



The generalised Astrometric Uncertainty Function can be of any form

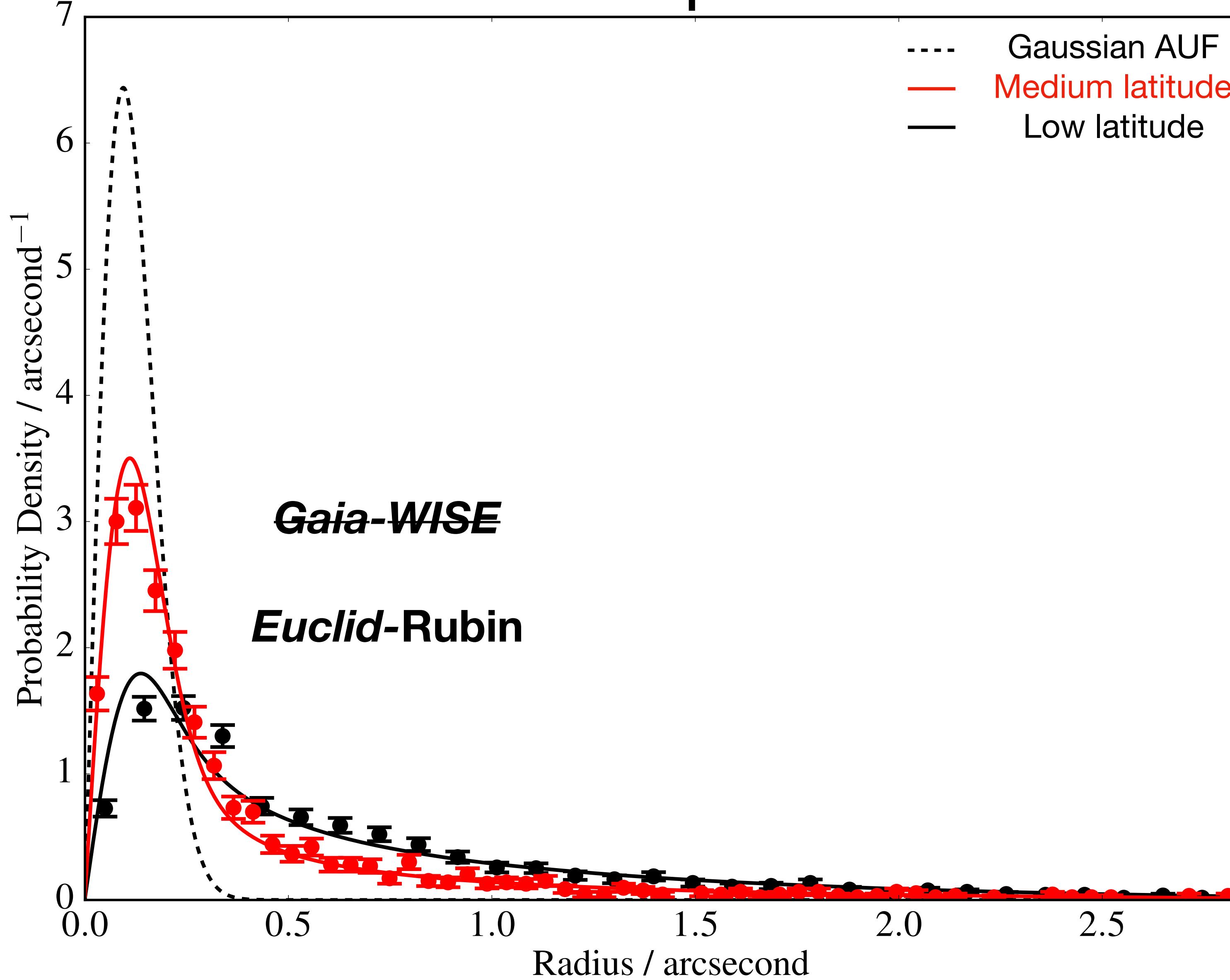
(cf. the “Astronomy Error Function,” Gauss’s original name for the Gaussian function)

$$p(D|H) = \int p(m|H) \prod_{i=1}^n p_i(x_i|m, H) d^3m$$

Budavári & Szalay (2008)

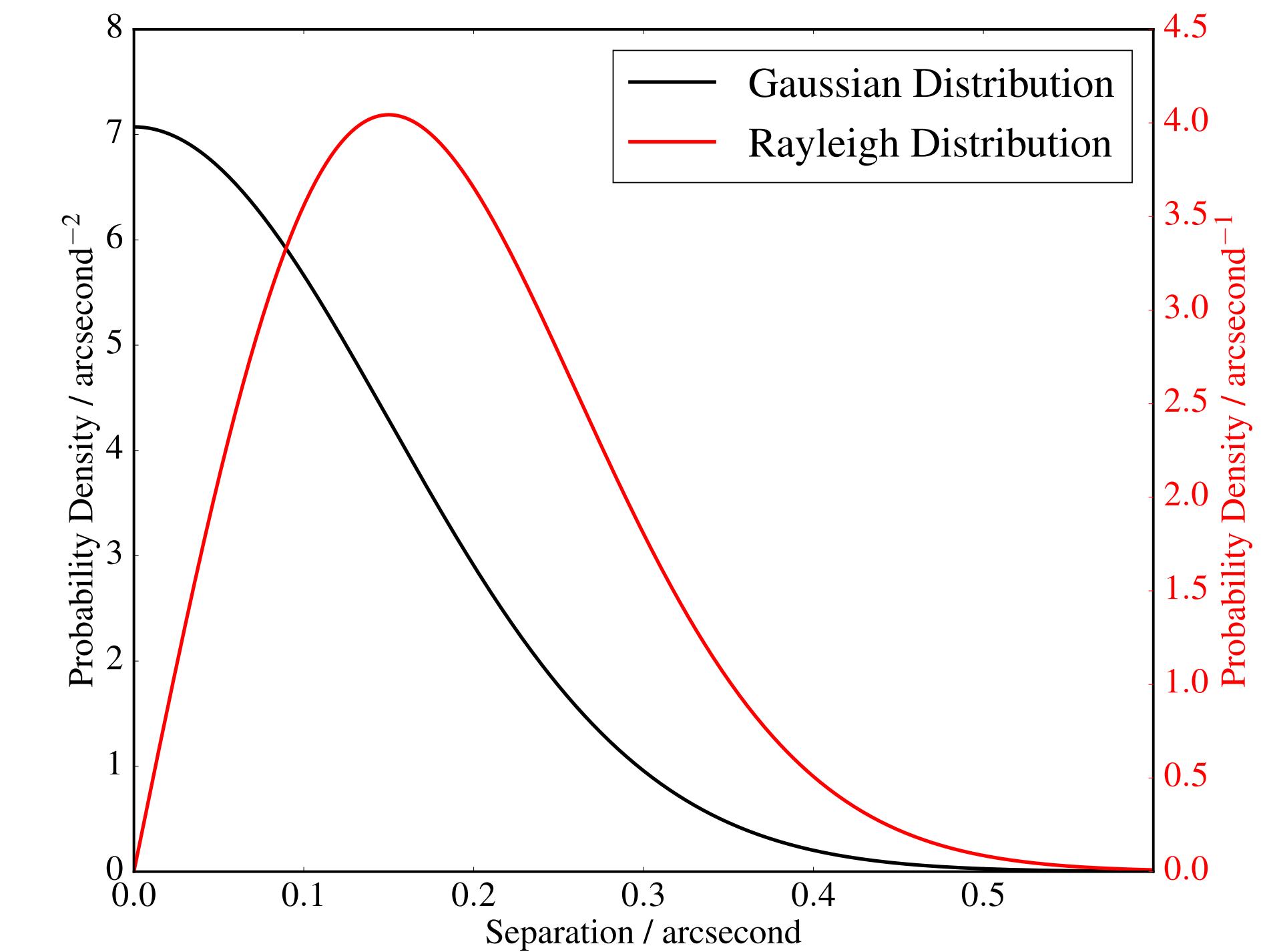
Additional Components of the AUF

$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$



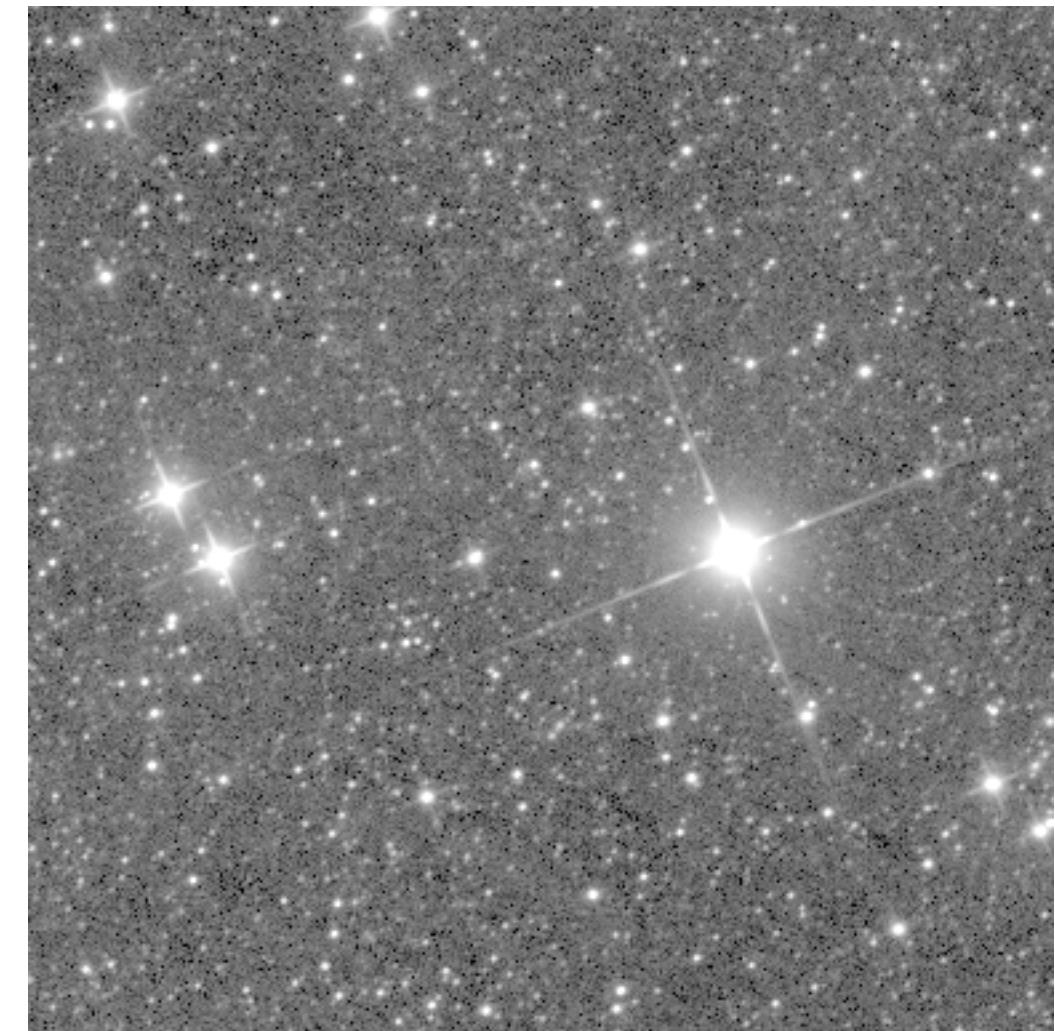
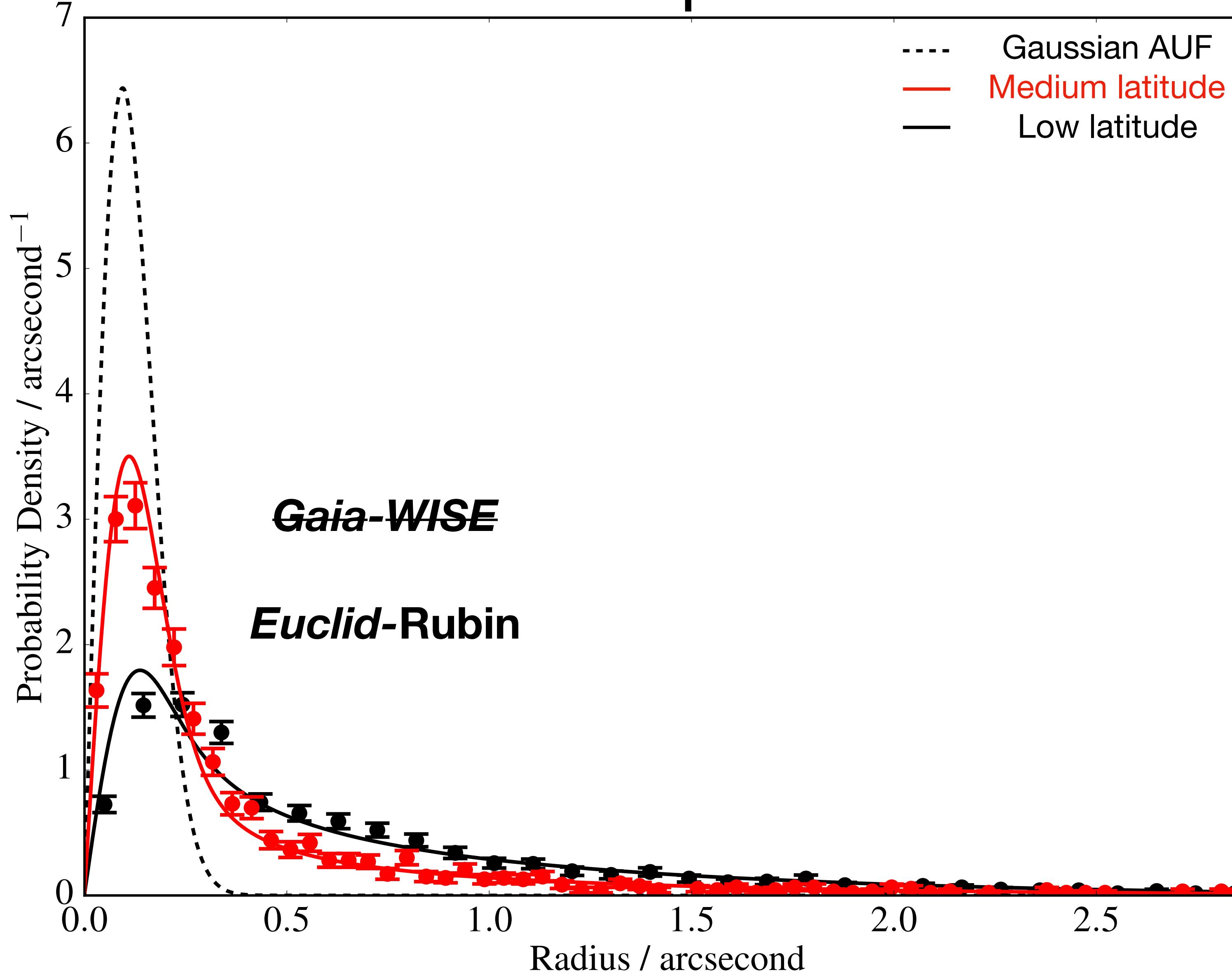
$$g(x, y, \sigma) = (2\pi\sigma^2)^{-1} \exp\left(-\frac{1}{2}\frac{x^2 + y^2}{\sigma^2}\right)$$

$$g(r, \sigma) = \frac{r}{\sigma^2} \exp\left(-\frac{1}{2}\frac{r^2}{\sigma^2}\right)$$



