

# Enhancing (amongst others) Rubin-*Euclid* Synergies with Robust Catalogue Cross-Matching

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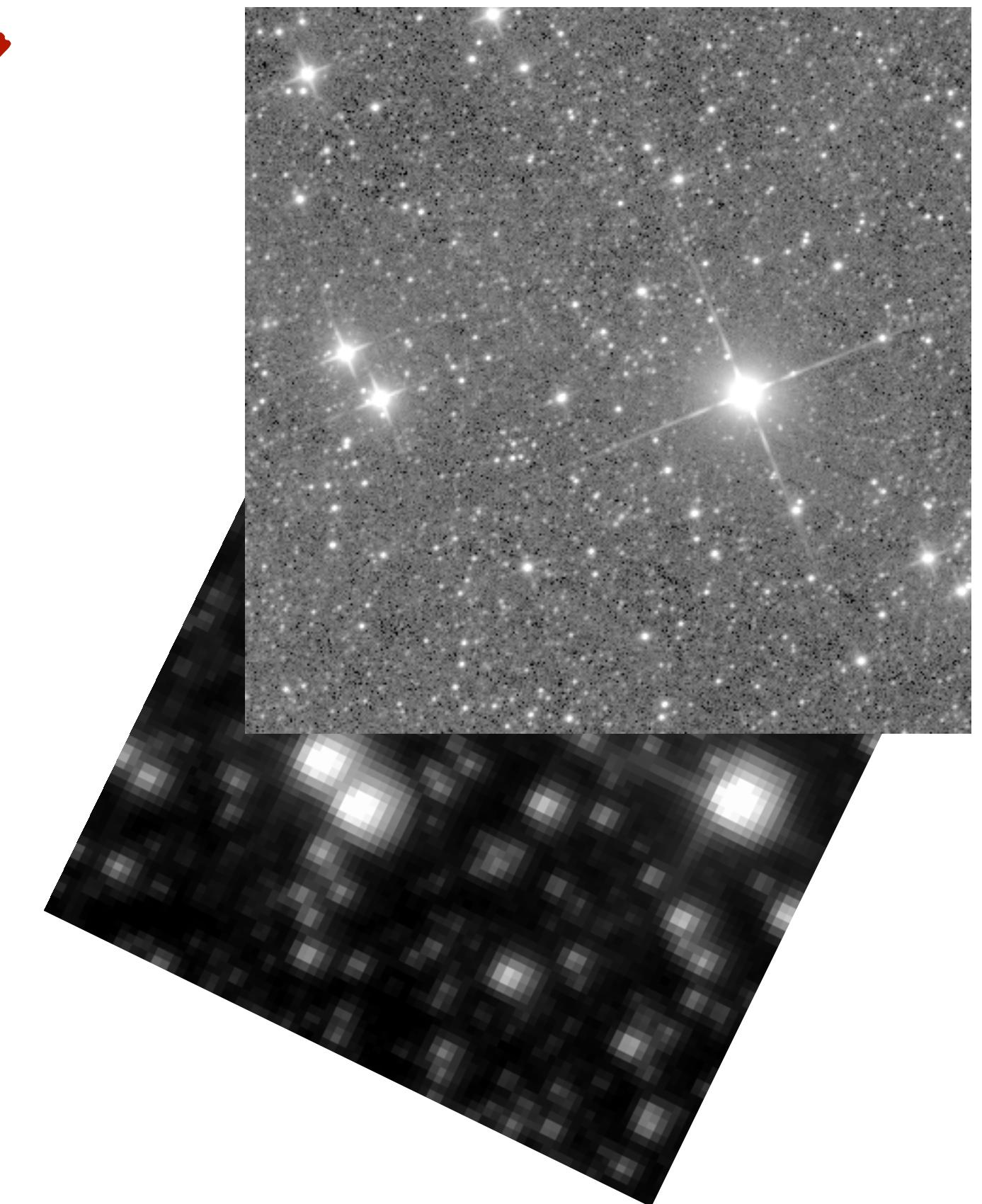
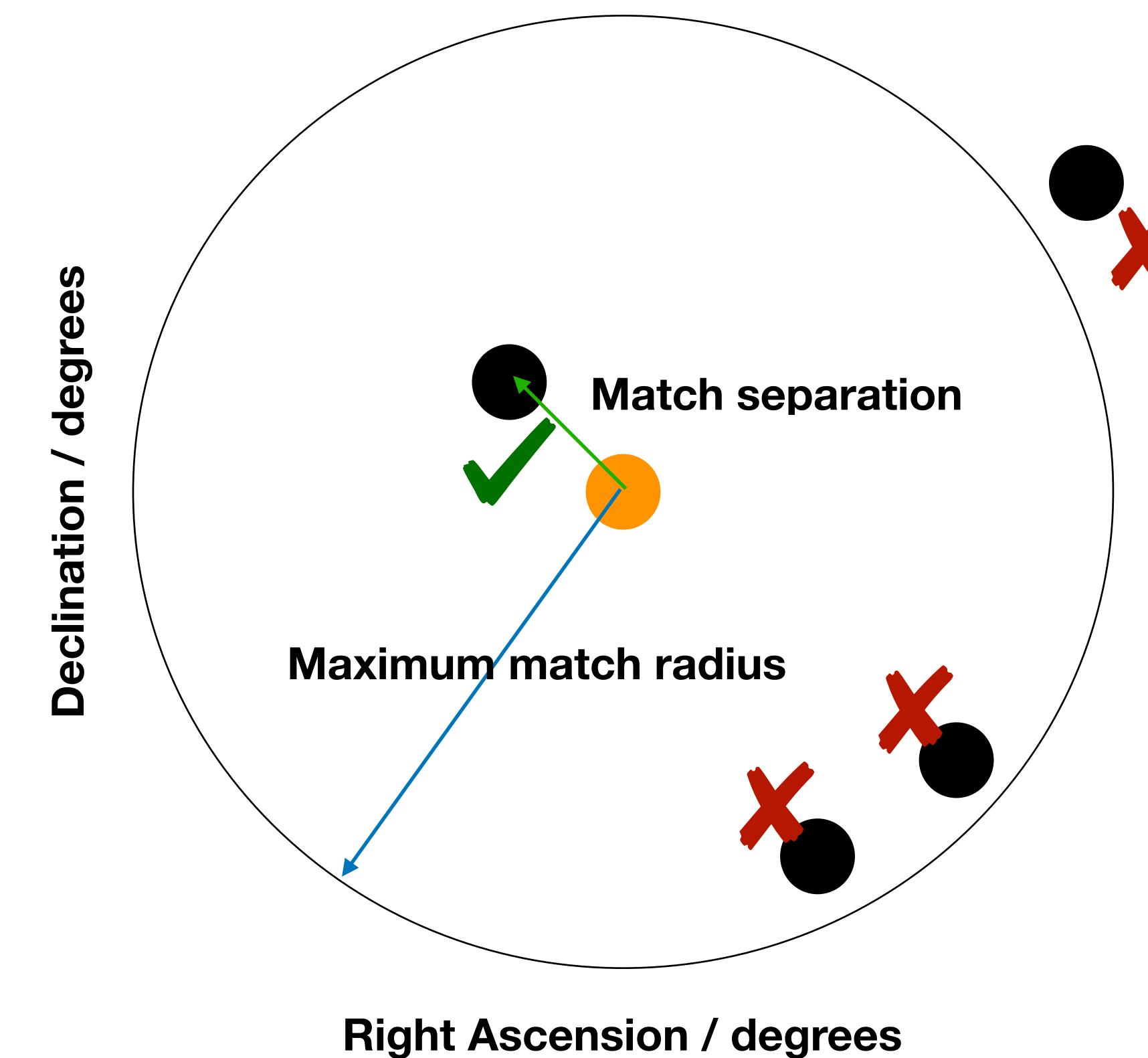
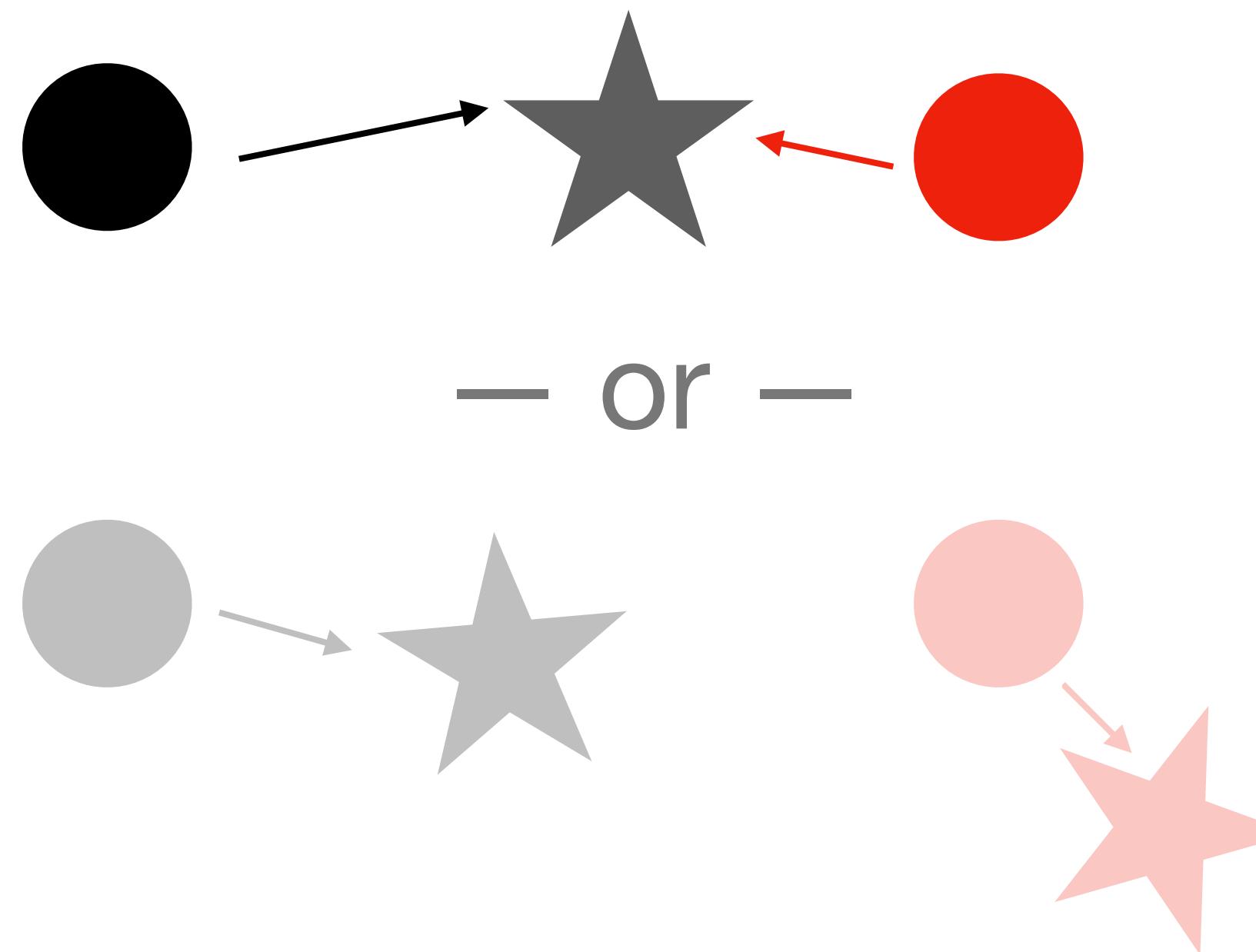


