

TUMGAD - Exercises

Generated: Wed May 13 18:54:52 CEST 2020

Seed: 586059998

—Disclaimers and Infos:—

1. You can find explanations to all the components in this repository and instructions on how to use the generator [here](#).
2. This paper was generated by automated software written by students. It might contain flaws. If you find one (or even think you've found one), please report it [here](#).
3. TUMGADs creators are not affiliated with the lecture organization whatsoever, the exercises/explanations are not guaranteed to be accurate or complete.
4. The algorithms in this tool are sometimes substantially oversimplified, this is due to the students having to execute them by hand in exams and thus it is impractical to increase the difficulty (e.g. RadixSort only deals with 3-digit numbers).
5. If you like this tool, a good thing you can do is spread the word or star the [repo on GitHub](#) to help out more of your fellow students as well as the creators.

Hashing w/ Chaining		Double Hashing	
MergeSort		QuickSort	
RadixSort		Binary Heaps	
BinomialHeaps		AVL Trees	
(a,b) Trees		BFS & DFS	
Floyd Warshall		Dijkstra	

Hashing with Chaining

Visualize [Hashing with Chaining](#). The size of a hashtable is set to $m = 11$. The following operations are to be executed:

Insert: 13, 15, 12, 2, 0, 20, 3, 11, 7, 5, 14

Use the following hash function:

$$h(x) = (7x + 7) \bmod 11$$

a) Compute the values to which each one of the above numbers map to and enter them into this table:

x	0	2	3	5	7	11	12	13	14	15	20
$h(x)$											

b) Execute the operations above in their given order and enter them into the hashtable preprints.

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Insert: _____

0	1	2	3	4	5	6	7	8	9	10

Double Hashing

Use [Double Hashing](#) and the following Hash functions to resolve any collisions.

$$\begin{aligned}h(x, i) &= (h(x) + i * h'(x)) \mod 11 \\h(x) &= (6x + 0) \mod 11 \\h'(x) &= 5 - (x \mod 5)\end{aligned}$$

Consider these operations:

Insert: 12, 7, 2, 11

Delete: 7, 2, 11

Insert: 5, 9, 7

Multiple hashtables with the size $m = 11$ are provided on the next page.

- Generate the **collision table**, in the printed template on this page for the numbers above.
- Execute the above operations in the provided order, also explicitly state **all checked positions** in the field "Position(s)" above the table (even in deletions).

This table shows the collisions the numbers could go through when inserting them into the hashtable:

x	$h(x)$	$h'(x)$	$h(x, 0)$	$h(x, 1)$	$h(x, 2)$	$h(x, 3)$	$h(x, 4)$

Space for additional calculations:

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

Operation: _____ Position(s): _____

0	1	2	3	4	5	6	7	8	9	10

MergeSort

Sort the following array according to the [MergeSort](#) algorithm:

4, 33, 6, 36, 35, 49, 34, 39, 21, 44, 32, 9, 48, 37, 16, 31

Indicate divisions of the array by clear vertical lines like so:

b, h, j, l, g, a		c, e, d, k, f, i
------------------	--	------------------

Step 1: _____

--

Step 2: _____

--

Step 3: _____

--

Step 4: _____

--

Step 5: _____

--

Step 6: _____

--

Step 7: _____

--

Step 8: _____

--

Step 9: _____

--

QuickSort

Sort the following array according to the [QuickSort](#) algorithm:

6, 15, 11, 14, 10, 4, 7, 3, 2

Choose the last element of the array as the pivot element.

It helps to clearly mark sub-arrays in each step like so:

Step one - pivot: i
b, h, f, l, g, a, c, e, d | i | j, k

pivot: _____

New Array: _____

pivot: _____

New Array: _____

pivot: _____

New Array: _____

pivot: _____

New Array: _____

pivot: _____

New Array: _____

pivot: _____

New Array: _____

pivot: _____

New Array: _____

pivot: _____

New Array: _____

RadixSort

a) Sort the following array of integers according to the [LSD RadixSort](#) algorithm:

608, 926, 798, 313, 779, 679, 536, 722, 794

First round:

0	1	2	3	4	5	6	7	8	9

New List: _____

Second round:

0	1	2	3	4	5	6	7	8	9

New List: _____

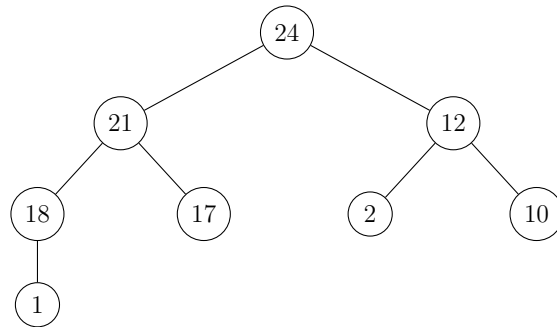
Third round:

0	1	2	3	4	5	6	7	8	9

Sorted Array: _____

Binary Heaps

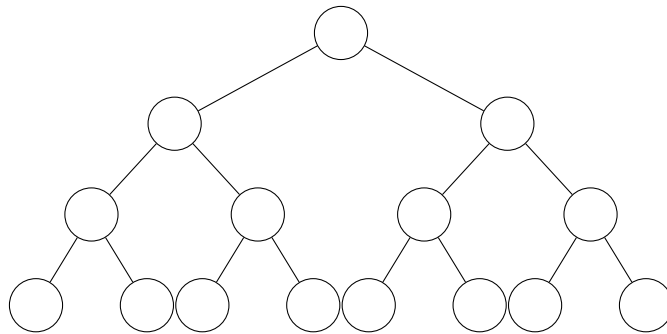
Given the following [Binary max-Heap](#):



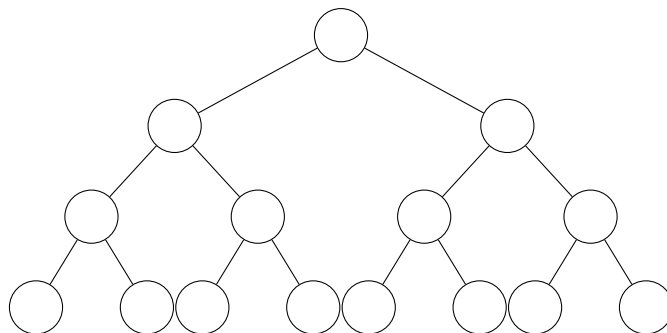
a) Perform the following insert-operations and their corresponding sift-operations on the above heap:

25, 13, 11, 7, 4

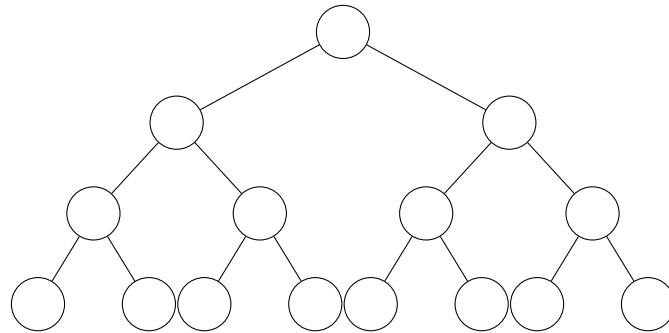
Insert: ____



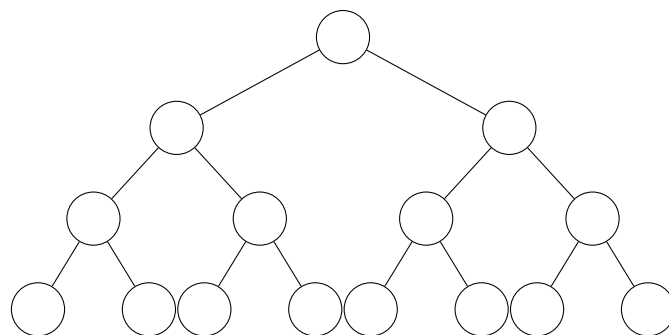
Insert: ____



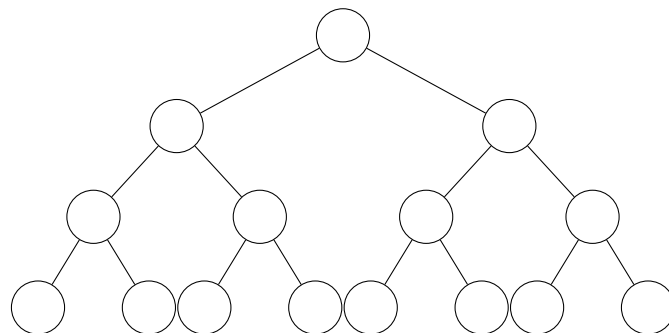
Insert: ____



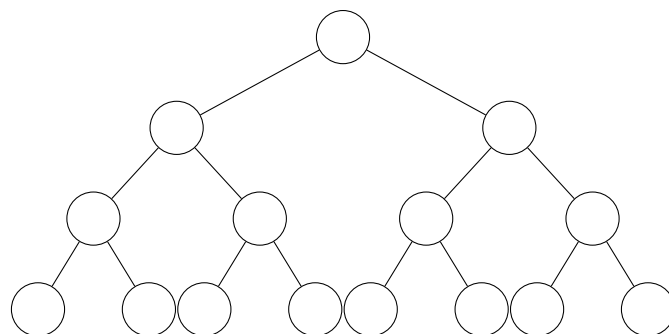
Insert: ____

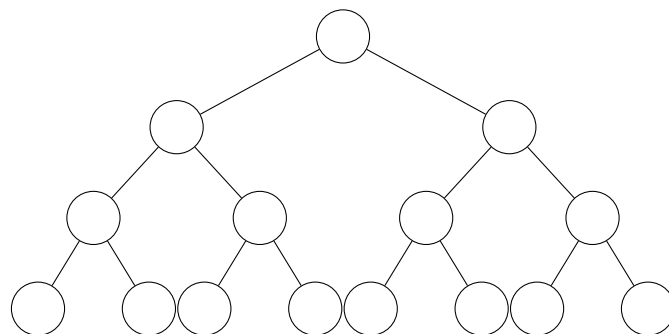
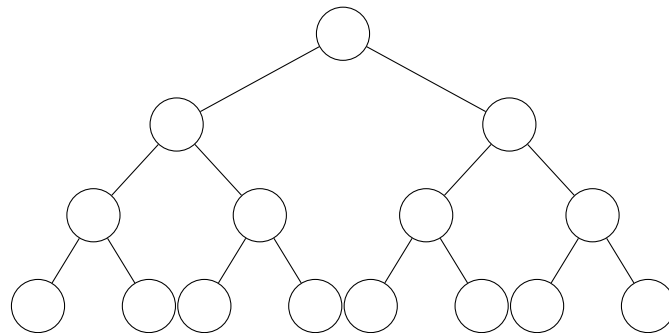
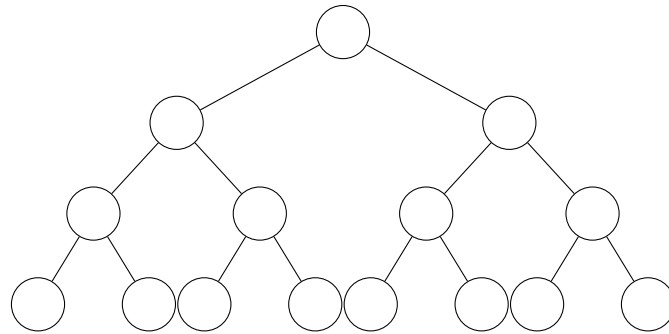
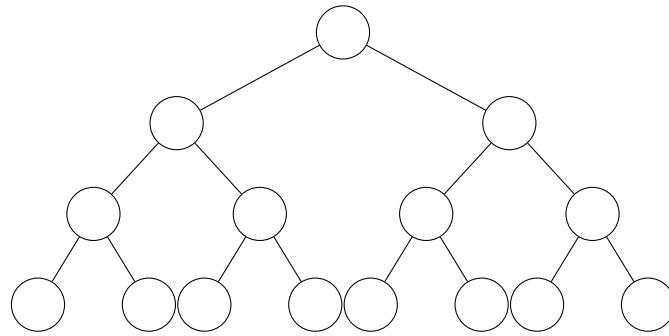


Insert: ____



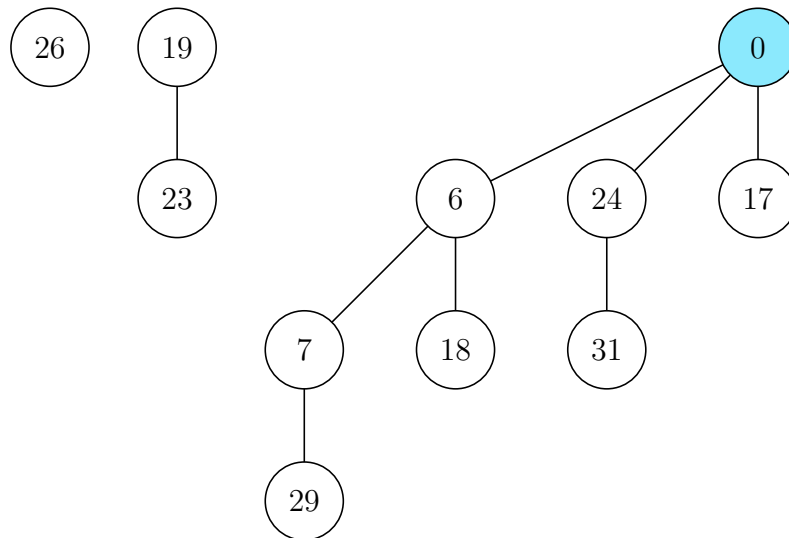
b) Now perform the known deleteMax() operation and its sift-operations 5 times





Binomial Heaps

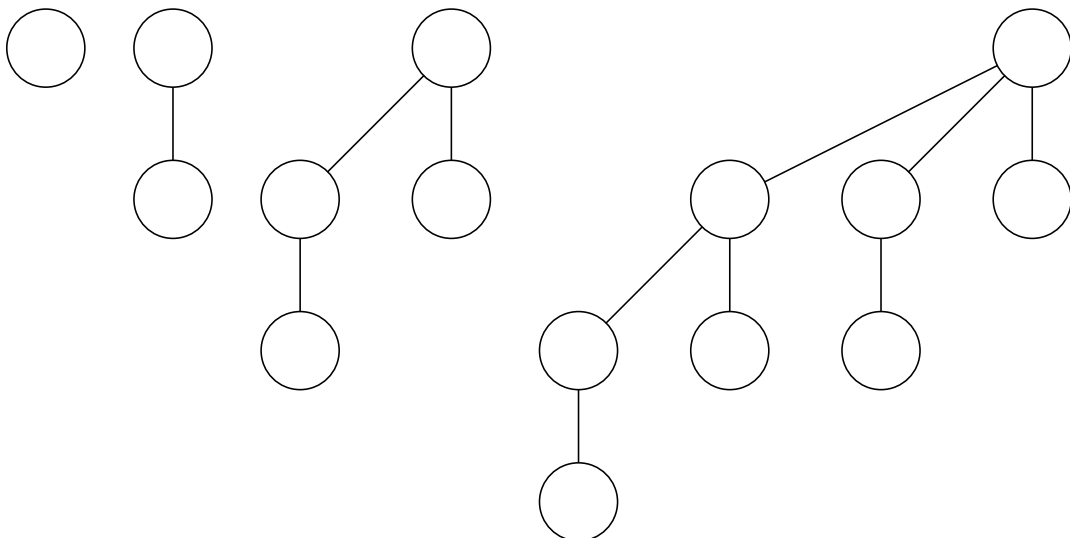
Given the following [Binomial Heap](#):



