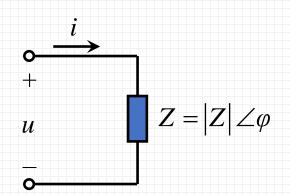


# 0.1



#### 电路如图所示,已知电压和电流为

$$u(t) = 10 \sin(400\pi t + 60^{\circ}) V$$
$$i(t) = -\frac{1}{\sqrt{2}} \cos(400\pi t - 150^{\circ}) A$$

- (a)  $\omega = \frac{400\pi \text{ rad/s}}{400\pi \text{ rad/s}}$ ,  $f = \frac{200\text{Hz}}{4000\text{Hz}}$ ,  $f = \frac{0.005\text{s}}{40000\text{s}}$ .
- (b) 有效值 *U*=<u>7.07V</u>, 有效值 *I*=<u>0.5A</u>.
- (c) u 和 i 的相位差  $\psi_u \psi_i = \underline{-60^\circ}$ .

### 比较相位时,要将时域表达式转换成标准正弦形式

$$i(t) = \frac{1}{\sqrt{2}}\cos(400\pi t - 150^{\circ} + 180^{\circ}) = \frac{1}{\sqrt{2}}\cos(400\pi t + 30^{\circ})$$
$$= \frac{1}{\sqrt{2}}\sin(400\pi t + 30^{\circ} + 90^{\circ}) = \frac{1}{\sqrt{2}}\sin(400\pi t + 120^{\circ})A$$
$$\varphi = \psi_{u} - \psi_{i} = 60^{\circ} - 120^{\circ} = -60^{\circ}$$

#### 0.2 下列哪些表达式是正确的, 哪些是错误的, 并改正。

$$(1) \quad \dot{I} = \frac{\dot{U}}{R + j\omega L}$$

(1) 
$$\dot{I} = \frac{\dot{U}}{R + j\omega L}$$
 (2)  $I = \frac{U}{\sqrt{R^2 + (\omega L)^2}}$ 

$$\mathbf{L} + \mathbf{V}(3) \ u = u_R + u_L$$

(4) 
$$U = U_L^2 + U_R^2$$

$$\dot{U} = \dot{U}_R + \dot{U}_L$$

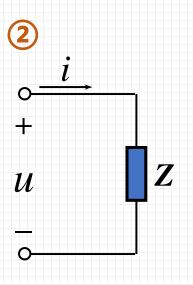
$$\dot{U} = \dot{U}_R + \dot{U}_L$$

$$\checkmark (6) P = I^2 R$$

$$(5) P = \frac{U_R^2}{R}$$

$$\checkmark$$
 (6)  $P = I^2 R$ 

$$(7) |Z| = \sqrt{R^2 + (\omega L)^2}$$



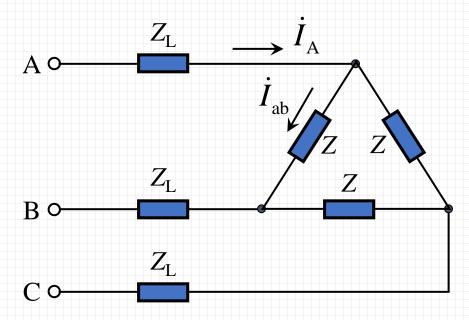
如果 
$$u(t) = 311\sin(\omega t + 45^{\circ})V$$
,  $Z = 25\angle 60^{\circ} \Omega$ 

那么 
$$i \times \frac{u}{Z} \times \frac{311\sin(\omega t + 45^\circ)}{25\angle 60^\circ} \times 12.44\sin(\omega t + 45^\circ - 60^\circ)A$$

$$\dot{I} = \frac{\dot{U}}{Z} = \frac{\frac{311}{\sqrt{2}} \angle 45^{\circ}}{25 \angle 60^{\circ}} = 8.8 \angle -15^{\circ} \text{ A}$$

$$i = 8.8\sqrt{2}\sin(\omega t - 15^{\circ}) \text{ A}$$

0.3 平衡三相电路中, $\dot{U}_{AB}$  是线电压, $\dot{U}_{AN}$  是相电压.



