

## CS21 Machine Problem: Sudoku Solver

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Lab 2

2020-04243

**Note:** Please input the lines in the program one line at a time. My program cannot handle if the input is inserted all at once.

Link for the Video:

<https://drive.google.com/file/d/1CRHYQtFF3cbtDNXcW42W-kCrjxVXzbln/view?usp=sharing>

### I. Summary

I will only provide a single summary since both of the solvers work the same way. The solvers utilize backtracking in solving the sudoku boards. It checks each element if it is a "0" and tries to solve it if it is a "0". Otherwise, it goes to the next element. If it has already solved a "0" and the next element will not have an answer, it will go back to its previous state before solving the "0". It will then try another answer for it until the board is solved.

Before explaining the function used, I will discuss how the input is stored and how it is represented in the program. The input is stored in .data line by line in ASCII format. Since .data is used, the first element will be stored at 0x10010000 and so on. For example, if the input line is 4020, it will be represented as 0x30323034 inside the data. Note that "0" is 0x30 in ASCII and the others have their respective representation as well. Also, when gathering the input, I used 32 bits for each line just to make it more understandable while working on it. The .data serves as our board and we can access the elements by using the correct address for each one (this will be explained more later). The board is stored as ASCII values, thus, it will be stored in a way that left and right are exchanged because MARS is in little endian. But this will not affect the final output since they will be printed in the way they should be.

There is only one function used in the program I made and it is `sudoku( )`. The `sudoku( )` is the function called in the main. This is where each element is checked if it is a "0". Also, the change in board also happens here. Before changing the "0" in the board, it first checks whether the current num is already in the current row, column or square. If it is already used on those places, the change will not be implemented and it will try to use the next possible num value. Meanwhile, if it is still not used, the current "0" in the board will be replaced by the current num. After that, the function will call itself to try to solve the next "0" in the board. The cycle will continue until the board is solved. Then, the deepest recursion will return 1 to the previous recursion. This will cause a domino effect on all the recursions made and they will end one after the other. Assuming that all the problems that will be given are solvable, the program already has solved board at the .data at this point. The program prints all the lines of the board and it will end.

### Shortest Summary:

Get input-> call `sudoku`-> Check from left to right, top to bottom if element is "0"-> if not "0", skip; if "0", check if num is already used in the current row, column or square-> if num is already used, try the next num. If there are no num left, go back to previous state; if still not used, change the element in the board-> recurse `sudoku`-> wait till finished-> print output

## II. Pseudocodes

The pseudocode I made is somewhat in the format of C combined with python language to make it easier for me to implement it on MIPS. Note that there is a more simplified version of it later. The “long” pseudocode will be the one that I will explain in the video to show its implementation on MIPS better.

Here is the long/detailed pseudocode for the 4x4 sudoku solver:

```
sudoku( ){
    sudoku_value=0
    for (row=0 to row<4):
        for (col=0 to col<4):
            if (board[row][col]==0x30):
                for (num=0x31 to num<0x35):
                    num_already_used =0

                    for (ROW=0 to ROW<4):
                        if (num_already_used==1) break
                        if (board[ROW][col]==num) num_already_used =1
                    end for loop

                    for (COL=0 to COL<4):
                        if (num_already_used==1) break
                        if (board[row][COL]==num) num_already_used =1
                    end for loop

                    for (ROW =floor(row/2)*2 to ROW <floor(row/2)*2+2; ROW):
                        for (COL = floor(col/2)*2 to COL <floor(col/2)*2+2):
                            if (num_already_used==1) break
                            if (board[ROW][col]==num) num_already_used =1
                        end for loop
                    end for loop

                    if (num_already_used ==0):
                        board[row][col]=num
                        sudoku_value=sudoku( )
                        if (sudoku_value==1):
                            sudoku_value=1
                            return sudoku_value
                        else: board[row][col]=0x30

                    end for loop
                end for loop
            end for loop
        end for loop
    sudoku_value=1
    return sudoku_value
}
```

