# Convolution\_model\_Step\_by\_Step\_v2a

November 10, 2020

# 1 Convolutional Neural Networks: Step by Step

Welcome to Course 4's first assignment! In this assignment, you will implement convolutional (CONV) and pooling (POOL) layers in numpy, including both forward propagation and (optionally) backward propagation.

**Notation**: - Superscript [l] denotes an object of the  $l^{th}$  layer. - Example:  $a^{[4]}$  is the  $4^{th}$  layer activation.  $W^{[5]}$  and  $b^{[5]}$  are the  $5^{th}$  layer parameters.

- Superscript (i) denotes an object from the  $i^{th}$  example.
  - Example:  $x^{(i)}$  is the  $i^{th}$  training example input.
- Subscript i denotes the  $i^{th}$  entry of a vector.
  - Example:  $a_i^{[l]}$  denotes the  $i^{th}$  entry of the activations in layer l, assuming this is a fully connected (FC) layer.
- $n_H$ ,  $n_W$  and  $n_C$  denote respectively the height, width and number of channels of a given layer. If you want to reference a specific layer l, you can also write  $n_H^{[l]}$ ,  $n_W^{[l]}$ ,  $n_C^{[l]}$ .
- $n_{H_{prev}}$ ,  $n_{W_{prev}}$  and  $n_{C_{prev}}$  denote respectively the height, width and number of channels of the previous layer. If referencing a specific layer l, this could also be denoted  $n_H^{[l-1]}$ ,  $n_W^{[l-1]}$ ,  $n_C^{[l-1]}$ .

We assume that you are already familiar with numpy and/or have completed the previous courses of the specialization. Let's get started!

# 1.1 Updates

If you were working on the notebook before this update...

- The current notebook is version "v2a".
- You can find your original work saved in the notebook with the previous version name ("v2")
- To view the file directory, go to the menu "File->Open", and this will open a new tab that shows the file directory.

# List of updates

- clarified example used for padding function. Updated starter code for padding function.
- conv\_forward has additional hints to help students if they're stuck.
- conv\_forward places code for vert\_start and vert\_end within the for h in range(...) loop; to avoid redundant calculations. Similarly updated horiz\_start and horiz\_end. Thanks to our mentor Kevin Brown for pointing this out.
- conv\_forward breaks down the Z[i, h, w, c] single line calculation into 3 lines, for clarity.
- conv\_forward test case checks that students don't accidentally use n\_H\_prev instead of n\_H, use n\_W\_prev instead of n\_W, and don't accidentally swap n\_H with n\_W
- pool\_forward properly nests calculations of vert\_start, vert\_end, horiz\_start, and horiz\_end to avoid redundant calculations.
- 'pool\_forward' has two new test cases that check for a correct implementation of stride (the
  height and width of the previous layer's activations should be large enough relative to the
  filter dimensions so that a stride can take place).
- conv\_backward: initialize Z and cache variables within unit test, to make it independent of unit testing that occurs in the conv\_forward section of the assignment.
- Many thanks to our course mentor, Paul Mielke, for proposing these test cases.

# **1.2 1 - Packages**

Let's first import all the packages that you will need during this assignment. - numpy is the fundamental package for scientific computing with Python. - matplotlib is a library to plot graphs in Python. - np.random.seed(1) is used to keep all the random function calls consistent. It will help us grade your work.

```
In [1]: import numpy as np
    import h5py
    import matplotlib.pyplot as plt

%matplotlib inline
    plt.rcParams['figure.figsize'] = (5.0, 4.0) # set default size of plots
    plt.rcParams['image.interpolation'] = 'nearest'
    plt.rcParams['image.cmap'] = 'gray'

%load_ext autoreload
%autoreload 2

np.random.seed(1)
```

# 1.3 2 - Outline of the Assignment

You will be implementing the building blocks of a convolutional neural network! Each function you will implement will have detailed instructions that will walk you through the steps needed:

• Convolution functions, including:

- Zero Padding
- Convolve window
- Convolution forward
- Convolution backward (optional)
- Pooling functions, including:
  - Pooling forward
  - Create mask
  - Distribute value
  - Pooling backward (optional)

This notebook will ask you to implement these functions from scratch in numpy. In the next notebook, you will use the TensorFlow equivalents of these functions to build the following model:

**Note** that for every forward function, there is its corresponding backward equivalent. Hence, at every step of your forward module you will store some parameters in a cache. These parameters are used to compute gradients during backpropagation.

#### 1.4 3 - Convolutional Neural Networks

Although programming frameworks make convolutions easy to use, they remain one of the hardest concepts to understand in Deep Learning. A convolution layer transforms an input volume into an output volume of different size, as shown below.

In this part, you will build every step of the convolution layer. You will first implement two helper functions: one for zero padding and the other for computing the convolution function itself.

#### 1.4.1 3.1 - Zero-Padding

Zero-padding adds zeros around the border of an image:

**Figure 1**: **Zero-Padding** Image (3 channels, RGB) with a padding of 2.

The main benefits of padding are the following:

- It allows you to use a CONV layer without necessarily shrinking the height and width of the volumes. This is important for building deeper networks, since otherwise the height/width would shrink as you go to deeper layers. An important special case is the "same" convolution, in which the height/width is exactly preserved after one layer.
- It helps us keep more of the information at the border of an image. Without padding, very few values at the next layer would be affected by pixels as the edges of an image.