$$(1) \dot{I}_{ab} \times \frac{\dot{U}_{AB}}{Z}$$

$$(2) \dot{I}_{ab} \times \frac{U_{AB}}{2Z_{L} + Z}$$

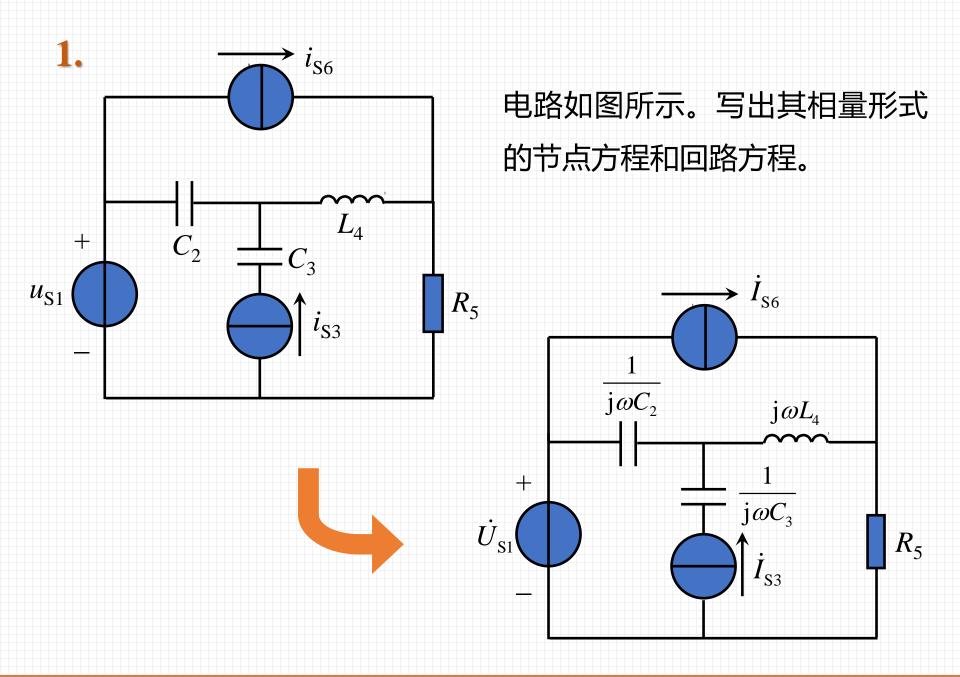
(3) 
$$\dot{I}_{ab} \times \frac{\dot{U}_{AN}}{Z_L + Z/3}$$
 (4)  $\dot{I}_A \times \frac{\dot{U}_{AB}}{2Z_L + Z}$ 

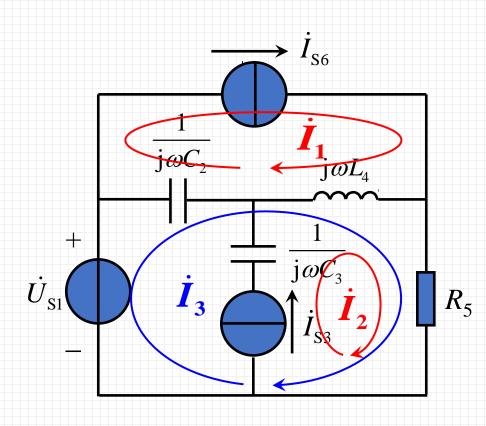
$$(4) \dot{I}_{A} \times \frac{U_{AB}}{2Z_{L} + Z}$$

$$(5) \dot{I}_{A} \times \frac{U_{AB}}{Z_{L} + Z}$$

(5) 
$$\dot{I}_{A} \times \frac{\dot{U}_{AB}}{Z_{L} + Z}$$
 (6)  $\dot{I}_{A} = \frac{\dot{U}_{AN}}{Z_{L} + Z/3}$ 







