

$$= -\frac{1}{2}$$

$$(9) \lim_{n \rightarrow \infty} \sum_{k=n}^{\infty} \frac{1}{k^2} = \lim_{n \rightarrow \infty} \frac{1}{n^2} + \lim_{n \rightarrow \infty} \frac{1}{(n+1)^2} + \dots + \lim_{n \rightarrow \infty} \frac{1}{(2n)^2} = 0$$

不能拆成无限项极限

$$b. \lim_{n \rightarrow \infty} (x_n - y_n) = \lim_{n \rightarrow \infty} x_n - \lim_{n \rightarrow \infty} y_n = 0$$

$$\therefore \lim_{n \rightarrow \infty} x_n = \lim_{n \rightarrow \infty} y_n \quad \text{需先证明极限存在.}$$

$$\therefore \lim_{n \rightarrow \infty} (x_n - y_n) = 0 \quad \therefore |x_n - y_n| < \varepsilon$$

$$\therefore y_n - x_n < \varepsilon$$

$$\therefore x_n \leq \delta$$

$$\therefore y_n - \delta < y_n - x_n < \varepsilon$$

$$\therefore \forall \varepsilon, \exists N \in \mathbb{N}, \text{ s.t. } n > N \text{ 有 } |y_n - \delta| < \varepsilon. \text{ 即 } \lim_{n \rightarrow \infty} y_n = \delta$$

$$\therefore \lim_{n \rightarrow \infty} x_n = \lim_{n \rightarrow \infty} y_n = \delta$$