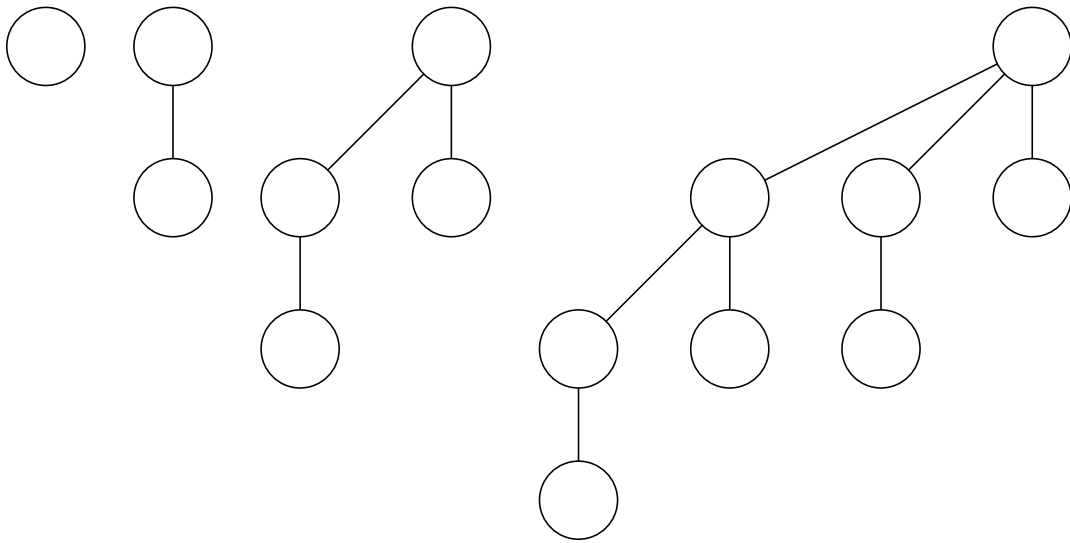
a) Execute the known `deleteMin()` operation **four times** on the above heap and be careful to meet the heap-criteria after each step.

You can use the pre-prints provided below, be sure to clearly mark trees that are unused:

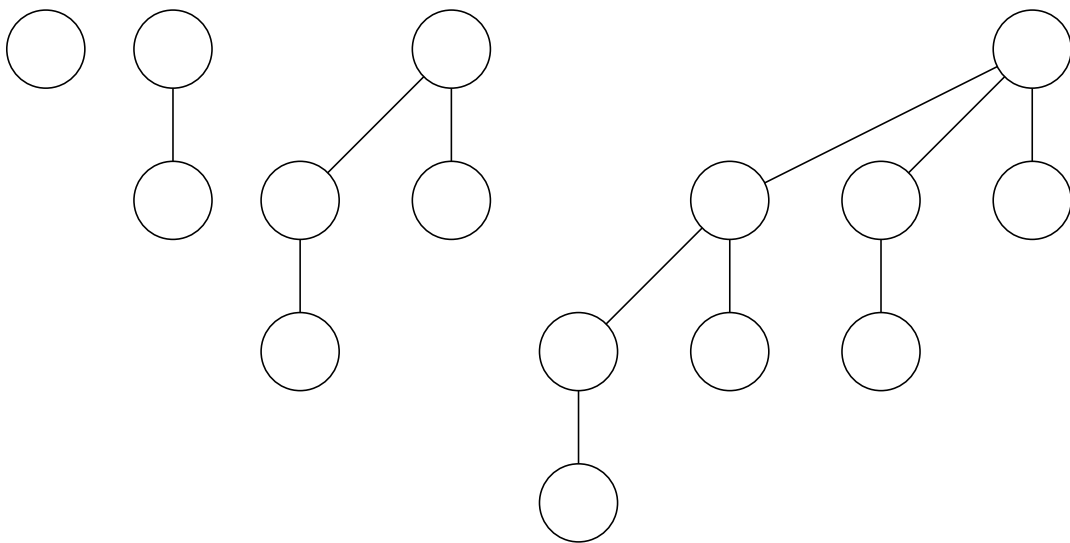
`deleteMin()`: min = _____



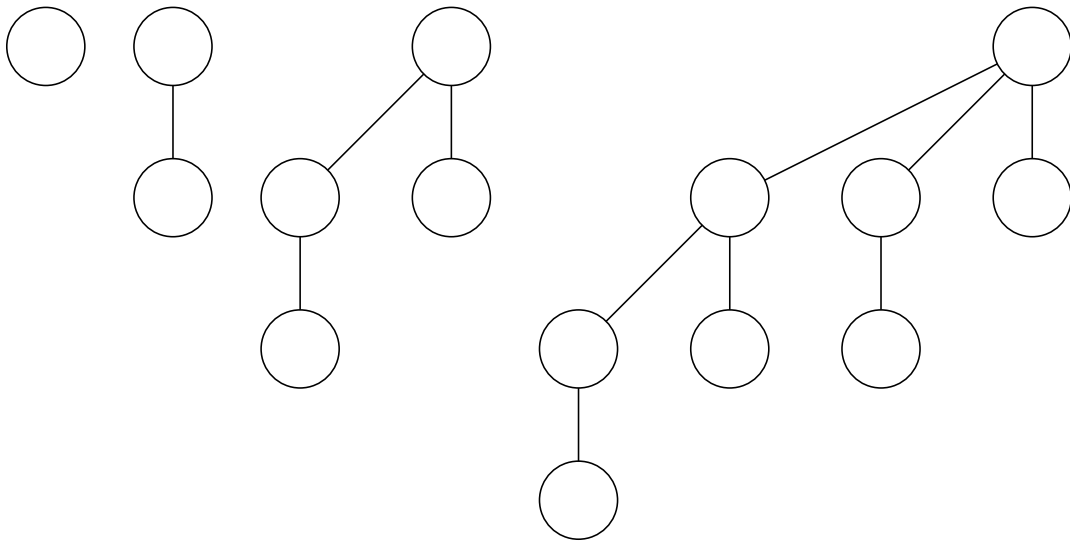
Insert: _____



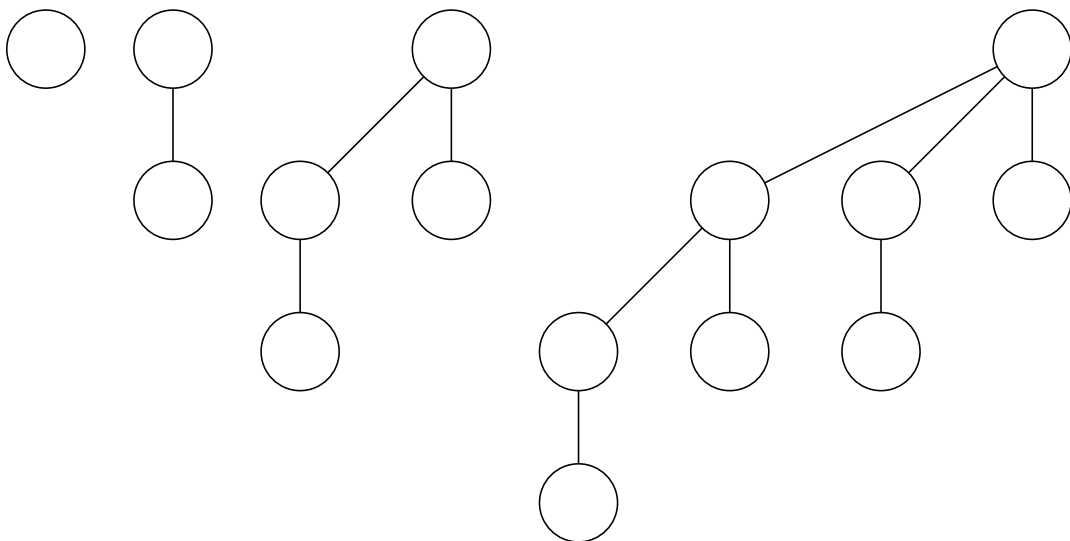
Insert: _____



Insert: _____

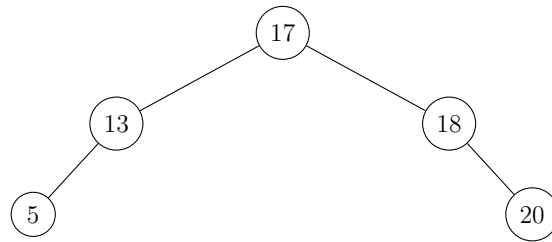


Insert: _____



AVL Trees

Given the following [AVL Tree](#):



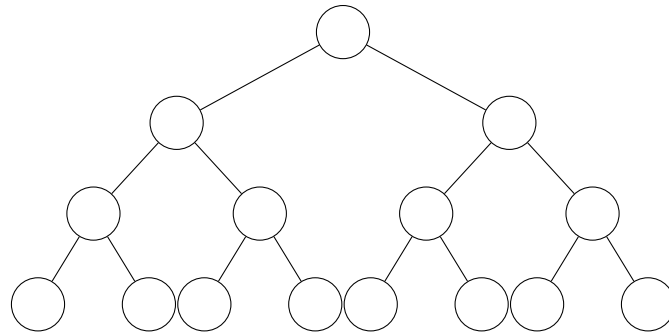
Perform the following operations in their given order on the tree above and check the boxes above the preprints if any rotation was performed.