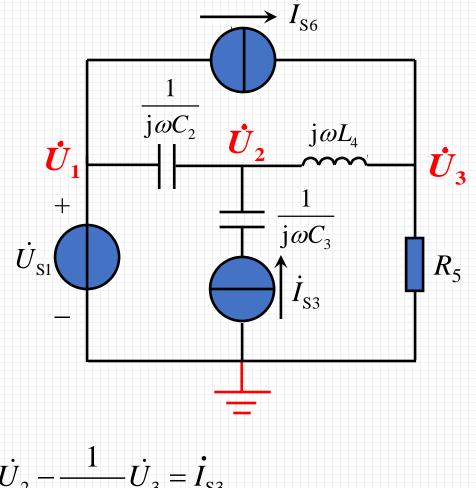
## 回路法:

$$\dot{I}_1 = \dot{I}_{S6} \qquad \boxed{1}$$

$$\dot{I}_2 = \dot{I}_{S3}$$

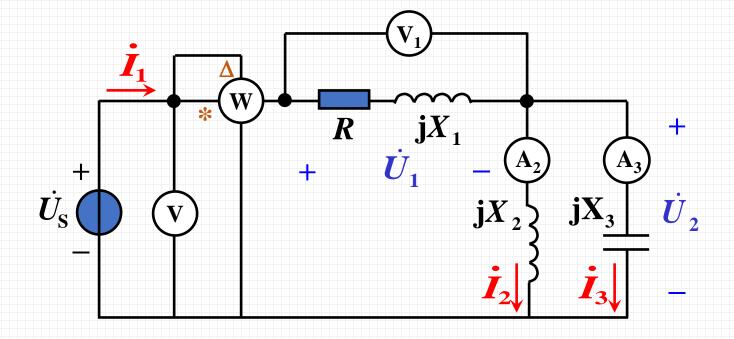
$$(\frac{1}{j\omega C_2} + j\omega L_4 + R_5)\dot{I}_3 - (\frac{1}{j\omega C_2} + j\omega L_4)\dot{I}_1 + (j\omega L_4 + R_5)\dot{I}_2 = \dot{U}_{S1}$$

## 节点法:



$$\begin{cases} \dot{U}_{1} = \dot{U}_{S1} \\ -j\omega C_{2}\dot{U}_{1} + (j\omega C_{2} + \frac{1}{j\omega L_{4}})\dot{U}_{2} - \frac{1}{j\omega L_{4}}\dot{U}_{3} = \dot{I}_{S3} \\ -\frac{1}{j\omega L_{4}}\dot{U}_{2} + (\frac{1}{j\omega L_{4}} + \frac{1}{R_{5}})\dot{U}_{3} = \dot{I}_{S6} \end{cases}$$

2.



电路如图所示。电压表 V 的读数是 220 V,  $V_1$  的读数是  $100\sqrt{2}$  V,  $A_2$  的读数是 30 A,  $A_3$  的读数是 20 A, 功率表的读数是 1000 W (有功功率)。 求参数 R、 $X_1$ 、 $X_2$  和  $X_3$ 。

设: 
$$\dot{U}_2 = U_2 \angle 0^\circ \text{ V}$$
  
那么:  $\dot{I}_2 = -j30\text{A}$ 

$$\dot{I}_3 = j20\text{A}$$

$$\dot{I}_1 = \dot{I}_2 + \dot{I}_3 = -j10\text{A}$$

$$P = I_1^2 R$$

$$R = P / I_1^2 = 1000 / 10^2 = 10\Omega$$

设: 
$$Z_1 = R + jX_1 = |Z_1| \angle \varphi_1$$
 则  $|Z_1| = \frac{U_1}{I_1} = \frac{100\sqrt{2}}{10} = 10\sqrt{2} \Omega$ 

$$X_1 = \sqrt{|Z_1|^2 - R^2} = \sqrt{(10\sqrt{2})^2 - 10^2} = 10\Omega$$
  $\varphi_1 = \operatorname{arctg} \frac{X_1}{R} = 45^\circ$ 

$$\therefore \dot{I}_1 = -j10 = 10\angle -90^\circ \text{A} \quad \therefore \dot{U}_1 = 100\sqrt{2}\angle -45^\circ \text{V}$$

$$\dot{U}_S = \dot{U}_1 + \dot{U}_2 = 100 - j100 + U_2 = 100 + U_2 - j100$$

$$U_S^2 = (100 + U_2)^2 + 100^2, \quad U_2 = \sqrt{220^2 - 100^2} - 100 = 96\text{V}$$