**Exercise**: Implement the following function, which pads all the images of a batch of examples X with zeros. Use np.pad. Note if you want to pad the array "a" of shape (5,5,5,5,5) with pad = 1 for the 2nd dimension, pad = 3 for the 4th dimension and pad = 0 for the rest, you would do:

```
a = np.pad(a, ((0,0), (1,1), (0,0), (3,3), (0,0)), mode='constant', constant_values
In [3]: # GRADED FUNCTION: zero_pad
```

```
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            Pad with zeros all images of the dataset X. The padding is applied to
            as illustrated in Figure 1.
            Argument:
            X -- python numpy array of shape (m, n_H, n_W, n_C) representing a bate
            pad -- integer, amount of padding around each image on vertical and hor
            Returns:
            X_pad -- padded image of shape (m, n_H + 2*pad, n_W + 2*pad, n_C)
            ### START CODE HERE ### (\approx 1 line)
            X_pad = np.pad(X, ((0, 0), (pad, pad), (pad, pad), (0, 0)), 'constant',
            ### END CODE HERE ###
            return X_pad
In [8]: np.random.seed(1)
        x = np.random.randn(4, 3, 3, 2)
        print("x is ", x)
        x_pad = zero_pad(x, 2)
        print ("x.shape = \n", x.shape)
        print ("x_pad.shape = \n", x_pad.shape)
        print ("x[1,1] = n", x[1,1])
        print ("x_pad[1,1] = \n", x_pad[1,1])
        fig, axarr = plt.subplots(1, 2)
        axarr[0].set_title('x')
        axarr[0].imshow(x[0,:,:,0])
        axarr[1].set_title('x_pad')
        axarr[1].imshow(x_pad[0,:,:,0])
        print("x_pad is ", x_pad)
x is [[[[ 1.62434536 -0.61175641]
   [-0.52817175 -1.07296862]
   [ 0.86540763 -2.3015387 ]]
  [[ 1.74481176 -0.7612069 ]
   [0.3190391 - 0.24937038]
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[ 1.46210794 -2.06014071]]

[[-0.3224172 -0.38405435] [1.13376944 -1.09989127] [-0.17242821 -0.87785842]]]

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x.shape =
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x_pad.shape =
 (4, 7, 7, 2)
x[1,1] =
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x_pad[1,1] =
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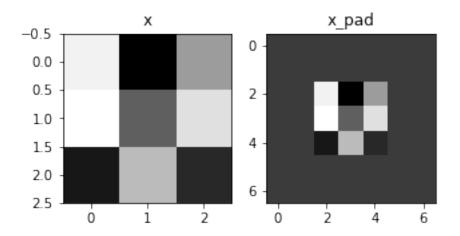
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## **Expected Output:**

```
x.shape =
 (4, 3, 3, 2)
x_pad.shape =
 (4, 7, 7, 2)
x[1,1] =
 [[ 0.90085595 -0.68372786]
 [-0.12289023 -0.93576943]
 [-0.26788808
               0.53035547]]
x_pad[1,1] =
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```

#### 1.4.2 3.2 - Single step of convolution

In this part, implement a single step of convolution, in which you apply the filter to a single position of the input. This will be used to build a convolutional unit, which:

- Takes an input volume
- Applies a filter at every position of the input
- Outputs another volume (usually of different size)

**Figure 2**: **Convolution operation** with a filter of 3x3 and a stride of 1 (stride = amount you move the window each time you slide)

In a computer vision application, each value in the matrix on the left corresponds to a single pixel value, and we convolve a 3x3 filter with the image by multiplying its values element-wise

with the original matrix, then summing them up and adding a bias. In this first step of the exercise, you will implement a single step of convolution, corresponding to applying a filter to just one of the positions to get a single real-valued output.

Later in this notebook, you'll apply this function to multiple positions of the input to implement the full convolutional operation.

Exercise: Implement conv\_single\_step(). Hint.

**Note**: The variable b will be passed in as a numpy array. If we add a scalar (a float or integer) to a numpy array, the result is a numpy array. In the special case when a numpy array contains a single value, we can cast it as a float to convert it to a scalar.

```
In [9]: # GRADED FUNCTION: conv_single_step
        def conv_single_step(a_slice_prev, W, b):
            Apply one filter defined by parameters W on a single slice (a_slice_pre
            of the previous layer.
            Arguments:
            a_slice_prev -- slice of input data of shape (f, f, n_C_prev)
            W -- Weight parameters contained in a window - matrix of shape (f, f, 1
            b -- Bias parameters contained in a window - matrix of shape (1, 1, 1)
            Returns:
            Z -- a scalar value, the result of convolving the sliding window (W, b,
            ### START CODE HERE ### (\approx 2 lines of code)
            # Element-wise product between a_slice_prev and W. Do not add the bias
            s = np.multiply(a_slice_prev, W)
            # Sum over all entries of the volume s.
            Z = np.sum(s)
            \# Add bias b to Z. Cast b to a float() so that Z results in a scalar va
            Z = Z + float(b)
            ### END CODE HERE ###
            return Z
In [10]: np.random.seed(1)
         a_slice_prev = np.random.randn(4, 4, 3)
         W = np.random.randn(4, 4, 3)
         b = np.random.randn(1, 1, 1)
         Z = conv_single_step(a_slice_prev, W, b)
         print("Z = ", Z)
Z = -6.99908945068
```

#### **Expected Output:**

**Z** -6.99908945068

## 1.4.3 3.3 - Convolutional Neural Networks - Forward pass

In the forward pass, you will take many filters and convolve them on the input. Each 'convolution' gives you a 2D matrix output. You will then stack these outputs to get a 3D volume:

**Exercise**: Implement the function below to convolve the filters  ${\tt W}$  on an input activation  ${\tt A\_prev}$ .

This function takes the following inputs: \* A\_prev, the activations output by the previous layer (for a batch of m inputs); \* Weights are denoted by W. The filter window size is f by f. \* The bias vector is b, where each filter has its own (single) bias.

Finally you also have access to the hyperparameters dictionary which contains the stride and the padding.

**Hint**: 1. To select a 2x2 slice at the upper left corner of a matrix "a\_prev" (shape (5,5,3)), you would do:

Notice how this gives a 3D slice that has height 2, width 2, and depth 3. Depth is the number of channels.