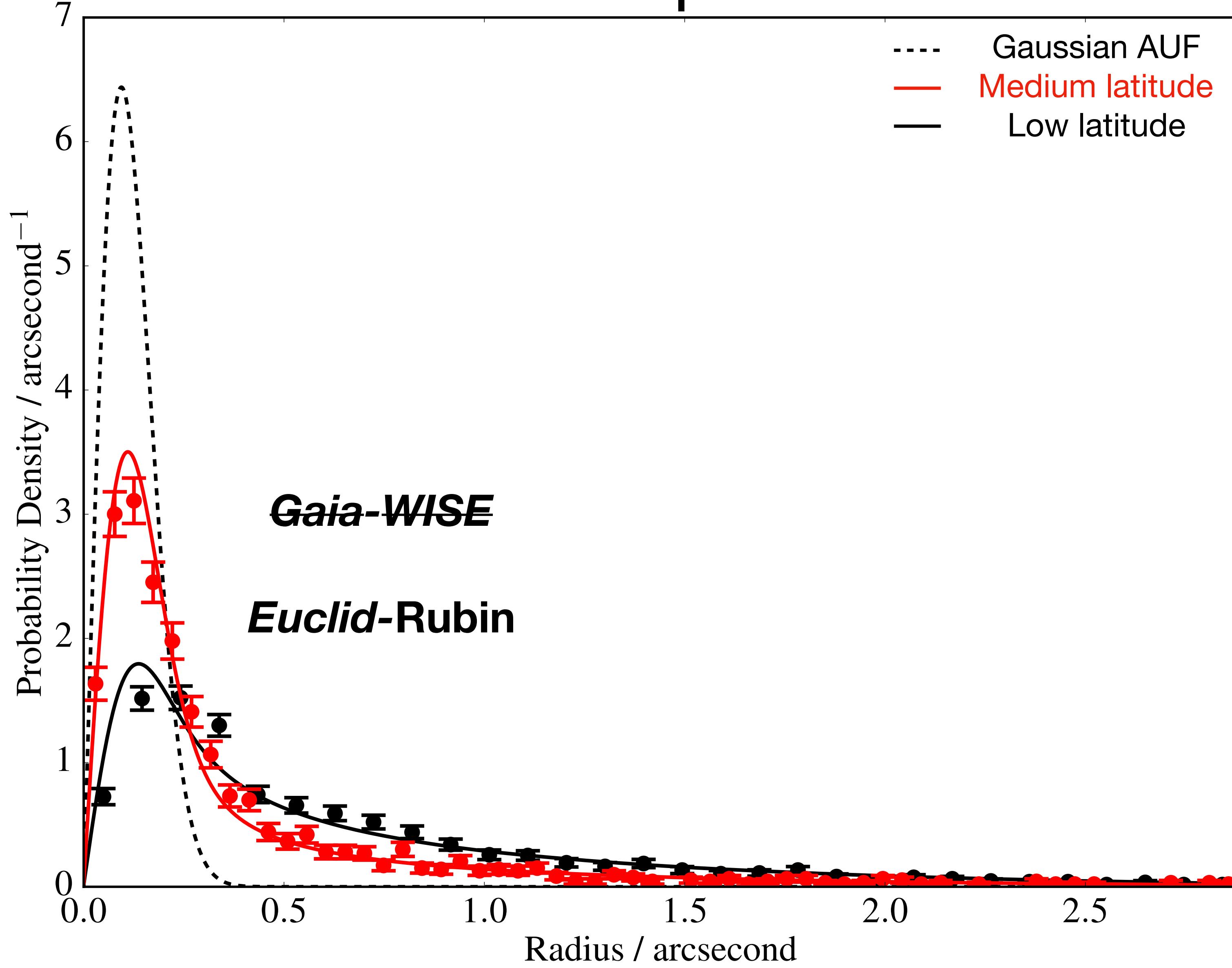
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Additional Components of the AUF

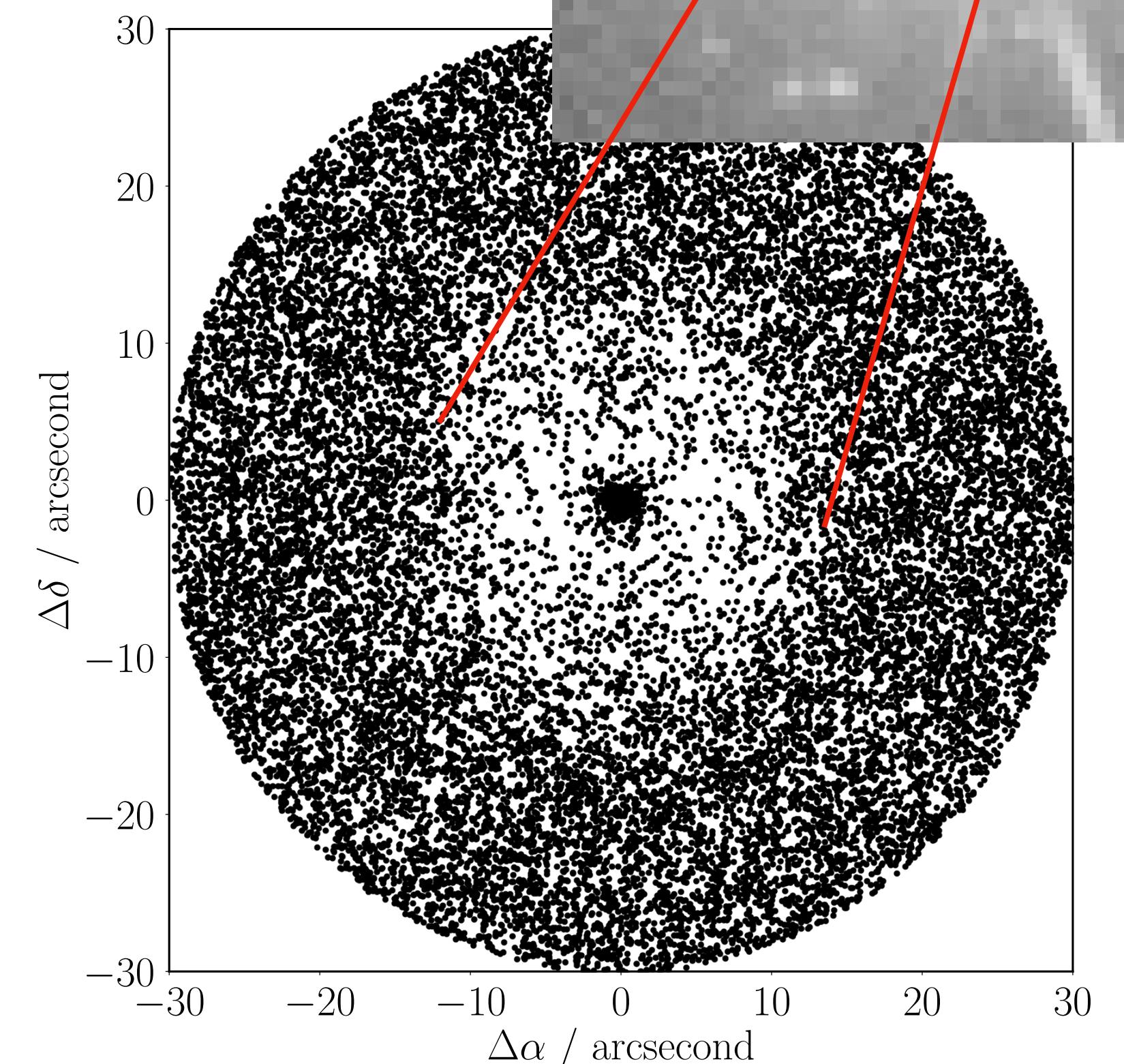
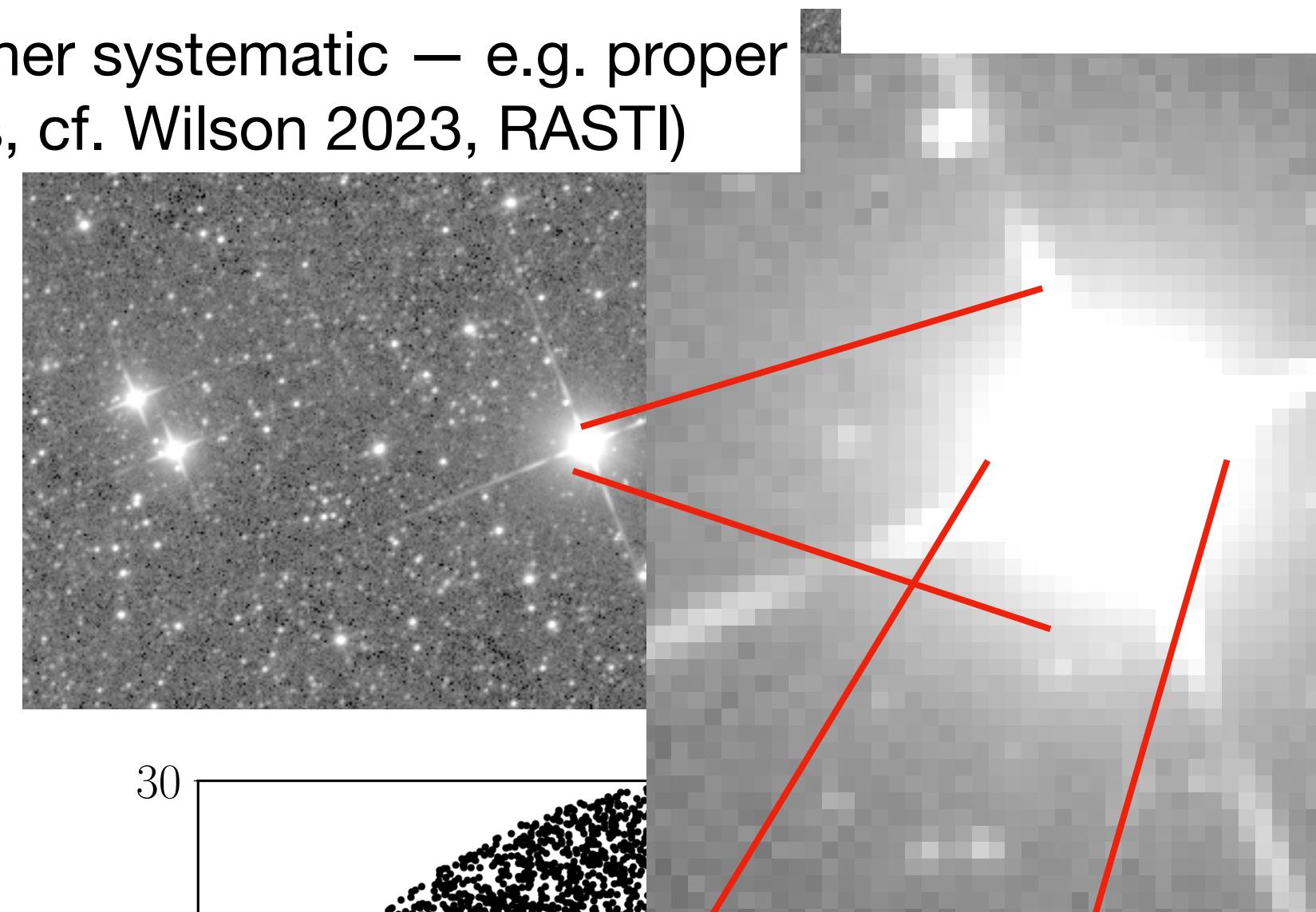
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WISE - Wright et al. (2010)

Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

(and any other systematic – e.g. proper motions, cf. Wilson 2023, RASTI)

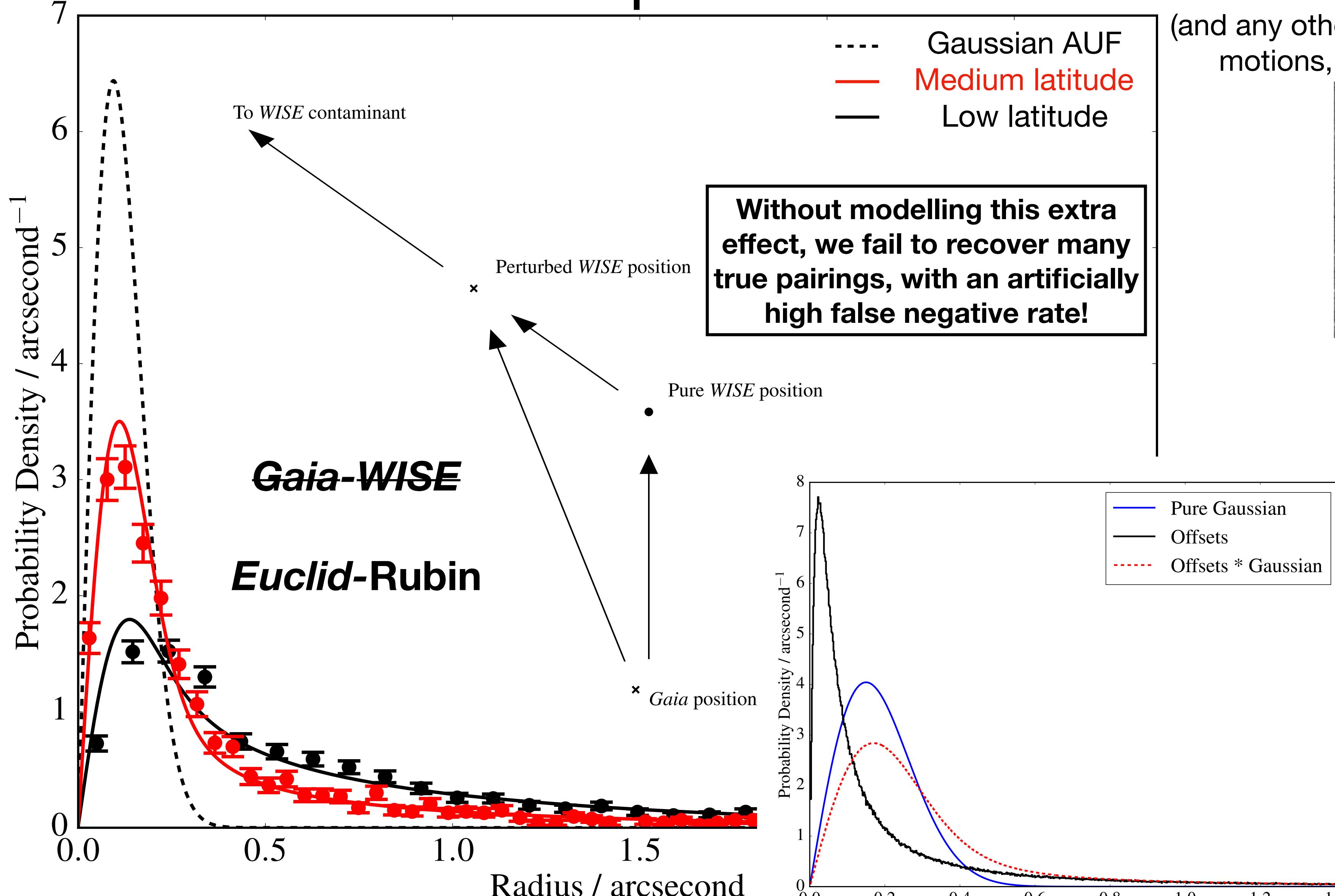


Wilson & Naylor (2017)

