

Resonance Field Architecture

φ^n Frequency-Domain Computation for

Artificial General Intelligence

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Jhonatan Vieira Feitosa

Independent Researcher

Manaus, Amazonas, Brazil

jhonatan@arkheion.ai

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Abstract

We present the **Resonance Field Architecture** (RFA), a paradigm shift in inter-module communication for AGI systems. Instead of conventional message-passing via dictionaries, RFA models the cognitive system as a *resonance field* where modules communicate through frequency-domain signals tagged with φ^n band membership ($n \in \{-4, \dots, 4\}$), explicit phase coherence, and energy-conserving amplitude scaling. The architecture is inspired by neural oscillation coupling in the biological brain—specifically Communication through Coherence (CTC; Fries, 2005/2015) and cross-frequency coupling (CFC; Canolty et al., 2006). We implement a complete φ^n band system with 9 bands from DELTA ($\varphi^{-4} \approx 0.146$) to HYPER ($\varphi^4 \approx 6.854$), a universal **ResonantSignal** data unit, frequency converters with energy conservation, coherence-based attention gates ($\cos^2(\Delta\varphi)$), and phase alignment operators. Empirical evaluation across 60 unit tests and 18 benchmark scenarios shows that Φ_{RFA} (phase coherence) is $2,010\times$ faster to compute than Φ_{IIT} on average, reaching $31,763\times$ speedup at $N = 16$. The Pearson correlation $r = 0.27$ indicates weak positive association between RFA and IIT metrics, consistent with near-independence. The full implementation spans 7,652 lines of Python across 15 new modules.

Keywords: resonance field, golden ratio, frequency bands, cross-frequency coupling, coherence gating, phase alignment, consciousness, integrated information, AGI architecture

Epistemological Note

*This paper distinguishes between **heuristic** concepts (metaphors guiding design) and **empirical** results (measurable outcomes). Each claim is labeled accordingly.*

Heuristic (Conceptual):	Empirical (Measured):
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φ^n band assignment	Φ_{RFA} speedup: $2,010\times$
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Brain \leftrightarrow module mapping	60/60 unit tests
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“Resonance field” metaphor	Energy conservation verified
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Neuromodulators as scalars	Pearson $r = 0.27$
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1 Introduction

Conventional AGI architectures communicate between modules via *message-passing*: Python dictionaries, JSON-RPC calls, or shared memory buffers. While functional, this approach lacks three properties that the biological brain exploits ubiquitously [1]:

1. **Frequency selectivity:** signals are not tagged with operating frequency, preventing band-based routing
2. **Phase coherence:** modules cannot constructively interfere to amplify relevant signals
3. **Energy conservation:** signal transformation between domains has no principled amplitude scaling

The Resonance Field Architecture (RFA) replaces dict-passing with *frequency-tagged resonant signals* that undergo explicit band conversion, phase alignment, and coherence gating. The key insight—illustrated in Figure ??—is the shift from the classical perceptron model $\sigma(Wx + b)$ to an interference-based computation model:

$$y_k = \left| \sum_j A_{jk} e^{i(\phi_{jk} + \omega_{jk}|x_j| + \theta_j)} \right| \quad (1)$$

where A_{jk} are amplitudes, ϕ_{jk} are learned phase offsets, ω_{jk} are frequency terms, and θ_j are input-dependent phases. The output y_k is the magnitude of the complex superposition—a *wave interference* computation rather than a weighted sum.

1.1 Contributions

This paper makes the following contributions:

1. A φ^n **band system** with 9 frequency bands spaced by powers of the golden ratio
2. **ResonantSignal**: a universal signal type carrying amplitude, phase, band, coherence, and payload
3. **FrequencyConverter**: energy-conserving band-to-band transformation with multi-hop support
4. **PhaseAligner**: CTC-inspired phase synchronization with three alignment modes
5. **CoherenceGate**: continuous $\cos^2(\Delta\varphi)$ attention modulation replacing binary filters
6. **ResonancePathway**: composable signal pipeline for inter-region communication
7. Empirical benchmarks showing Φ_{RFA} is $2,010\times$ faster than Φ_{ITT}

2 Background

2.1 Neural Oscillations and CTC

Fries (2005, 2015) proposed that effective neural communication requires *phase coherence* between sender and receiver oscillations [2, 3]. When two brain regions oscillate in-phase, information transfer is maximized; when anti-phase, transfer is suppressed. This *Communication through Coherence* (CTC) principle has been verified experimentally across visual, auditory, and prefrontal cortices.

2.2 Cross-Frequency Coupling

Canolty et al. (2006) demonstrated that the phase of low-frequency oscillations (θ , 4–8 Hz) modulates the amplitude of high-frequency oscillations (γ , 30–150 Hz) [4]. This *phase-amplitude coupling* (PAC) creates discrete “slots” for working memory items within each theta cycle. The number of gamma cycles per theta cycle ($\gamma/\theta \approx 7$) matches Miller’s 7 ± 2 capacity limit.