This will be useful when you will define a\_slice\_prev below, using the start/end indexes you will define. 2. To define a\_slice you will need to first define its corners vert\_start, vert\_end, horiz\_start and horiz\_end. This figure may be helpful for you to find out how each of the corner can be defined using h, w, f and s in the code below.

Figure 3: Definition of a slice using vertical and horizontal start/end (with a 2x2 filter) This figure shows only a single channel.

Reminder: The formulas relating the output shape of the convolution to the input shape is:

$$n_H = \lfloor \frac{n_{H_{prev}} - f + 2 \times pad}{stride} \rfloor + 1$$

$$n_W = \lfloor \frac{n_{W_{prev}} - f + 2 \times pad}{stride} \rfloor + 1$$

 $n_C$  = number of filters used in the convolution

For this exercise, we won't worry about vectorization, and will just implement everything with for-loops.

#### Additional Hints if you're stuck

• You will want to use array slicing (e.g.varname[0:1,:,3:5]) for the following variables: a\_prev\_pad,W,b

Copy the starter code of the function and run it outside of the defined function, in separate cells.

Check that the subset of each array is the size and dimension that you're expecting.

• To decide how to get the vert\_start, vert\_end; horiz\_start, horiz\_end, remember that these are indices of the previous layer.

Draw an example of a previous padded layer (8  $\times$  8, for instance), and the current (output layer) (2  $\times$  2, for instance).

The output layer's indices are denoted by h and w.

- Make sure that a\_slice\_prev has a height, width and depth.
- Remember that a\_prev\_pad is a subset of A\_prev\_pad. Think about which one should be used within the for loops.

```
In [11]: # GRADED FUNCTION: conv_forward
         def conv_forward(A_prev, W, b, hparameters):
             Implements the forward propagation for a convolution function
             Arguments:
             A_prev -- output activations of the previous layer,
                numpy array of shape (m, n_H_prev, n_W_prev, n_C_prev)
             W -- Weights, numpy array of shape (f, f, n_C_prev, n_C)
             b -- Biases, numpy array of shape (1, 1, 1, n_C)
             hparameters -- python dictionary containing "stride" and "pad"
             Returns:
             Z -- conv output, numpy array of shape (m, n_H, n_W, n_C)
             cache -- cache of values needed for the conv_backward() function
             ### START CODE HERE ###
             # Retrieve dimensions from A_prev's shape (≈1 line)
             (m, n_H_prev, n_W_prev, n_C_prev) = A_prev.shape
             # Retrieve dimensions from W's shape (≈1 line)
             (f, f, n_C_prev, n_C) = W.shape
             # Retrieve information from "hparameters" (≈2 lines)
             stride = hparameters['stride']
             pad = hparameters['pad']
             # Compute the dimensions of the CONV output volume using the formula of
             # Hint: use int() to apply the 'floor' operation. (\approx2 lines)
             n_H = int((n_H_prev - f + 2*pad)/stride) + 1
             n_W = int((n_H_prev - f + 2*pad)/stride) + 1
             # Initialize the output volume Z with zeros. (\approx 1 line)
             Z = np.zeros((m, n_H, n_W, n_C))
```

# Create A\_prev\_pad by padding A\_prev

```
# loop over the batch of training example # 100p over the batch of the batch of training example # 100p over the b
                                 for i in range(m):
                                          a_prev_pad = A_prev_pad[i] # Select ith training example's pad
                                                                                                                       # loop over vertical axis of the or
                                          for h in range(n H):
                                                     # Find the vertical start and end of the current "slice" (pprox 2
                                                     vert start = h * stride
                                                     vert\_end = h * stride + f
                                                     for w in range(n_W): # loop over horizontal axis of the
                                                               # Find the horizontal start and end of the current "slice
                                                               horiz_start = w * stride
                                                               horiz_end = horiz_start + f
                                                               for c in range(n_C): # loop over channels (= #filters) or
                                                                         # Use the corners to define the (3D) slice of a_prev_p
                                                                         a_slice_prev = a_prev_pad[vert_start:vert_end, horiz_st
                                                                         # Convolve the (3D) slice with the correct filter W as
                                                                         weights = W[:,:,:,c]
                                                                         biases = b[:,:,:,c]
                                                                         Z[i, h, w, c] = conv_single_step(a_slice_prev, weights
                                 ### END CODE HERE ###
                                 # Making sure your output shape is correct
                                 assert(Z.shape == (m, n_H, n_W, n_C))
                                 # Save information in "cache" for the backprop
                                cache = (A_prev, W, b, hparameters)
                                return Z, cache
In [12]: np.random.seed(1)
                      A_prev = np.random.randn(10, 5, 7, 4)
                      W = np.random.randn(3,3,4,8)
                      b = np.random.randn(1, 1, 1, 8)
                      hparameters = { "pad" : 1,
                                                            "stride": 2}
                      Z, cache_conv = conv_forward(A_prev, W, b, hparameters)
                      print("Z's mean = \n", np.mean(Z))
                      print ("Z[3,2,1] = n", Z[3,2,1])
                      print("cache_conv[0][1][2][3] = \n", cache_conv[0][1][2][3])
Z's mean =
  0.690632578491
```

A\_prev\_pad = zero\_pad(A\_prev, pad)

#### **Expected Output:**

```
Z's mean =
  0.692360880758

Z[3,2,1] =
  [ -1.28912231     2.27650251     6.61941931     0.95527176     8.25132576
     2.31329639     13.00689405     2.34576051]

cache_conv[0][1][2][3] = [-1.1191154     1.9560789     -0.3264995     -1.34267579]
```

Finally, CONV layer should also contain an activation, in which case we would add the following line of code:

```
# Convolve the window to get back one output neuron
Z[i, h, w, c] = ...
# Apply activation
A[i, h, w, c] = activation(Z[i, h, w, c])
```

You don't need to do it here.