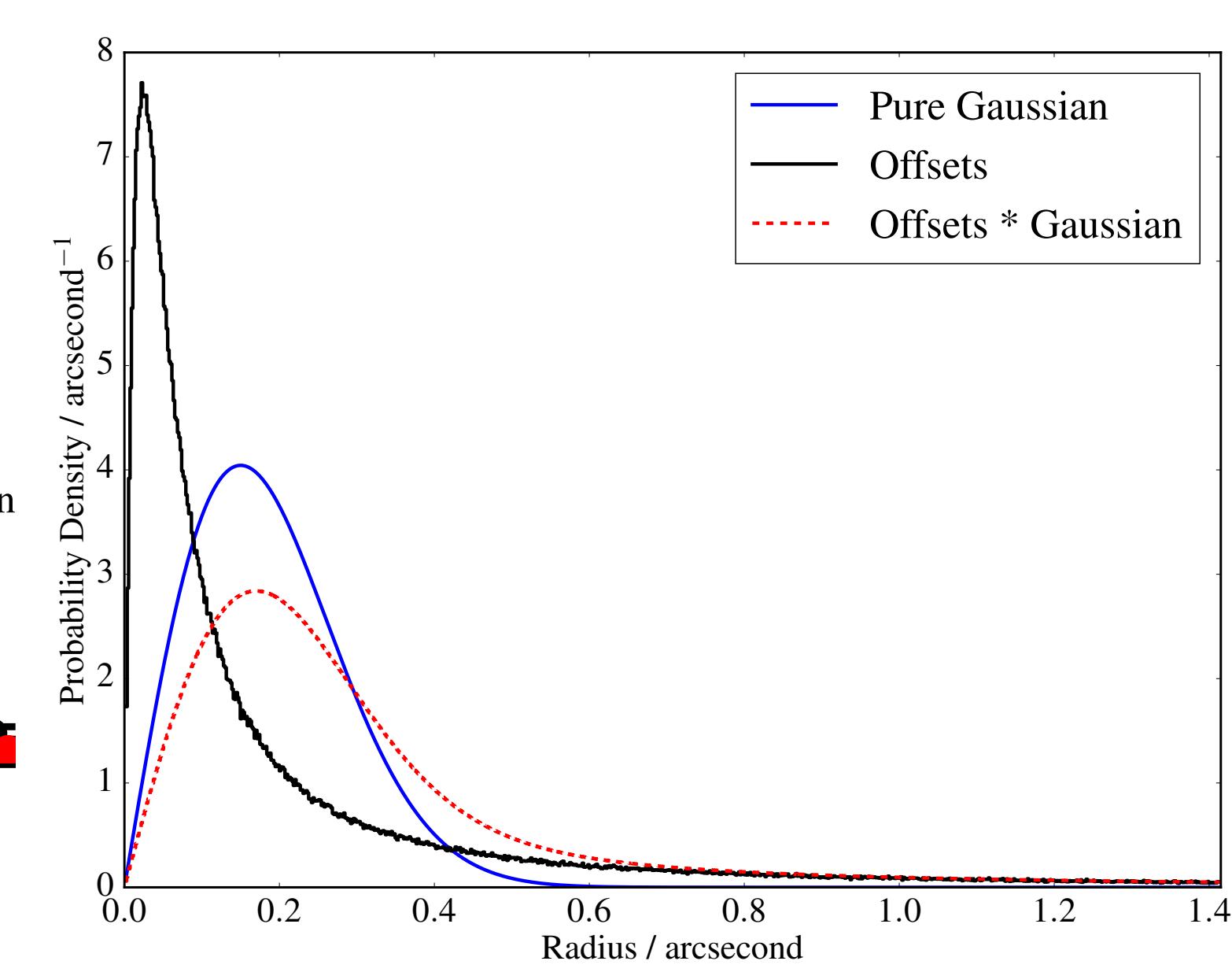
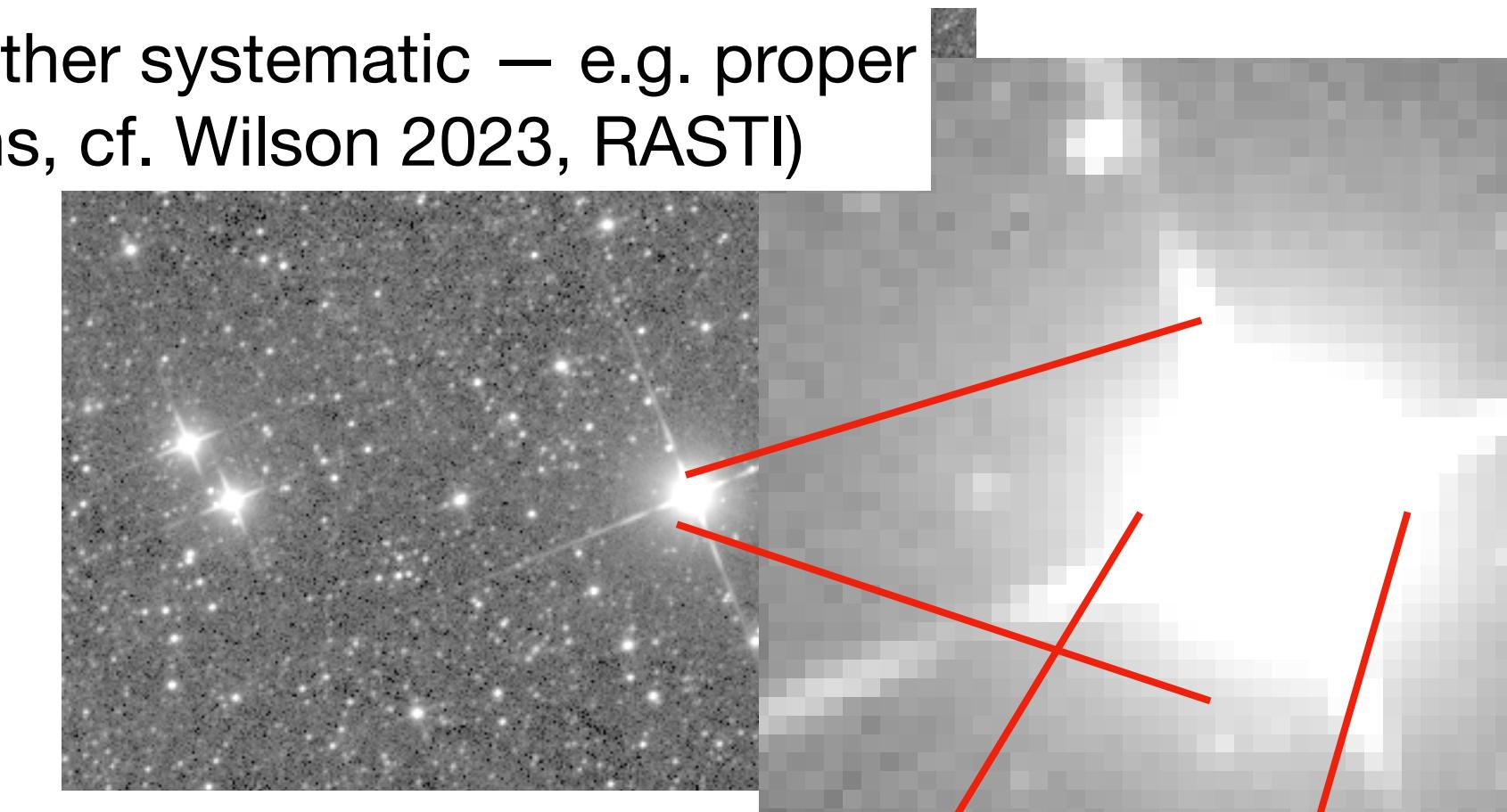
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Additional Components of the AUF

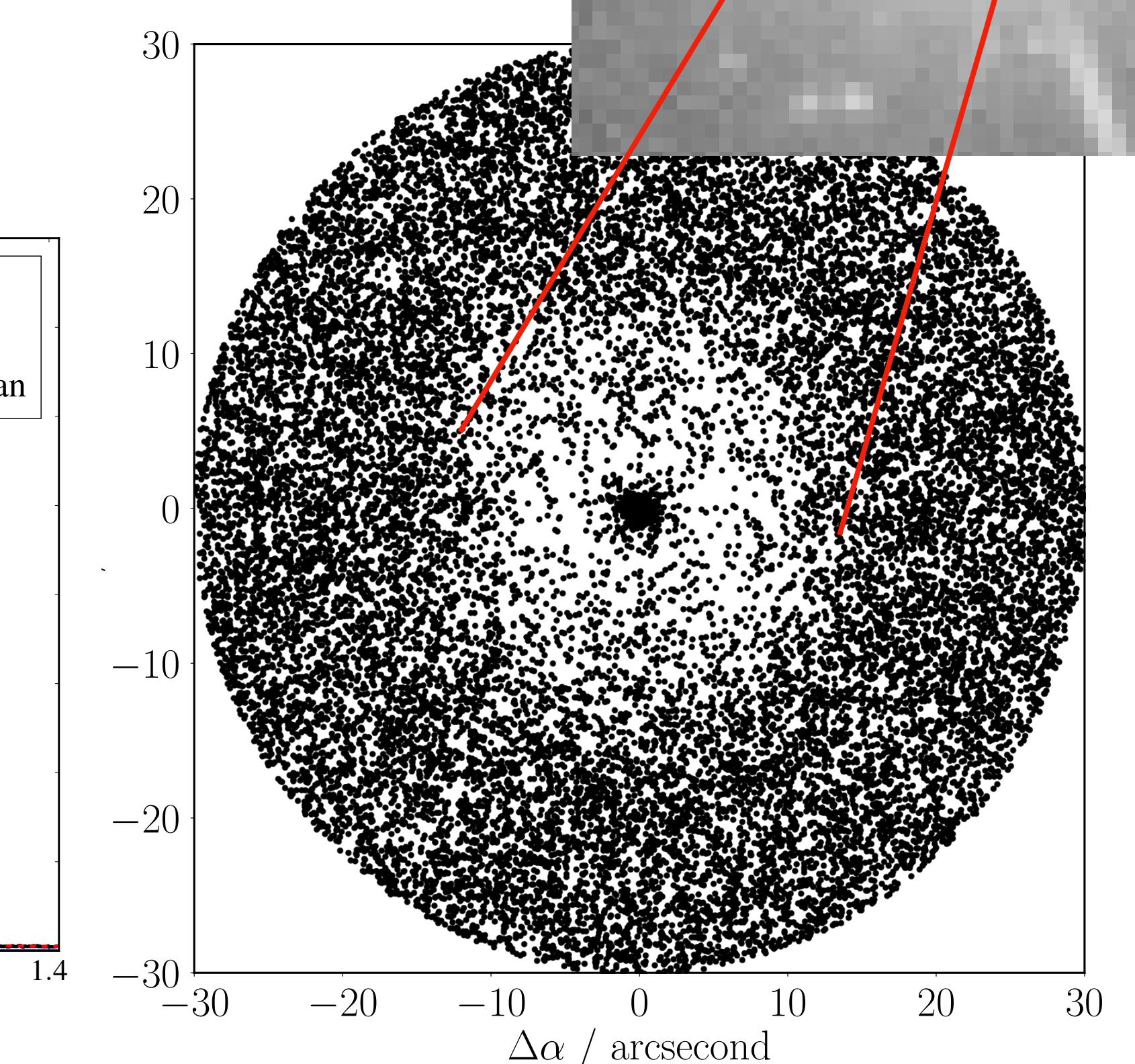
$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \lambda} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \phi} N_\phi f_\phi^\omega \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$



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Wilson & Naylor (2018b)



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Wilson & Naylor (2017)

Wilson & Naylor (2017)

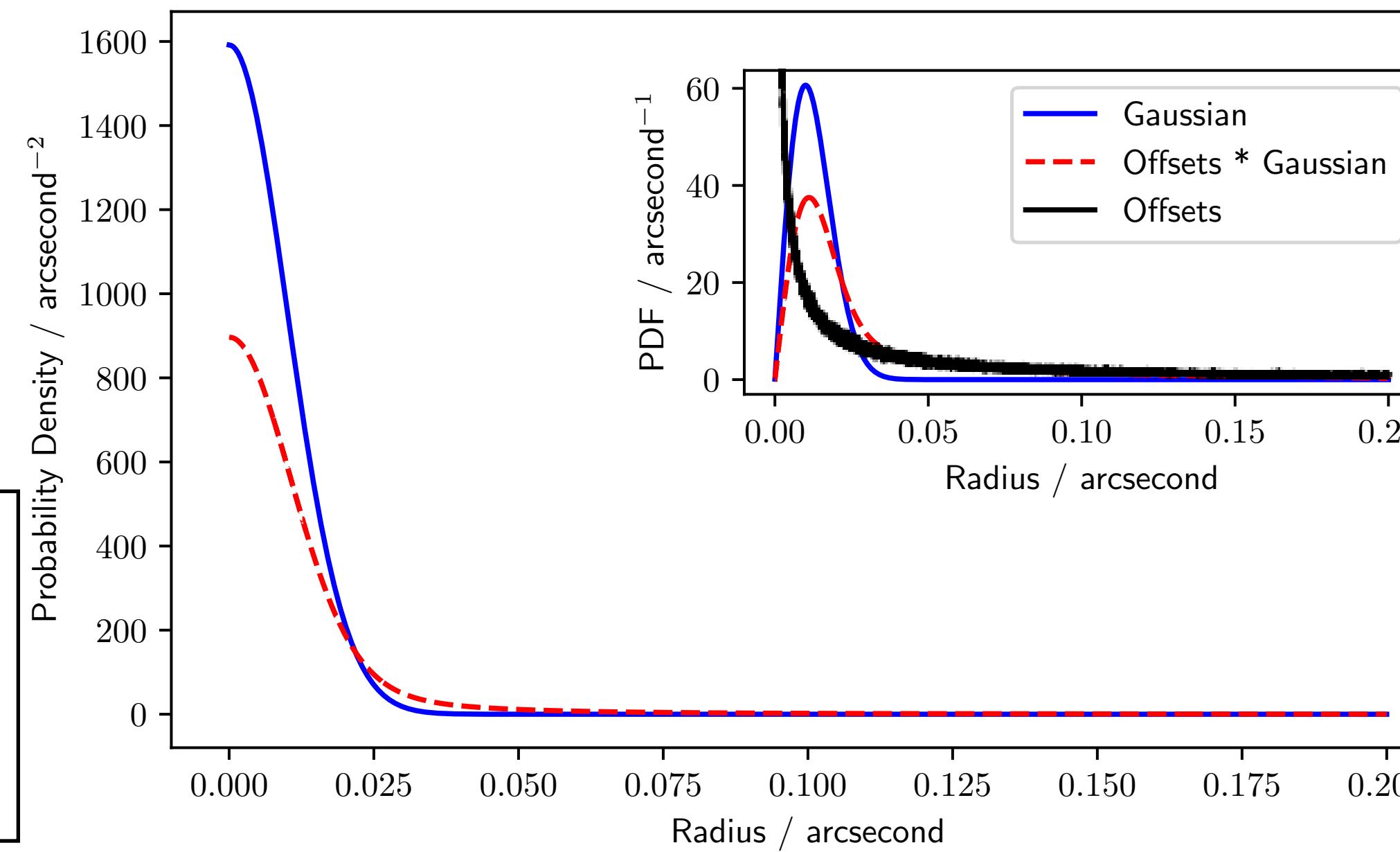
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The Rubin AUF: Galactic Plane