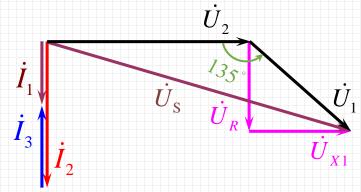
$$X_2 = U_2 / I_2 = 96 / 30 = 3.2 \Omega, \quad X_3 = -U_2 / I_3 = -96 / 20 = -4.8 \Omega$$

### U2 也可以用相量图求出.

$$\dot{U}_{S} = \dot{U}_{1} + \dot{U}_{2}$$

$$\dot{U}_{1} = \dot{U}_{R} + \dot{U}_{X1}$$

$$\dot{I}_{1} = \dot{I}_{2} + \dot{I}_{3}$$



$$U_{\rm S}^2 = U_2^2 + U_1^2 - 2U_1U_2\cos 135^\circ$$

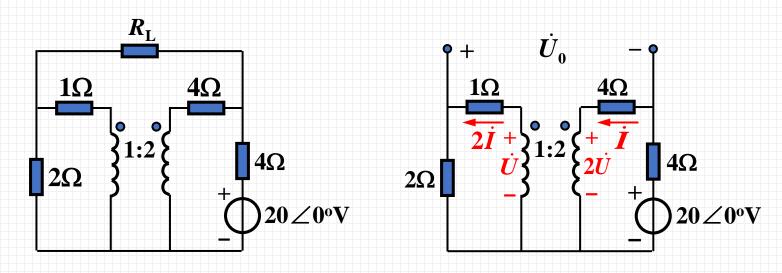
$$U_2^2 - 2 \times 100\sqrt{2} \times (-\frac{\sqrt{2}}{2})U_2 + (100\sqrt{2})^2 - 220^2 = 0$$

$$U_2^2 + 200U_2 - 28400 = 0, U_2 = 96V$$

$$U_2 = 96V$$

(忽略负值)

3. R<sub>L</sub>取值为多大时获得最大功率? 最大功率是多少?



解法: 戴维南定理+理想变压器

求开路电压

左: 
$$\dot{U} = 3 \times 2\dot{I}$$

右: 
$$20\angle 0^{\circ} = 8\dot{I} + 2\dot{U}$$

$$\dot{U} = 6\angle 0^{\circ}$$

$$\dot{I} = 1\angle 0^{\circ}$$

$$\dot{U} = 6\angle 0^{\circ}$$

$$\dot{I} = 1\angle 0^{\circ}$$

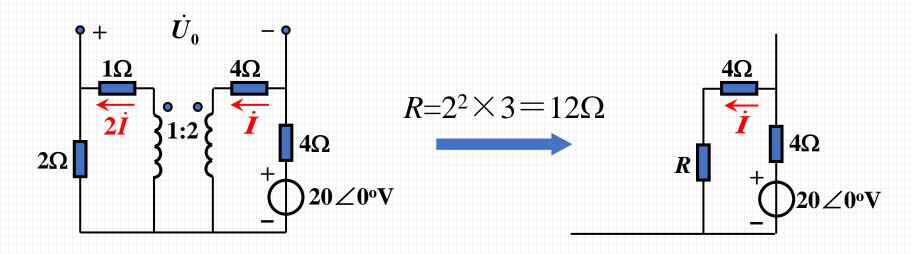
$$\dot{U} = 6\angle 0^{\circ}$$

$$\dot{I} = 12\angle 180^{\circ}$$

$$\dot{U}_{0} = 2\times 2\dot{I} - 20\angle 0^{\circ} + 4\dot{I} = 12\angle 180^{\circ}$$
V