# 1.5 4 - Pooling layer

The pooling (POOL) layer reduces the height and width of the input. It helps reduce computation, as well as helps make feature detectors more invariant to its position in the input. The two types of pooling layers are:

- Max-pooling layer: slides an (f, f) window over the input and stores the max value of the window in the output.
- Average-pooling layer: slides an (*f*, *f*) window over the input and stores the average value of the window in the output.

These pooling layers have no parameters for backpropagation to train. However, they have hyperparameters such as the window size f. This specifies the height and width of the  $f \times f$  window you would compute a *max* or *average* over.

#### 1.5.1 4.1 - Forward Pooling

Now, you are going to implement MAX-POOL and AVG-POOL, in the same function.

**Exercise**: Implement the forward pass of the pooling layer. Follow the hints in the comments below.

**Reminder**: As there's no padding, the formulas binding the output shape of the pooling to the input shape is:

```
n_H = \lfloor \frac{n_{Hprev} - f}{stride} \rfloor + 1
                             n_W = \lfloor \frac{n_{W_{prev}} - f}{stride} \rfloor + 1
                                  n_C = n_{C_{nrev}}
In [17]: # GRADED FUNCTION: pool_forward
         def pool_forward(A_prev, hparameters, mode = "max"):
              Implements the forward pass of the pooling layer
              Arguments:
              A_prev -- Input data, numpy array of shape (m, n_H_prev, n_W_prev, n_0
              hparameters -- python dictionary containing "f" and "stride"
              mode -- the pooling mode you would like to use, defined as a string (
              Returns:
              A -- output of the pool layer, a numpy array of shape (m, n_H, n_W, n_
              cache -- cache used in the backward pass of the pooling layer, contain
              # Retrieve dimensions from the input shape
              (m, n_H_prev, n_W_prev, n_C_prev) = A_prev.shape
              # Retrieve hyperparameters from "hparameters"
              f = hparameters["f"]
              stride = hparameters["stride"]
              # Define the dimensions of the output
              n_H = int(1 + (n_H_prev - f) / stride)
              n_W = int(1 + (n_W_prev - f) / stride)
              n C = n C prev
              # Initialize output matrix A
              A = np.zeros((m, n_H, n_W, n_C))
              ### START CODE HERE ###
              for i in range(m):
                                                             # loop over the training ex
                                                               # loop on the vertical as
                  for h in range(n_H):
                       # Find the vertical start and end of the current "slice" (pprox 2
                       vert_start = h*stride
                      vert\_end = h * stride + f
                       for w in range(n_W):
                                                               # loop on the horizontal
                           # Find the vertical start and end of the current "slice"
```

```
horiz_start = w*stride
                         horiz\_end = w*stride + f
                         for c in range (n_C):
                                                        # loop over the channels
                             # Use the corners to define the current slice on the
                             a_prev_slice = A_prev[i,vert_start:vert_end,horiz_start
                             # Compute the pooling operation on the slice.
                             # Use an if statement to differentiate the modes.
                             # Use np.max and np.mean.
                             if mode == "max":
                                 A[i, h, w, c] = np.max(a_prev_slice)
                             elif mode == "average":
                                 A[i, h, w, c] = np.mean(a_prev_slice)
             ### END CODE HERE ###
             # Store the input and hparameters in "cache" for pool_backward()
             cache = (A_prev, hparameters)
             # Making sure your output shape is correct
             assert(A.shape == (m, n_H, n_W, n_C))
             return A, cache
In [18]: # Case 1: stride of 1
         np.random.seed(1)
         A_prev = np.random.randn(2, 5, 5, 3)
         hparameters = {"stride" : 1, "f": 3}
         A, cache = pool_forward(A_prev, hparameters)
         print("mode = max")
         print("A.shape = " + str(A.shape))
        print("A =\n", A)
        print()
         A, cache = pool_forward(A_prev, hparameters, mode = "average")
         print ("mode = average")
         print("A.shape = " + str(A.shape))
         print("A = \backslash n", A)
mode = max
A.shape = (2, 3, 3, 3)
A =
 [[[ 1.74481176 0.90159072 1.65980218]
   [ 1.74481176    1.6924546    1.65980218]]
```

```
[[ 1.14472371 0.90159072 2.10025514]
  [ 1.14472371  0.90159072  1.65980218]
  1.65980218]]
 2.18557541]]]
[[[ 1.19891788  0.84616065  0.82797464]
  [[ 1.96710175  0.84616065  1.27375593]
  [ 1.96710175  0.84616065  1.23616403]
  1.2245077 ]]
 [[ 1.96710175  0.86888616  1.27375593]
  [ 1.96710175  0.86888616  1.23616403]
  mode = average
A.shape = (2, 3, 3, 3)
A =
[[[-3.01046719e-02 -3.24021315e-03 -3.36298859e-01]]
  [ 1.43310483e-01 1.93146751e-01 -4.44905196e-01]
  [ 1.28934436e-01 2.22428468e-01
                              1.25067597e-01]]
 [[ -3.81801899e-01 1.59993515e-02
                               1.70562706e-011
  [ 4.73707165e-02 2.59244658e-02
                              9.20338402e-02]
  [ 3.97048605e-02 1.57189094e-01
                              3.45302489e-0111
 [[ -3.82680519e-01 2.32579951e-01
                              6.25997903e-011
  [ -2.47157416e-01 -3.48524998e-04
                               3.50539717e-01]
  3.23771981e-01 -3.43175716e-01]
[[[ -1.73134159e-01
  \begin{bmatrix} 3.80634669e-02 & 7.26706274e-02 & -2.30268958e-01 \end{bmatrix}
  [ 2.03009393e-02
                1.41414785e-01 -1.23158476e-02]]
 [[4.44976963e-01 -2.61694592e-03 -3.10403073e-01]
  [ 5.08114737e-01 -2.34937338e-01
                              -2.39611830e-01]
  [ 1.18726772e-01
                 1.72552294e-01
                              -2.21121966e-0111
 [[ 4.29449255e-01 8.44699612e-02
                              -2.72909051e-011
  [ 6.76351685e-01 -1.20138225e-01 -2.44076712e-01]
  [ 1.50774518e-01 2.89111751e-01 1.23238536e-03]]]]
```