Insert: 9, 12, 23, 3, 7

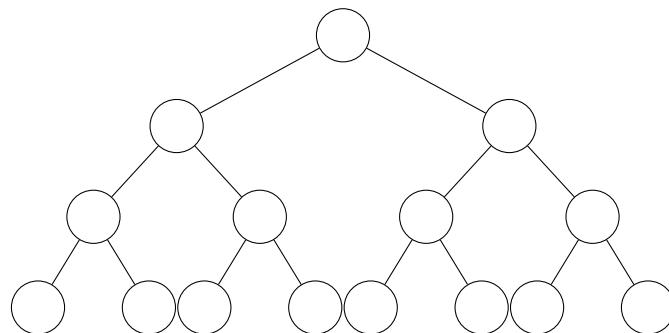
Delete: 13, 3

Insert: 1, 2

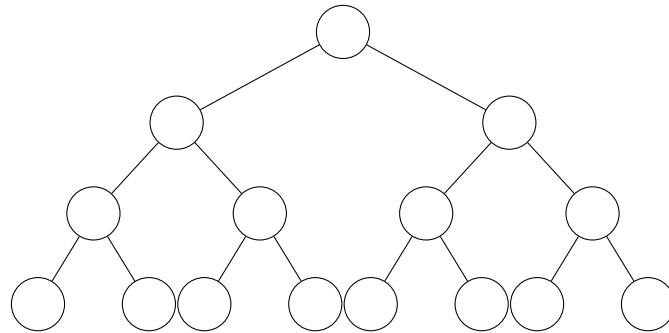
Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



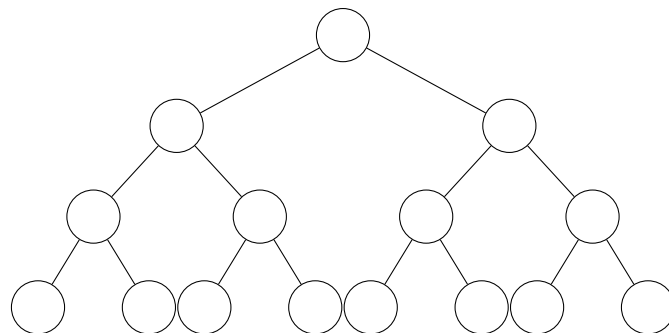
Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



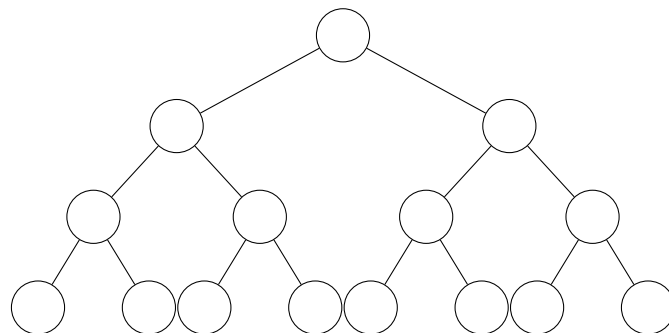
Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



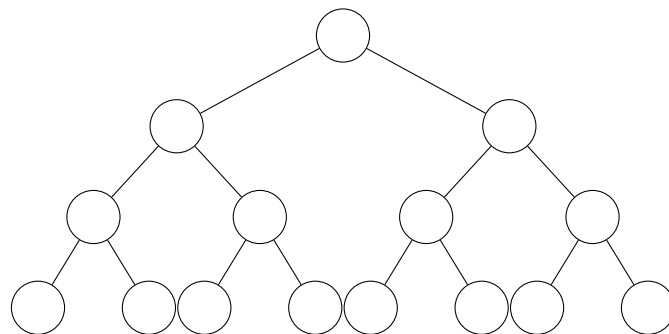
Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



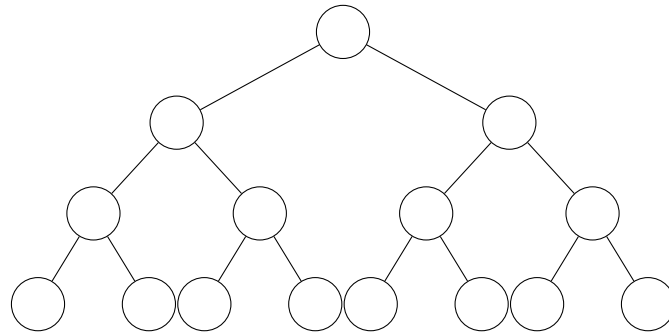
Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



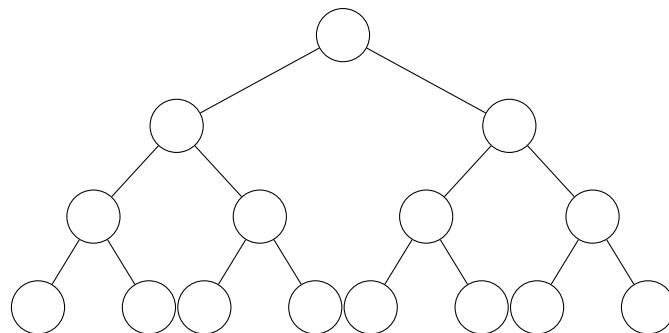
Delete: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