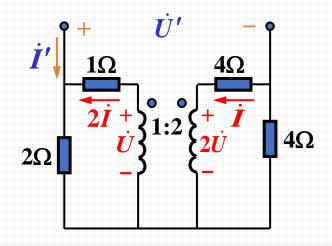
#### 求开路电压

#### 法二:



$$\dot{I} = 20 \angle 0^{\circ} / (R + 4 + 4) = 1 \angle 0^{\circ} A$$
 $\dot{U}_{0} = 2 \times 2\dot{I} - 20 \angle 0^{\circ} + 4\dot{I} = 12 \angle 180^{\circ} V$ 
并不简便

#### 加压求流求内阻

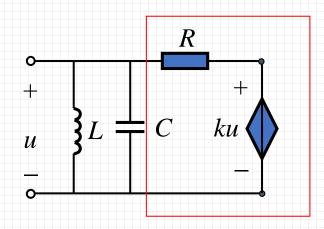


$$\begin{cases} \dot{U} = 2\dot{I} + 2(2\dot{I} + \dot{I}') \\ 4\dot{I} + 2\dot{U} + 4(\dot{I} + \dot{I}') = 0 \\ \dot{U}' = 2(2\dot{I} + \dot{I}') + 4(\dot{I} + \dot{I}') \end{cases} \longrightarrow \dot{U}' = 2.8\dot{I}'$$

则  $R_L = 2.8\Omega$  时获得最大功率.

最大功率  $P = 12^2/(4 \times 2.8) = 12.9W$ 

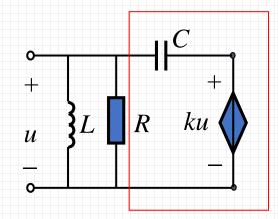
## 4. 求图示电路的谐振频率以及在谐振时的入端阻抗(0<k<1)



$$R_{\mbox{$\frac{1}{3}$}} = \frac{u}{(1-k)u/R} = \frac{R}{1-k}$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

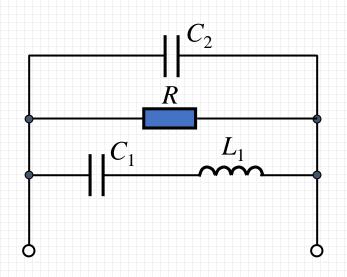
$$Z(\omega_0) = \frac{R}{1-k}$$

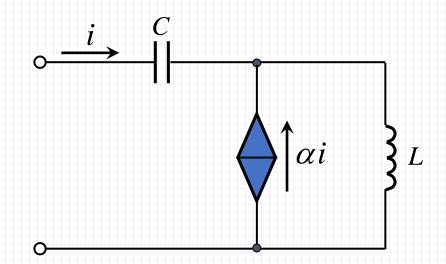


$$Z_{\stackrel{\text{ge}}{=}} = \frac{\dot{U}}{(1-k)\dot{U}j\omega C} = \frac{1}{(1-k)j\omega C}$$

$$\omega_0 = \frac{1}{\sqrt{LC(1-k)}}$$

$$Z(\omega_0) = R$$





$$\omega_{01} = \frac{1}{\sqrt{L_1 C_1}}$$

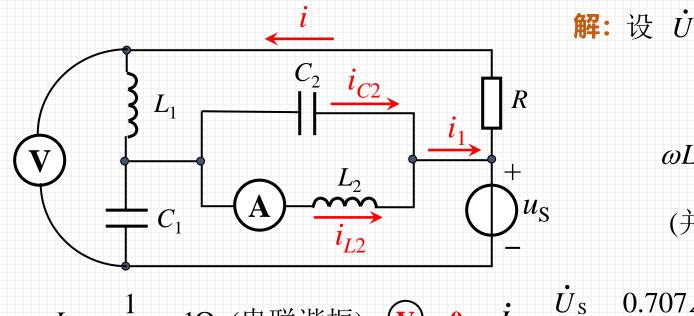
$$\omega_{02} = \frac{1}{\sqrt{L_1 \frac{C_1 C_2}{C_1 + C_2}}}$$

$$\dot{U} = -j\frac{1}{\omega C}\dot{I} + j\omega L\dot{I}(1+\alpha)$$

$$Z = \frac{\dot{U}}{\dot{I}} = -j\frac{1}{\omega C} + j(1+\alpha)\omega L$$

$$\omega_0 = \frac{1}{\sqrt{(1+\alpha)LC}}$$

5. 电路如图所示.  $u_S(t) = \sin t \, V$ ,  $L_1 = L_2 = 1 \, H$ ,  $C_1 = C_2 = 1 \, F$ ,  $R = 1 \, \Omega$ . 求电压表和电流表的读数 (rms).