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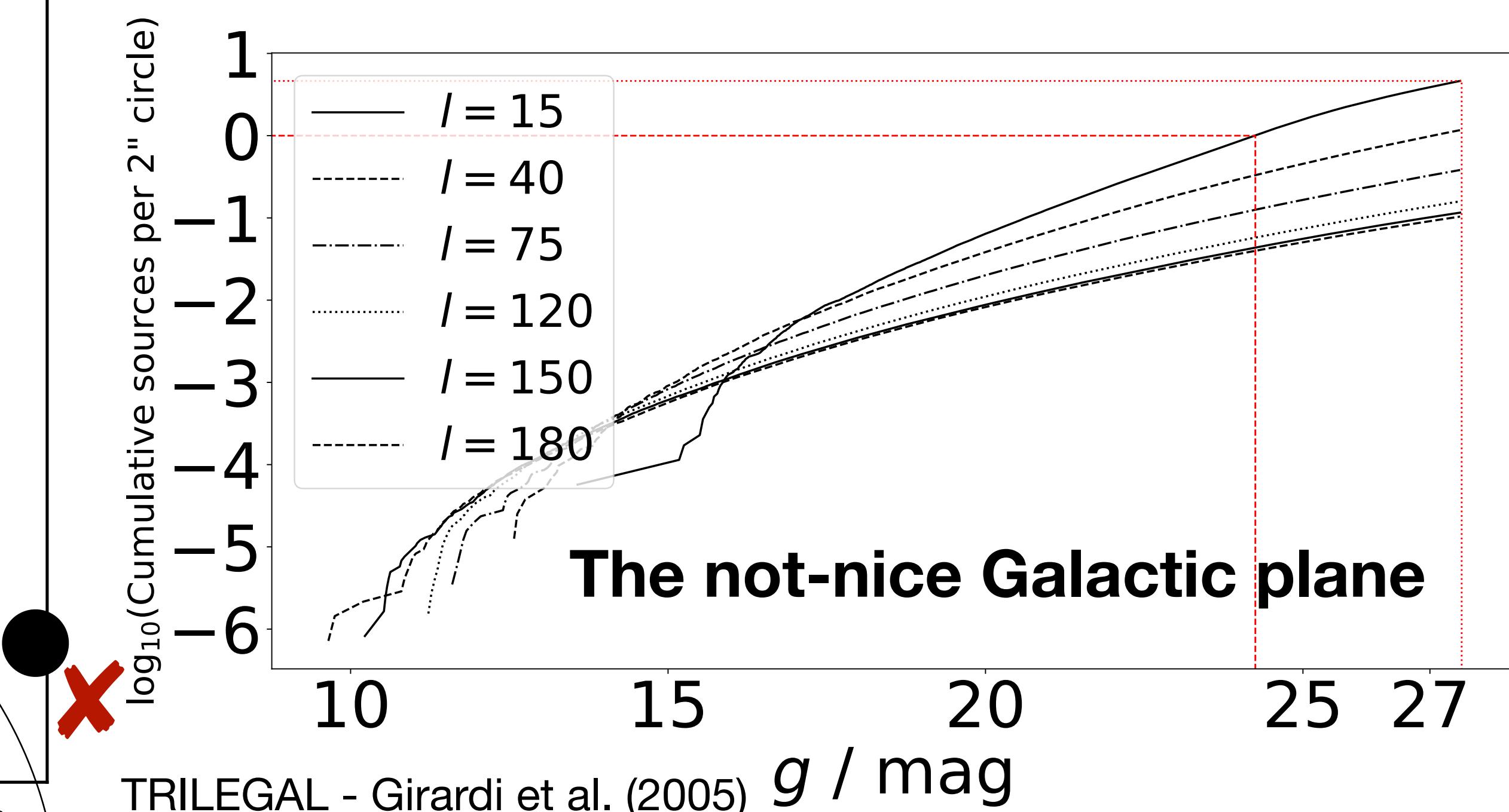
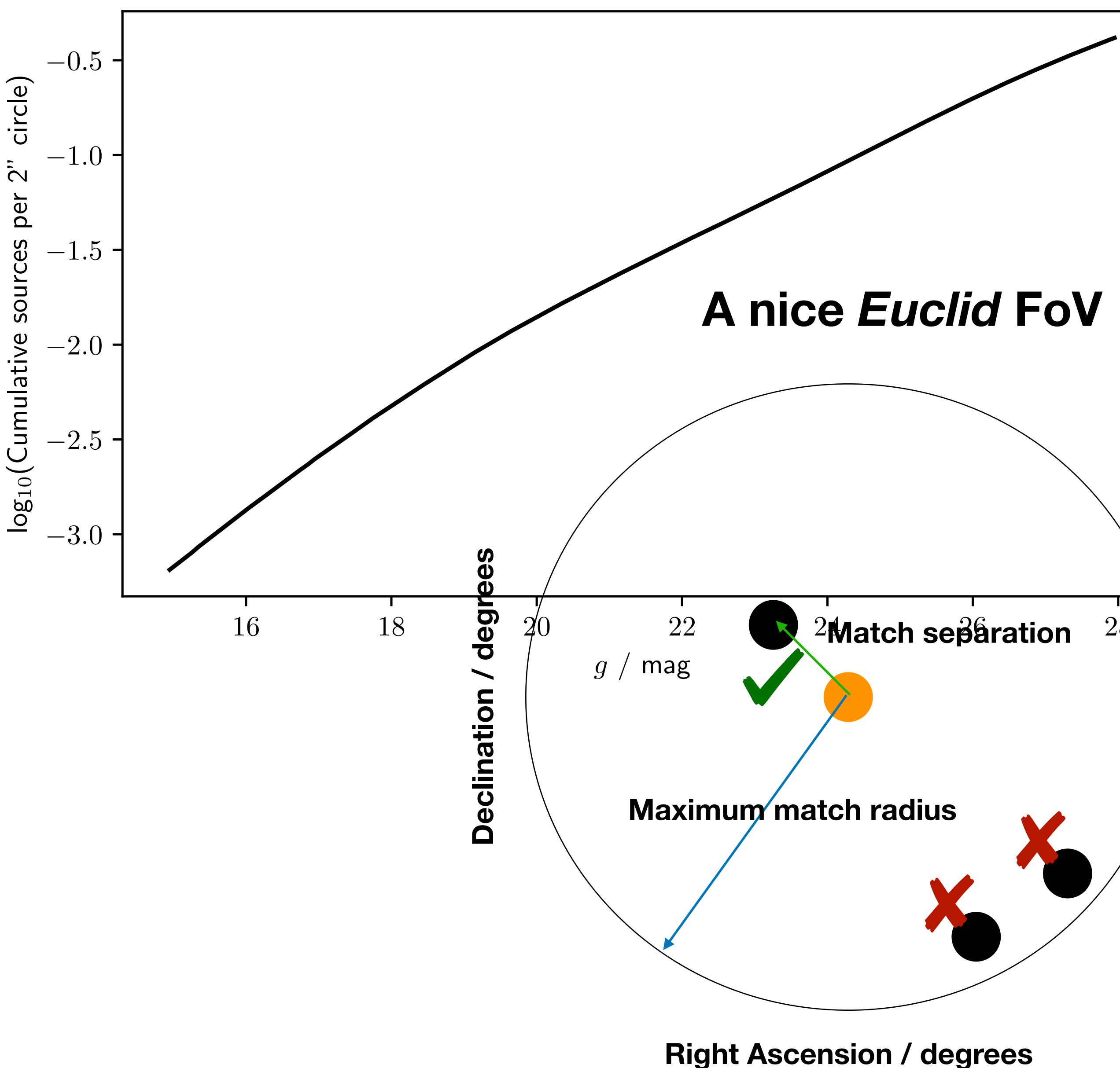
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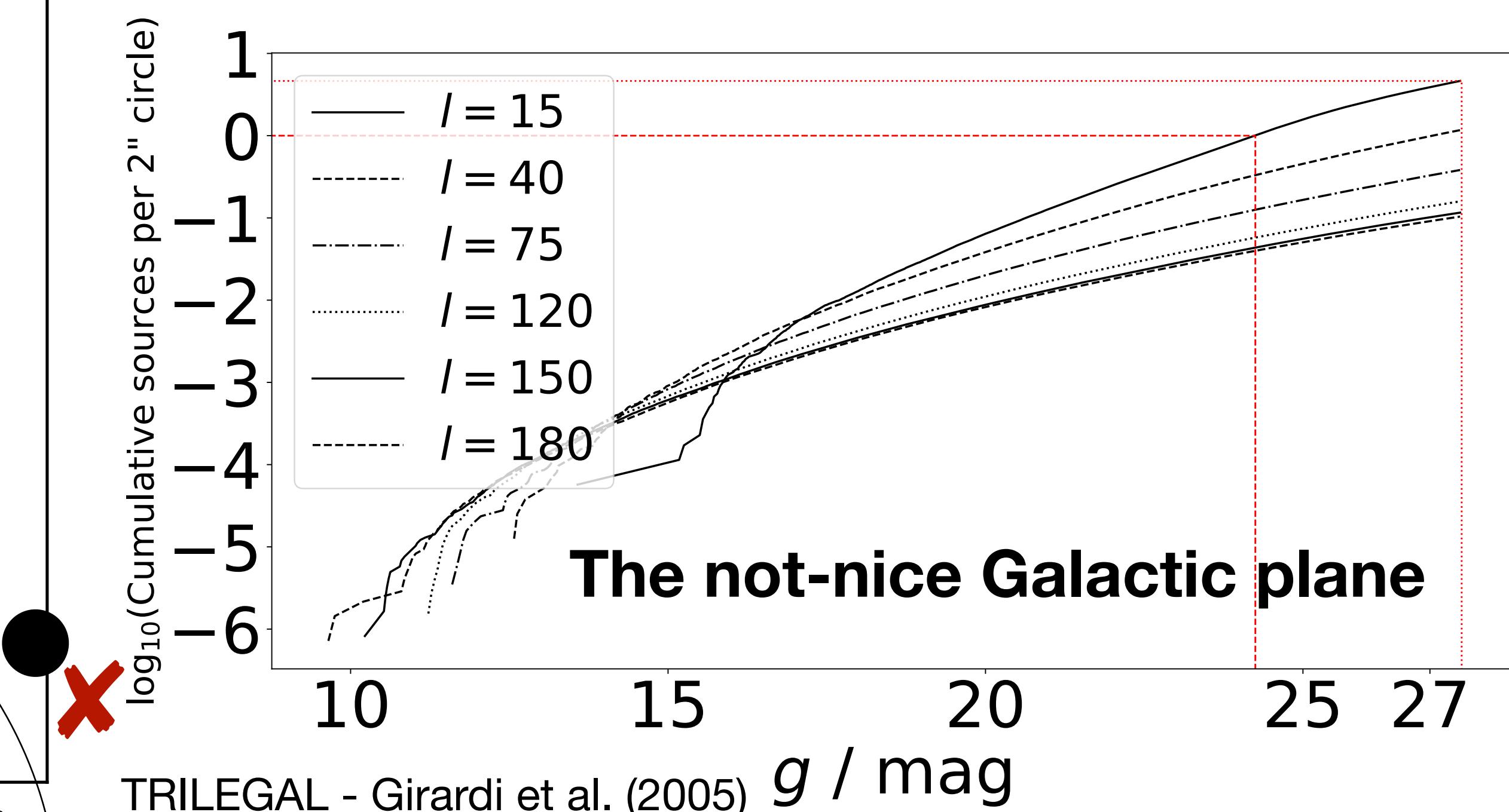
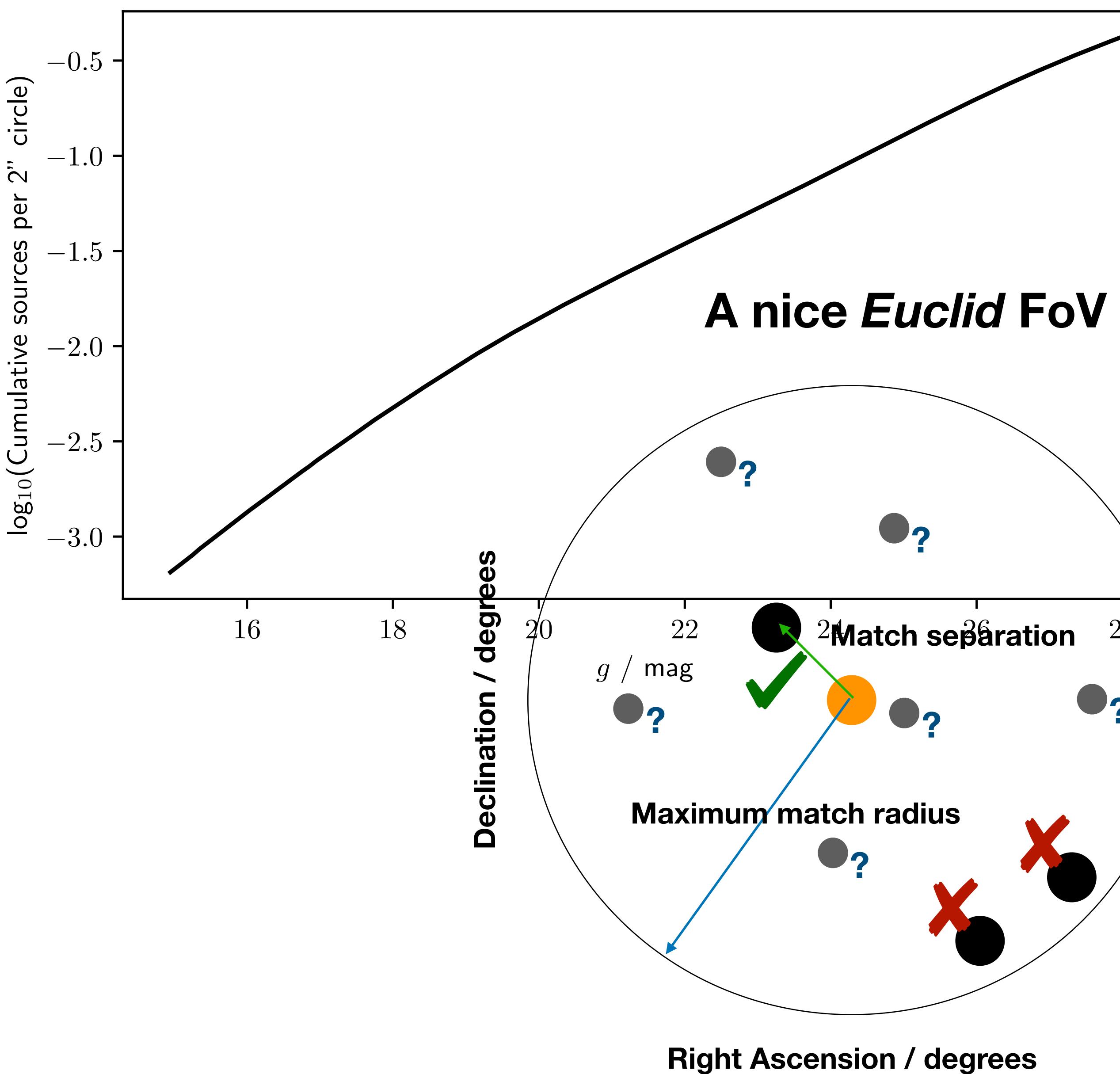
# “Simple” Cross-Matching



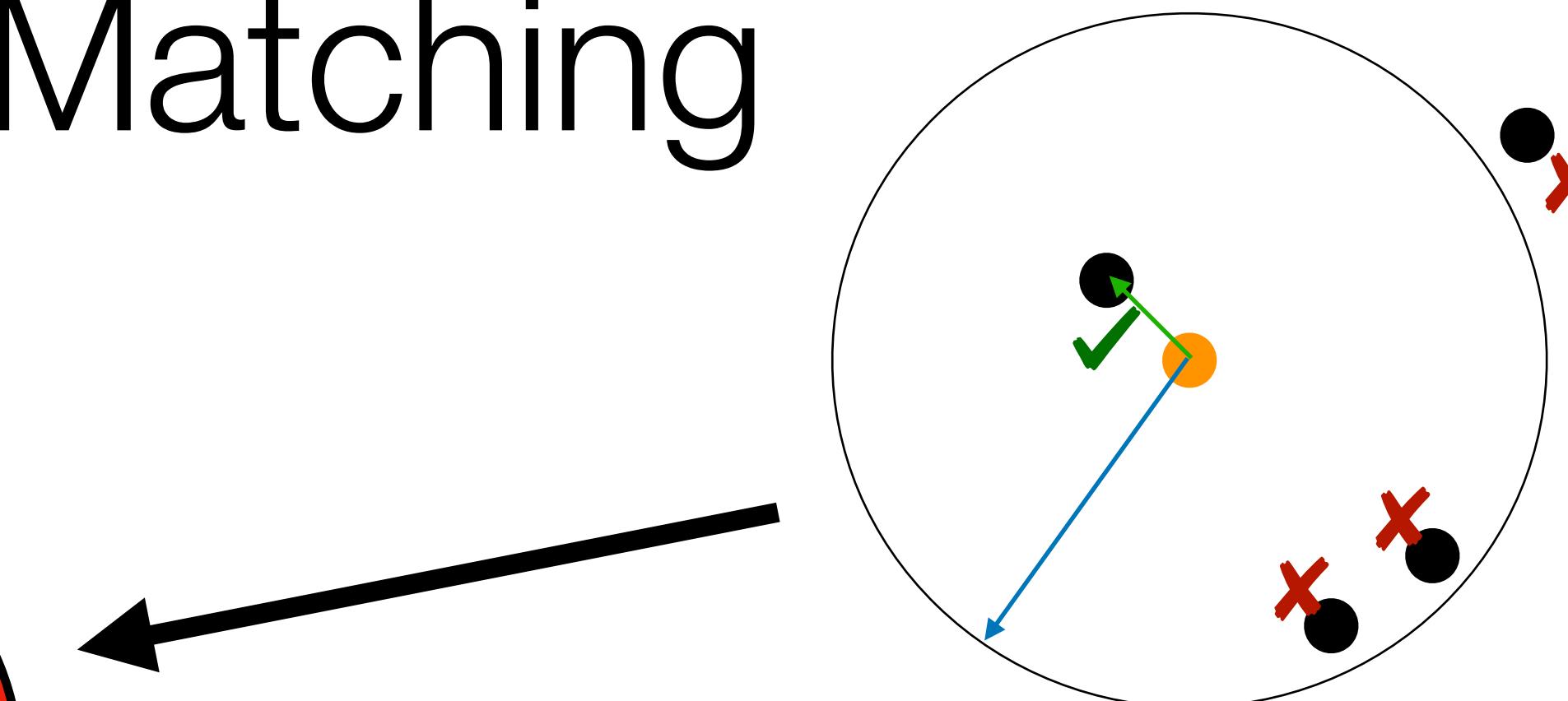
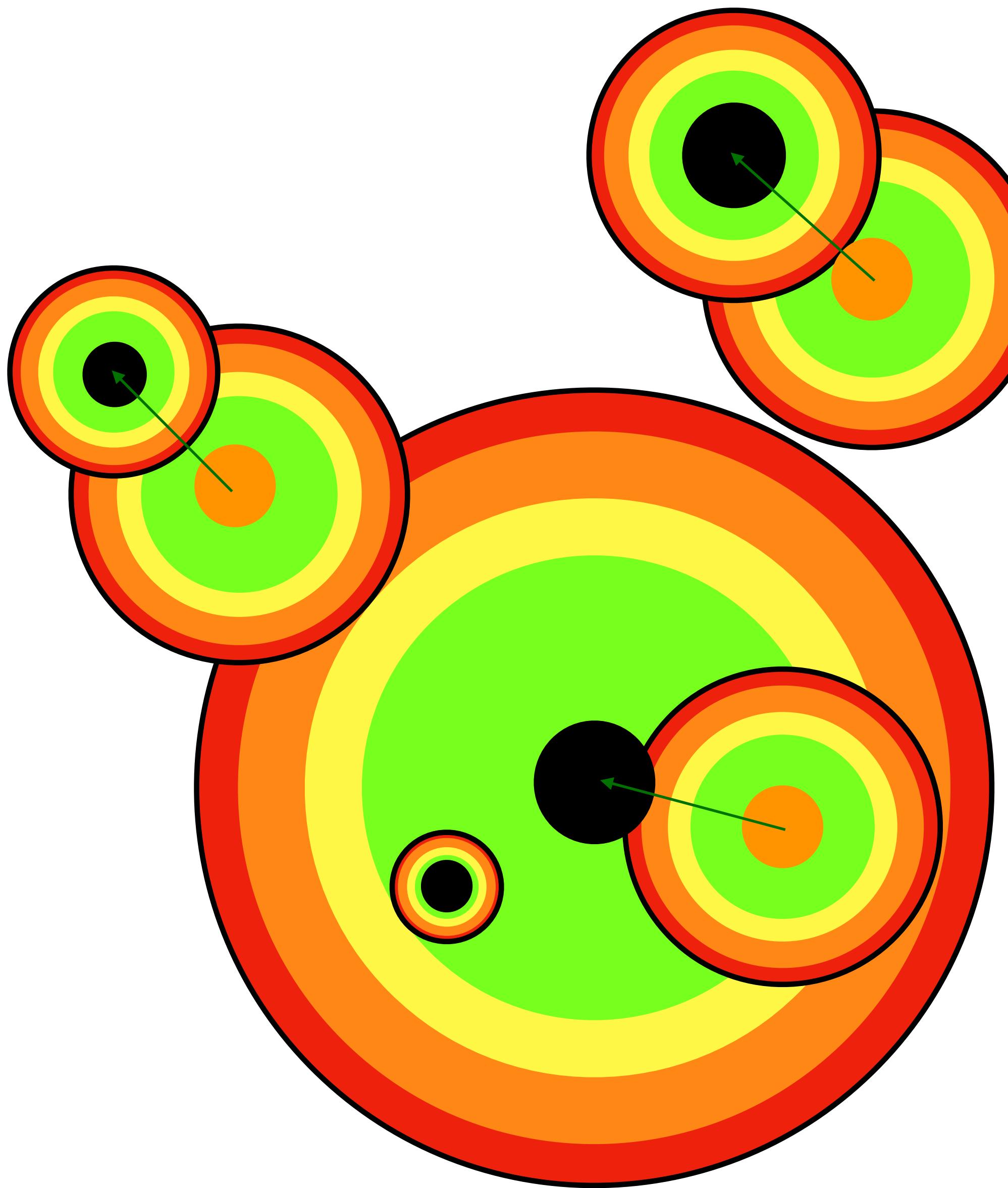
# The Problem With Vera C. Rubin Obs.'s LSST



# The Problem With Vera C. Rubin Obs.'s LSST



# Probabilistic Cross-Matching



Probability of two sources having their on-sky separation given the hypothesis they are counterparts