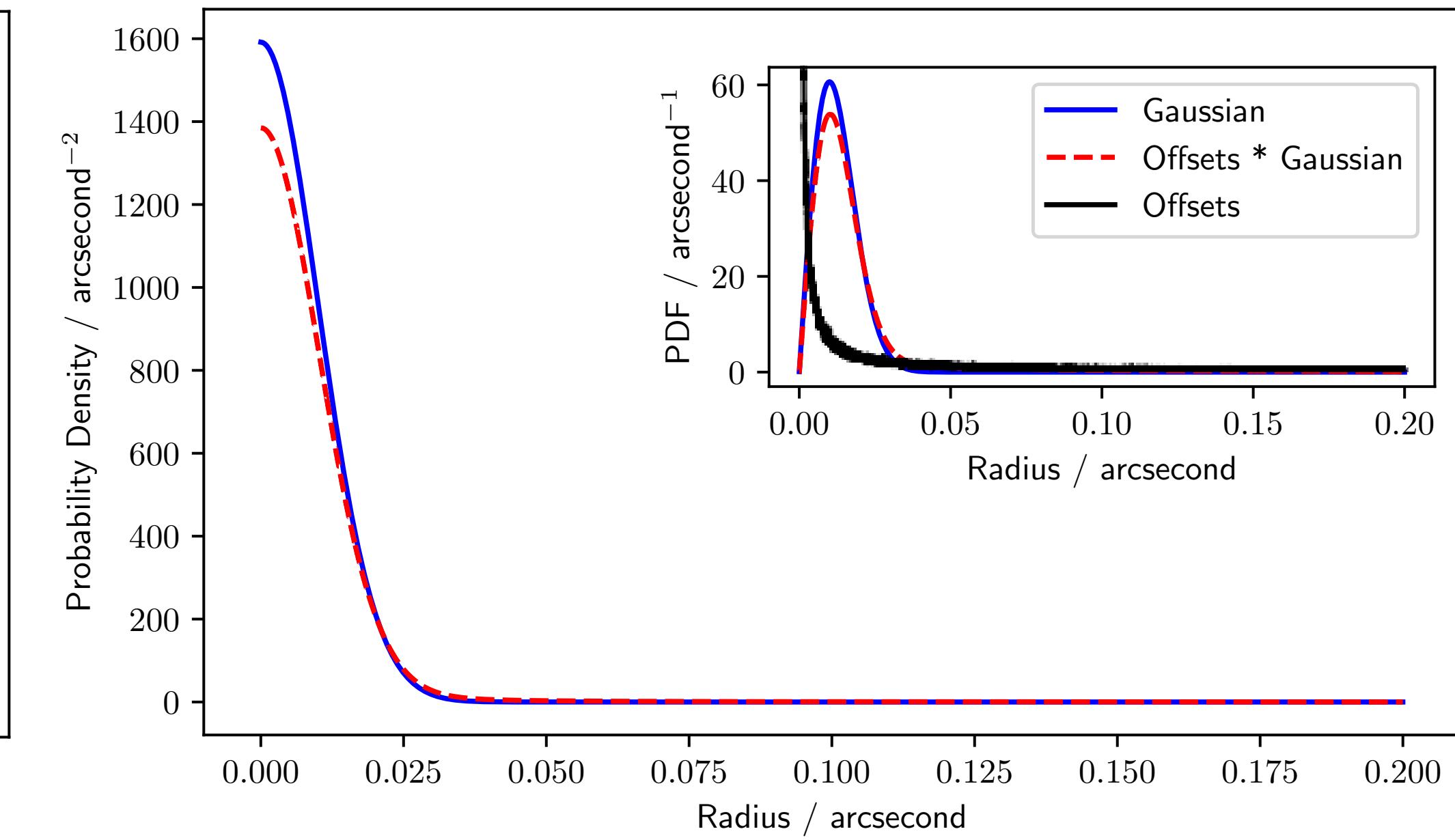
Galactic Centre

Single-visit

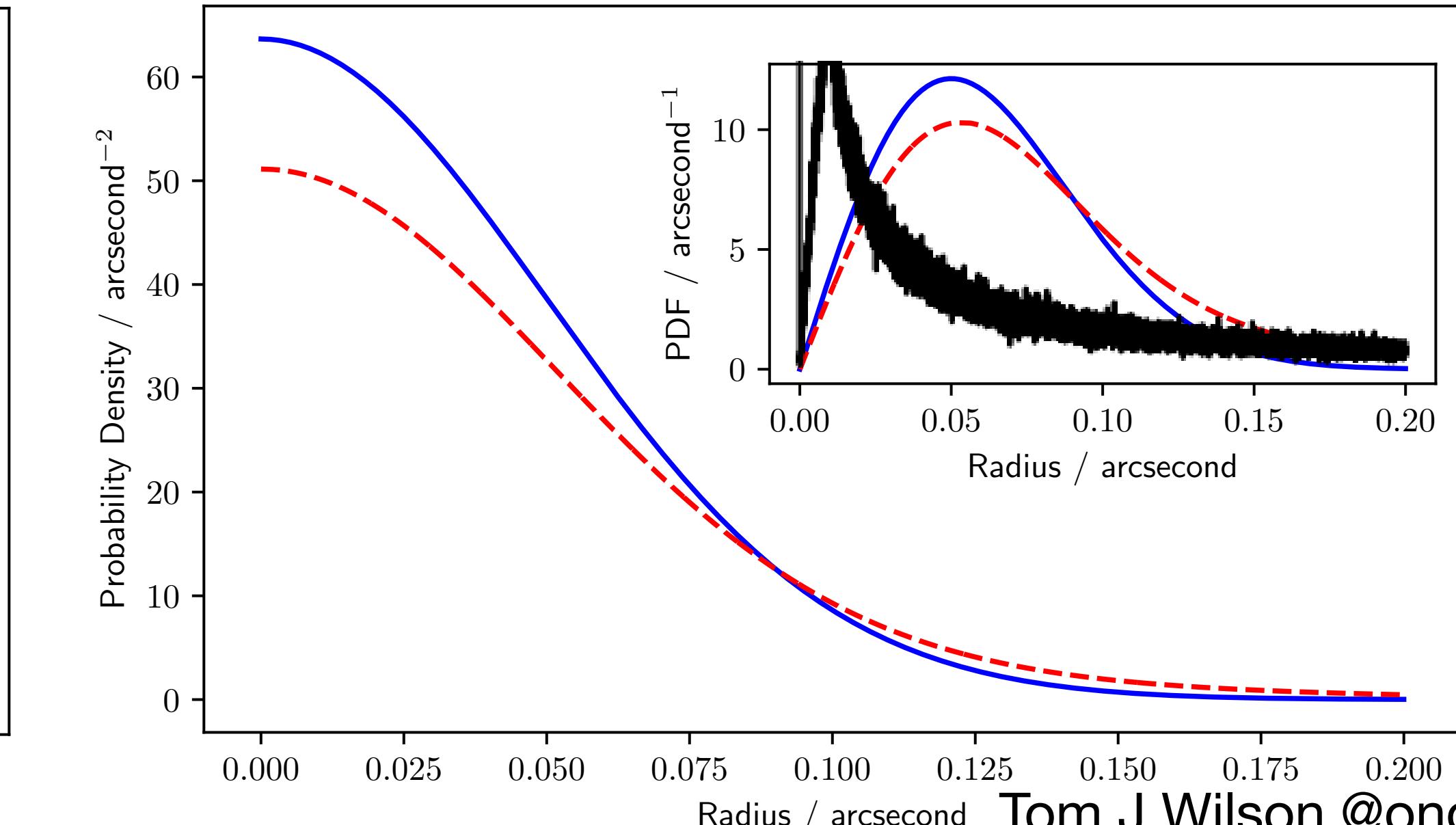
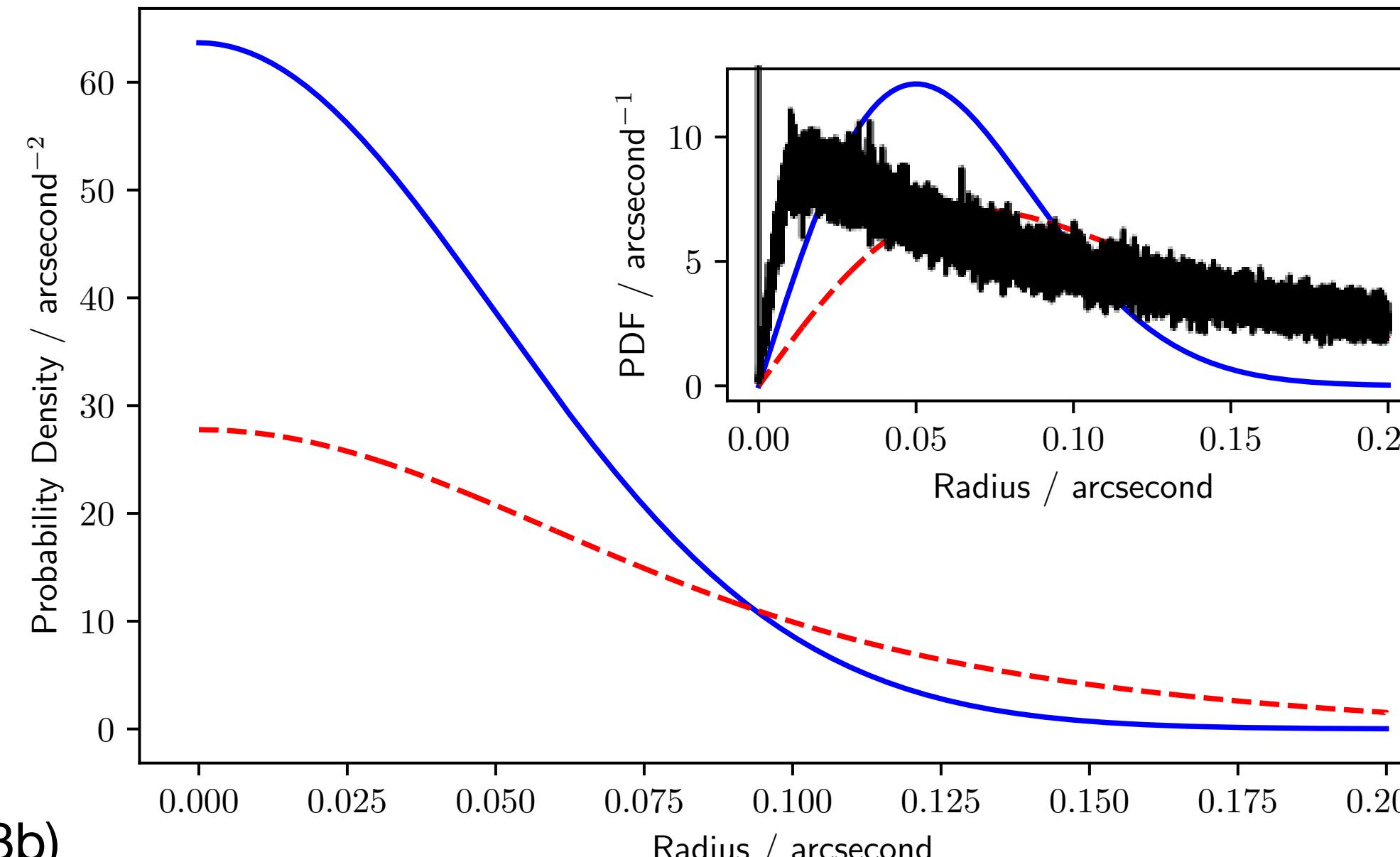
**Without modelling
this extra effect, we
fail to recover many
true pairings, with an
artificially high false
negative rate!**