解:设 
$$\dot{U}_{\rm S} = \frac{1}{\sqrt{2}} \angle 0^{\circ} \text{V}$$

$$= 0.707 \angle 0^{\circ} \text{V}$$

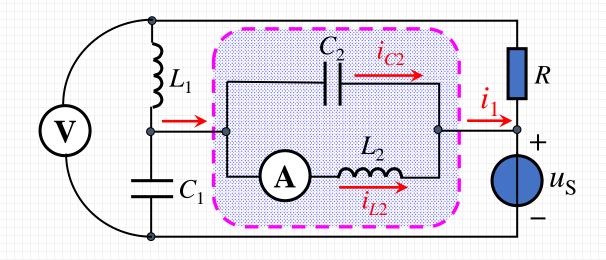
$$\omega L_2 = \frac{1}{\omega C_2} = 1\Omega$$
(并联谐振)  $\dot{I}_1 = 0$ 

$$\omega L_1 = \frac{1}{\omega C_1} = 1\Omega$$
 (串联谐振),  $\mathbf{V} = \mathbf{0}$   $\dot{I} = \frac{\dot{U}_S}{R} = \frac{0.707 \angle 0^{\circ}}{1} = 0.707 \angle 0^{\circ} A$ 

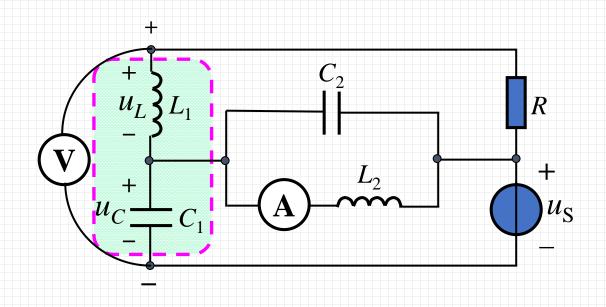
$$\dot{I}_{L2} = \frac{\frac{1}{j\omega C_1}\dot{I} - \dot{U}_S}{j\omega L_2} = \frac{-j0.707 - 0.707}{j1} = -0.707 + j0.707 = 1.00 \angle 135^{\circ} A$$

$$(A) = 1A$$

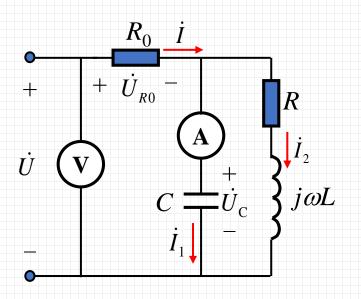
将发生并联谐振的电路看成一个二端网络(或一条广义的支路),则流进或流出端口的电流(或通过该广义支路的电流)为零,但网络内部的各个支路的电流并不一定为零。



将发生串联谐振的电路看成一个二端网络(或一条广义的支路),则两个端钮之间的电压(或广义支路两端的电压)为零,但网络内部的各个支路上的电压并不一定为零。



**6.** ω = 1000 rad/s时,电路发生谐振。  $R_0 = 25\Omega$ ,  $C = 16\mu\text{F}$ , 电压表的读数是 100 V, 电流表的读数是 1.2 A, 求 R 和 L.



$$I_1 = 1.2A$$

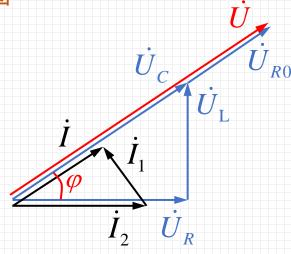
$$U_{\rm C} = \frac{1.2}{(1000 \times 1.6 \times 10^{-6})} = 75 \text{V}$$