$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$

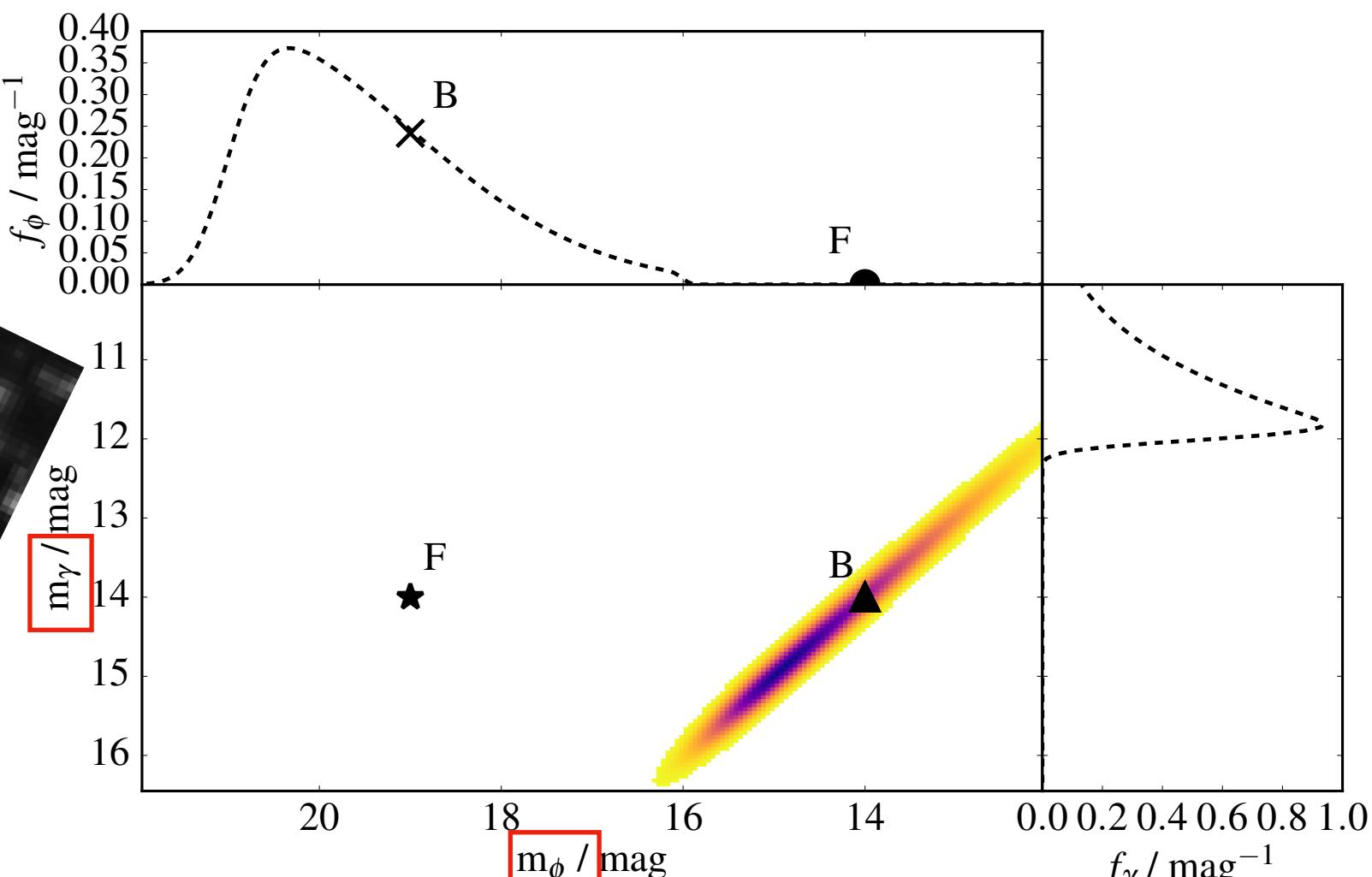
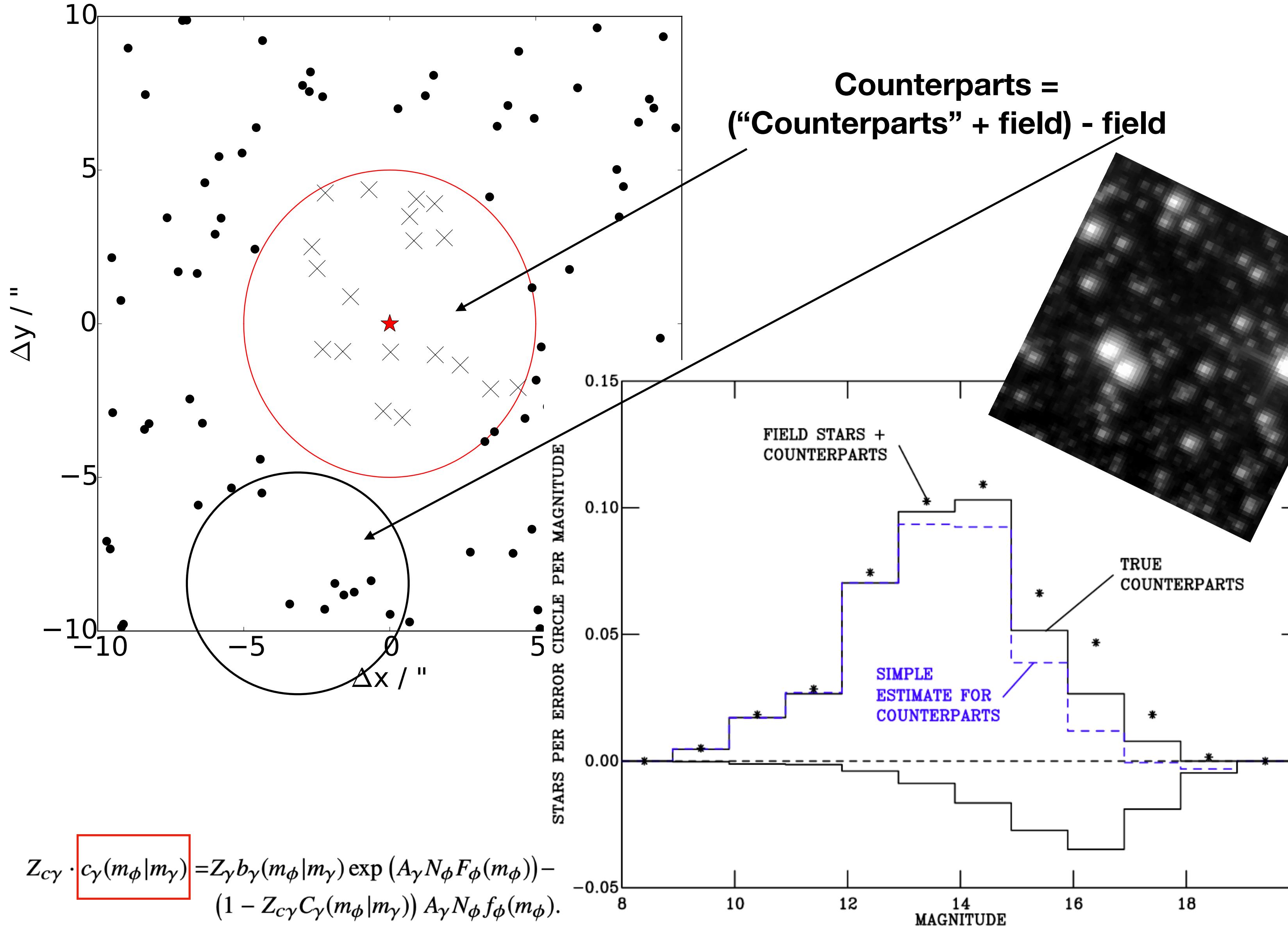
Probability of sources having their brightnesses given they are unrelated to one another (“field stars”)

Probability of sources having their brightnesses given they are counterparts

Wilson & Naylor (2018a)

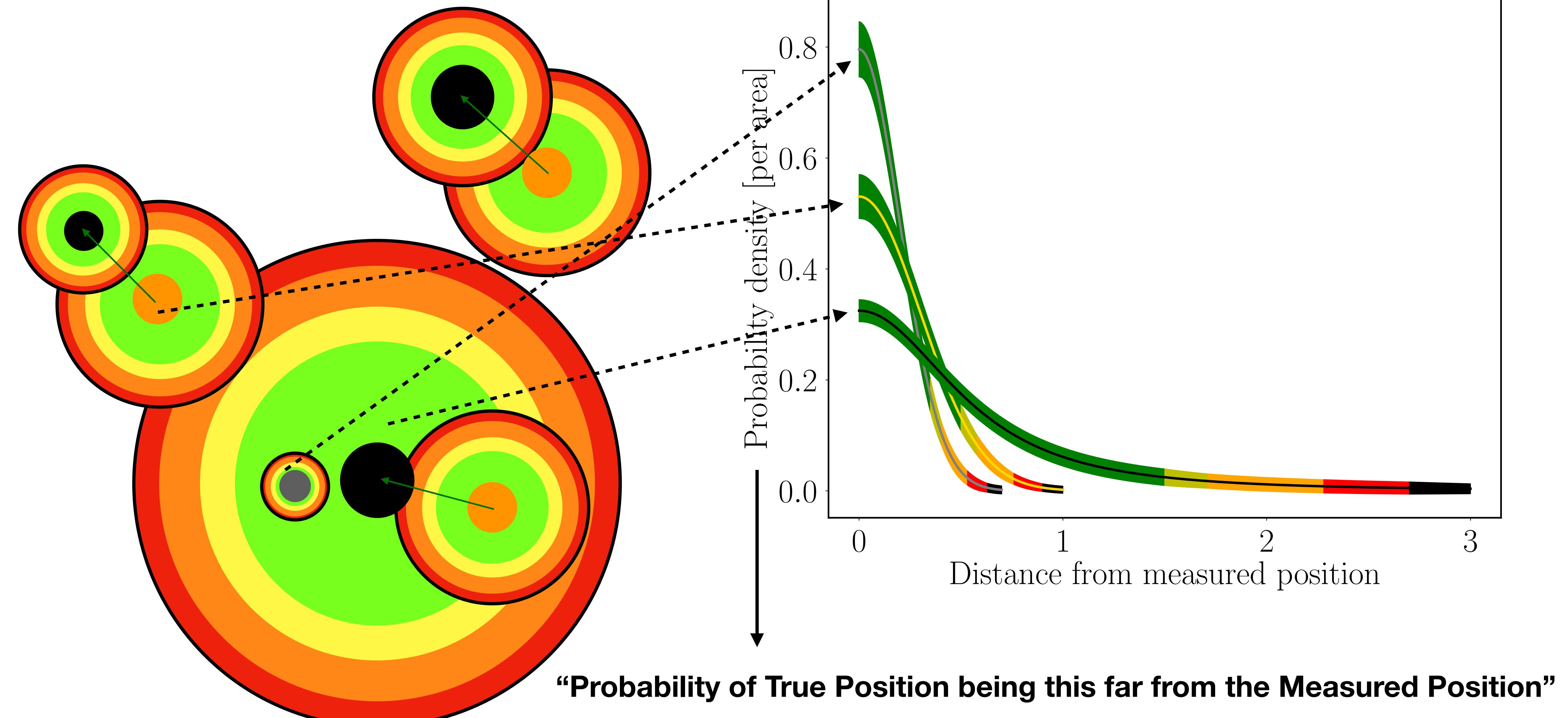
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# Photometry: Rejecting False Positives

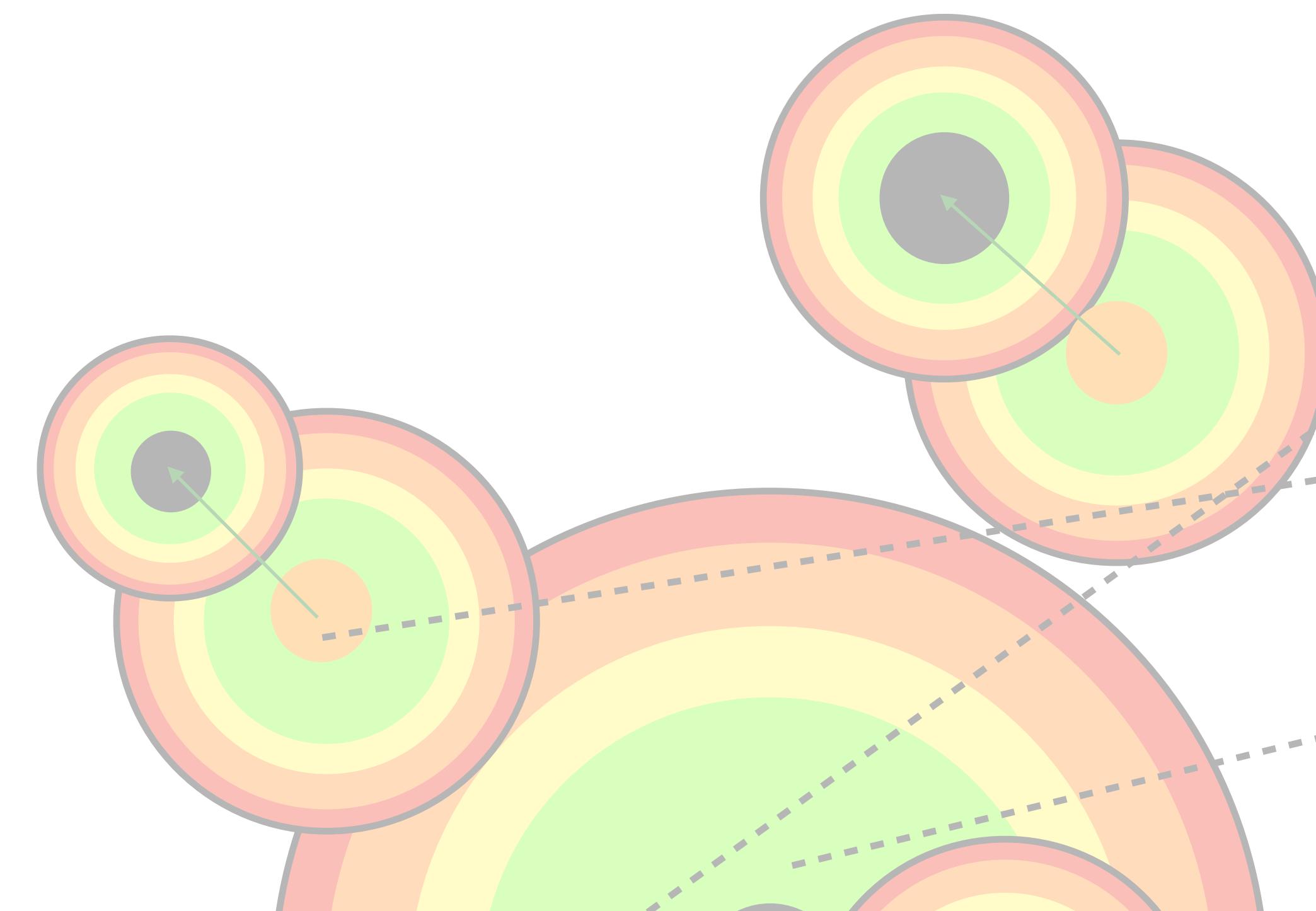


Where needed, photometry-based likelihoods ( $c$  and  $f$ ) allow us to mitigate high false positive rates

# Probabilistic Cross-Matching: the AUF



# Probabilistic Cross-Matching: the AUF



One assumption made in basically all literature: positional errors of sources are Gaussian!



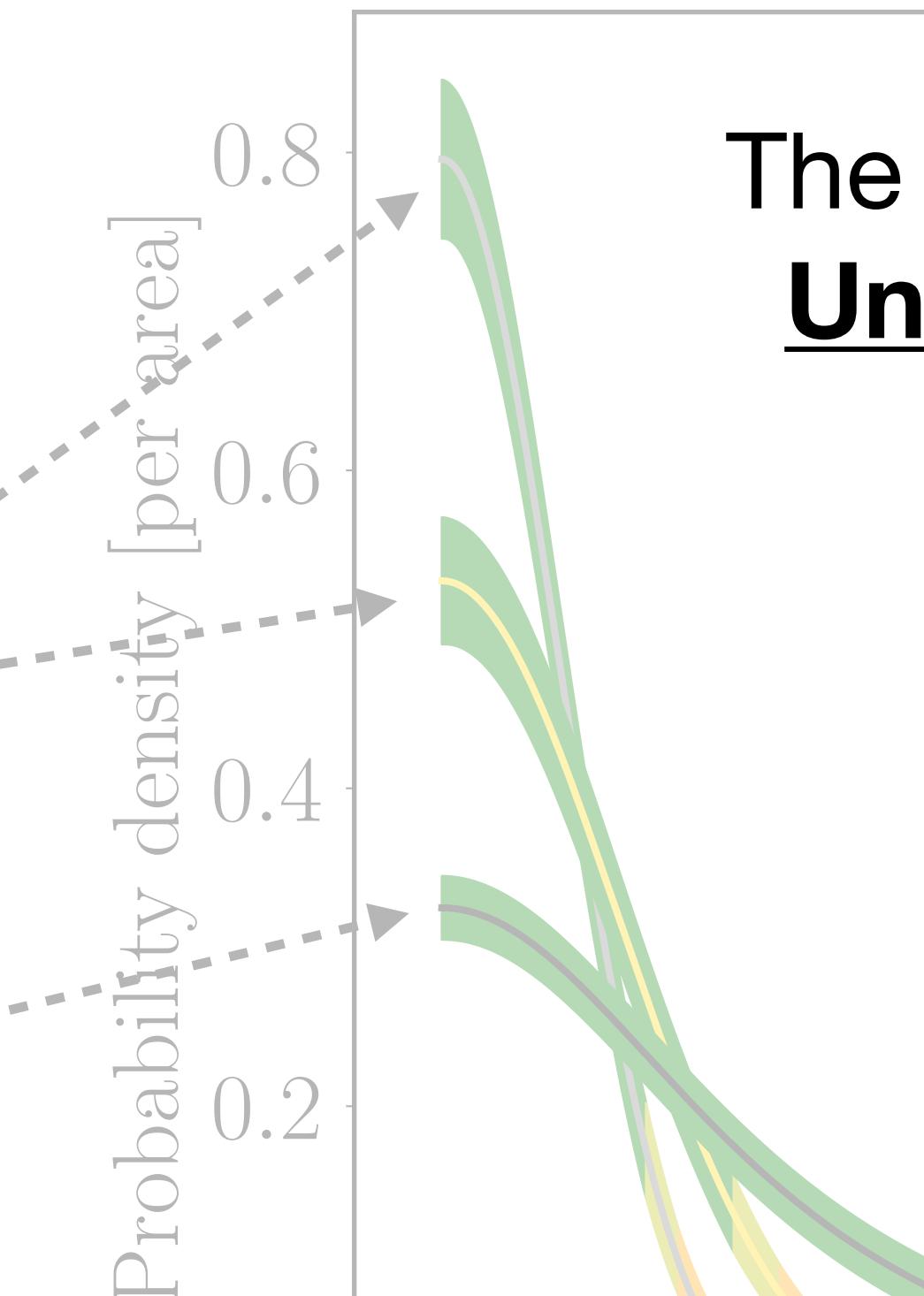
$$dp(r|id) = r \times e^{-r^2/2} dr.$$

de Ruiter, Willis, & Arp (1977)