# \*\* Expected Output\*\*

```
mode = max
A.shape = (2, 3, 3, 3)
[[[ 1.74481176 0.90159072 1.65980218]
  1.65980218]]
 [[ 1.14472371 0.90159072 2.10025514]
  [ 1.14472371  0.90159072  1.65980218]
  1.65980218]]
 [[ 1.13162939     1.51981682     2.18557541]
  2.18557541]]]
 [[[ 1.19891788  0.84616065  0.82797464]
  [ 0.69803203  0.84616065  1.2245077 ]
  [[ 1.96710175  0.84616065  1.27375593]
  [ 1.96710175  0.84616065  1.23616403]
  [[ 1.96710175
             0.86888616 1.273755931
  [ 1.96710175  0.86888616  1.23616403]
  mode = average
A.shape = (2, 3, 3, 3)
A =
[[[[-3.01046719e-02 -3.24021315e-03 -3.36298859e-01]]
  \begin{bmatrix} 1.43310483e-01 & 1.93146751e-01 & -4.44905196e-01 \end{bmatrix}
  [ 1.28934436e-01 2.22428468e-01
                               1.25067597e-01]]
 [[ -3.81801899e-01 1.59993515e-02
                                1.70562706e-01]
  [ 4.73707165e-02 2.59244658e-02
                               9.20338402e-021
  [ 3.97048605e-02 1.57189094e-01
                                3.45302489e-01]]
 [ [ -3.82680519e-01 ]
                 2.32579951e-01
                               6.25997903e-01]
  [ -2.47157416e-01 -3.48524998e-04
                                3.50539717e-01]
  [ -9.52551510e-02
                 2.68511000e-01
                               4.66056368e-01]]]
```

```
[[[ -1.73134159e-01 3.23771981e-01 -3.43175716e-01]
   [ 3.80634669e-02 7.26706274e-02 -2.30268958e-01]
   [ 2.03009393e-02 1.41414785e-01 -1.23158476e-02]]
  [ 4.44976963e-01 -2.61694592e-03 -3.10403073e-01]
   [ 5.08114737e-01 -2.34937338e-01 -2.39611830e-01]
   [ 1.18726772e-01 1.72552294e-01 -2.21121966e-01]]
  [[ 4.29449255e-01 8.44699612e-02 -2.72909051e-01]
   [ 6.76351685e-01 -1.20138225e-01 -2.44076712e-01]
   [ 1.50774518e-01 2.89111751e-01 1.23238536e-03]]]]
In [19]: # Case 2: stride of 2
        np.random.seed(1)
        A_prev = np.random.randn(2, 5, 5, 3)
        hparameters = {"stride" : 2, "f": 3}
        A, cache = pool_forward(A_prev, hparameters)
        print("mode = max")
        print("A.shape = " + str(A.shape))
        print ("A = \n", A)
        print()
        A, cache = pool_forward(A_prev, hparameters, mode = "average")
        print("mode = average")
        print("A.shape = " + str(A.shape))
        print ("A = \backslash n", A)
mode = max
A.shape = (2, 2, 2, 3)
 [[[[ 1.74481176 0.90159072 1.65980218]
   [ 1.74481176    1.6924546    1.65980218]]
  [[ 1.13162939    1.51981682    2.18557541]
   [ 1.13162939    1.6924546    2.18557541]]]
 [[[ 1.19891788  0.84616065  0.82797464]
  [[ 1.96710175  0.86888616  1.27375593]
   mode = average
A.shape = (2, 2, 2, 3)
A =
[[[-0.03010467 -0.00324021 -0.33629886]
```

# **Expected Output:**

```
mode = max
A.shape = (2, 2, 2, 3)
A =
 [[[ 1.74481176 0.90159072 1.65980218]
  [ 1.74481176    1.6924546    1.65980218]]
  [[ 1.13162939     1.51981682     2.18557541]
  2.18557541]]]
 [[[ 1.19891788  0.84616065  0.82797464]
  [[ 1.96710175  0.86888616  1.27375593]
  mode = average
A.shape = (2, 2, 2, 3)
 [[[-0.03010467 -0.00324021 -0.33629886]]
   [ 0.12893444  0.22242847  0.1250676 ]]
  [[-0.38268052 \quad 0.23257995 \quad 0.6259979]
  [-0.09525515 \quad 0.268511
                        0.46605637]]]
 [[-0.17313416 \quad 0.32377198 \quad -0.34317572]
   [ 0.02030094  0.14141479  -0.01231585]]
  [[0.42944926 \quad 0.08446996 \quad -0.27290905]
   [ 0.15077452  0.28911175  0.00123239]]]]
```

Congratulations! You have now implemented the forward passes of all the layers of a convolutional network.

The remainder of this notebook is optional, and will not be graded.

# 1.6 5 - Backpropagation in convolutional neural networks (OPTIONAL / UN-GRADED)

In modern deep learning frameworks, you only have to implement the forward pass, and the framework takes care of the backward pass, so most deep learning engineers don't need to bother with the details of the backward pass. The backward pass for convolutional networks is complicated. If you wish, you can work through this optional portion of the notebook to get a sense of what backprop in a convolutional network looks like.

When in an earlier course you implemented a simple (fully connected) neural network, you used backpropagation to compute the derivatives with respect to the cost to update the parameters. Similarly, in convolutional neural networks you can calculate the derivatives with respect to the cost in order to update the parameters. The backprop equations are not trivial and we did not derive them in lecture, but we will briefly present them below.