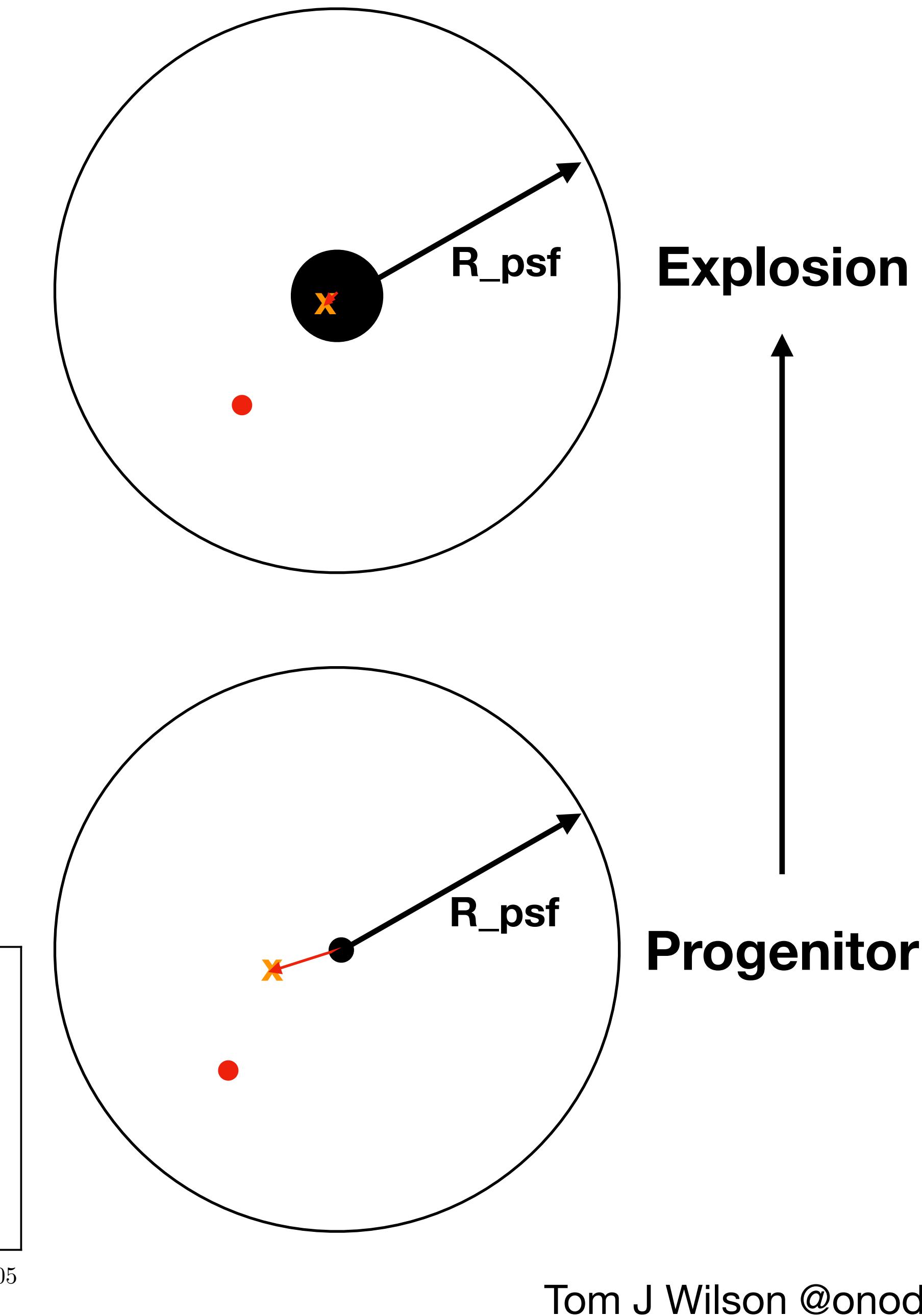
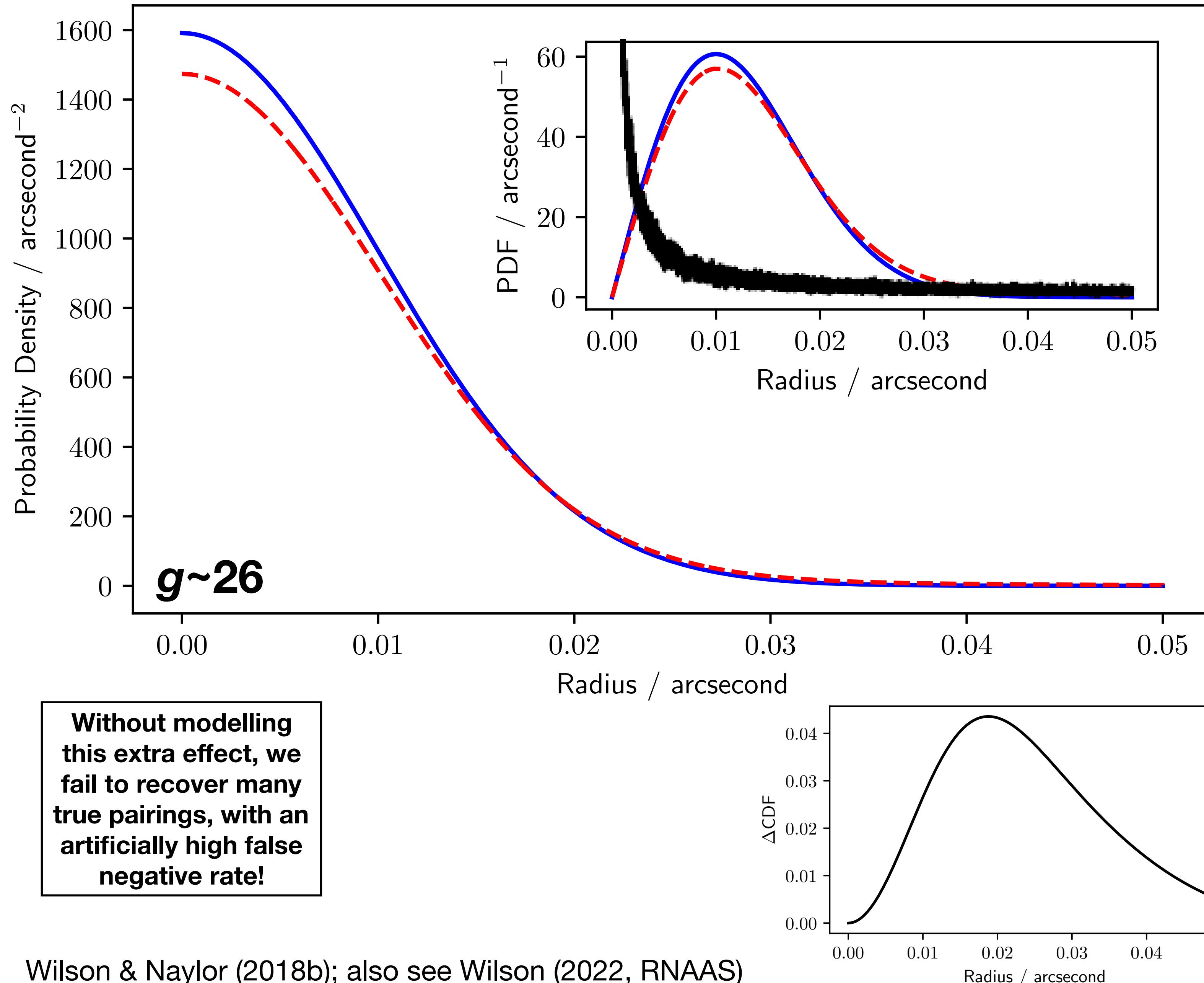
Not the Galactic Centre



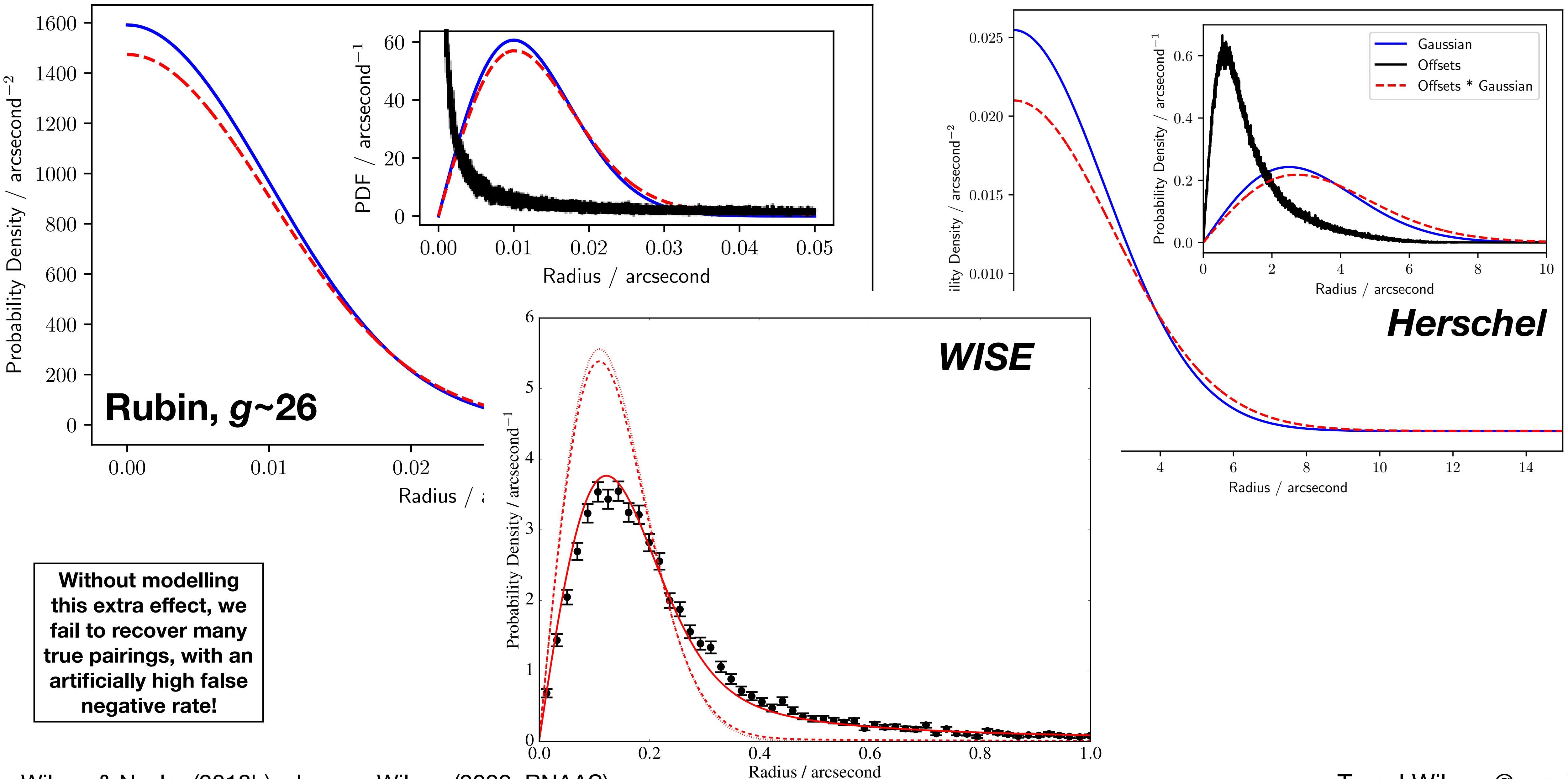
Co-add



The Rubin AUF: Extra-Galactic, Transients



The Rubin AUF: Extra-Galactic, Transients



Matching Across Catalogues using the Astrometric Uncertainty Function and Flux



<https://github.com/macauff/macauff>

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Cross-Match Tools, Framework, Usage

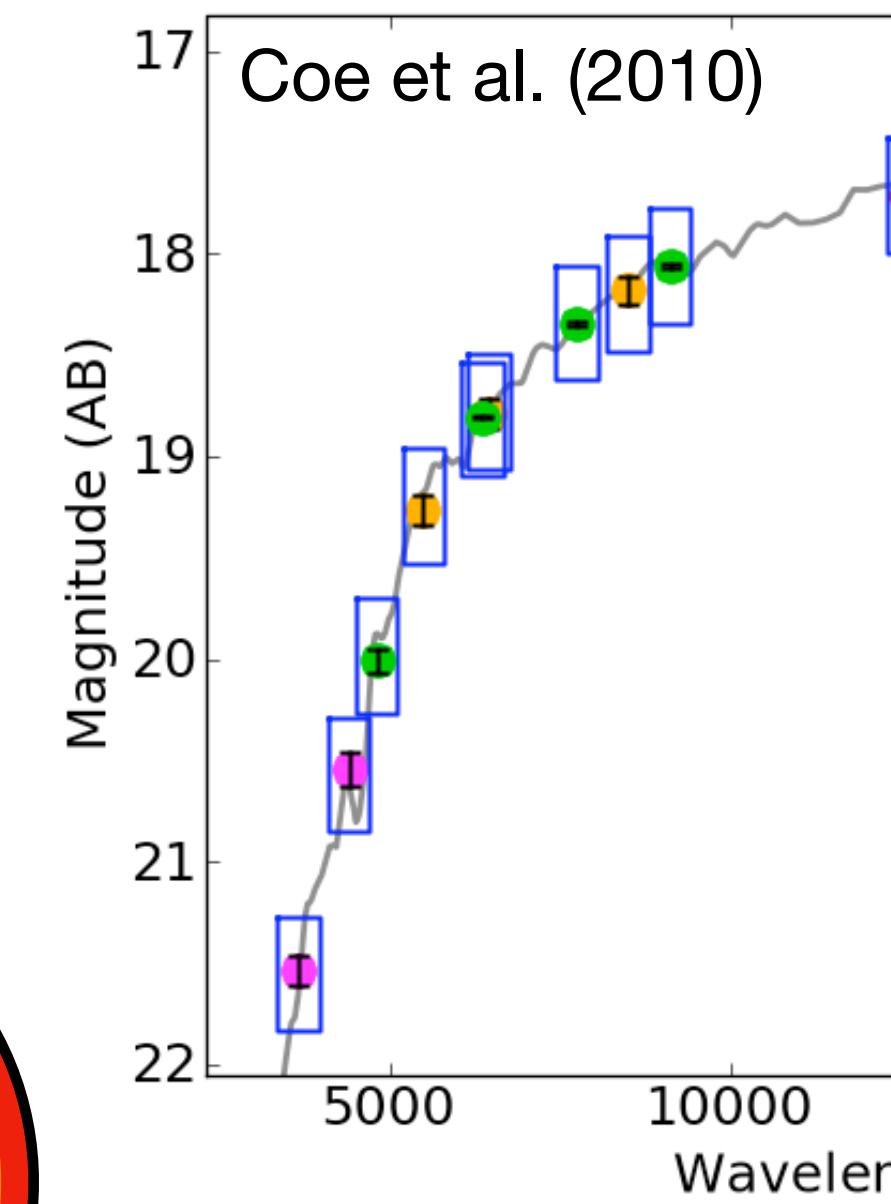
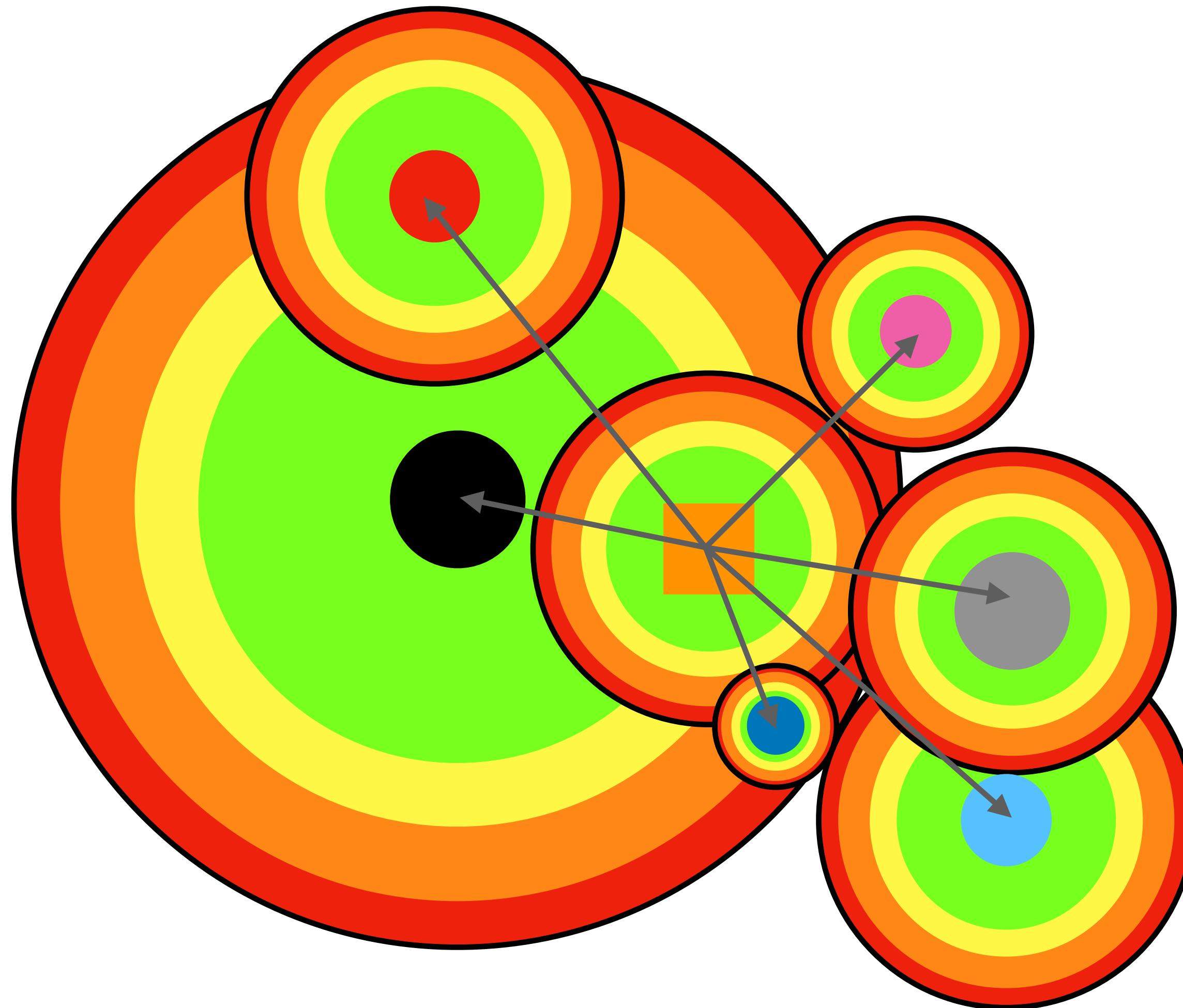


The Rubin “Super-Match”

Bringing Independent Results together to Notify of Associations across Multiple catalogues

LSST -> *Gaia*, *WISE*, VISTA, *Euclid*, SDSS, ... matches

Quick and easy construction of spectral energy distributions for each LSST source
Includes SED probabilities, individual match reliability, contamination statistics etc.