//checks board from top to bottom  
//checks board from left to right  
//checks if current element is a “0”  
//tries to solve using “1” to “4”  
//checks if num is already in the column  
//checks if num is already in the row  
//checks if num is already in the 2x2 square  
//changes current “0” to num  
//recurse to solve next “0”  
//domino effect to end all recursion  
//previous change is wrong; go back to last state  
//no values of num can be used; mistake was made  
//finished to change all “0” in board

Here is the long/detailed pseudocode for the 9x9 sudoku solver. It is almost the same as the 4x4 solver except for the values used.

```
sudoku( ){
    sudoku_value=0
    for (row=0 to row<9):
        for (col=0 to col<9):
            if (board[row][col]==0x30):
                for (num=0x31 to num<0x3A):
                    num_already_used =0

                    for (ROW=0 to ROW<9):
                        if (num_already_used==1) break
                        if (board[ROW][col]==num) num_already_used =1
                    end for loop

                    for (COL=0 to COL<9):
                        if (num_already_used==1) break
                        if (board[row][COL]==num) num_already_used =1
                    end for loop

                    for (ROW =floor(row/3)*3 to ROW <floor(row/3)*3+3; ROW):
                        for (COL = floor(col/3)*3 to COL <floor(col/3)*3+3):
                            if (num_already_used==1) break
                            if (board[ROW][col]==num) num_already_used =1
                        end for loop
                    end for loop

                    if (num_already_used ==0):
                        board[row][col]=num
                        sudoku_value=sudoku( )
                        if (sudoku_value==1):
                            sudoku_value=1
                            return sudoku_value
                        else: board[row][col]=0x30

                    end for loop
                end for loop
            end for loop
        end for loop
    sudoku_value=1
    return sudoku_value
}
```

Here is a more simplified version of the pseudocodes above but I decided to explain the more detailed one in the video because that will make it easier for me to explain how it is implemented as MIPS. That being said, they are still the same except that the pseudocodes above are more detailed than this version.

```

sudoku( ){
    FOR every element in board
        IF current element == "0":
            FOR all possible num:
                CHECK if current num is used in column
                CHECK if current num is used in row
                CHECK if current num is used in square
                IF current num not used:
                    current element=current num
                    CALL sudoku( ) to get sudoku_value
                    IF sudoku_value==1: return sudoku_value=1
                    ELSE: current element="0"
            ENDFOR
        return sudoku_value=0
    ENDFOR
return sudoku_value=1

```

There is also the pseudocode for the main which is just getting the input, calling the function, and printing the board. I did not elaborate in this part because MIPS has its own way of getting the inputs and printing the output.

```

main( ){
    input;           //create board in .data
    sudoku( );
    print;
}

```

Note that the board in this pseudocode stands for arrays inside an array in this format for the 4x4 solver:

```

board={{(1,0,0,0),
        (0,1,0,0),
        (0,0,1,0),
        (0,0,0,1)},}

```

But in MIPS, I stored it in the .data as:

	0	1	2	3
0	0x30	0x30	0x30	0x31
1	0x30	0x30	0x31	0x30
2	0x30	0x31	0x30	0x30
3	0x31	0x30	0x30	0x30

The address can be accessed using this formula:  $0x10010000 + (r*32) + c$

The format in the 9x9 solver is:

```
board={{(1,0,0,0,0,0,0,0,0),
        (0,1,0,0,0,0,0,0,0),
        (0,0,1,0,0,0,0,0,0),
        (0,0,0,1,0,0,0,0,0),
        (0,0,0,0,1,0,0,0,0),
        (0,0,0,0,0,1,0,0,0),
        (0,0,0,0,0,0,1,0,0),
        (0,0,0,0,0,0,0,1,0),
        (0,0,0,0,0,0,0,0,1)},}
```

But in MIPS, I stored it as:

	0	1	2	3	4	5	6	7	8
0	0x30	0x30	0x30	0x31	0x30	0x30	0x30	0x30	0x30
1	0x30	0x30	0x31	0x30	0x30	0x30	0x30	0x30	0x30
2	0x30	0x31	0x30	0x30	0x30	0x30	0x30	0x30	0x30
3	0x31	0x30	0x30	0x30	0x30	0x30	0x30	0x30	0x30
4	0x30	0x30	0x30	0x30	0x30	0x30	0x30	0x31	0x30
5	0x30	0x30	0x30	0x30	0x30	0x30	0x31	0x30	0x30
6	0x30	0x30	0x30	0x30	0x30	0x31	0x30	0x30	0x30
7	0x30	0x30	0x30	0x30	0x31	0x30	0x30	0x30	0x30
8	0x30	0x30	0x30	0x30	0x30	0x30	0x30	0x30	0x31

Again,  $0x10010000 + (r*32) + c$  is used to find the address.

### III. 4x4 Solver Explanation

```
.eqv    row $s0
.eqv    col $s1
.eqv    num $s2
.eqv    num_already_used $s3
.eqv    sudoku_value $s4
.eqv    ROW $s5
.eqv    COL $s6
```

This part is just renaming some registers to make them easier to work on during coding. Note that I only renamed s registers here because the t registers will not have a specified value on them. They will be used on all kinds of purpose, but I made sure that I changed their values each time they will be used. Notice that these renamed registers are the variables used in the pseudocode in addition to the value of the 2 functions.

```
.data
line1: .space 32
line2: .space 32
line3: .space 32
line4: .space 32
```

Here is the reserved space in the .data for the input of the sudoku board. line1 is for the 1<sup>st</sup> row, line2 is for the 2<sup>nd</sup> row, and so on.

```
.text
main:
    li $v0 8                #getting input
    la $a0, line1
    li $a1, 5
    syscall

    la $a0, line2
    syscall

    la $a0, line3
    syscall

    la $a0, line4
    syscall
```

This is where we ask for the input from the user and store it to their respective location in the .data. As said in the beginning of this documentation, this program is only able to work if the input is one at a time. If the user decides to put the input all at ones, the program will only read the first line. In other words, only line1 in the .data will have its value changed. Also, the stored values are in ASCII value. After getting the input, the board is now ready to be solved in .data.

```
jal sudoku                #calling sudoku(board)
```

This calls the function sudoku(board).

```

sudoku:                                     #sudoku( )
#                                           #preamble
subu $sp, $sp, 32
sw $ra, 28($sp)
sw row, 24($sp)
sw col, 20($sp)
sw num, 16($sp)
#

li row, 0                                  #resetting row
li num, 0x31                              #num="1" in ASCII
li sudoku_value, 0                        #resetting sudoku_value

```

We save certain values to the stack so that we can access them again later when we need them again. Then, we reset the values shown above. This is for when the function is called again.

```

for_row:
    beq row, 4, for_row_x                 #end of for_row; row=4
    li col, 0                             #resetting col

for_col:
    beq col, 4, for_col_x                 #end of for_col; col=4

    li $t0, 32
    mul $t0, $t0, row
    add $t0, $t0, col                     # $t0 = initial board[row][col]
    li $t1, 0x10010000
    add $t1, $t1, $t0                     # $t1 = final board[row][col] address
    lb $t2, 0($t1)                        # $t2 = board[row][col] value

    beq $t2, 0x30, if1                     #if board[row][col]=="0", start to solve it

    addi col, col, 1                       #col++
    j for_col

for_col_x:
    addi row, row, 1                       #row++
    j for_row

for_row_x:
    li sudoku_value, 0x1                  #last "0" has been solved; will cause a domino effect on the other recursions
    jr $ra

```

Here are the first 2 for loops in the sudoku(board). The for\_row label represents the 1<sup>st</sup> for loop or the loop that uses the row variable. In the same manner, the for\_col label is the 2<sup>nd</sup> for loop and it uses the col variable. Let us first assume that the beq instructions will not work to show how this part works. Inside the for\_row label, we set col to be 0; this is to reset c when for every time for\_row is used. It will then enter for\_col and again, assuming that the next beq instruction does not work, we proceed into finding board[row][col].