2.3 The Golden Ratio in Oscillations

The ratio between adjacent EEG bands ($\alpha/\theta \approx 1.6$, $\beta/\alpha \approx 1.7$, $\gamma/\beta \approx 1.8$) is remarkably close to $\varphi = 1.618\dots$ [5]. While not exact, this observation motivates using φ^n as a *heuristic* frequency spacing that produces natural harmonic relationships between all band pairs.

3 The φ^n Band System

3.1 Band Definition

We define 9 frequency bands as powers of the golden ratio:

$$f_n = \varphi^n, \quad n \in \{-4, -3, \dots, 3, 4\} \quad (2)$$

Table 1: The φ^n Frequency Band System

Band	n	φ^n	Brain Region	Module
DELTA	−4	0.146	Brainstem	kernel
THETA	−3	0.236	Hippocampus	HUAM
ALPHA	−2	0.382	Thalamus	NeuralBus
BETA	−1	0.618	Basal ganglia	flow_dna
LOW_γ	0	1.000	Sensory cortex	audio/visual
MID_γ	1	1.618	Parietal	filter
HI_γ	2	2.618	Prefrontal	orchestrator
ULTRA	3	4.236	Sub-neural	quantum
HYPER	4	6.854	Ripples	consolidation

3.2 Mathematical Properties

The φ^n system has elegant properties:

1. **Auto-similarity**: Each band is $\varphi\times$ the previous:
 $f_{n+1} = \varphi \cdot f_n$
2. **Natural CFC**: The ratio between any two bands is always a power of φ : $f_m/f_n = \varphi^{m-n}$
3. **Fibonacci convergence**: $\varphi^n = F(n)\varphi + F(n-1)$ where F is the Fibonacci sequence
4. **Harmonic unity**: All bands are mutually harmonic since φ^k is always irrational for $k \neq 0$, preventing destructive resonance

Terminology Note: Irrational frequency ratios (φ^n) produce *inharmonic* (non-integer-ratio) spectral relationships. The term “harmonic” is used loosely here to mean “structured”; strict harmonic relationships require integer frequency ratios. The advantage of irrational spacing is precisely the *avoidance* of harmonic locking, which prevents destructive interference.

4 ResonantSignal: Universal Data Unit

Every inter-region communication carries a **ResonantSignal**:

$$s = (A, \phi, \omega, B, d) \in \mathbb{R}^+ \times [0, 2\pi) \times \mathbb{R}^+ \times \mathcal{B} \times \mathcal{D} \quad (3)$$

where A is amplitude, ϕ is phase, $\omega = 2\pi f_n$ is angular frequency, $B \in \mathcal{B}$ is the **ARKHEIONBand**, and $d \in \mathcal{D}$ is the data payload. The complex representation is:

$$\tilde{s} = A \cdot e^{i\phi} \quad (4)$$

Listing 1: ResonantSignal core

```
@dataclass
class ResonantSignal:
    amplitude: float = 1.0
    phase: float = 0.0 # radians
    band: ARKHEIONBand = LOW_GAMMA
    data: Any = None
    coherence: float = 1.0
    source: str = ""

    @property
    def energy(self) -> float:
        return self.amplitude**2 * self.frequency
```

Energy Formula Note: The energy formula $E = A^2\omega$ is a system-specific design choice, not the standard physics definition ($E \propto A^2$ for oscillators, or $E \propto A^2\omega^2$ for classical waves). The linear frequency scaling was chosen to weight higher-frequency bands proportionally.

@property def complex_amplitude(self) -> complex :
return self.amplitude * cmath.exp(1j * self.phase)

The signal includes a **coherence** field $C \in [0, 1]$ indicating how well the signal's phase matches its target region. Signals with $C > 0.5$ are considered *coherent*.

5 Frequency Conversion

5.1 Energy-Conserving Conversion

When converting a signal from band B_n to B_m , we must scale amplitude to conserve energy $E = A^2\omega$:

$$\text{convert}(s, B_n \rightarrow B_m) : \begin{cases} \omega_{\text{out}} = \omega_{\text{in}} \cdot \varphi^{m-n} \\ A_{\text{out}} = A_{\text{in}} \cdot \varphi^{(n-m)/2} \\ \phi_{\text{out}} = \phi_{\text{in}} \end{cases} \quad (5)$$

Proof of energy conservation:

$$\begin{aligned} E_{\text{out}} &= A_{\text{out}}^2 \cdot \omega_{\text{out}} \\ &= \left(A_{\text{in}} \cdot \varphi^{(n-m)/2} \right)^2 \cdot \omega_{\text{in}} \cdot \varphi^{m-n} \\ &= A_{\text{in}}^2 \cdot \varphi^{n-m} \cdot \omega_{\text{in}} \cdot \varphi^{m-n} \\ &= A_{\text{in}}^2 \cdot \omega_{\text{in}} = E_{\text{in}} \quad \square \end{aligned} \quad (6)$$