<https://github.com/macauff/macauff>
<https://github.com/macauff/birnam>

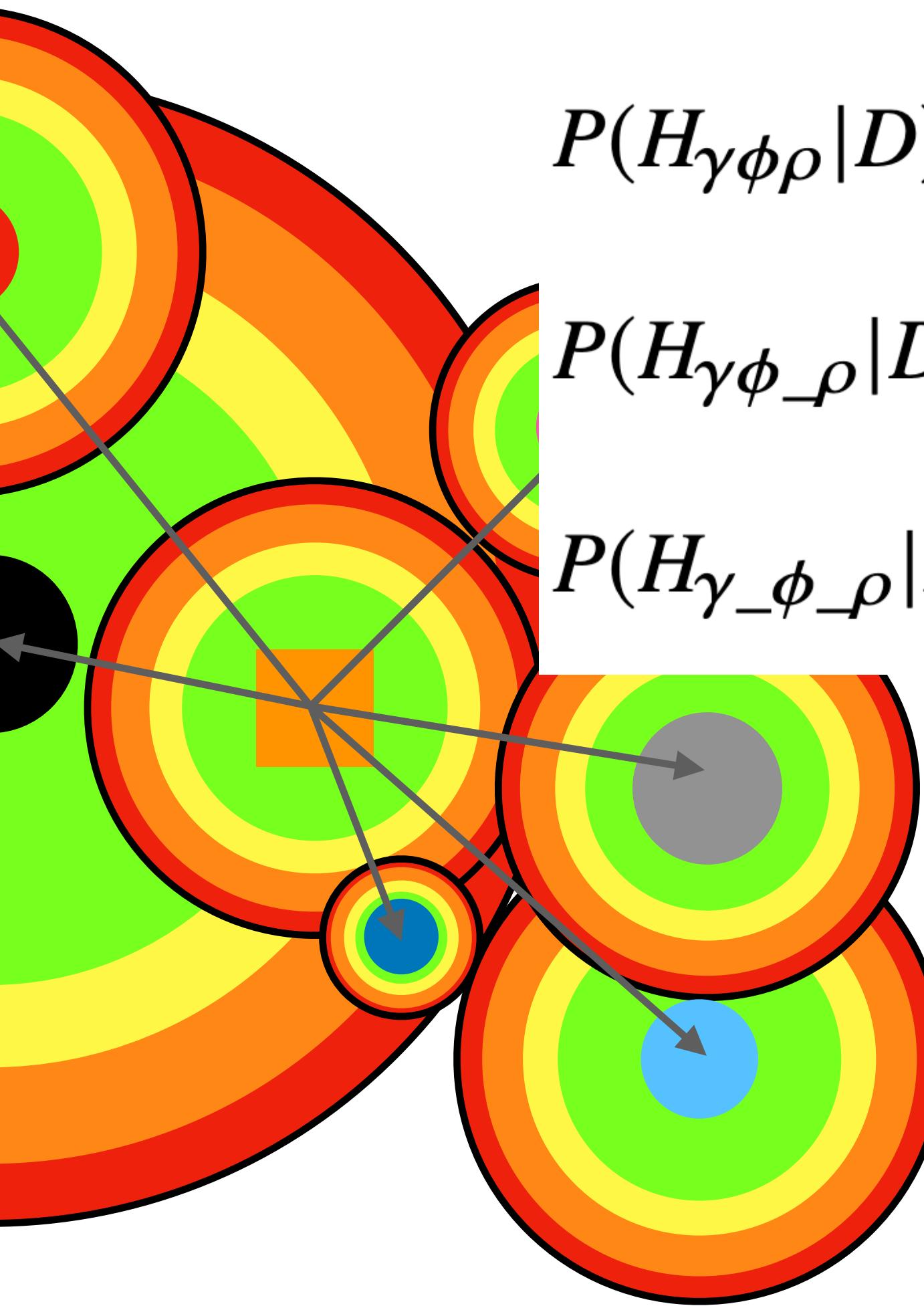
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Quick and easy construction of spectral energy distributions for each LSST source
Includes SED probabilities, individual match reliability, contamination statistics etc.



$$P(H_{\gamma\phi\rho}|D) = \frac{1}{K} N_{\gamma\phi} G_{\gamma\phi} N_{\gamma\rho} G_{\gamma\rho} = A_{\gamma\phi} A_{\gamma\rho},$$

$$P(H_{\gamma\phi_\rho}|D) = \frac{1}{K} N_{\gamma\phi} G_{\gamma\phi} N_\gamma N_\rho = B_{\gamma\phi} A_{\gamma\rho},$$

$$P(H_{\gamma_\phi_\rho}|D) = \frac{1}{K} N_\gamma N_\phi N_\gamma N_\rho = B_{\gamma\phi} B_{\gamma\rho},$$

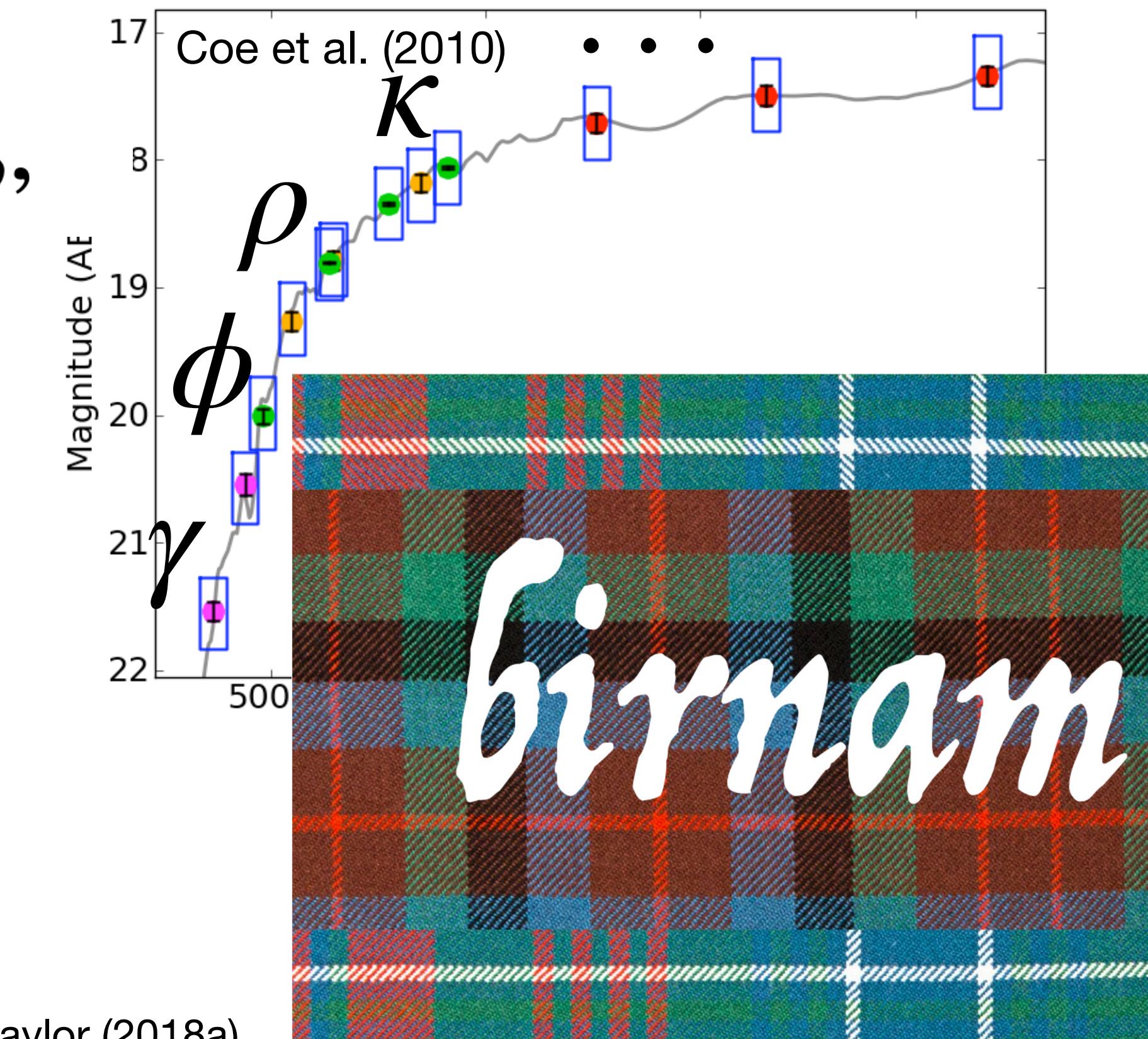
$$A_{\gamma\phi} = \frac{N_{\gamma\phi} G_{\gamma\phi}}{N_\gamma N_\phi + N_{\gamma\phi} G_{\gamma\phi}}$$

$$B_{\gamma\phi} = \frac{N_\gamma N_\phi}{N_\gamma N_\phi + N_{\gamma\phi} G_{\gamma\phi}}$$

Wilson & Naylor (2018a)

Wilson & Naylor (in prep.)

Pineau et al. (2017)

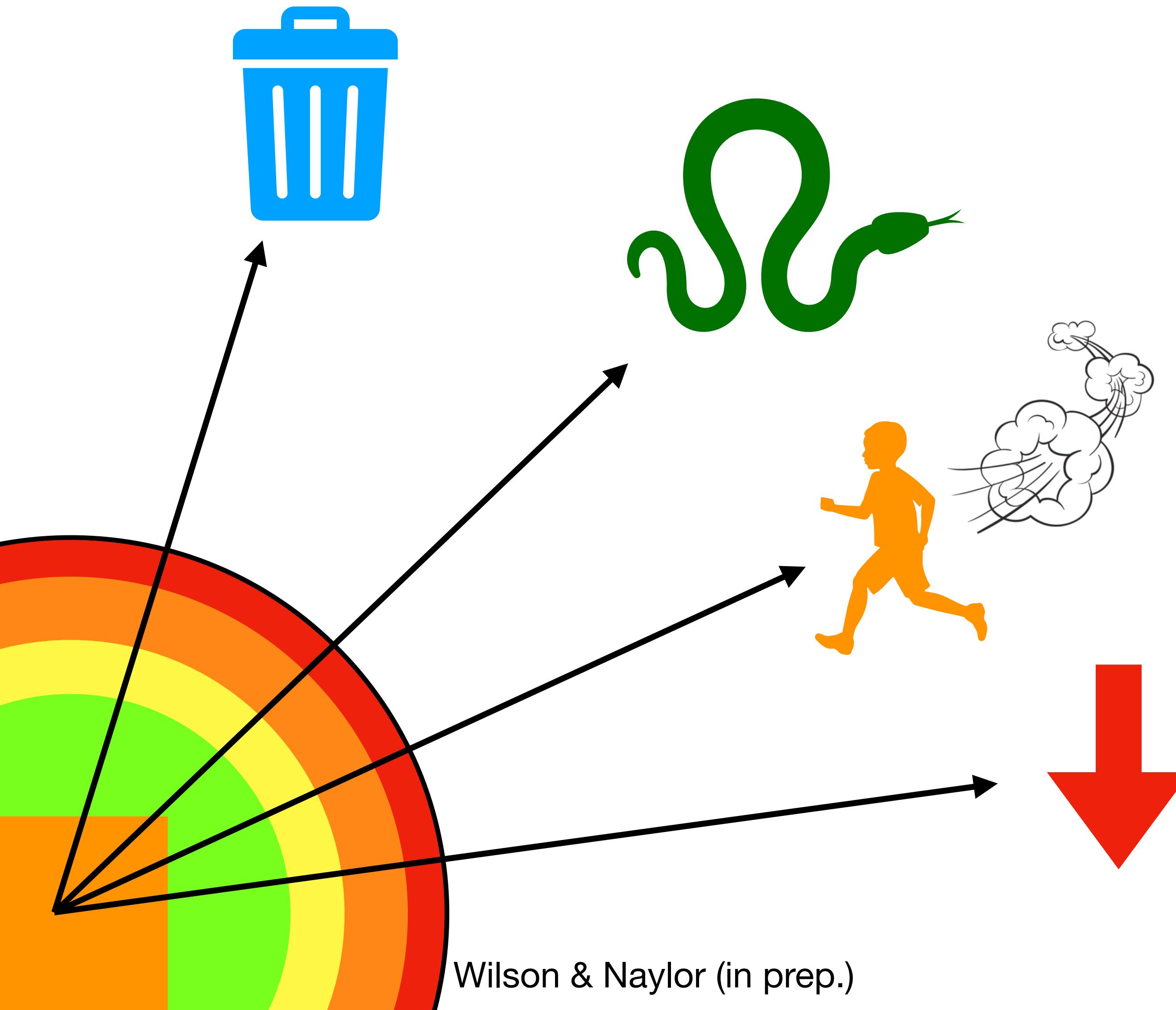


<https://github.com/macauff/macauff>
<https://github.com/macauff/birnam>

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Confirming Lonely Rubin Sources

Blanks And Near-misses, Questionable sources, Upper-limits, and Objects of varying brightness



Wilson & Naylor (in prep.)

Most LSST sources will be “lonely” with 15x as many sources as the next dataset.