## 1.6.1 5.1 - Convolutional layer backward pass

Let's start by implementing the backward pass for a CONV layer.

**5.1.1 - Computing dA:** This is the formula for computing dA with respect to the cost for a certain filter  $W_c$  and a given training example:

$$dA + = \sum_{h=0}^{n_H} \sum_{w=0}^{n_W} W_c \times dZ_{hw}$$
 (1)

Where  $W_c$  is a filter and  $dZ_{hw}$  is a scalar corresponding to the gradient of the cost with respect to the output of the conv layer Z at the hth row and wth column (corresponding to the dot product taken at the ith stride left and jth stride down). Note that at each time, we multiply the the same filter  $W_c$  by a different dZ when updating dA. We do so mainly because when computing the forward propagation, each filter is dotted and summed by a different a\_slice. Therefore when computing the backprop for dA, we are just adding the gradients of all the a\_slices.

In code, inside the appropriate for-loops, this formula translates into:

**5.1.2 - Computing dW:** This is the formula for computing  $dW_c$  ( $dW_c$  is the derivative of one filter) with respect to the loss:

$$dW_c + = \sum_{h=0}^{n_H} \sum_{w=0}^{n_W} a_{slice} \times dZ_{hw}$$
 (2)

Where  $a_{slice}$  corresponds to the slice which was used to generate the activation  $Z_{ij}$ . Hence, this ends up giving us the gradient for W with respect to that slice. Since it is the same W, we will just add up all such gradients to get dW.

In code, inside the appropriate for-loops, this formula translates into:

$$dW[:,:,:,c] += a\_slice * dZ[i, h, w, c]$$

**5.1.3 - Computing db:** This is the formula for computing db with respect to the cost for a certain filter  $W_c$ :

$$db = \sum_{h} \sum_{w} dZ_{hw} \tag{3}$$

As you have previously seen in basic neural networks, db is computed by summing dZ. In this case, you are just summing over all the gradients of the conv output (Z) with respect to the cost. In code, inside the appropriate for-loops, this formula translates into:

```
db[:,:,:,c] += dZ[i, h, w, c]
```

**Exercise**: Implement the conv\_backward function below. You should sum over all the training examples, filters, heights, and widths. You should then compute the derivatives using formulas 1, 2 and 3 above.

```
In [26]: def conv_backward(dZ, cache):
             Implement the backward propagation for a convolution function
             Arguments:
             dZ -- gradient of the cost with respect to the output of the conv layer
             cache -- cache of values needed for the conv_backward(), output of conv_backward()
             Returns:
             dA_prev -- gradient of the cost with respect to the input of the conv
                        numpy array of shape (m, n_H_prev, n_W_prev, n_C_prev)
             dW -- gradient of the cost with respect to the weights of the conv lay
                   numpy array of shape (f, f, n_C_prev, n_C)
             db -- gradient of the cost with respect to the biases of the conv layer
                   numpy array of shape (1, 1, 1, n_C)
             ### START CODE HERE ###
             # Retrieve information from "cache"
             (A_prev, W, b, hparameters) = cache
             # Retrieve dimensions from A_prev's shape
             (m, n_H_prev, n_W_prev, n_C_prev) = A_prev.shape
             # Retrieve dimensions from W's shape
             (f, f, n_C_prev, n_C) = W.shape
             # Retrieve information from "hparameters"
             stride = hparameters["stride"]
             pad = hparameters["pad"]
             # Retrieve dimensions from dZ's shape
             (m, n_H, n_W, n_C) = dZ.shape
```

```
dA_prev = np.zeros((m, n_H_prev, n_W_prev, n_C_prev))
                                dW = np.zeros((f, f, n_C_prev, n_C))
                                db = np.zeros((1, 1, 1, n_C))
                                # Pad A prev and dA prev
                               A_prev_pad = zero_pad(A_prev, pad)
                                dA_prev_pad = zero_pad(dA_prev, pad)
                                for i in range(m):
                                                                                                                                    # loop over the training example # 100p over the training example 
                                          # select ith training example from A_prev_pad and dA_prev_pad
                                         a_prev_pad = A_prev_pad[i]
                                         da_prev_pad = dA_prev_pad[i]
                                         for h in range(n_H):
                                                                                                                                         # loop over vertical axis of
                                                   for w in range(n_W):
                                                                                                                                        # loop over horizontal axis
                                                             for c in range(n_C):
                                                                                                                                        # loop over the channels of
                                                                       # Find the corners of the current "slice"
                                                                       vert start = h*stride
                                                                      vert end = h*stride + f
                                                                      horiz start = w*stride
                                                                      horiz end = w*stride + f
                                                                       # Use the corners to define the slice from a_prev_pad
                                                                       a_slice = a_prev_pad[vert_start:vert_end,horiz_start:h
                                                                       # Update gradients for the window and the filter's par
                                                                       da_prev_pad[vert_start:vert_end, horiz_start:horiz_end
                                                                       dW[:,:,:,c] += a\_slice * dZ[i, h, w, c]
                                                                       db[:,:,:,c] += dZ[i, h, w, c]
                                          # Set the ith training example's dA_prev to the unpadded da_prev_p
                                         dA_prev[i, :, :, :] = da_prev_pad[pad:-pad, pad:-pad, :]
                                ### END CODE HERE ###
                                # Making sure your output shape is correct
                                assert (dA_prev.shape == (m, n_H_prev, n_W_prev, n_C_prev))
                                return dA_prev, dW, db
In [28]: # We'll run conv_forward to initialize the 'Z' and 'cache_conv",
                      # which we'll use to test the conv_backward function
                     np.random.seed(1)
                     A_prev = np.random.randn(10, 4, 4, 3)
                     W = np.random.randn(2,2,3,8)
```