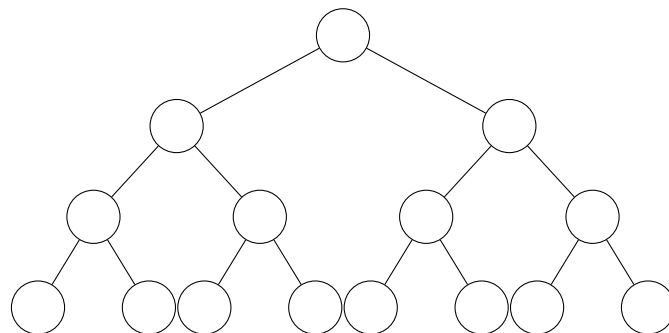
Delete: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



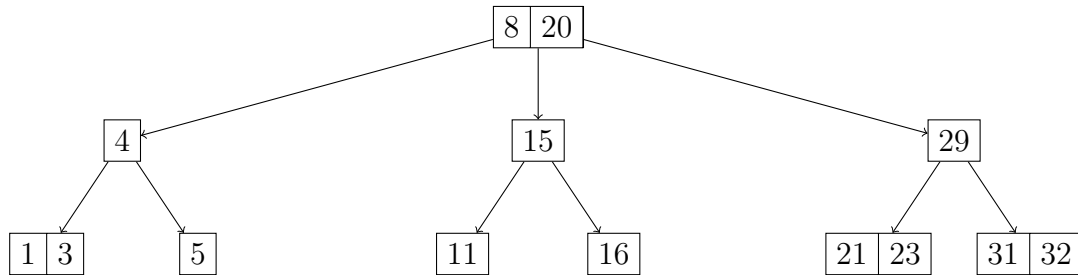
Insert: ____ ☐ l rotation ☐ r rotation ☐ l-r rotation ☐ r-l rotation ☐ no rotation



Now give the Pre-Order visitation sequence of the AVL-Tree:

(a,b) Trees

Given the following [\(a,b\) Tree](#) with $a = 2$ and $b = 3$:



Perform the following operations in their given order on the tree above:

Delete: 3, 5, 31, 4, 20
Insert: 34, 18, 10, 30, 26

Delete: _____

Delete: _____

Delete: _____

Delete: _____

Delete: _____

Insert: _____

Insert: _____

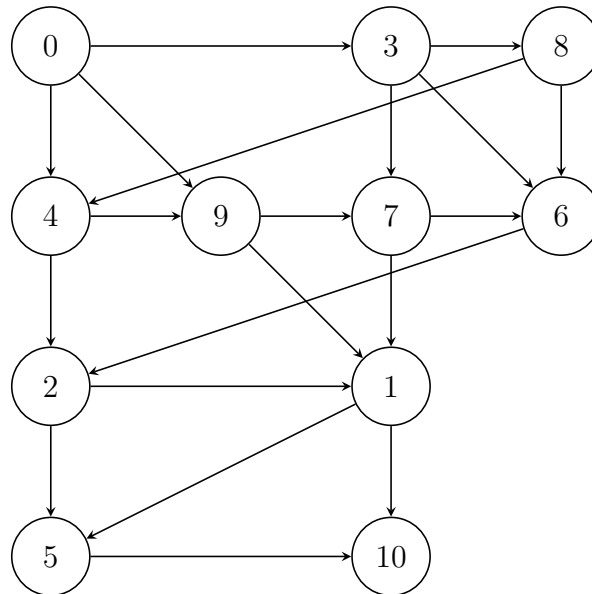
Insert: _____

Insert: _____

Insert: _____

Graph Traversal (DFS & BFS)

Given the following directed graph:

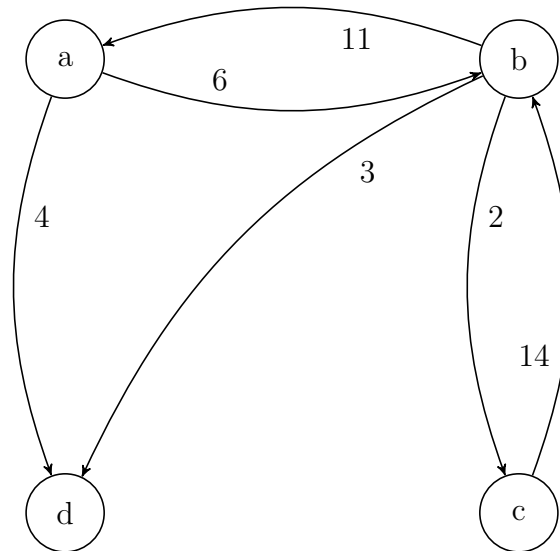


- a) In which order will the nodes in the graph be visited when traversing the graph with [Breadth-First Search](#)?
Start at node 0.

- b) In which order will the nodes in the graph be visited when traversing the graph with [Depth-First Search](#)?
Start at node 0 again.