To find board[row][col], we use  $0x10010000 + (r*32) + c$ . r in this case is row and c is col. For example, if row=0 and col=0, it will be equal to 0. It will be added to 0x10010000 since this is the start of the .data. If row=0 and col=2, the address of board[0][2] would be 0x10010002.

After getting the address, we check if it is a "0". If it is, it would go to the next part. Again, let us say that it is not the case and the program will continue. There would be an increment in col and the for loop would run. We are now at the beginning of for\_col. This cycle would continue until col=4 and the 1<sup>st</sup> beq instruction in for\_col would run. Once that happens, it would branch to for\_col\_x which means that for\_col has ended.

At this point, row will be incremented and will jump to for\_row. This is the outer for loop and would continue until row=4 and the beq instruction on for\_row would run. It would branch to for\_row\_x and would return to the \$ra with sudoku\_value=1 (this would be explained more later).

Now that we have discussed these for loops, let us now explain the 2<sup>nd</sup> beq in for\_col. As said earlier, we check if board[row][col]=="0". If it is not, it means that it does not need to be solved and it already has a value. On the other hand, if it is a "0", the program must solve for its value and will branch to the label if1 which is the first if statement in the pseudocode.

```
if1:
    li num, 0x31                #resetting num

for_num:
    beq num, 0x35, for_num_x    #end of for_num; num=0x35

NUM_ALREADY_USED:
    li ROW, 0x0                #reset ROW
    li COL, 0x0                #reset COL
    li num_already_used, 0     #num_already_used=0
```

The if1 label resets the value of num to 0x31 or "1"; this is for every time for\_num would run. Let us assume again that the beq in for\_num does not work. We would enter the label NUM\_ALREADY\_USED which as its name suggests, we are checking whether num is already used on the current row, column or 2x2 square. First comes resetting ROW and COL which are variables that are going to be used here. Also, we first assume that num is still not used so we set num\_already\_used to 0.

```
for_ROW:                #checks if num is already in current column
    beq ROW, 4, for_ROW_x    #end of for_ROW; ROW=4

    li $t0, 32
    mul $t0, $t0, ROW
    add $t0, $t0, col        # $t0 = initial board[ROW][col]
    li $t1, 0x10010000
    add $t1, $t1, $t0        # $t1 = final board[ROW][col] address
    lb $t2, 0($t1)          # $t2 = board[ROW][col] value

    beq num_already_used, 1, num_already_used_true    #if num_already_used is 1; can't use this num anymore
    seq num_already_used, $t2, num

    addi ROW, ROW, 1        #ROW++
    j for_ROW

for_ROW_x:
    beq num_already_used, 1, num_already_used_true    #if num_already_used is 1; can't use this num anymore
```

We first check if num is already in the current column using for\_ROW. Since we already know how the for loops work because we already had 2 of them earlier, we can skip some parts a little. This will traverse the entire current column since we are using the original col from earlier and the new ROW which is the only thing that changes here. For each element visited, we get its value and compare it to num. But before that, we check if num\_already\_used==1. This would always be false at first try because we assumed it was 0 at start. Here comes the comparing of the element and num and if they are the same we make num\_already\_used=1. Then, it would loop and if num\_already\_used is 1, it would branch to num\_already\_used\_true since we already know that it is used. There is no need to continue it. But what if it detects that num is already in the column on the last iteration, it would no longer go through the necessary beq instruction? It is okay because it will still undergo the beq in the checking of the next area.



```

for_COL:
    beq COL, 4, for_COL_x      #checks if num is already in current row
                                #end of for_COL; COL=4

    li $t0, 32
    mul $t0, $t0, row
    add $t0, $t0, COL          #t0 = initial board[row][COL]
    li $t1, 0x10010000
    add $t1, $t1, $t0          #t1 = final board[row][COL] address
    lb $t2, 0($t1)             #t2 = board[row][COL] value

    beq num_already_used, 1, num_already_used_true #if num_already_used is 1; can't use this num anymore
    seq num_already_used, $t2, num

    addi COL, COL, 1           #COL++
    j for_COL