#### 谐振时:

$$U_{R0} = 25V \qquad I = 1A$$

$$I_2 = \sqrt{I_1^2 + I^2} = 1.562$$
A

#### 解: 相量图



$$\phi = \arctan(I_1 / I) = 50.2^{\circ}$$

$$|Z| = \frac{U_C}{I_2} = \frac{75}{1.562} = 48.01\Omega$$

$$R = 48.01\cos 50.2^{\circ} = 30.7\Omega$$

$$L = 48.01 \sin 50.2^{\circ} / 1000 = 36.9 \text{mH}$$

#### 解二

设  $\dot{U} = 100 \angle 0^{\circ} \text{V}$ 

分析可知u、i、u2同相,则i1领先u290度

$$\dot{I}_1 = j1.2A$$

$$\dot{U}_2 = \dot{I}_1 * \frac{1}{j\omega C} = 75 \angle 0^{\circ} V$$

$$\dot{I} = \frac{\dot{U} - \dot{U}_2}{R_0} = 1A$$

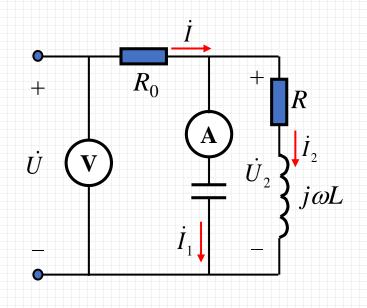
$$\dot{I}_2 = \dot{I} - \dot{I}_1 = 1 - j1.2 = 1.562 \angle 50.2^{\circ} \text{ A}$$

由于谐振, 无功在电感与电容间交换, 则

$$Q_{L} = I_{2}^{2}\omega L \qquad Q_{C} = -I_{1}^{2} \frac{1}{\omega C}$$

$$I_{1}^{2} \frac{1}{\omega C} = I_{2}^{2}\omega L$$

$$\Rightarrow L = \frac{I_{1}^{2}}{\omega^{2}CI_{2}^{2}} = 0.0369H$$



$$\Rightarrow L = \frac{I_1^2}{\omega^2 C I_2^2} = 0.0369 \text{H} \qquad R = \sqrt{\left(\frac{U_2}{I_2}\right)^2 - (\omega L)^2} = \sqrt{\left(\frac{75}{1.562}\right)^2 - (39.6)^2} = 30.7\Omega$$

#### 解三

设  $\dot{U} = 100 \angle 0$ °V

则因为电容电流  $I_c$ 相量领先电压相量  $U_c$  90°, 有:

$$\dot{I}_C = j1.2A$$
  $jX_C = \frac{1}{j\omega C} = \frac{1}{j\times 1000\times 16\times 10^{-6}} = -j62.5\Omega$ 

$$\dot{U}_C = \dot{I}_C j X_C = 75 \text{V}$$
  $\dot{U}_{R0} = \dot{U} - \dot{U}_C = 100 - 75 = 25 \text{V}$ 

$$\dot{I} = \frac{\dot{U}_{R0}}{R_0} = \frac{25\angle 0^{\circ}}{25} = 1\angle 0^{\circ} \text{ A}$$

所以R, L, C 并联支路等效为一个  $\frac{U_c}{\dot{I}} = 75\Omega$  的电阻。即:

$$\frac{\frac{1}{j\omega C} \times (R + j\omega L)}{\frac{1}{j\omega C} + (R + j\omega L)} = 75\Omega$$

设 
$$R + j\omega L = Z$$

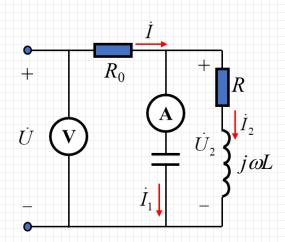
则有: 
$$\frac{-\mathrm{j}62.5 \times Z}{-\mathrm{j}62.5 + Z} = 75$$