APSP / Floyd-Warshall Algorithm

Given the following directed graph:



Follow the [Floyd-Warshall algorithm](#) for APSP and enter the node distance matrix after each step.

Assume the algorithm continues with the next element lexicographically.

As always, unknown distances should be abstracted as infinity.

Initial Matrix:

	a	b	c	d
a				
b				
c				
d				

Matrix for $k = \underline{\hspace{1cm}}$:

	a	b	c	d
a				
b				
c				
d				

Matrix for $k = \underline{\hspace{1cm}}$:

	a	b	c	d
a				
b				
c				
d				

Matrix for $k = \underline{\hspace{1cm}}$:

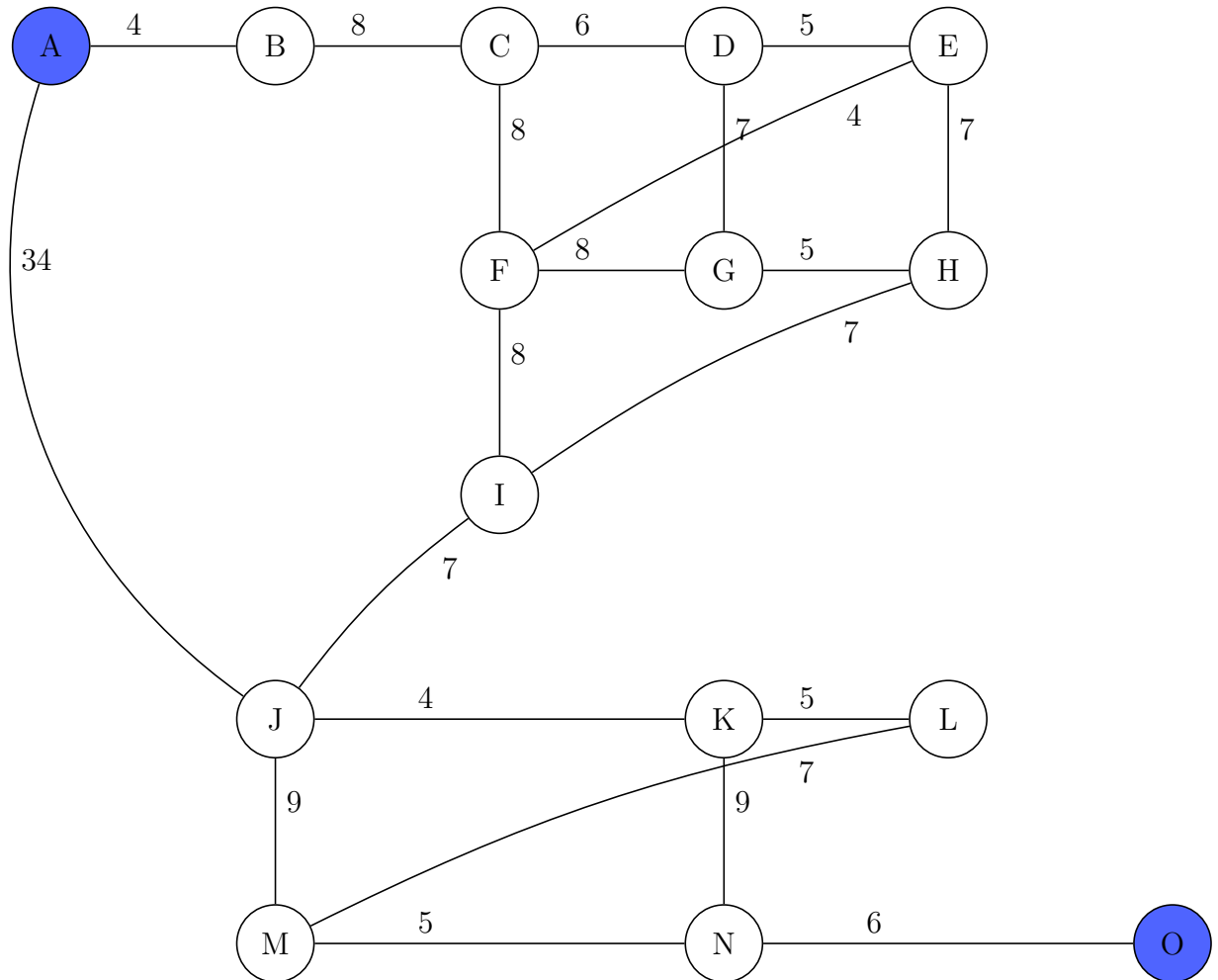
	a	b	c	d
a				
b				
c				
d				

Matrix for $k = \underline{\hspace{1cm}}$:

	a	b	c	d
a				
b				
c				
d				

Dijkstra's Algorithm

Given the following graph:



a) Follow the [Algorithm of Dijkstra](#) as covered in the lecture and find the shortest path from node *A* to node *O*.

Note the algorithm's priority queue after every step, as well as the changes made to the queue in the step.

If nodes have equal priorities, the algorithm follows the node that was inserted first.

Priority Queue	Updates in Queue

b) What is the shortest path between the nodes and how long is it?

A →
Length: _____