# Initialize dA\_prev, dW, db with the correct shapes

```
b = np.random.randn(1,1,1,8)
         hparameters = { "pad" : 2,
                         "stride": 2}
         Z, cache_conv = conv_forward(A_prev, W, b, hparameters)
         # Test conv backward
         dA, dW, db = conv backward(Z, cache conv)
         print("dA_mean =", np.mean(dA))
         print("dW mean =", np.mean(dW))
         print("db_mean =", np.mean(db))
dA_mean = 1.45243777754
dW mean = 1.72699145831
db mean = 7.83923256462
  ** Expected Output: **
  dA mean
  1.45243777754
  dW_mean
  1.72699145831
  db_mean
  7.83923256462
```

# 1.7 5.2 Pooling layer - backward pass

Next, let's implement the backward pass for the pooling layer, starting with the MAX-POOL layer. Even though a pooling layer has no parameters for backprop to update, you still need to backpropagation the gradient through the pooling layer in order to compute gradients for layers that came before the pooling layer.

## 1.7.1 5.2.1 Max pooling - backward pass

Before jumping into the backpropagation of the pooling layer, you are going to build a helper function called <code>create\_mask\_from\_window()</code> which does the following:

$$X = \begin{bmatrix} 1 & 3 \\ 4 & 2 \end{bmatrix} \quad \to \quad M = \begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix} \tag{4}$$

As you can see, this function creates a "mask" matrix which keeps track of where the maximum of the matrix is. True (1) indicates the position of the maximum in X, the other entries are False (0). You'll see later that the backward pass for average pooling will be similar to this but using a different mask.

**Exercise**: Implement create\_mask\_from\_window(). This function will be helpful for pooling backward. Hints: - np.max() may be helpful. It computes the maximum of an array. - If you have a matrix X and a scalar x: A = (X == x) will return a matrix A of the same size as X such that:

```
A[i,j] = True if X[i,j] = x

A[i,j] = False if X[i,j] != x
```

Here, you don't need to consider cases where there are several maxima in a matrix.

```
In [29]: def create_mask_from_window(x):
               Creates a mask from an input matrix x, to identify the max entry of x
               Arguments:
               x -- Array of shape (f, f)
               Returns:
               mask -- Array of the same shape as window, contains a True at the pos-
               ### START CODE HERE ### (\approx1 line)
               mask = (x == np.max(x))
               ### END CODE HERE ###
               return mask
In [30]: np.random.seed(1)
          x = np.random.randn(2,3)
          mask = create_mask_from_window(x)
          print('x = ', x)
          print("mask = ", mask)
x = [[1.62434536 - 0.61175641 - 0.52817175]]
 [-1.07296862 \quad 0.86540763 \quad -2.3015387 \ ]
mask = [[ True False False]
 [False False False]]
   Expected Output:
   [[ 1.62434536 -0.61175641 -0.52817175] [-1.07296862 0.86540763 -2.3015387 ]]
   mask =
   [[ True False False] [False False False]]
   Why do we keep track of the position of the max? It's because this is the input value that
ultimately influenced the output, and therefore the cost. Backprop is computing gradients with
```

respect to the cost, so anything that influences the ultimate cost should have a non-zero gradient. So, backprop will "propagate" the gradient back to this particular input value that had influenced the cost.

## 1.7.2 5.2.2 - Average pooling - backward pass

In max pooling, for each input window, all the "influence" on the output came from a single input value-the max. In average pooling, every element of the input window has equal influence on the output. So to implement backprop, you will now implement a helper function that reflects this.

For example if we did average pooling in the forward pass using a 2x2 filter, then the mask you'll use for the backward pass will look like:

$$dZ = 1 \quad \rightarrow \quad dZ = \begin{bmatrix} 1/4 & 1/4 \\ 1/4 & 1/4 \end{bmatrix} \tag{5}$$

This implies that each position in the dZ matrix contributes equally to output because in the forward pass, we took an average.

**Exercise**: Implement the function below to equally distribute a value dz through a matrix of dimension shape. Hint

```
In [41]: def distribute_value(dz, shape):
             Distributes the input value in the matrix of dimension shape
             Arguments:
             dz -- input scalar
             shape -- the shape (n_H, n_W) of the output matrix for which we want to
             Returns:
             a -- Array of size (n_H, n_W) for which we distributed the value of d
             ### START CODE HERE ###
             # Retrieve dimensions from shape (\approx 1 line)
              (n_H, n_W) = shape
             # Compute the value to distribute on the matrix (\approx 1 line)
             average = dz/(n_H*n_W)
             print (average)
             # Create a matrix where every entry is the "average" value (≈1 line)
             a = average * np.ones((n_H, n_W))
             ### END CODE HERE ###
             return a
In [42]: a = distribute_value(2, (2,2))
         print('distributed value =', a)
0.5
distributed value = [[0.5 0.5]]
 [ 0.5 0.5]]
  Expected Output:
  distributed_value =
```

[[ 0.5 0.5] [ 0.5 0.5]]

#### 1.7.3 5.2.3 Putting it together: Pooling backward

You now have everything you need to compute backward propagation on a pooling layer.