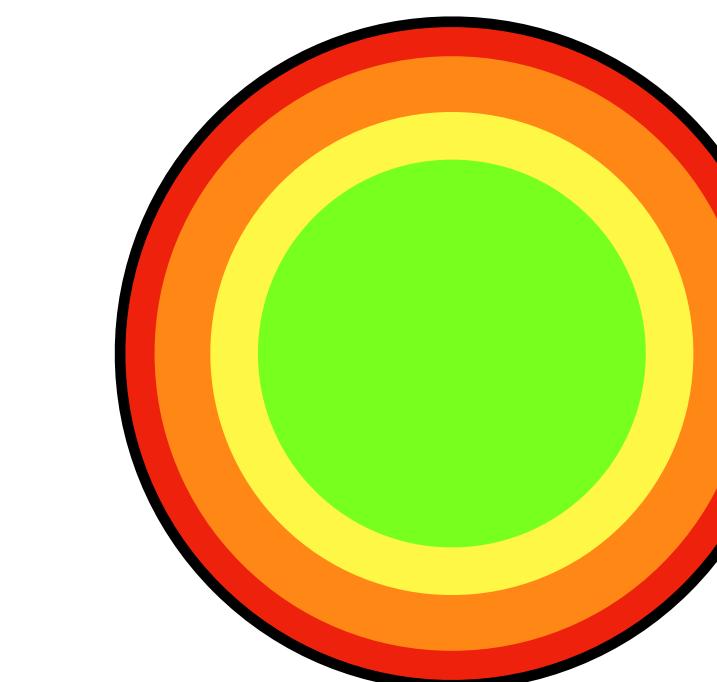
$$P(i) = \frac{\frac{Xc(m_i) g(\Delta x_i, \Delta y_i)}{Nf(m_i)}}{1 - X + \sum_j \frac{Xc(m_j) g(\Delta x_j, \Delta y_j)}{Nf(m_j)}}$$

Naylor, Broos, & Feigelson (2013)

“Probability of True Position being this far from the Measured Position”



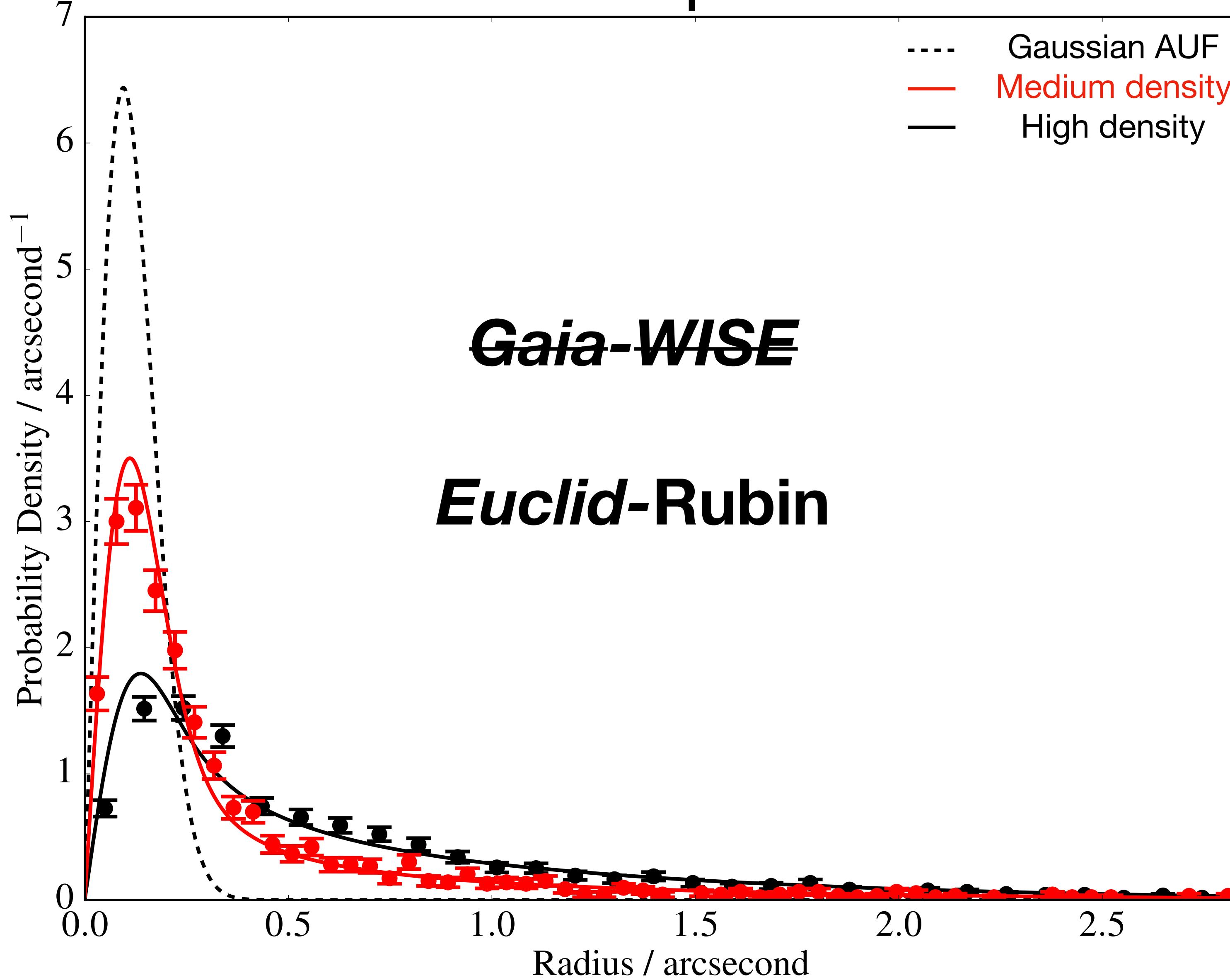
The generalised Astrometric Uncertainty Function can be of any form



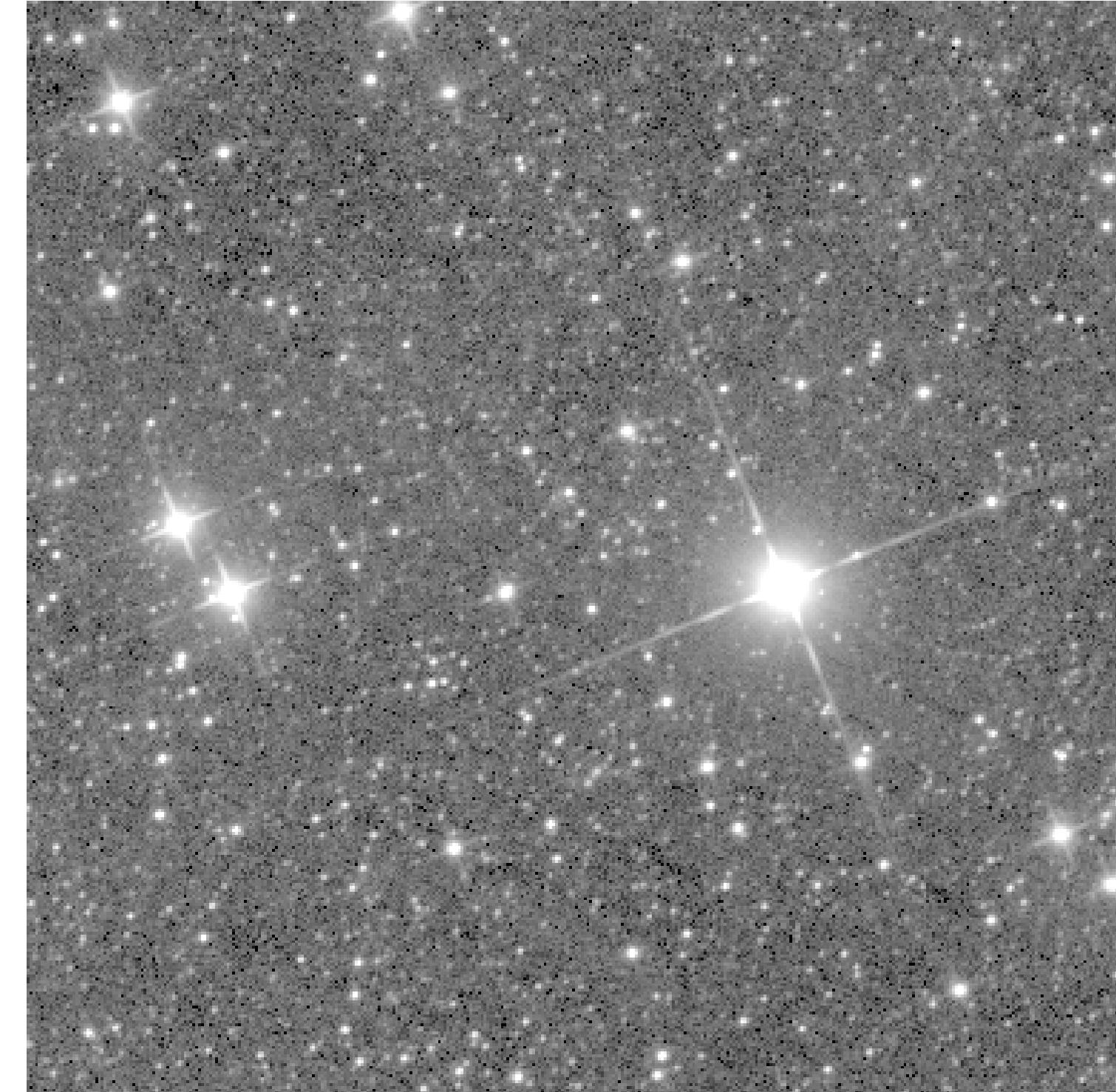
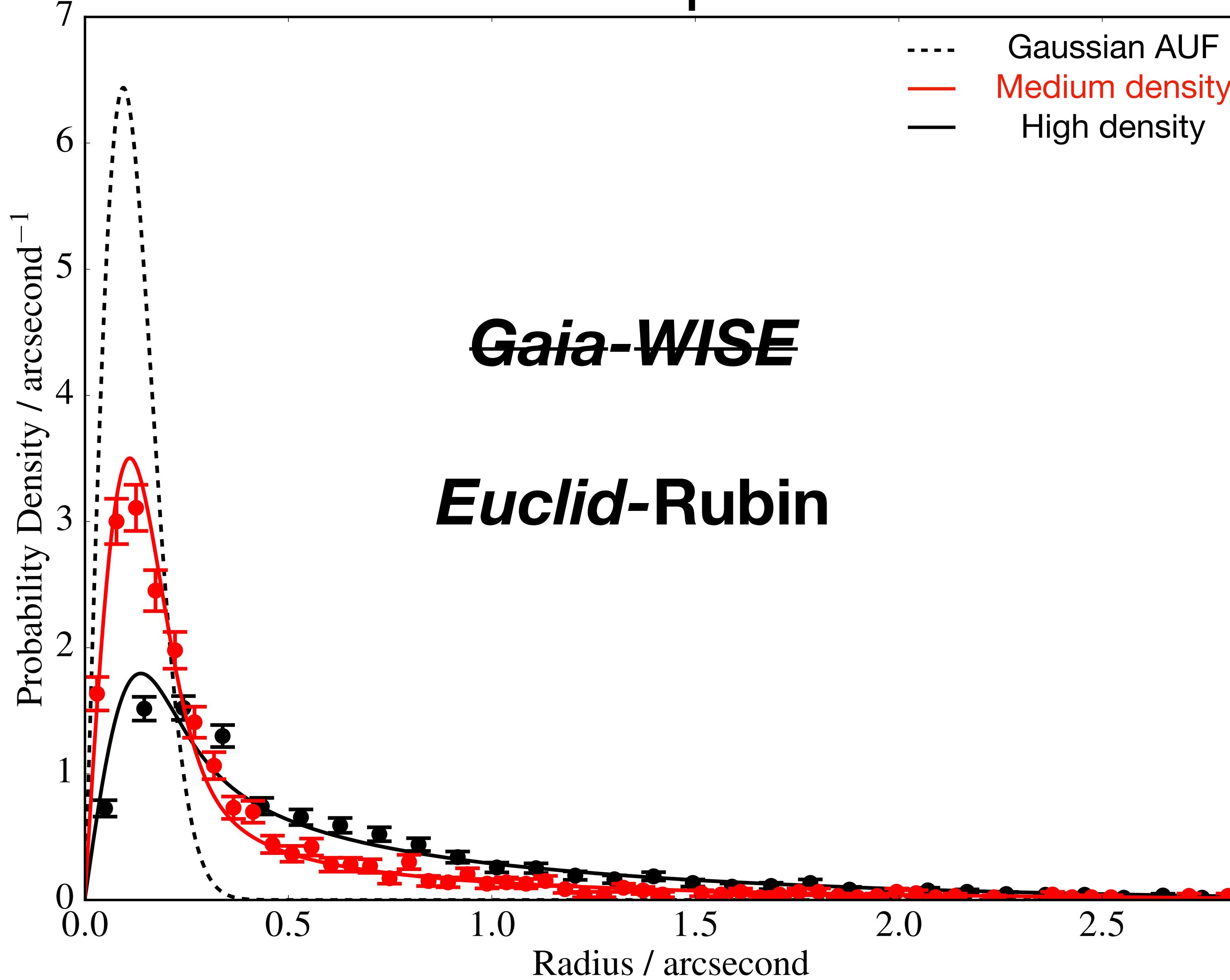
$$p(D|H) = \int p(m|H) \prod_{i=1}^n p_i(x_i|m, H) d^3m$$

Budavári & Szalay (2008)