We will follow up all non-matches, and confirm whether these objects are:

- Image artefacts
- Astrophysically variable objects
- High proper motion sources
- Regular objects that are simply too faint to be seen in the opposing catalogue



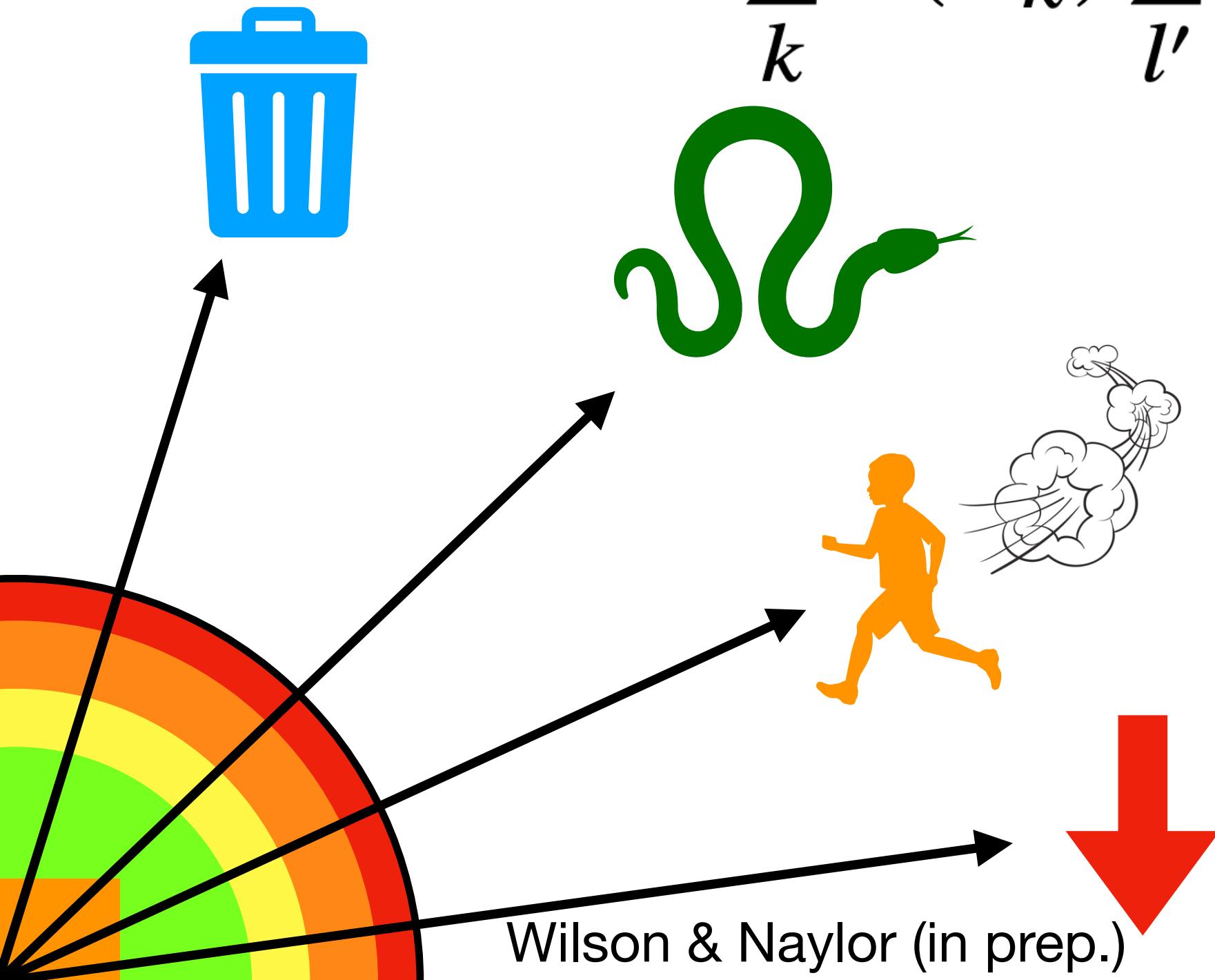
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Confirming Lonely Rubin Sources

Blanks And Near-misses, Questionable sources, Upper-limits, and Objects of varying brightness

$$P(H_i, M_j | \mathbf{D}) = \frac{P(H_i)P(M_j | H_i)p(\mathbf{D} | H_i, M_j)}{p(\mathbf{D})}$$

$$P(H_i, M_j | \mathbf{D}) = \frac{P(H_i)L_j}{\sum_k P(H_k) \sum_{l'} L_{l'} + \sum_{k'} P(H_{k'})}$$



$$L = \frac{Gc}{Nf}$$

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How To Use Our Cross-Matches

(Or, how this impacts you on a day-to-day basis)

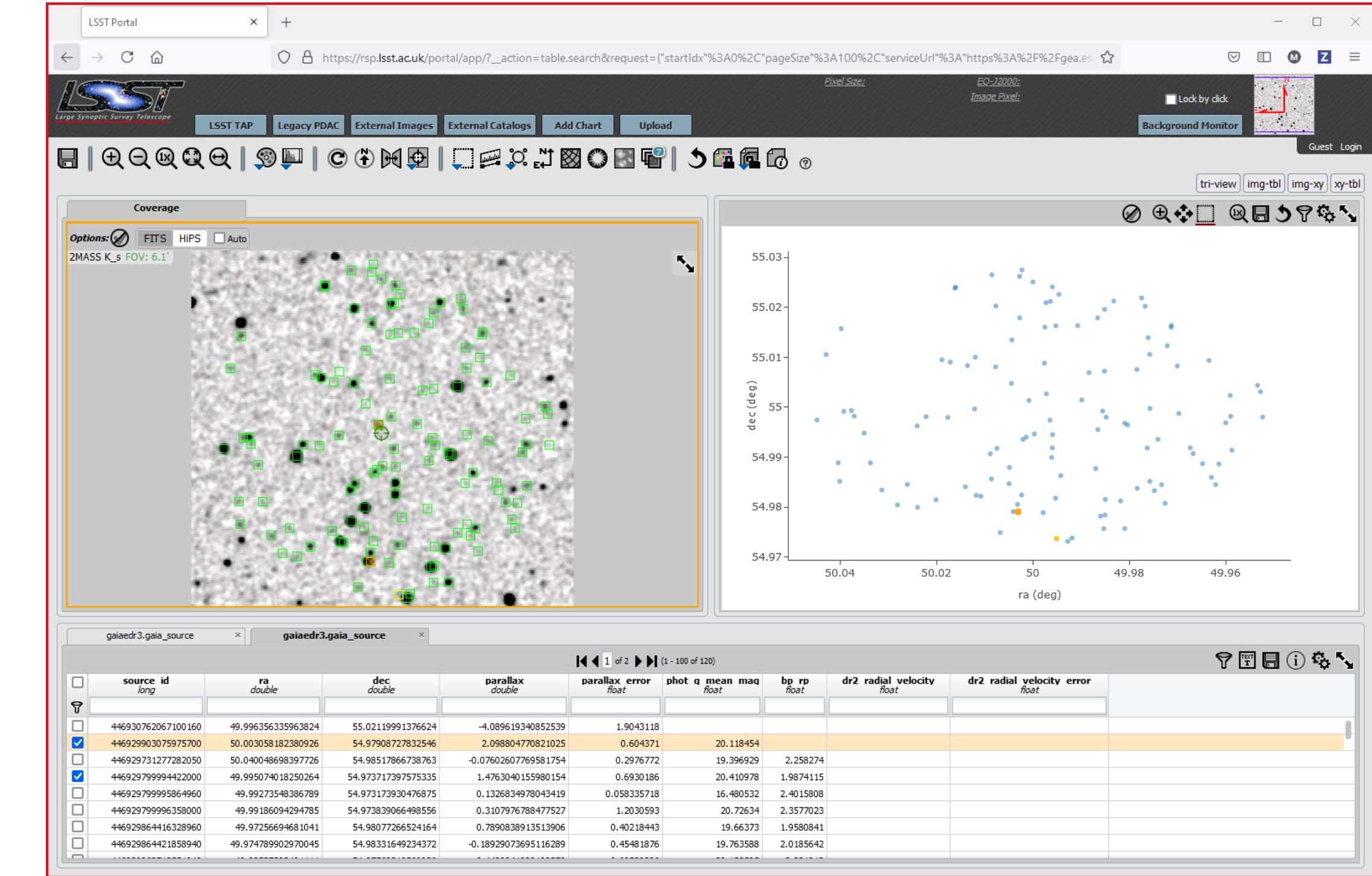


Three tables per cross-match: merged catalogue dataset, and 2x non-match dataset (one per catalogue)

Example columns:

- Designations of the two sources (e.g., WISE J... and Gaia EDR3...)
- RA and Dec (or Galactic l/b) of the two sources
- Magnitudes (corrected for necessary effects, such as e.g. **Gaia**) in all bandpasses for both objects
- Match probability — probability of the most likely permutation (see equation 26 of Wilson & Naylor 2018a)
- Eta - Photometric likelihood ratio (counterpart vs non-match probability, just for brightnesses; see eq37 of WN18a)
- Xi - Astrometric likelihood ratio (just position match/non-match comparison; see eq38 of WN18a)
- Average contamination - simulated mean (percentile) brightening of the two sources, based on number density of catalogue
- Probability of sources having blended contaminant above e.g. 1% relative flux

We will provide two match runs per catalogue pair match: one with, and one without, the photometry considered, to allow for the recovery of sources with “weird” colours but otherwise agreeable astrometry



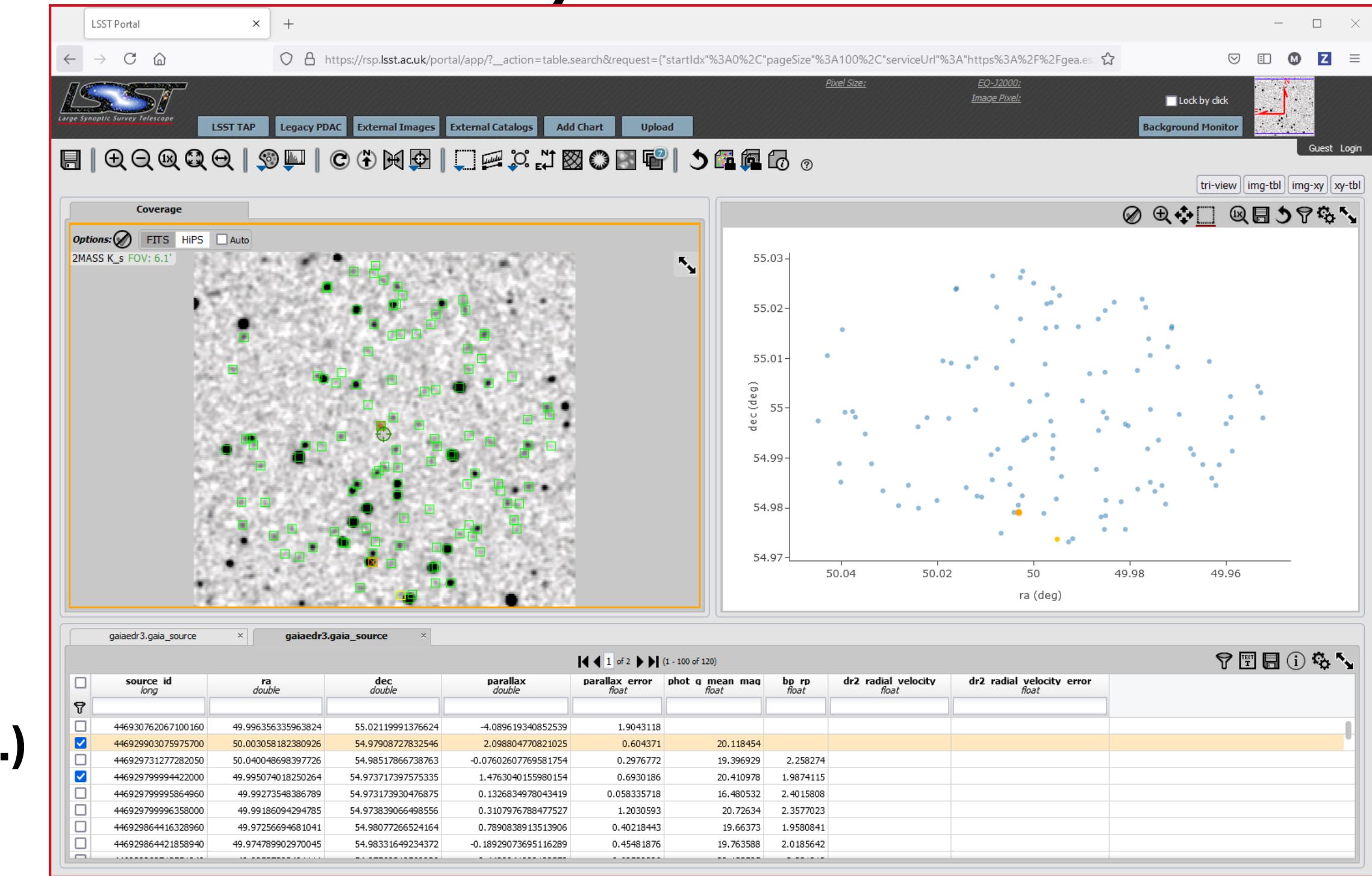
How To Use Our Super- and Lonely-Matches

(Or, how this impacts you on a day-to-day basis)



Example columns:

- Designations of N sources (e.g., WISE J..., Gaia EDR3..., 2MASS J...)
- Super-match probability — probability of the given permutation

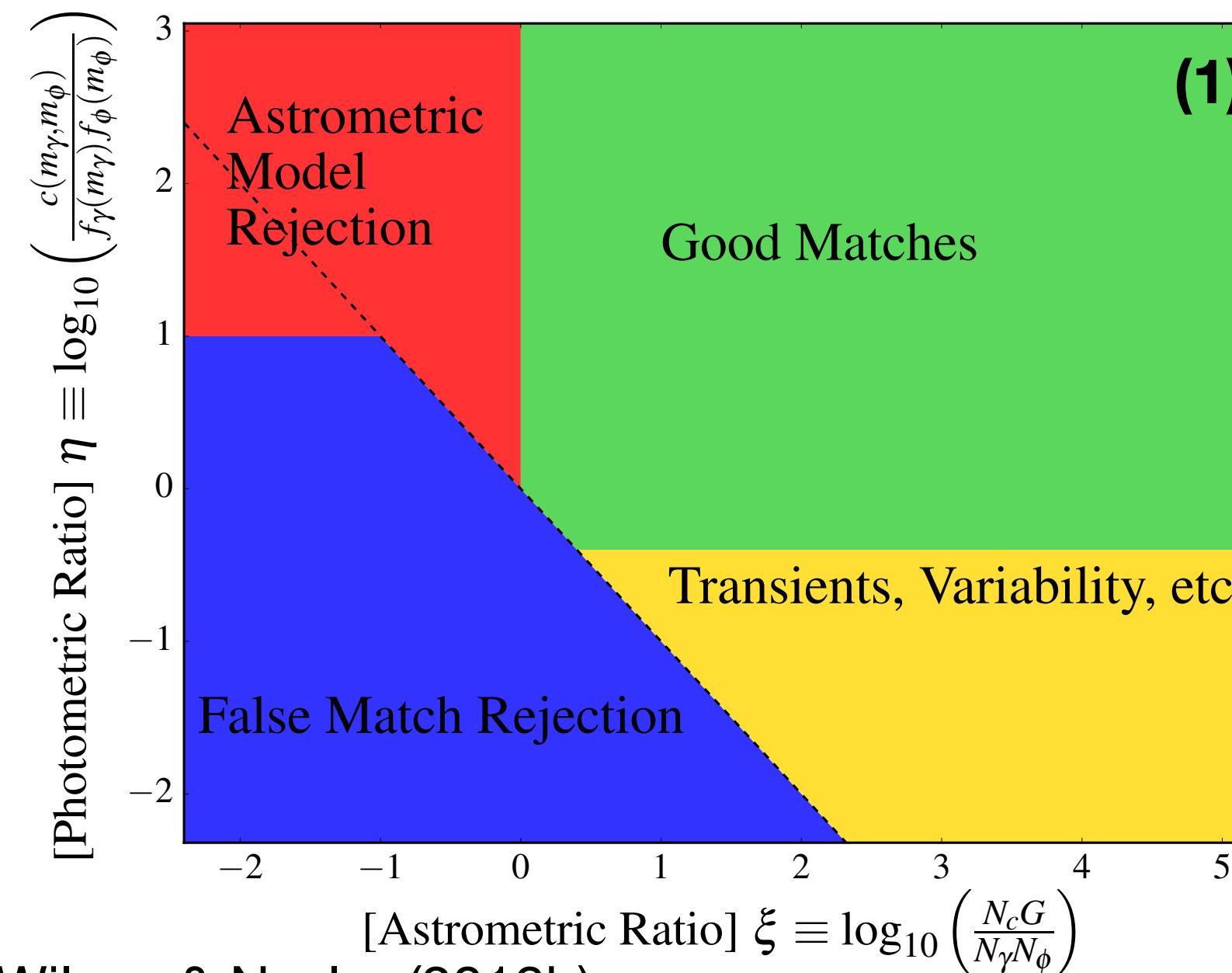


Example columns:

- Designations of the two sources (e.g., WISE J... and Gaia EDR3...)
- RA and Dec (or Galactic l/b) of the two sources
- Magnitudes in all bandpasses for both objects
- Match probability — different to that from a macauff cross-match!
- Hypothesis of non-match (proper motion, artifact, transient, ...)