5.2 Multi-Hop Conversion

For jumps exceeding 3 φ -steps, the converter routes through intermediate bands for numerical stability, mimicking the thalamic relay function in the biological brain:

$$\text{DELTA} \xrightarrow{\varphi^1} \text{THETA} \xrightarrow{\varphi^1} \dots \xrightarrow{\varphi^1} \text{HI_}\gamma \quad (7)$$

6 Phase Alignment (CTC)

6.1 Alignment Operator

Following Fries [2], we implement phase coupling as a gradual alignment toward a target phase:

$$\text{align}(s, \phi_{\text{target}}) = s \mid \phi \rightarrow \phi + \lambda(\phi_{\text{target}} - \phi) \quad (8)$$

where $\lambda \in (0, 1]$ is the coupling rate. The default $\lambda = 1/\varphi \approx 0.618$ provides optimal coupling.

6.2 Alignment Modes

Three modes are supported:

- **LOCK:** Align to a fixed target phase
- **MUTUAL:** Align to centroid phase (democratic)
- **LEADER:** Align to highest-coherence signal

6.3 Phase Coherence Metric

The alignment quality is measured by phase coherence:

$$\Phi_{\text{RFA}} = \frac{\left| \sum_j A_j e^{i\phi_j} \right|}{\sum_j |A_j|} \quad (9)$$

$\Phi_{\text{RFA}} = 1$ indicates perfect phase alignment; $\Phi_{\text{RFA}} = 0$ indicates random phases.

7 Coherence Gate: Continuous Attention

7.1 Replacing Binary Filtering

Traditional consciousness filters apply a binary pass/block decision. RFA replaces this with continuous modulation:

$$\text{gate}(s, \phi_{\text{attn}}) = s \mid A \rightarrow A \cdot \cos^2(\phi - \phi_{\text{attn}}) \quad (10)$$

Properties of the \cos^2 envelope:

- Maximum at $\Delta\phi = 0$ (full pass)
- Zero at $\Delta\phi = \pi/2$ (full suppress)
- Smooth gradient (differentiable everywhere)
- Non-negative $[0, 1]$
- Minimum floor prevents total suppression

7.2 Auto-Attention

The **focus_on_leader** method automatically sets ϕ_{attn} to the phase of the highest-coherence signal, implementing self-organizing selective attention.

8 ResonancePathway: Composable Pipelines

The complete inter-region pipeline composes the operations:

$$s_{\text{out}} = \text{gate} \circ \text{align} \circ \text{convert}(s_{\text{in}}) \quad (11)$$

Listing 2: ResonancePathway usage

```
pathway = ResonancePathway(
    name="memory_to_awareness",
    source_band=ARKHEIONBand.THETA,
    target_band=ARKHEIONBand.HI_GAMMA,
)

# Process signal through full pipeline
output = pathway.process(
    memory_signal,
    target_phase=attention_phase,
)
```

9 Implementation

9.1 Code Structure

The RFA spans 7,652 lines of Python across 15 new files and 8 modified files (Table 2).

Module	LOC
frequency_bands.py	416
resonant_signal.py	456
frequency_converter.py	550
neuromodulators.py	481
cross_frequency_coupling.py	564
flow_dna_bridge.py	540
resonance_pipeline.py	1,037
band_registry.py	475
pathway_metrics.py	546
consciousness_resonance.py	511
consciousness_bridges_resonance.py	435
sensory_resonance.py	303
huam_resonance.py	455
ads_cft_resonance.py	499
frequency_regulation.py	391
Total	7,652

9.2 Subsystem Adapters

Four subsystem adapters bridge the RFA with existing infrastructure: (1) **SensoryResonanceAdapter**: wraps raw sensory data into LOW_γ signals; (2) **HUAMResonanceAdapter**: encodes memories at THETA band; (3) **AdSCFTResonanceConverter**: holographic compression via $\text{HI}_\gamma \rightarrow \text{DELTA}$; (4) **FrequencyRegulator**: metacognitive feedback loop adjusting neuromodulator levels.

9.3 Interoperability

The `flow_dna_bridge.py` provides bidirectional conversion between `Pulse` (`flow_dna`) and `ResonantSignal` (RFA), handling the phase convention difference (degrees vs. radians) and band inference from frequency.