# Additional Components of the AUF

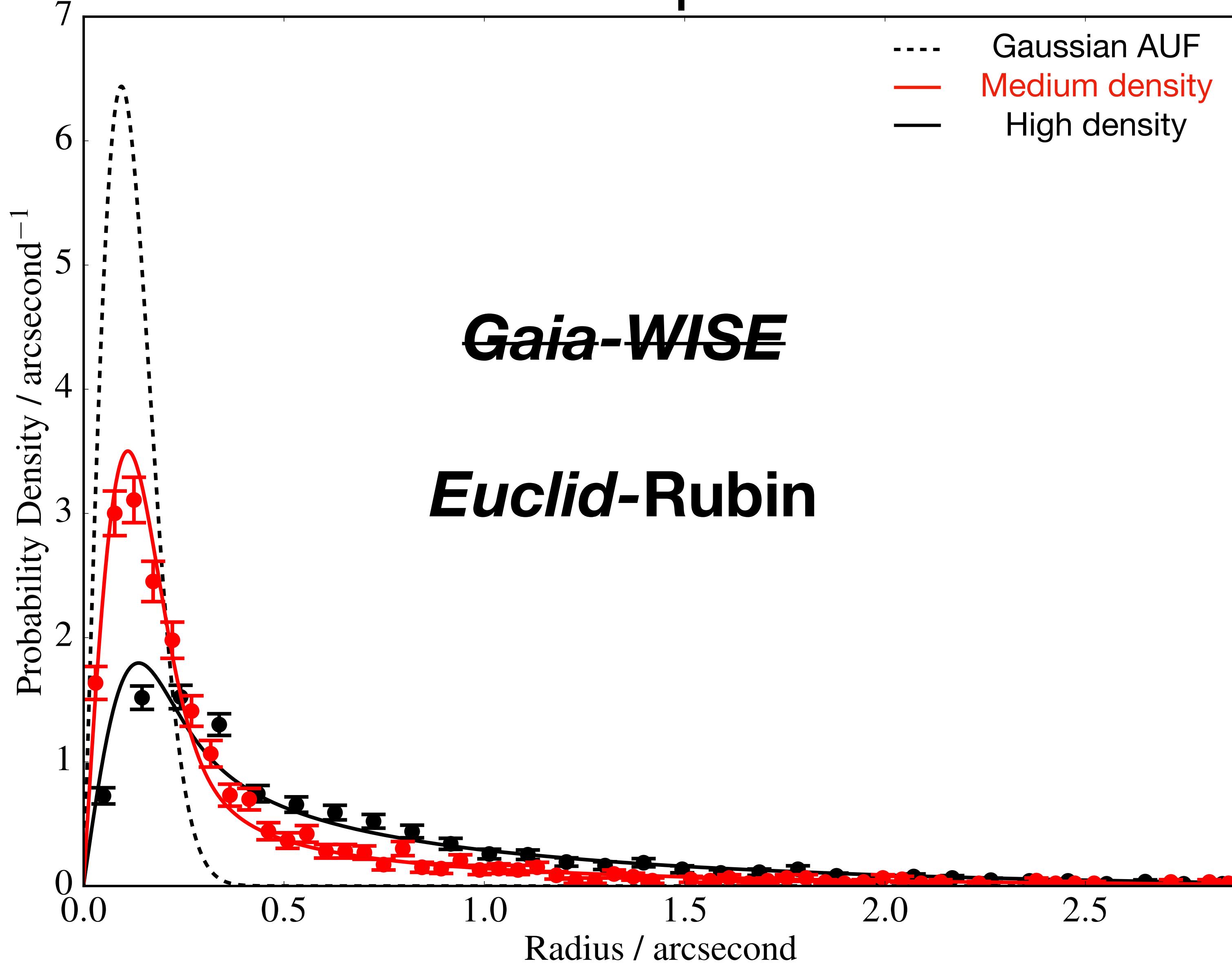


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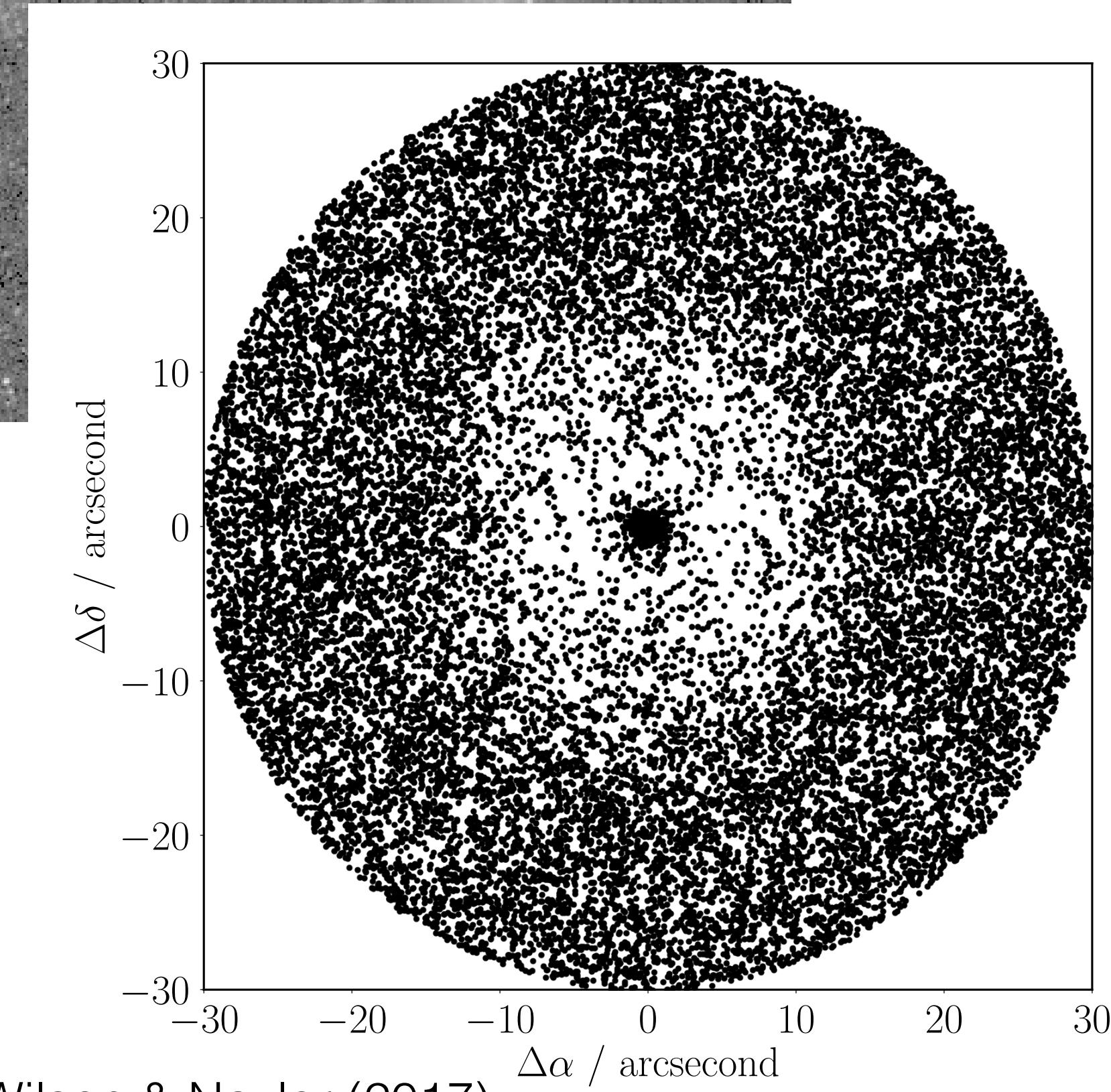
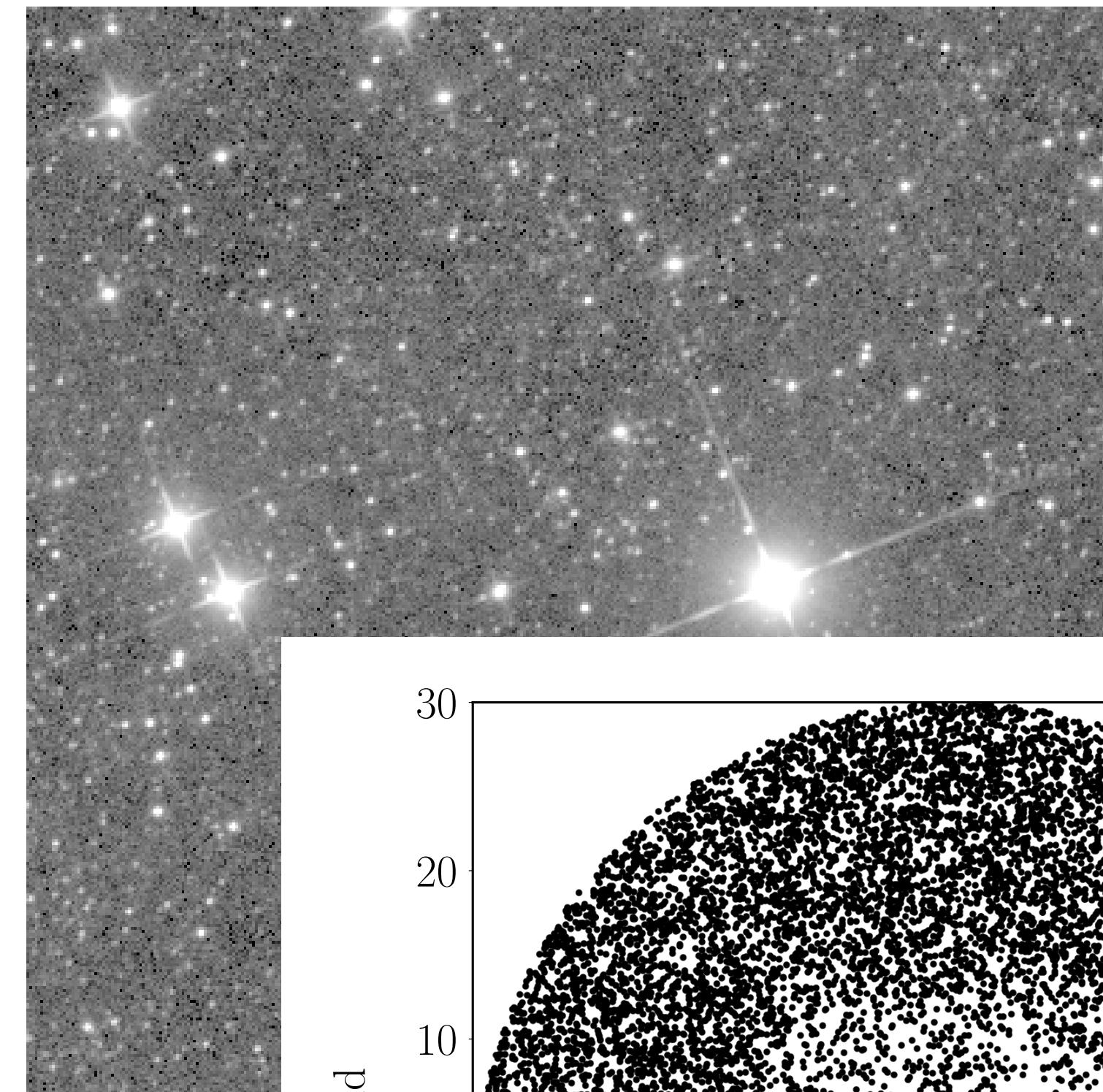
# Additional Components of the AUF

(and any other systematic — e.g. proper motions, cf. Wilson 2023, RASTI)



WISE - Wright et al. (2010)

Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

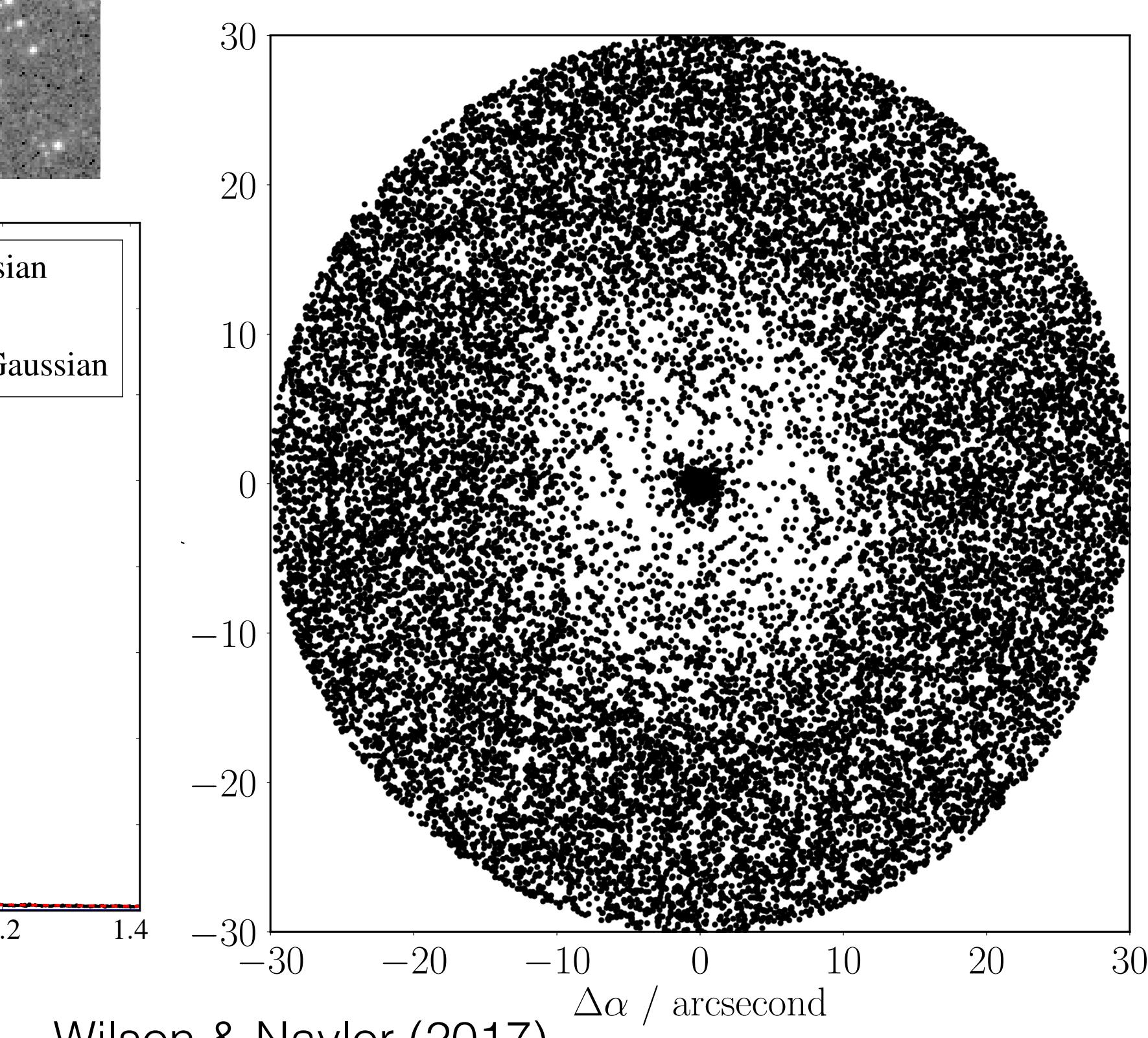
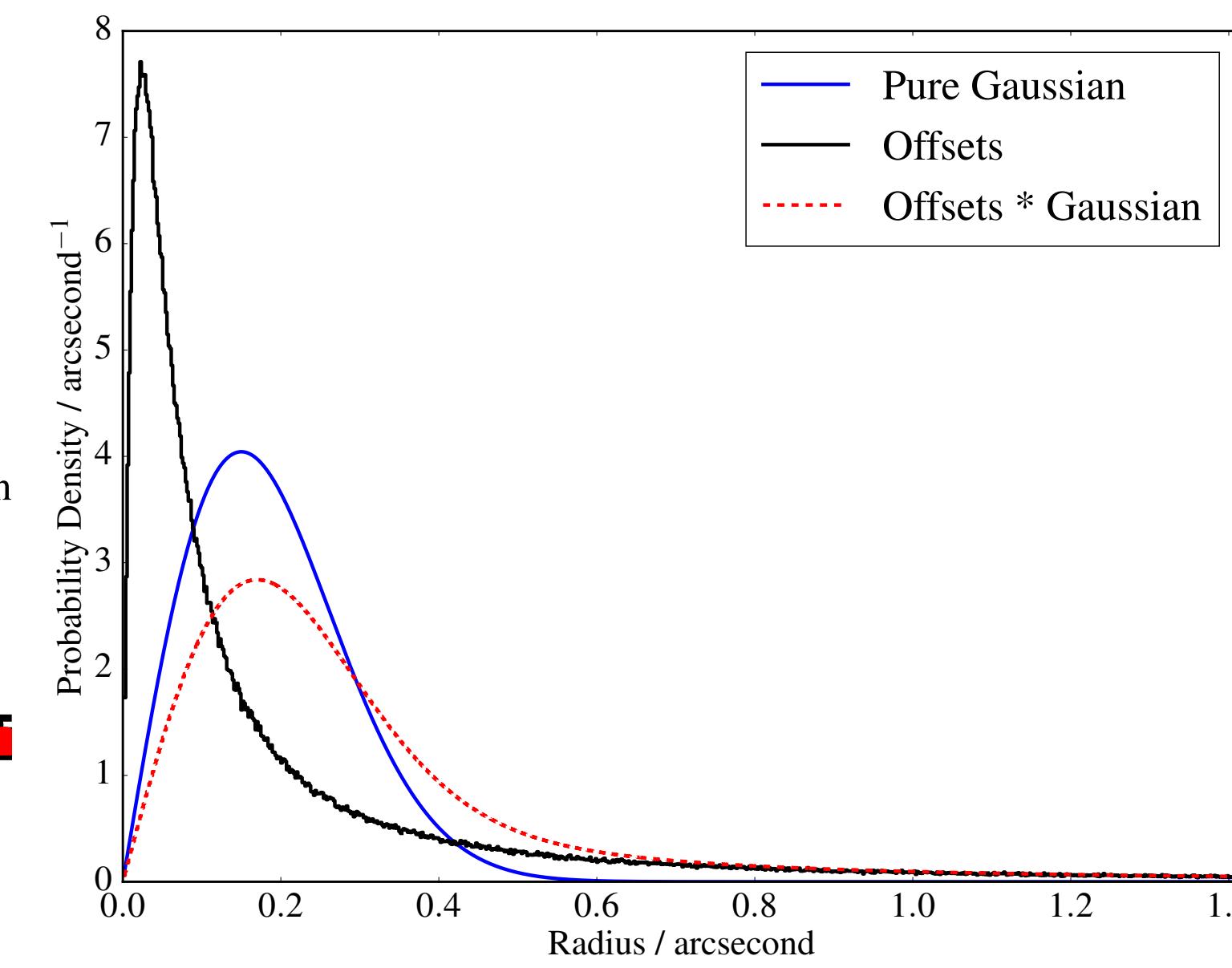
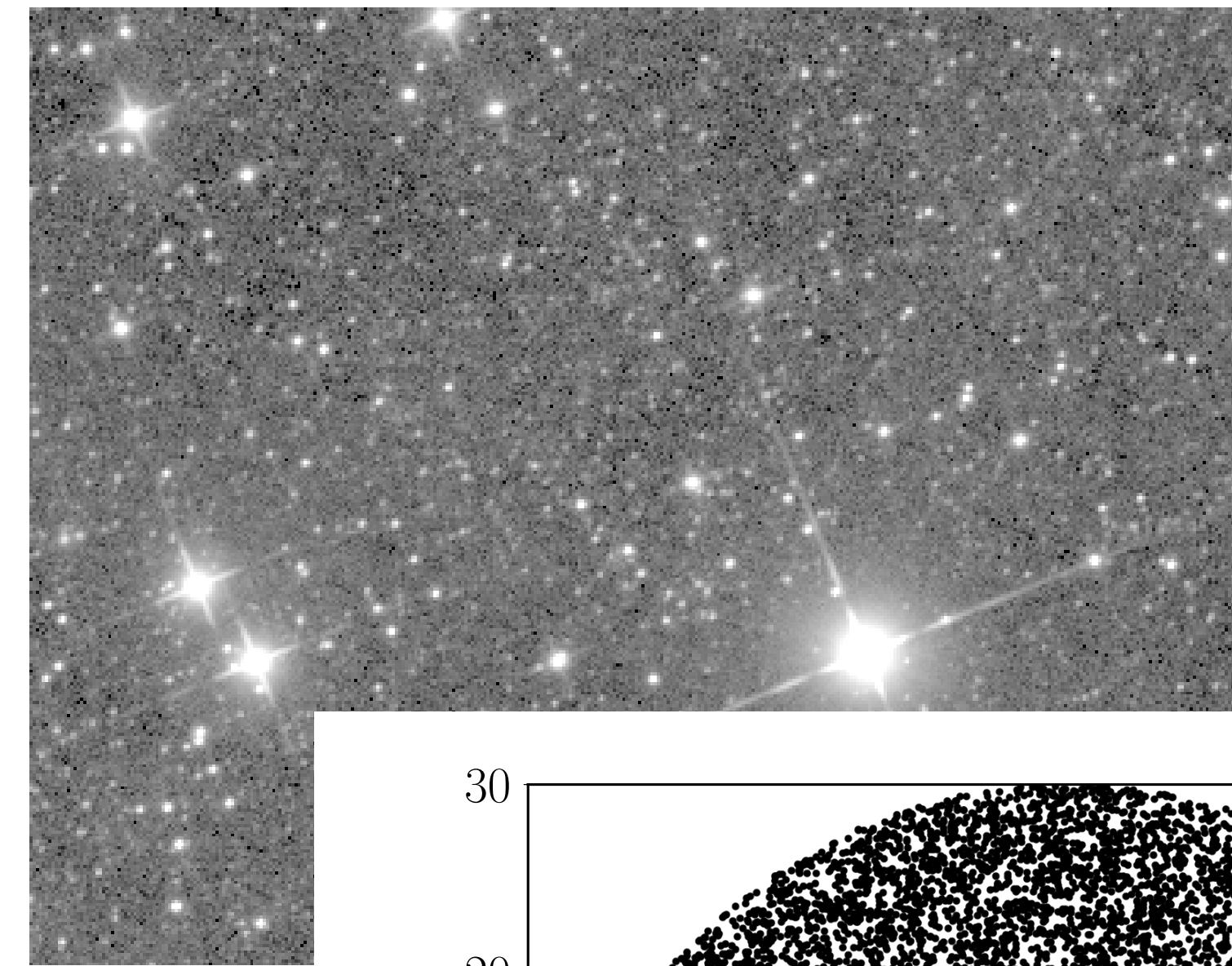
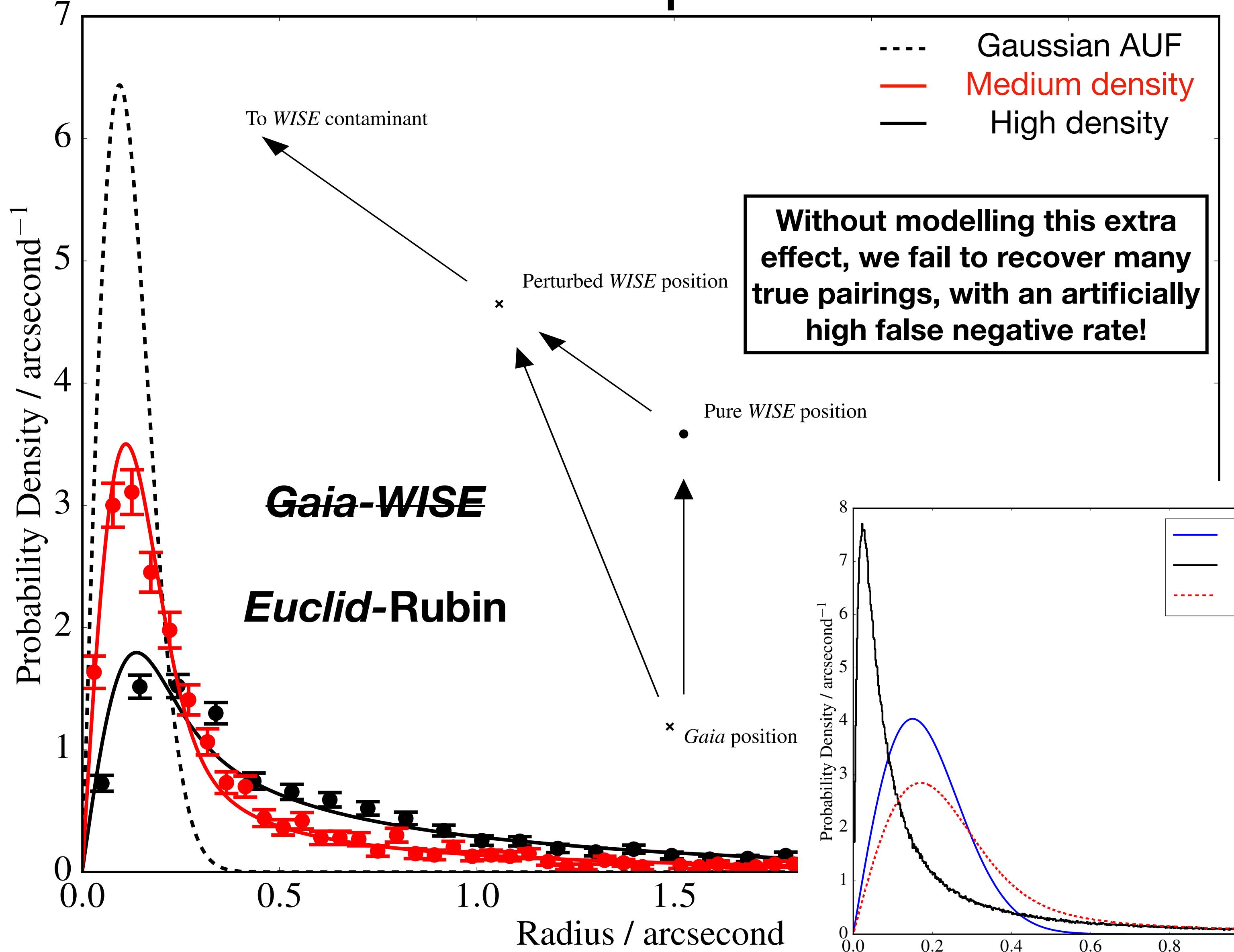