Exercise: Implement the pool\_backward function in both modes ("max" and "average"). You will once again use 4 for-loops (iterating over training examples, height, width, and channels). You should use an if/elif statement to see if the mode is equal to 'max' or 'average'. If it is equal to 'average' you should use the distribute\_value() function you implemented above to create a matrix of the same shape as a\_slice. Otherwise, the mode is equal to 'max', and you will create a mask with create\_mask\_from\_window() and multiply it by the corresponding value of dA.

```
In [47]: def pool_backward(dA, cache, mode = "max"):
                                      Implements the backward pass of the pooling layer
                                      Arguments:
                                      dA -- gradient of cost with respect to the output of the pooling layer
                                      cache -- cache output from the forward pass of the pooling layer, com
                                      mode -- the pooling mode you would like to use, defined as a string (
                                      Returns:
                                      dA_prev -- gradient of cost with respect to the input of the pooling .
                                       ### START CODE HERE ###
                                       # Retrieve information from cache (≈1 line)
                                       (A_prev, hparameters) = cache
                                       # Retrieve hyperparameters from "hparameters" (\approx2 lines)
                                      stride = hparameters["stride"]
                                      f = hparameters["f"]
                                       # Retrieve dimensions from A_prev's shape and dA's shape (\approx2 lines)
                                      m, n_H_prev, n_W_prev, n_C_prev = A_prev.shape
                                      m, n_H, n_W, n_C = dA.shape
                                      # Initialize dA_prev with zeros (\approx 1 line)
                                      dA_prev = np.zeros((m, n_H_prev, n_W_prev, n_C_prev))
                                      for i in range(m):
                                                                                                                                                                # loop over the training example # 100p over the training example 
                                                  # select training example from A_prev (\approx 1 line)
                                                  a_prev = A_prev[i]
                                                  for h in range(n_H):
                                                                                                                                                                    # loop on the vertical axis
                                                              for w in range(n_W):
                                                                                                                                                                   # loop on the horizontal as
```

for c in range(n\_C):

# loop over the channels (d

```
vert_start = h*stride
                              vert\_end = h*stride + f
                              horiz start = w*stride
                              horiz end = w*stride + f
                              # Compute the backward propagation in both modes.
                              if mode == "max":
                                  # Use the corners and "c" to define the current sa
                                  a_prev_slice = a_prev[vert_start:vert_end, horiz_s
                                  # Create the mask from a_prev_slice (≈1 line)
                                  mask = create_mask_from_window(a_prev_slice)
                                  # Set dA_prev to be dA_prev + (the mask multiplied
                                  dA_prev[i, vert_start: vert_end, horiz_start: hori
                              elif mode == "average":
                                  # Get the value a from dA (\approx 1 line)
                                  da = dA[i, h, w, c]
                                  # Define the shape of the filter as fxf (\approx 1 line)
                                  shape = (f, f)
                                  # Distribute it to get the correct slice of dA_pre
                                  dA_prev[i, vert_start: vert_end, horiz_start: hori
             ### END CODE ###
             # Making sure your output shape is correct
             assert (dA_prev.shape == A_prev.shape)
             return dA_prev
In [48]: np.random.seed(1)
         A_prev = np.random.randn(5, 5, 3, 2)
         hparameters = {"stride" : 1, "f": 2}
         A, cache = pool_forward(A_prev, hparameters)
         dA = np.random.randn(5, 4, 2, 2)
         dA_prev = pool_backward(dA, cache, mode = "max")
         print ("mode = max")
         print('mean of dA = ', np.mean(dA))
         print('dA_prev[1,1] = ', dA_prev[1,1])
         print()
         dA_prev = pool_backward(dA, cache, mode = "average")
         print("mode = average")
         print('mean of dA = ', np.mean(dA))
         print('dA\_prev[1,1] = ', dA\_prev[1,1])
```

# Find the corners of the current "slice" ( $\approx 4$  lines)

```
mode = max
mean of dA = 0.145713902729
dA_prev[1,1] = [[0.
                                0.
                                          ]
[ 5.05844394 -1.68282702]
 0.
               0.
                         11
-0.0775291933795
-0.608709441027
0.259706150465
0.546744911744
0.110341110892
-0.0250388083209
-0.034111185974
-0.0297635469437
0.004352352075
-0.280504682187
-0.12927361448
-0.249256706913
0.0621997903469
-0.0741602880927
0.123802830994
-0.0436757899356
0.246583796955
0.0533834753339
0.547674932242
-0.474090230723
-0.161729172064
0.225371722912
0.632081426702
-0.0621586944289
0.0109172482946
-0.0565785606284
0.332864278147
-0.071826965869
0.17001745997
-0.0799503997247
-0.318139688811
0.0783869301159
0.125796203359
0.323306470633
-0.0276117566043
-0.154340515928
0.140690274155
0.0601842730594
0.0701662692807
-0.0182781759368
0.290084642498
```

0.0923731790939

```
0.476164677085
0.27776417464
0.164762449025
-0.406859585154
0.150579820074
0.105070550912
0.202737918201
0.261110523677
-0.100219547947
0.206001404613
-0.140576357755
0.488719518752
-0.332987916629
-0.4401721401
-0.412680316456
-0.222638896041
-0.27977884964
0.489019725926
-0.0816248745195
-0.335668947344
0.278595744195
-0.146630984705
-0.309213344135
0.218959731912
0.155840544145
-0.108739170739
0.35188500006
0.0322753949277
0.404237399714
0.1256852205
0.389701385155
0.0273506741064
-0.304936099245
0.612342162265
-0.136443541996
-0.0497094657222
-0.17509962623
-0.0508486122411
mode = average
mean of dA = 0.145713902729
dA_prev[1,1] = [[ 0.08485462   0.2787552 ]
 [ 1.26461098 -0.25749373]
 [ 1.17975636 -0.53624893]]
```

# **Expected Output:**

mode = max:

mean of dA =

```
0.145713902729

dA_prev[1,1] =

[[ 0. 0. ] [ 5.05844394 -1.68282702] [ 0. 0. ]]

mode = average

mean of dA =

0.145713902729

dA_prev[1,1] =

[[ 0.08485462 0.2787552 ] [ 1.26461098 -0.25749373] [ 1.17975636 -0.53624893]]
```

# 1.7.4 Congratulations!

Congratulations on completing this assignment. You now understand how convolutional neural networks work. You have implemented all the building blocks of a neural network. In the next assignment you will implement a ConvNet using TensorFlow.

```
In [ ]:
```