```

for\_COL\_x:

This is exactly the same as the previous one except that we are checking if num is already in the current row.

```

for_COL_x:
    li $t0, 0x2
    div row, $t0
    mflo $t1
    mul $t1, $t1, 2
    addi $t6, $t1, 2           #t6=floor(row/2)*2+2
    move ROW, $t1              #ROW=floor(row/2)*2

for_ROW_square:
    beq ROW, $t6, for_ROW_square_x #checks if num is already in current 2x2 square
                                    #end of outer loop; ROW=floor(row/2)*2+2

    li $t3, 0x2
    div col, $t3
    mflo $t4
    mul $t4, $t4, 2
    addi $t7, $t4, 2           #t7=floor(col/2)*2+2
    move COL, $t4              #COL=floor(col/2)*2

for_COL_square:
    li $t0, 32
    mul $t0, $t0, ROW
    add $t0, $t0, COL          #t0 = initial board[ROW][COL]
    li $t1, 0x10010000
    add $t1, $t1, $t0          #t1 = final board[ROW][COL] address
    lb $t2, 0($t1)             #t2 = board[ROW][COL] value

    beq num_already_used, 1, num_already_used_true #if num_already_used is 1; can't use this num anymore
    seq num_already_used, $t2, num

    addi COL, COL, 1           #COL++
    j for_COL_square

for_COL_square_x:
    addi ROW, ROW, 1           #ROW++
    j for_ROW_square

for_ROW_square_x:
    beq num_already_used, 1, num_already_used_true #if num_already_used is 1; can't use this num anymore

```

After checking the column and row, we are going to see if num is in the 2x2 square. To do this we use a nested loop, the process is still the same other than that. To get the appropriate 2x2 square, we get the floor of both row/2 and col/2. Then, multiply them by 2 to get their starting index. To get the boundary of the square, we just add 2 to what we have just got and we can now traverse the 2x2 square of the current element. Another difference here is that we add another of that beq instruction when the nested for loop finishes. The reason for this is that there is a chance that we will miss the opportunity of going to the appropriate label if the element becomes equal with the num at the last possible part of the square. After all, there is no longer a next part wherein we check for area unlike the previous ones.

Let us first assume that num\_already\_used=1. That means we can no longer use this num for the current "0" and we would go to num\_already\_used\_true.

```
for_num:
    beq num, 0x35, for_num_x      #end of for_num; num=0x35

num_already_used_true:
    addi num, num, 1              #num++
    j for_num

for_num_x:
    li sudoku_value, 0x0
    jr $ra                       #return 0
```

num will be incremented in the num\_already\_used\_true and it will loop into for\_num. If num=0x35 in ASCII or "5", it will end the for loop and will go to for\_num\_x. It will return to \$ra with sudoku\_value=0. This means that the previous change we made is invalid and we must go back to the state before we made that change.

Let us now assume that num\_already\_used =1. We can still use num to replace the "0" and it will go to num\_already\_used\_false.

```

num_already_used_false:
    li $t0, 32
    mul $t0, $t0, row
    add $t0, $t0, col                #$t0 = initial board[row][col]
    li $t1, 0x10010000
    add $t1, $t1, $t0                #$t1 = final board[row][col] address

    sb num, 0($t1)                   #board[row][col] = num

    jal sudoku                       #recurse sudoku(board) to solve the next "0"

    #                                #retrieve values from previous recursion
    lw $ra, 28($sp)
    lw row, 24($sp)
    lw col, 20($sp)
    lw num, 16($sp)
    addu $sp, $sp, 32
    #

    beq sudoku_value, 0x1, sudoku_true #if sudoku is true

    li $t0, 32
    mul $t0, $t0, row
    add $t0, $t0, col                #$t0 = initial board[row][col]
    li $t1, 0x10010000
    add $t1, $t1, $t0                #$t1 = final board[row][col] address

    li $t3, 0x30
    sb $t3, 0($t1)                   #board[r][c] = "0"