Wilson & Naylor (2017)

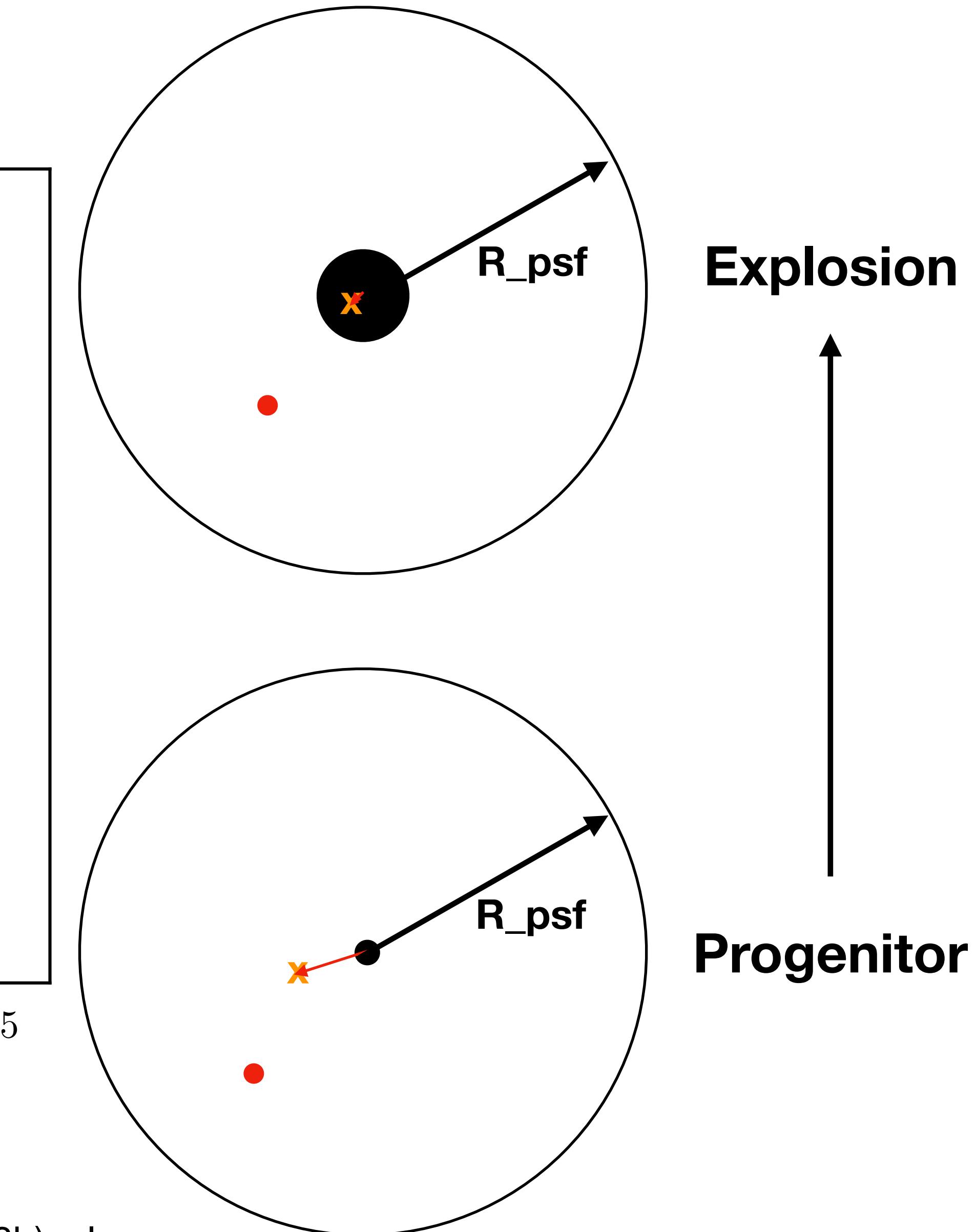
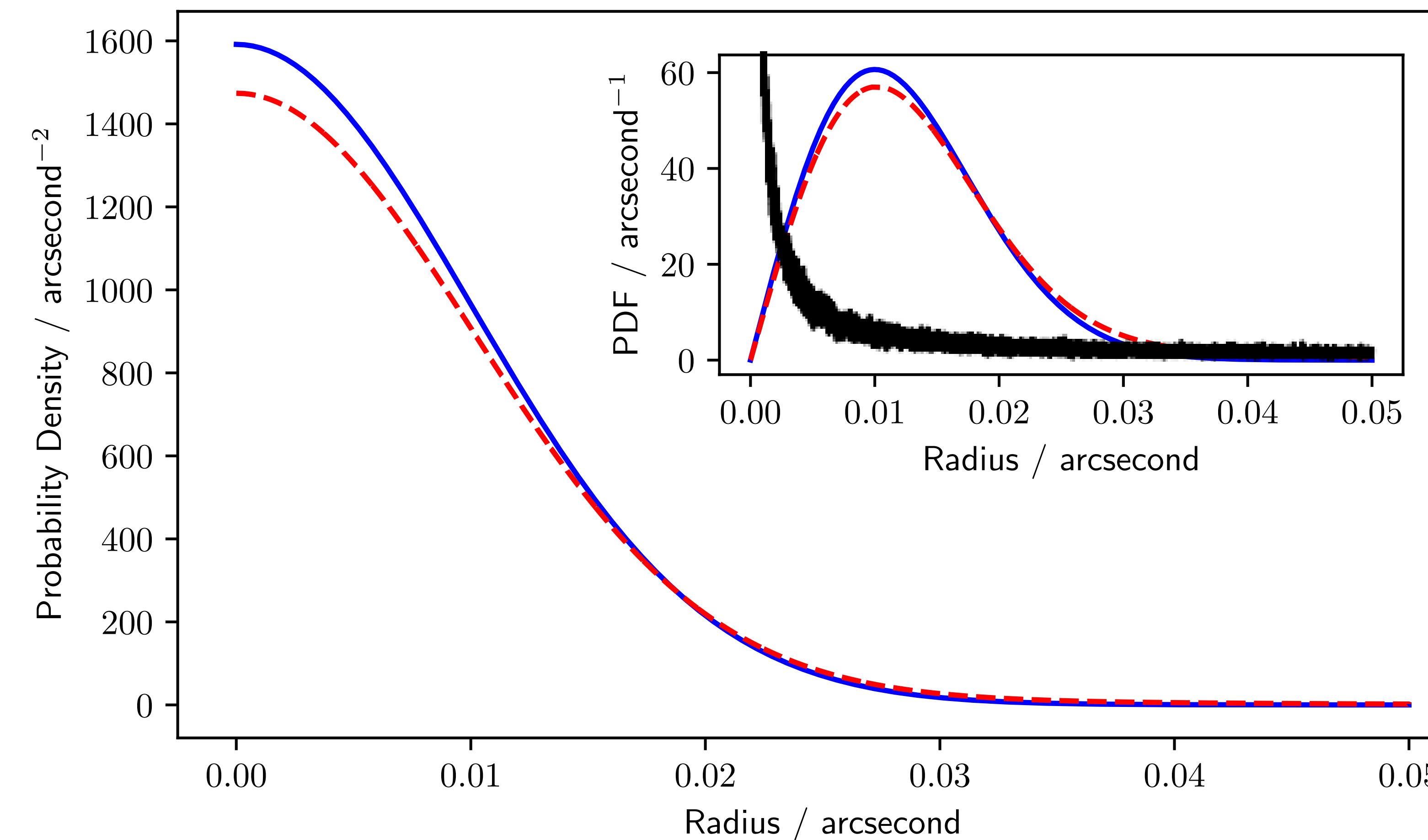
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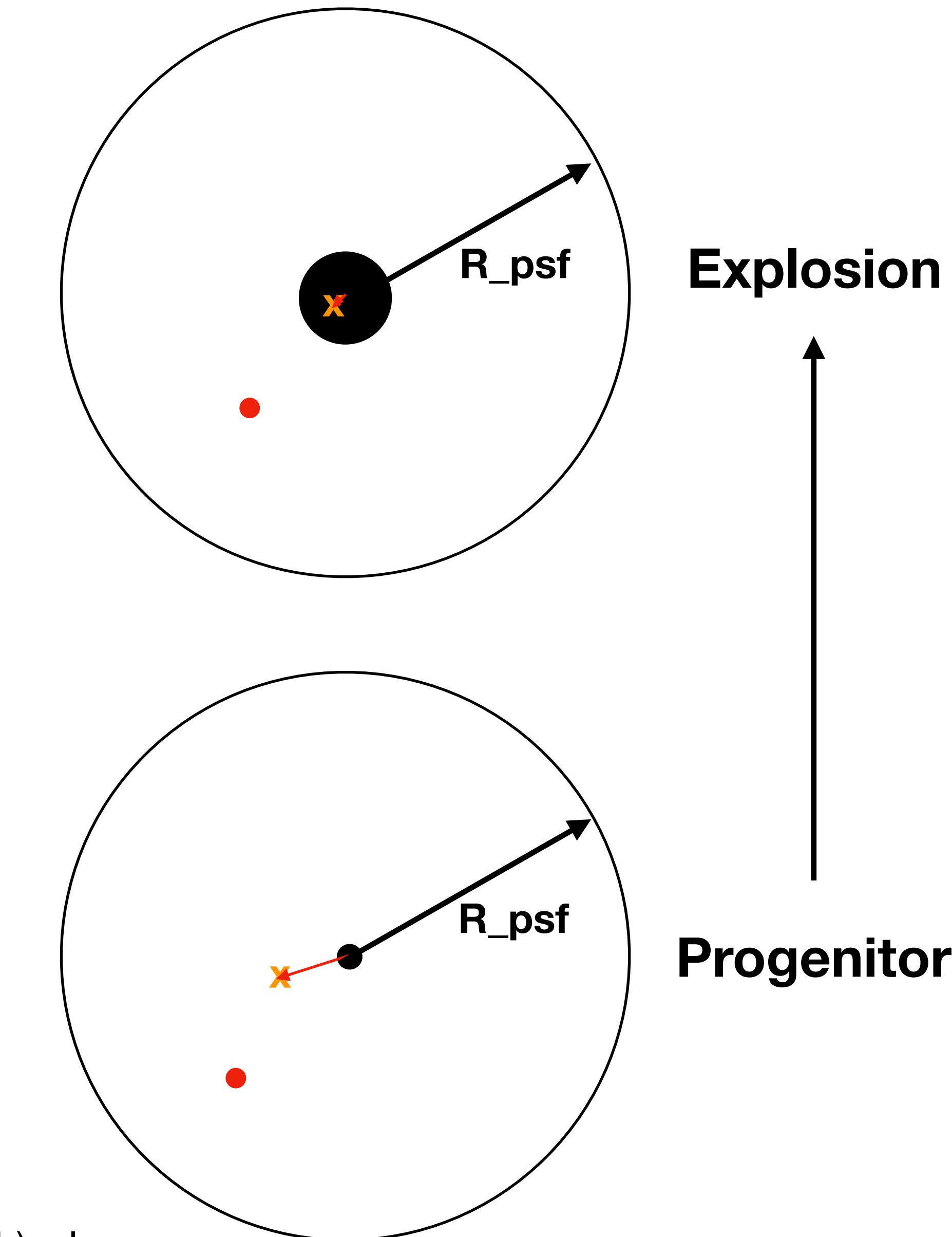
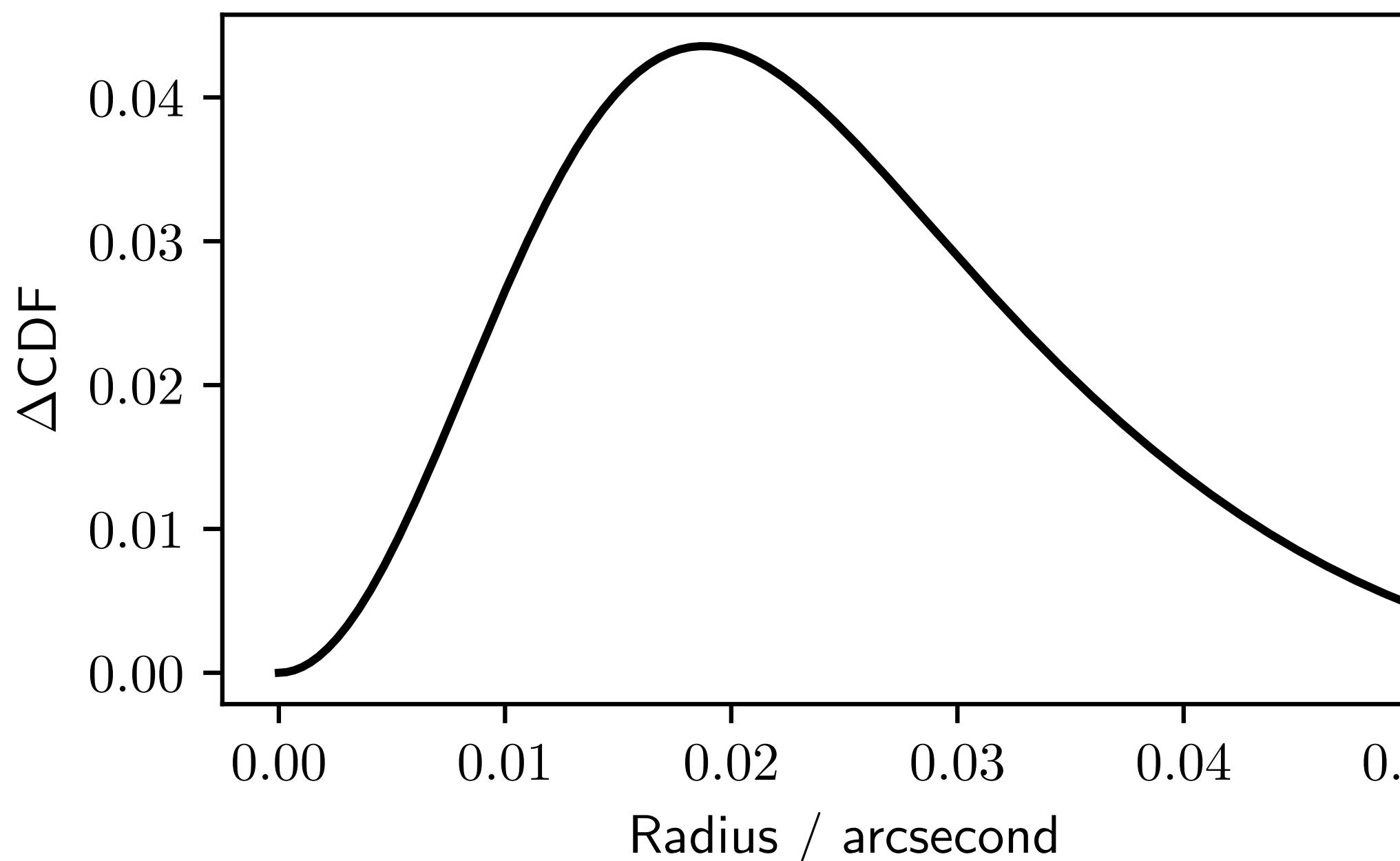
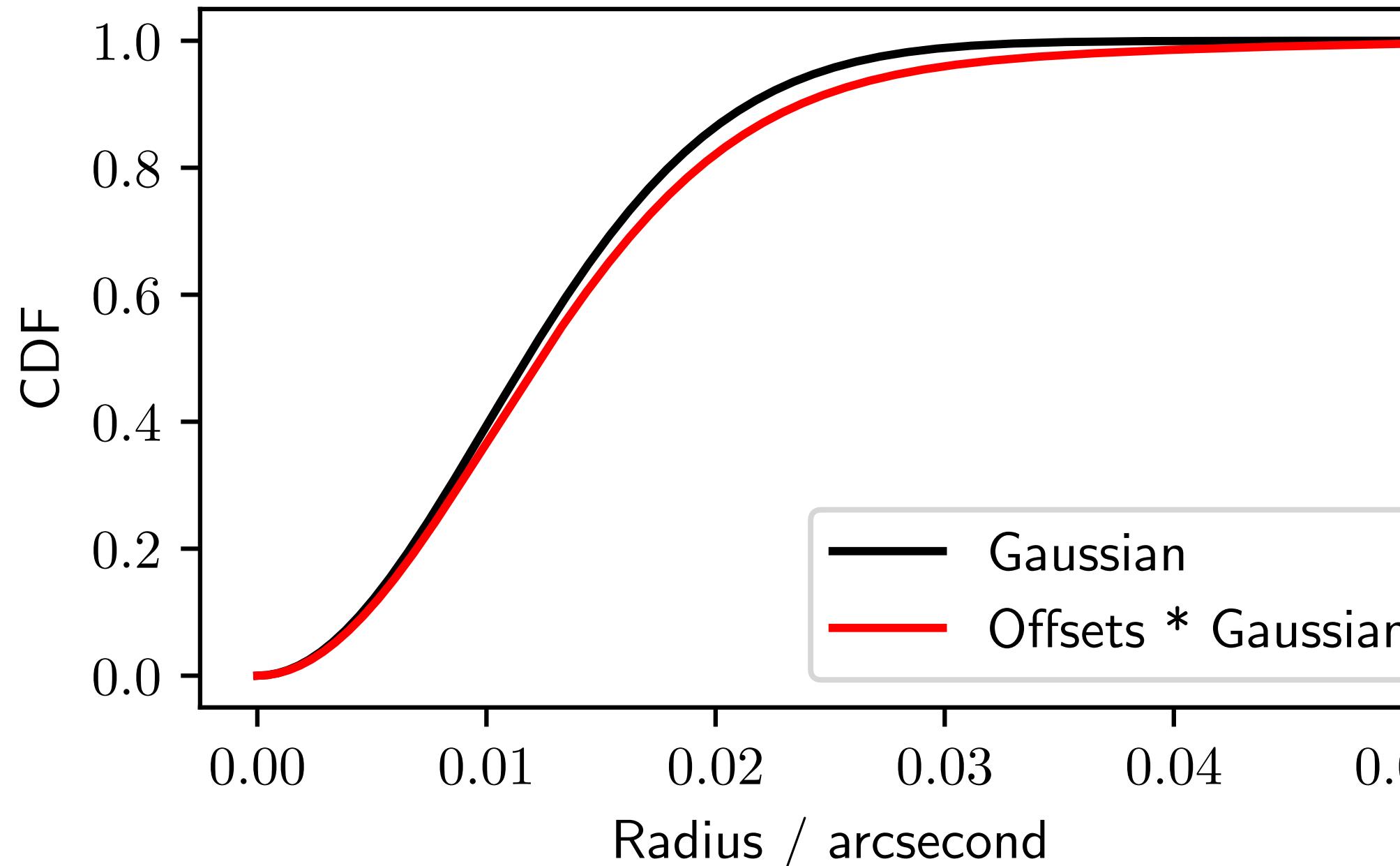
# Effects of Crowding: Transients