Why Use Our Cross-Matches (and Extensions)?

- 0) Getting cross-matches, even for “well behaved” fields
- 1) Finding “odd” objects, either using the inclusion vs non-inclusion of the photometry in the two match runs, or via the likelihood ratio space – separately-planned “real time” matching service for transient objects
- 2) Removing e.g. IR excess or correcting for extinction-like crowding brightening, through Average Contamination; crucial for “1% photometry” in both precision *and* accuracy
- 3) Recovering additional sources missed by other match services – either in crowded fields (we recover up to twice as many *Gaia-WISE* matches than the *Gaia* best neighbour matches), or with our extension to unknown proper motion modelling as an extra systematic

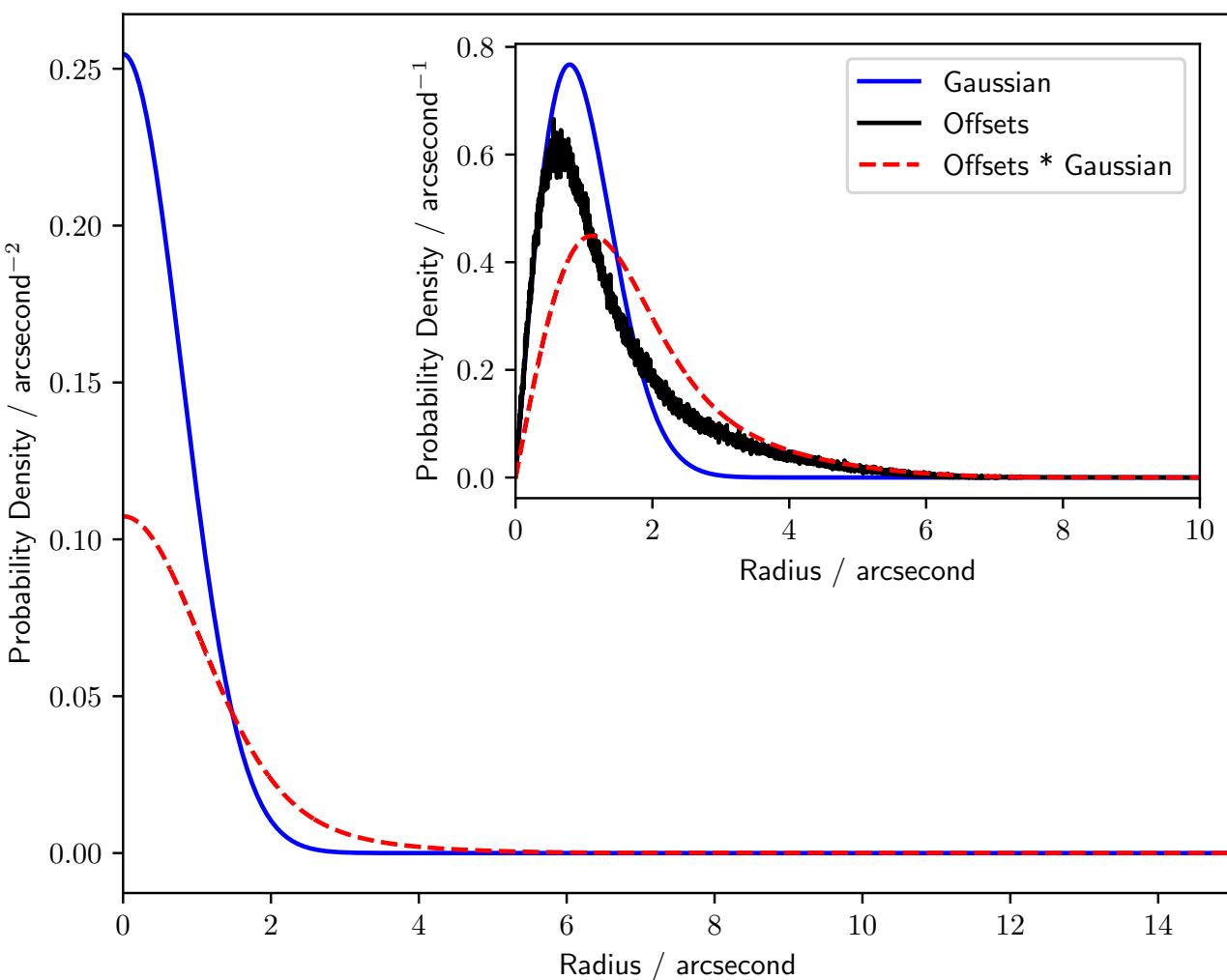
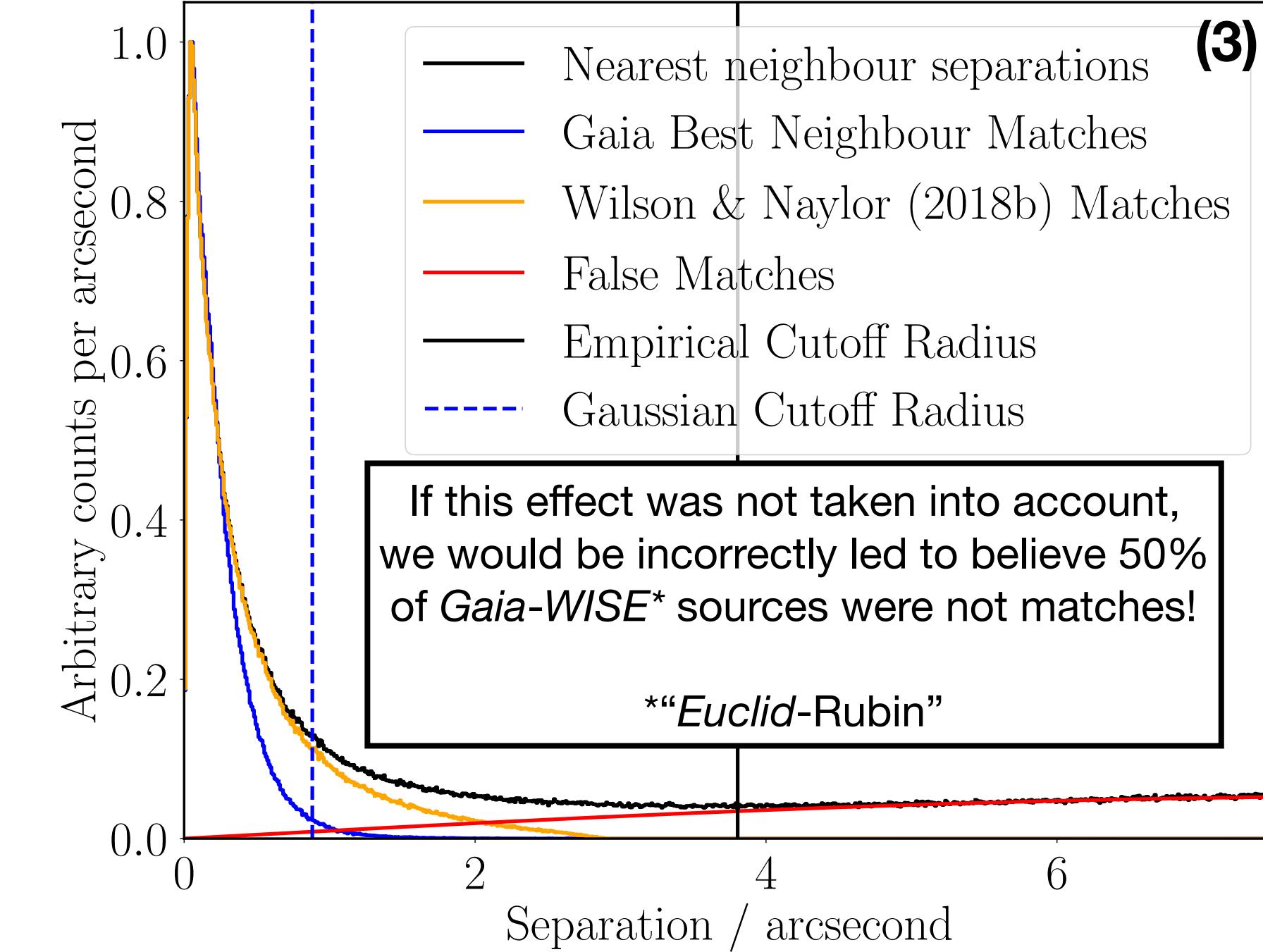
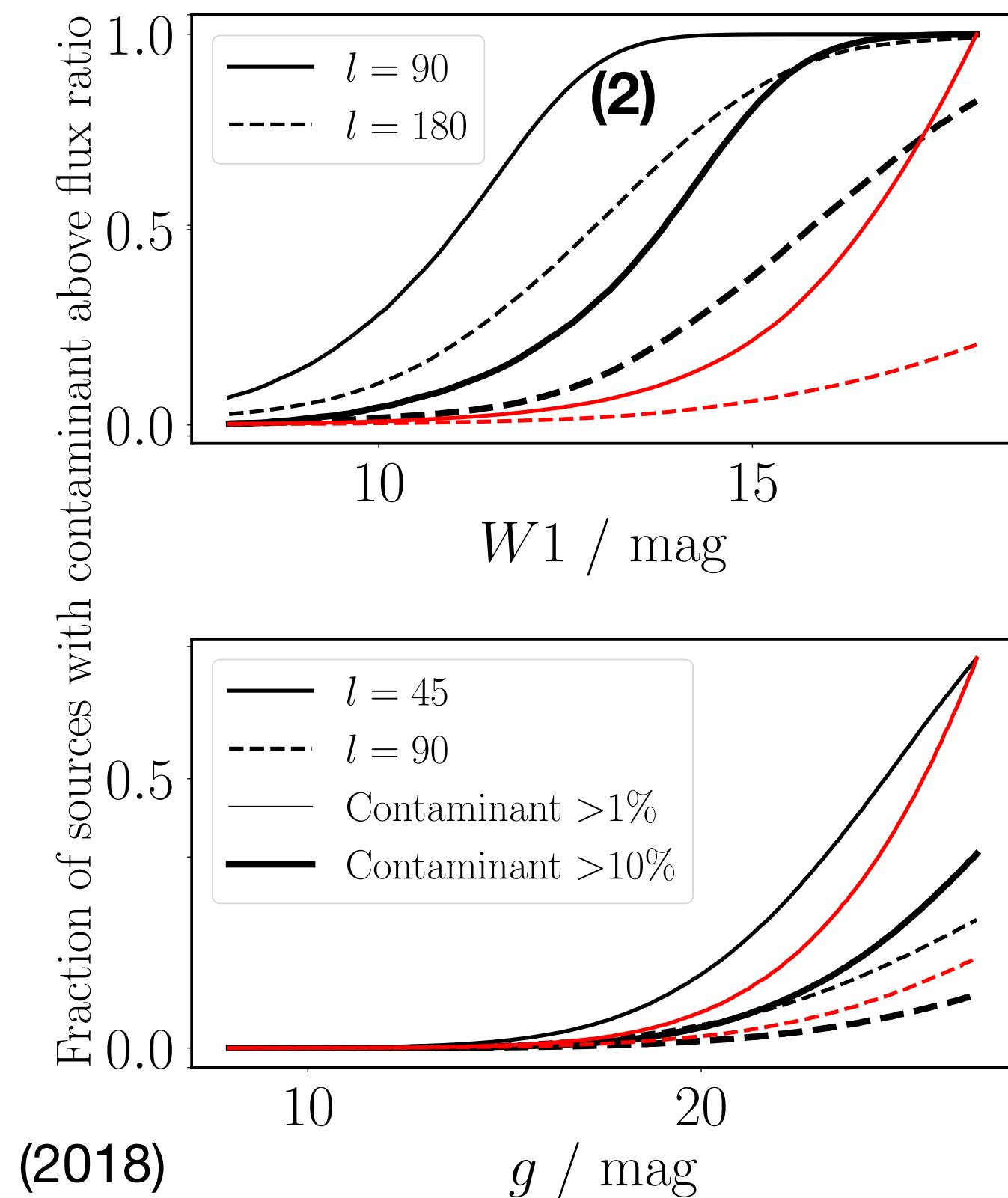


Wilson & Naylor (2018b)

WISE - Wright et al. (2010)

Gaia matches - Marrese et al. (2019)

Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)



Conclusions

- Upcoming LSST:UK cross-match service macauff — let me know your thoughts/needs/hopes/dreams
 - Provide tables of cross-matches between LSST and <your favourite catalogue here!>
- Our cross-matches include two key elements for avoiding issues with the crowded LSST sky
 - A generalised approach to the Astrometric Uncertainty Function allows for the inclusion of the effects of perturbation due to blended sources and unknown proper motions — reduce false -ves!
 - Use of the photometry of sources allows for the rejection of false matches (with >1 “extra” source per 2 arcsecond circle in most of the LSST sky) — reduce false +ves!
- Will include additional information on the crowding of sources, allowing for selection of uncontaminated objects, or modelling of excess flux — crucial for removal of red excess in SEDs
 - LSST will suffer of order 10% flux contamination, which could be confused with extinction
- macauff cross-match tools are being extended currently
 - We will provide an easy-to-use “SED grabber” tool for each LSST source
 - And follow up the ~93% of non-matched Rubin objects to confirm flux upper limits in other surveys



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.github.io 
 

Wilson & Naylor, 2017, MNRAS, 468, 2517
Wilson & Naylor, 2018a, MNRAS, 473, 5570
Wilson & Naylor, 2018b, MNRAS, 481, 2148

Wilson, 2022, RNAAS, 6, 60

Wilson, 2023, RASTI, 2, 1

<https://github.com/macauff/macauff>



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