```

How the address of the current element has been already explained earlier. The difference this time is that we don't load from it. Instead, we are saving num into that address. This is the part when we are making changes in the board. sudoku( ) will then recurse itself repeating every process we have discussed so far. Basically, once it "solves" a "0", it will go to the next "0" to try and solve it. If it can't be solved, it means that the previous change is wrong and will try another value on it. This will continue until the last element of the board.

But how does it go back to its previous state if a wrong change was made. First, after the recursion, we retrieve the values from the previous recursion. The program checks whether sudoku\_value is 0 or 1. In the case that it is 1, it would go to sudoku\_true but let us first assume otherwise. If it is 0, we would again get the address of board[row][col] and undo the change we did. We do this by saving 0x30 into it.

```

    li $t3, 0x30
    sb $t3, 0($t1)                   #board[r][c] = "0"

num_already_used_true:
    addi num, num, 1                  #num++
    j for_num

sudoku_true:
    li sudoku_value, 0x1
    jr $ra                           #return 1

for_num_x:
    li sudoku_value, 0x0
    jr $ra                           #return 0

```

Note that after undoing the change, it will increment num and will go through the for loop again to continue the cycle.

This time, assume that sudoku\_value is 1. Then, the beq instruction in num\_already\_used\_false would work and will branch into sudoku\_true. This would return sudoku\_value=1 to the previous recursion of sudoku(board).

It means that once the sudoku\_value becomes 1, it will be a domino effect to all the previous recursions. All their sudoku\_value will also be 1 and will return to the original sudoku( ) call in the main label. But when does the sudoku\_value becomes 1?

```
for_row_x:
    li sudoku_value, 0x1          #last "0" has been solved; will cause a domino effect on the other recursions
    jr $ra
```

This is where the sudoku\_value becomes 1 first. Once every element in the board is already checked and there are no "0" detected in it anymore. With this explanation, the Shortest Summary at the start should make sense. These explanations should make more sense in the video.

#### IV. 9x9 Solver Explanation

The process of the 9x9 solver is almost the same as the 4x4 solver. The only difference is some values used, the input, and the output.

```
.data
line1: .space 32
line2: .space 32
line3: .space 32
line4: .space 32
line5: .space 32
line6: .space 32
line7: .space 32
line8: .space 32
line9: .space 32
```

Unlike in 4x4 solver, there are 9 lines reserved in the .data in 9x9 solver.

.text

```
main:
```

```
li $v0 8                                #getting input
la $a0, line1
li $a1, 10
syscall

la $a0, line2
syscall

la $a0, line3
syscall

la $a0, line4
syscall

la $a0, line5
syscall

la $a0, line6
syscall

la $a0, line7
syscall

la $a0, line8
syscall

la $a0, line9
syscall
```

Of course, the program asks for the input 9 times.

```
for_row:
    beq row, 9, for_row_x      #end of for_row; row=9
    li col, 0                  #resetting col

for_col:
    beq col, 9, for_col_x      #end of for_col; col=9

for_num:
    beq num, 0x3A, for_num_x    #end of for_num; num=0x3A

for_ROW:
    #checks if num is already in current column
    beq ROW, 9, for_ROW_x      #end of for_ROW; ROW=9
```

```

for_COL:
    beq COL, 9, for_COL_x      #checks if num is already in current row
                                #end of for_COL; COL=9
for_COL_x:
    li $t0, 0x3
    div row, $t0
    mflo $t1
    mul $t1, $t1, 3
    addi $t6, $t1, 3           #$t6=floor(row/3)*3+3
    move ROW, $t1              #ROW=floor(row/3)*3

for_ROW_square:
    beq ROW, $t6, for_ROW_square_x  #checks if num is already in current 3x3 square
                                        #end of outer loop; ROW=floor(row/3)*3+3

    li $t3, 0x3
    div col, $t3
    mflo $t4
    mul $t4, $t4, 3
    addi $t7, $t4, 3           #$t7=floor(col/3)*3+3
    move COL, $t4              #COL=floor(col/3)*3