Wilson & Naylor (2018b); also  
see Wilson (2022, RNAAS)

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# Effects of Crowding: Transients

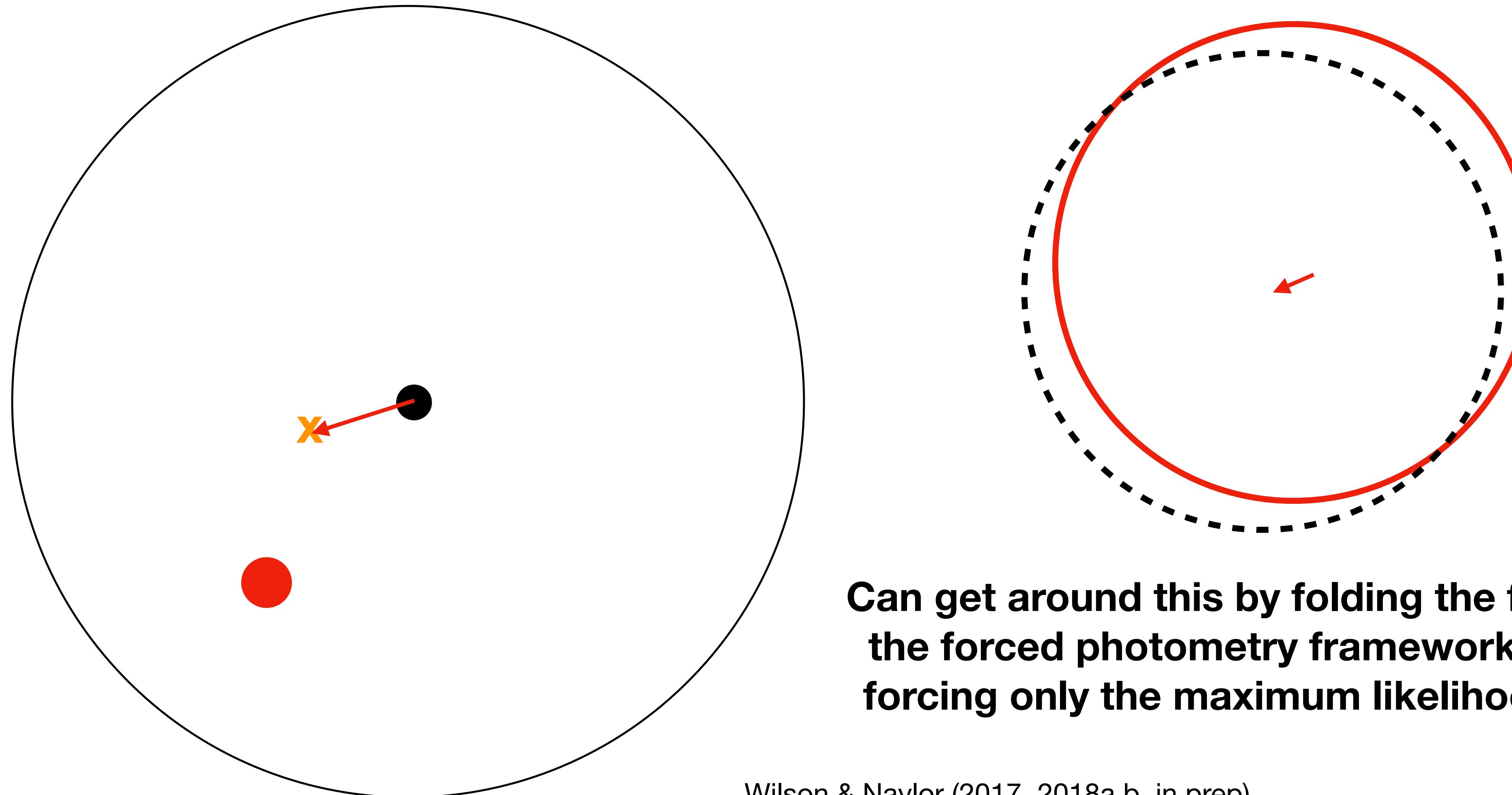


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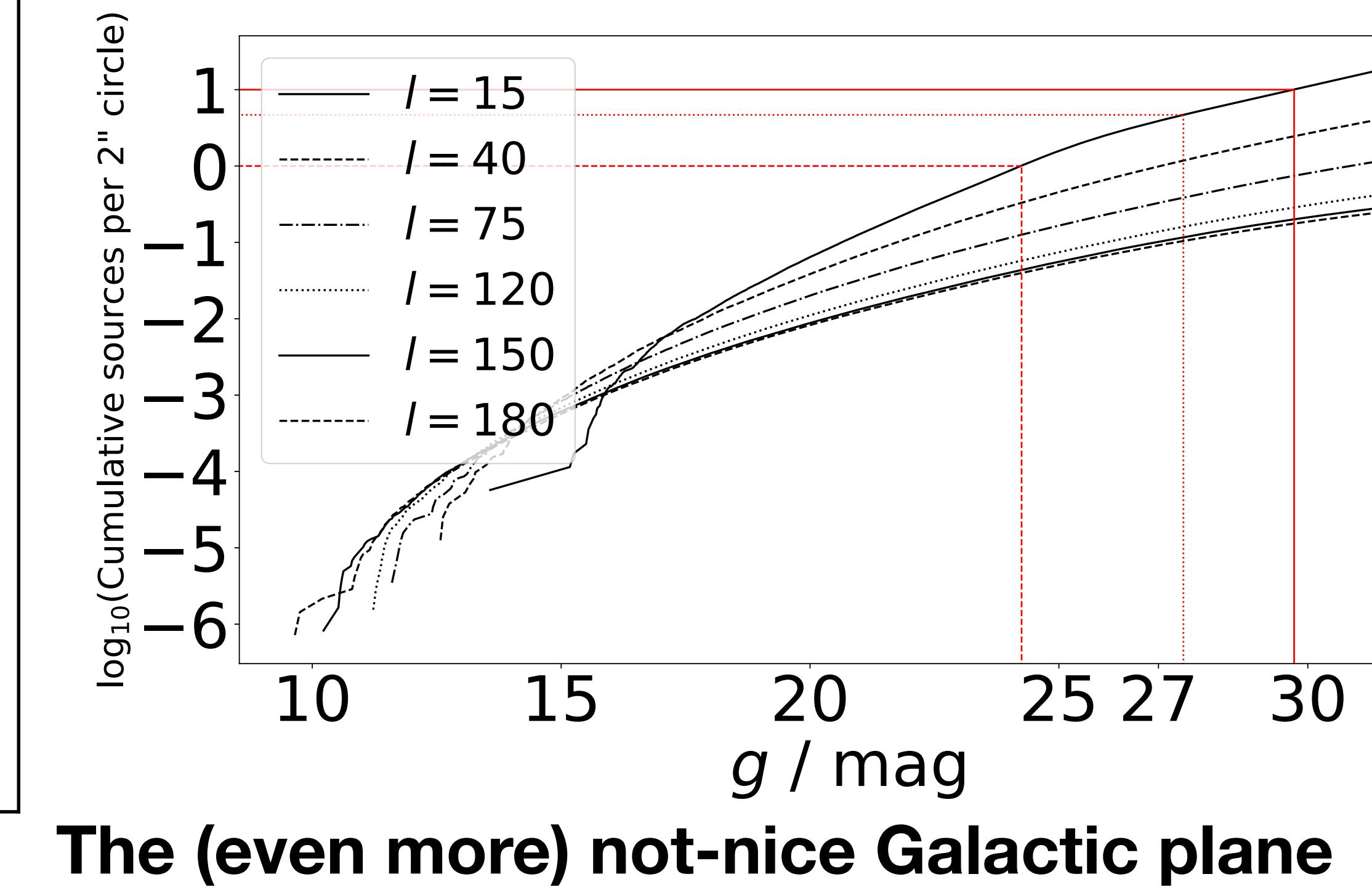
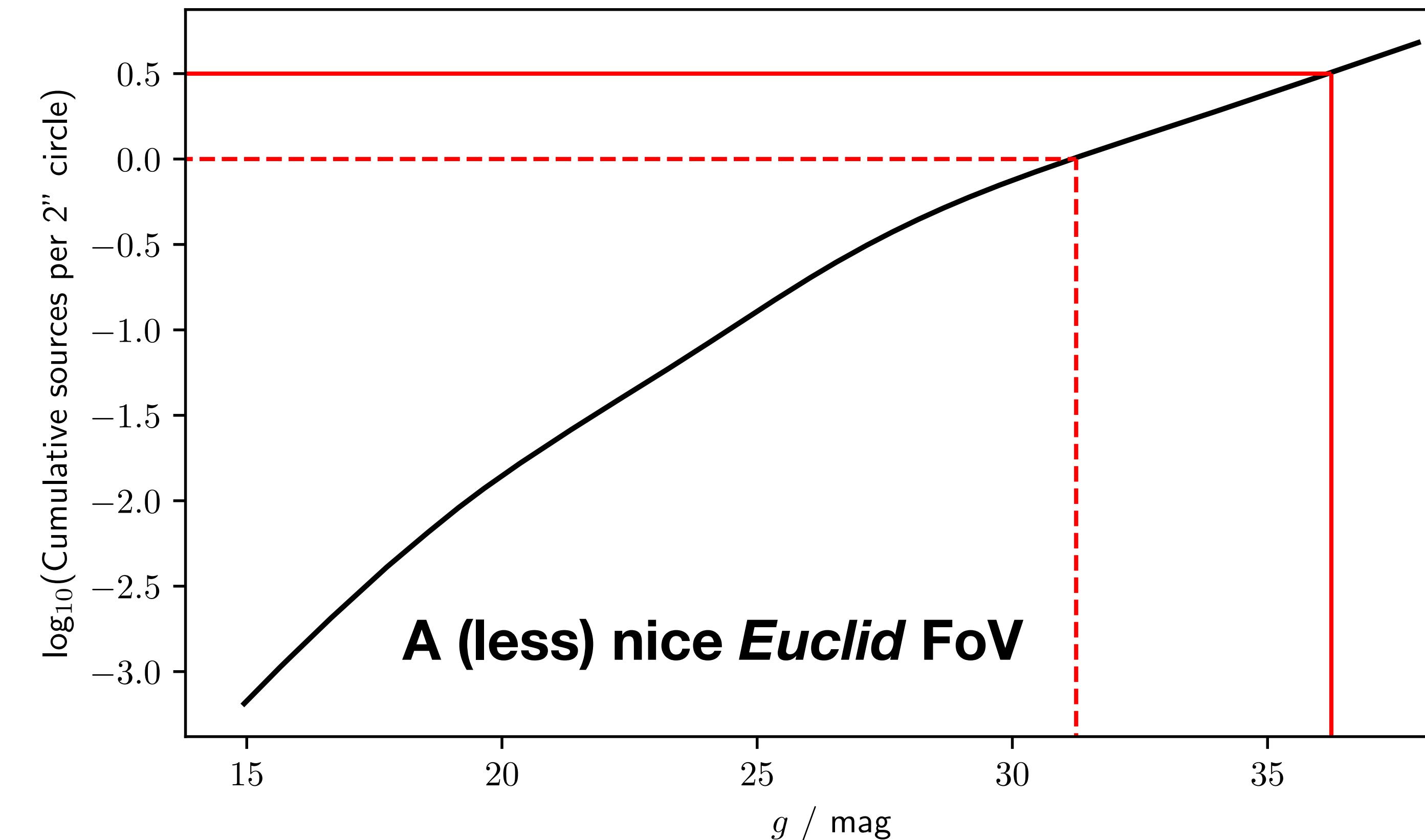
# Why Not (Always) Forced Photometry?