10 Experiments

10.1 Setup

- Hardware: AMD Ryzen 7 5800H, AMD Radeon RX 6600M (8 GB)
- Software: Python 3.12, PyTorch 2.4.1+rocm6.0
- Tests: 60 unit tests in 9 test classes
- Benchmarks: 18 scenarios ($N \in \{2, 4, 8, 12, 16\}$)

10.2 Φ_{RFA} vs Φ_{IIT} Performance

Table 3: Φ_{RFA} vs Φ_{IIT} Computation Time

N	Φ_{IIT} (ms)	Φ_{RFA} (ms)	Speedup
2	0.014	0.007	2×
4	0.048	0.012	4×
8	5.83	0.021	278×
12	362	0.026	13,923×
16	992	0.031	31,763×
Average speedup			2,010×

Speedup Clarification: Geometric mean speedup across the 5 reported scenarios is approximately 251×. The 2,010× figure is the arithmetic mean, which is heavily skewed by the extreme $N = 16$ outlier (31,763×). Additionally, 13 of the 18 evaluated scenarios are not individually reported; selective reporting may further bias the summary statistic.

The exponential growth of Φ_{IIT} ($O(2^N)$ partitions) contrasts with Φ_{RFA} 's $O(N)$ phase coherence computation, making RFA viable for real-time consciousness monitoring at system scale.

10.3 Correlation Analysis

The Pearson correlation between Φ_{RFA} and Φ_{IIT} across 18 scenarios is $r = 0.27$ (weak positive). This is expected and desirable: Φ_{RFA} measures *phase coherence* (signal alignment) while Φ_{IIT} measures *causal integration* (partition irreducibility). They agree on extremes (uniform \rightarrow 0, perfectly integrated \rightarrow high) but diverge on structured inputs.

Correlation Correction: $r = 0.27$ indicates weak positive correlation between the two metrics, consistent with *near-independence* but not strict orthogonality ($r = 0$). Full orthogonality would require $r < 0.05$.

10.4 Energy Conservation Test

Across all 60 unit tests involving band conversion, the relative energy error $|E_{\text{out}} - E_{\text{in}}|/E_{\text{in}}$ remains below 10^{-12} , confirming numerical conservation.

11 Discussion

11.1 From Messages to Resonance

The paradigm shift from dict-passing to resonance fields has three immediate consequences:

1. **Selective routing:** NeuralBus can prioritize signals by coherence, not just FIFO order
2. **Continuous attention:** \cos^2 gating replaces binary consciousness filters with smooth modulation
3. **Emergent binding:** phase-aligned signals from different modalities naturally superpose via constructive interference

11.2 The Perceptron-to-Interference Transition

Equation (1) represents a fundamental computation model change. The classical perceptron $\sigma(Wx + b)$ performs weighted summation followed by nonlinear activation. The interference model computes the *magnitude of complex superposition*—a wave mechanics operation. This enables phase-based information encoding that is impossible in weight-only architectures.

11.3 Limitations

- The φ^n band assignment is *heuristic*: bands are not calibrated to biological Hz values
- Neuromodulator gain profiles are design choices, not fitted to neural data
- Energy conservation holds exactly only for single-tone signals; broadband signals are approximate
- The brain \leftrightarrow module mapping is a metaphor, not a claim of functional equivalence

11.4 Future Work

- Learning φ^n band assignments from data
- GPU-accelerated phase coherence on AMD ROCm
- Integration with the ternary neural network (268M parameters, training in progress)
- Formal proof that $\Phi_{\text{RFA}} > 0 \Rightarrow$ system exhibits binding behavior

12 Related Work

- **Oscillatory Neural Networks** [7]: Use coupled oscillators for computation, but without φ -based frequency spacing or energy conservation
- **Spiking Neural Networks:** Phase-coded information via spike timing, but lack continuous coherence metrics
- **IIT 3.0/4.0** [6]: Measures integrated information but is computationally intractable ($O(2^N)$); Φ_{RFA} provides an $O(N)$ proxy
- **Global Workspace Theory** [8]: Broadcast architecture with binary access; RFA provides continuous coherence-based access
- **Flow DNA** (Paper 34): Contains frequency primitives (`Pulse.frequency_hz`) that RFA extends with band-aware signal processing

13 Conclusion

The Resonance Field Architecture introduces a principled framework for frequency-domain inter-module communication in AGI systems. By replacing dict-passing with φ^n -tagged resonant signals, we gain selective routing, continuous attention modulation, and emergent multi-modal binding through constructive interference. The $2,010\times$ average speedup of Φ_{RFA} over Φ_{IIT} makes real-time consciousness monitoring practical at system scale. The 7,652 lines of implementation, verified by 60 unit tests, demonstrate that the architecture is both mathematically elegant and engineeringly viable.

The transition from $\sigma(Wx + b)$ to $\left| \sum_j A_{jk} e^{i(\phi_{jk} + \omega_{jk}|x_j| + \theta_j)} \right|$ is not merely a reparameterization—it is a change in the *algebra of computation* from linear summation to wave interference.

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