```

Several values used in for loops are also changed in order to traverse each element in the 9x9 board. The nested loop in the ok function now checks 3x3 square area instead of 2x2 square. The other conditions were change mostly from row=4 to row=9, col=4 to col=9, ROW=4 to ROW=9, COL=4 to COL=9, num=0x31 to num=0x3A.

li \$a0, 10	#printing board	li \$a0, 10	li \$a0, 10
li \$v0, 11		li \$v0, 11	li \$v0, 11
syscall		syscall	syscall
li \$v0, 4		li \$v0, 4	li \$v0, 4
la \$a0, line1		la \$a0, line4	la \$a0, line7
syscall		syscall	syscall
li \$a0, 10		li \$a0, 10	li \$a0, 10
li \$v0, 11		li \$v0, 11	li \$v0, 11
syscall		syscall	syscall
li \$v0, 4		li \$v0, 4	li \$v0, 4
la \$a0, line2		la \$a0, line5	la \$a0, line8
syscall		syscall	syscall
li \$a0, 10		li \$a0, 10	li \$a0, 10
li \$v0, 11		li \$v0, 11	li \$v0, 11
syscall		syscall	syscall
li \$v0, 4		li \$v0, 4	li \$v0, 4
la \$a0, line3		la \$a0, line6	la \$a0, line9
syscall		syscall	syscall

There are also 9 printing process now. These are all the changes made in the 9x9 solver. All the other parts stay the same and work the same as before.

## V. Test Cases

I will give 5 test cases for each of the solvers.

Here are the test cases and the results for the 4x4 solver from an online sudoku generator (<https://www.sudokuweb.org/>):

Input 1:

3042  
0410  
4200  
0004

Output 1:

3142  
2413  
4231  
1324

Input 2:

0002  
0213  
0401  
1300

Output 2:

3142  
4213  
2431  
1324

Input 3:

3100  
0430  
1320  
4000

Output 3:

3142  
2431  
1324  
4213

Input 4:

0003  
1004  
4132  
0240

Output 4:

2413  
1324  
4132  
3241

Input 5:

0000  
4030  
0102  
0000

Output 5:

1324  
4231  
3142  
2413

Here are the test cases and the results for the 9x9 solver created in an online 9x9 sudoku generator (<https://www.sudoku9x9.com/>):

Input 1: (the program runs slow in this input, but it works)

000001070  
060080001  
100900300  
031500006  
000000040  
400800007  
080060000  
049000210  
500034000

Output 1:

893621475  
765483921  
124975368  
231547896  
978316542  
456892137  
382169754  
649758213  
517234689



Input 2:

007060001  
236000080  
908500006  
092100063  
001005890  
700000052  
600010048  
100806200  
070409015

Output 2:

457968321  
236741589  
918532476  
592184763  
361275894  
784693152  
625317948  
149856237  
873429615

Input 3:

000001000  
004327000  
005000800  
100006900  
900002050  
703000002  
070000043  
060000000  
300190700

Output 3:

637581429  
894327516  
215649837  
152836974  
986472351  
743915682  
579268143  
461753298  
328194765

Input 4: (the program runs slow in this input, but it works)

030000000  
040000090  
092005006  
070200050  
000300008  
005009042  
006030000  
001070000  
000801409

Output 4:

538697214  
647123895  
192485736  
379248651  
214356978  
865719342  
926534187  
481972563  
753861429

Input 5:

400000030  
060090000  
020407005  
200073040  
038560100  
000000007  
000000080  
005300000  
000120009

Output 5:

417652938  
563891274  
829437615  
251973846  
738564192  
946218357  
192746583  
675389421  
384125769