1. *Euclid* positions may not be perturbed (although still subject to some centroid noise), but (e.g.) Rubin positions will be noisy and biased



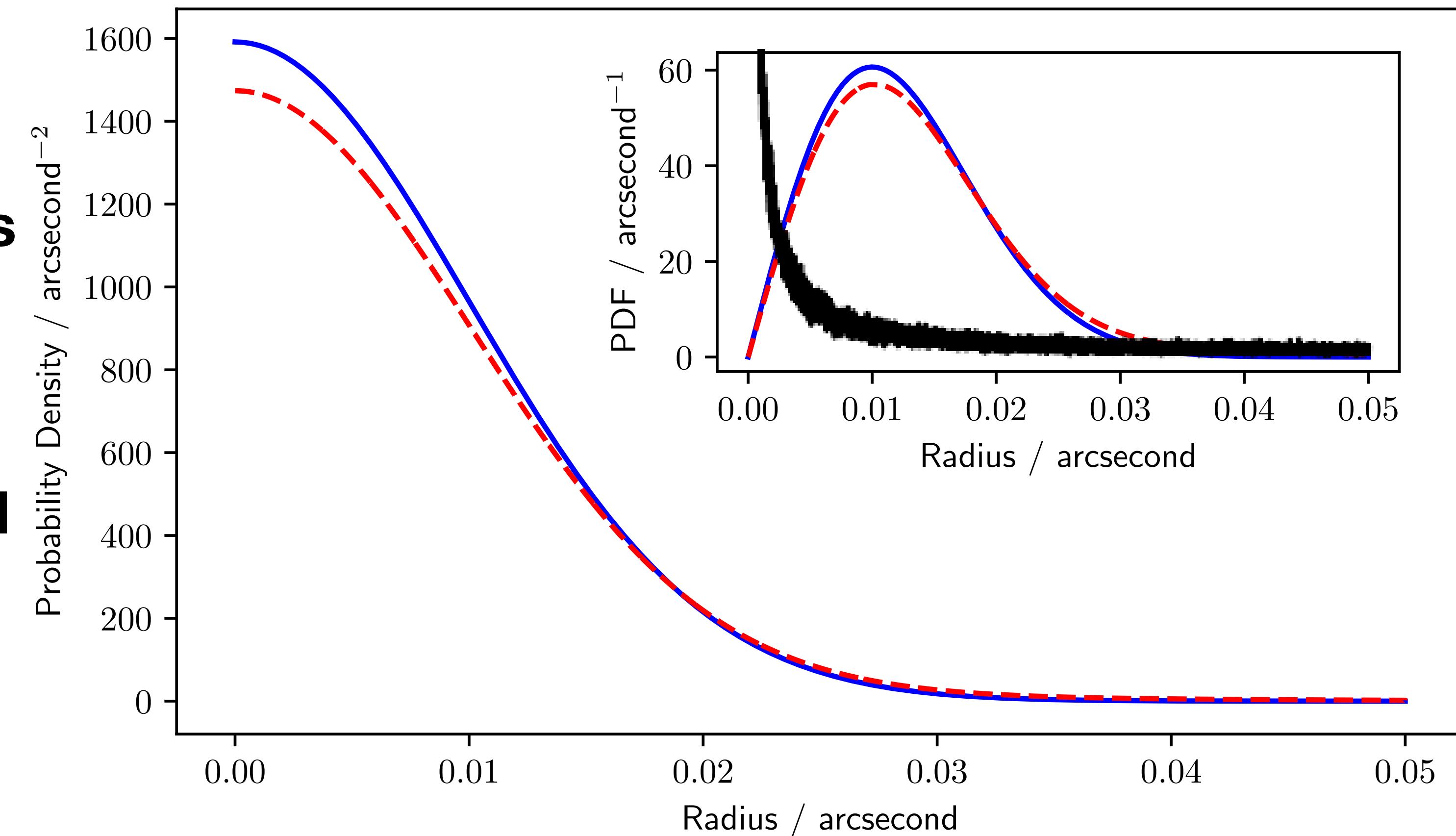
# Why Not (Always) Forced Photometry?

**2. The AUF allows us to probe for systematic effects below the completeness limit of either (and both!) surveys**



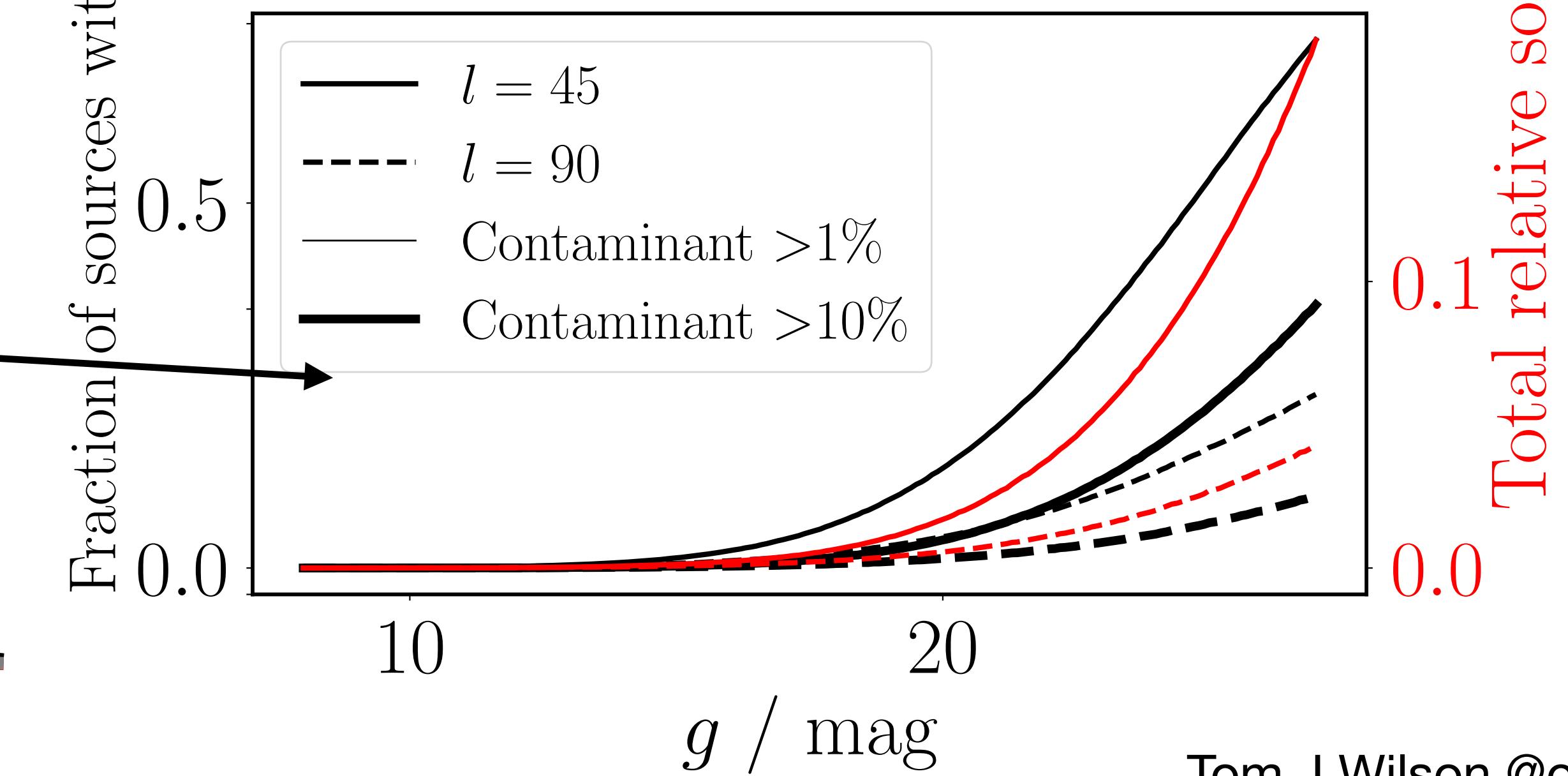
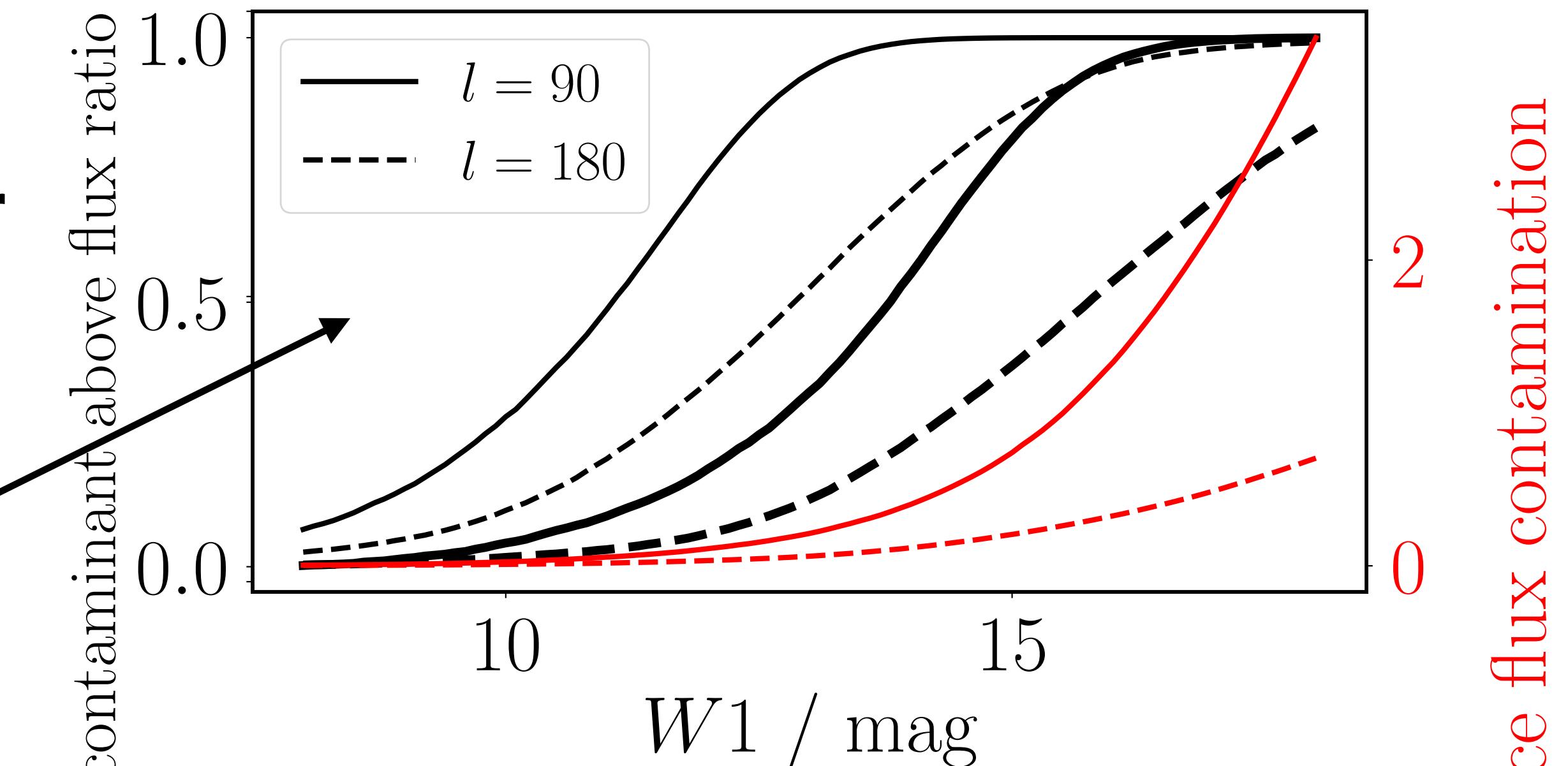
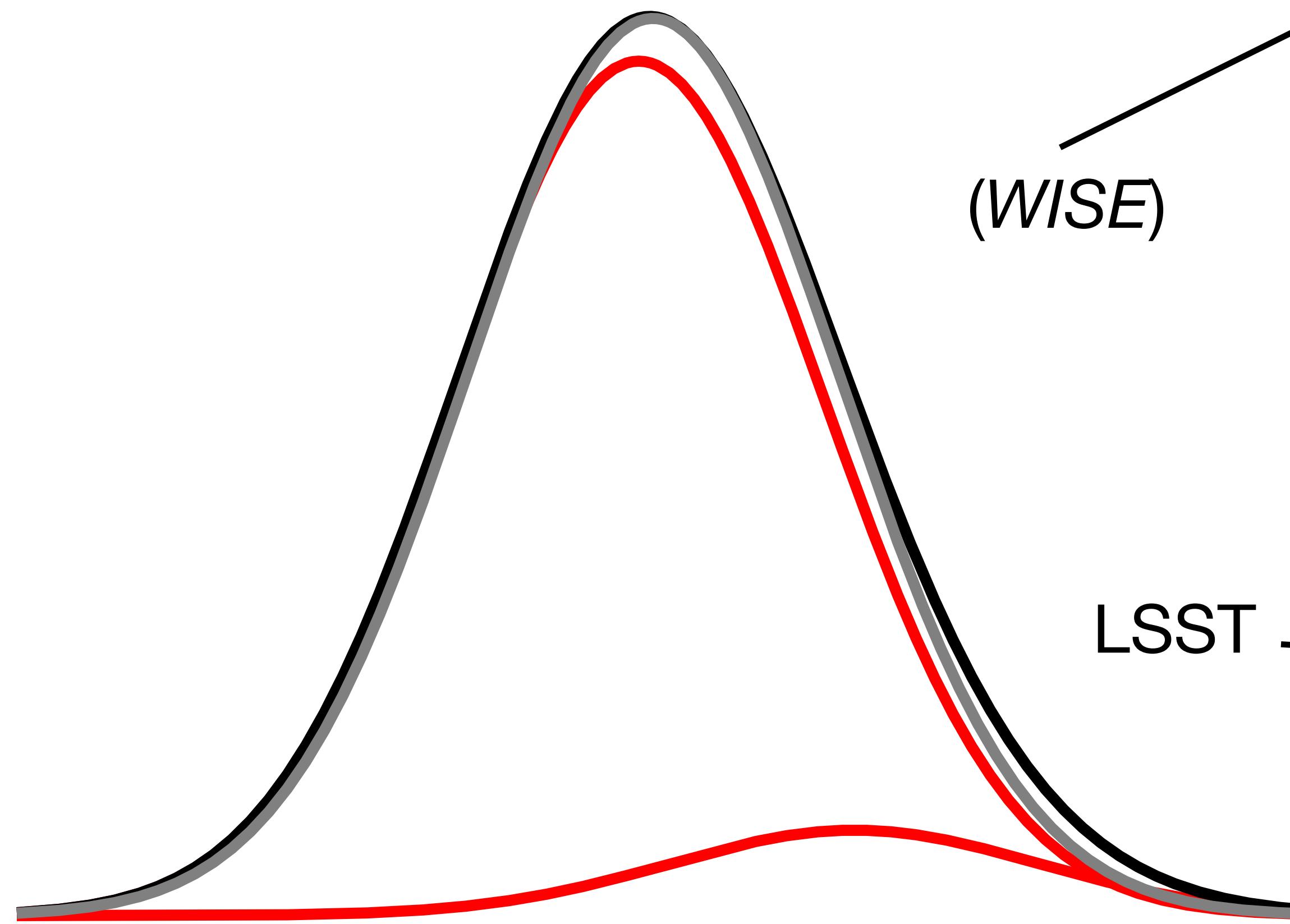
# Why Not (Always) Forced Photometry?

**3. Forced photometry largely works if you assume all of your objects are detected in the ‘base’ dataset, and the effects of “invisible” perturbers will therefore be missed**



# Why Not (Always) Forced Photometry?

4. If objects are missed, even “good” *Euclid* forced photometry (and in fact for non-forced photometry!) fluxes can be wrong if there are hidden perturbers!



# Conclusions

- The Astrometric Uncertainty Function is crucial to correctly understanding the true positions of sources in crowded fields – & unfortunately almost all of Rubin counts as “crowded” to some level!
- Using the AUF reduces the false negative rate from probabilistic cross-matching
- Can also use in-situ photometry and colours to reject interlopers and reduce false positive matches
- Where significant biases in positions are expected (or precision is required) forced photometry should be used with care
- Direct cross-matching should also be used over forced photometry in cases where significant number of sources are “missing” from one or other dataset – either due to simple survey completeness limits or e.g. colour selection effects
- Use of simulations of the perturbation component of the AUF can assist in the removal of flux biases – both for forced and non-forced photometry
- Software package [macauff](#) developed to robustly cross-match photometric catalogues in crowded fields – let me know what catalogues you would like to see robustly matched to one another!



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Wilson & Naylor, 2017, MNRAS, 468, 2517  
Wilson & Naylor, 2018a, MNRAS, 473, 5570  
Wilson & Naylor, 2018b, MNRAS, 481, 2148

Wilson, 2022, RNAAS, 6, 60  
Wilson, 2023, RASTI, 2, 1

<https://github.com/Onoddil/macauff>



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