$$Z = 30.7 + j36.9\Omega$$

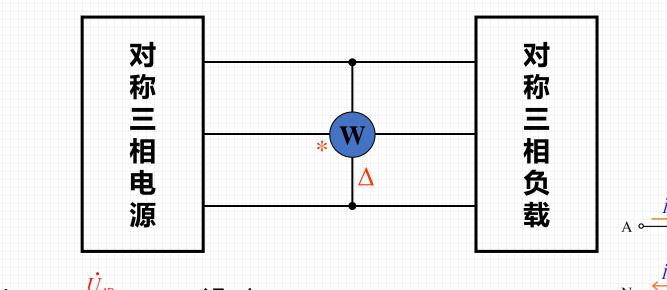
$$R = 30.7\Omega$$

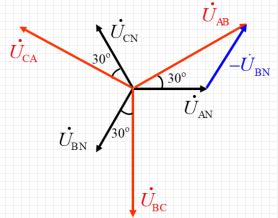
$$\omega L = 36.9\Omega$$

$$L = 36.9 \text{mH}$$



## 7. W的读数有何物理意义

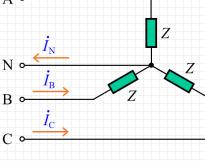




设 
$$\dot{U}_{AN} = U_{P} \angle 0^{\circ}$$

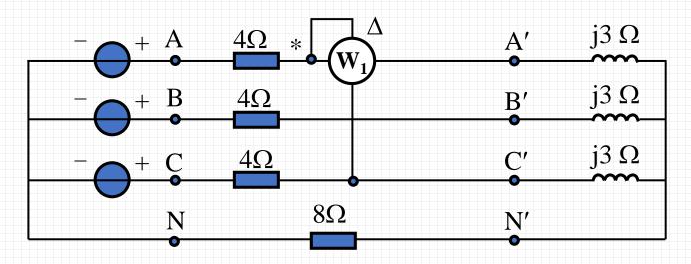
$$\begin{aligned} \boxed{\mathbf{W}} &= U_{\mathrm{CA}} I_{B} \cos \left( \phi_{u_{\mathrm{CA}}} - \phi_{i_{\mathrm{B}}} \right) \\ &= \sqrt{3} U_{\mathrm{P}} I_{\mathrm{P}} \cos \left( \left( 150^{\circ} \right) - \left( -120^{\circ} - \phi_{\mathrm{P}} \right) \right) \\ &= \sqrt{3} U_{\mathrm{P}} I_{\mathrm{P}} \cos \left( 270^{\circ} + \phi_{\mathrm{P}} \right) \\ &= \sqrt{3} U_{\mathrm{P}} I_{\mathrm{P}} \sin \phi_{\mathrm{P}} \end{aligned}$$

测量对称三相负载吸收的无功功率

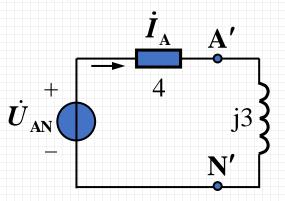


 $\times \sqrt{3}$ 

平衡三相电路的相电压是 220V。求: (1)线电流和通过中线的的电流; (2) 求功率表的读数; (3)电源发出的有功功率和无功功率; (4)能用两表法测量负载吸收的功率吗? 如果能, 画出另一块表, 求读数。



#### 解: (1) 抽单相:



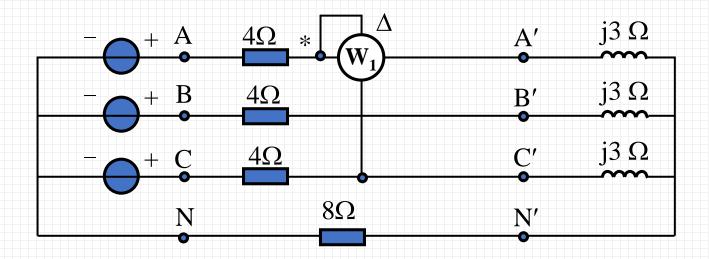
$$\dot{U}_{AN} = 220 \angle 0^{\circ} \text{ V}$$

$$\dot{I}_{A} = \frac{220 \angle 0^{\circ}}{4 + i3} = 44 \angle -36.9^{\circ} A$$

$$I_1 = 44A$$
  $I_N = 0$ 

### (2) 求功率表的读数

$$\dot{I}_{A} = 44 \angle -36.9^{\circ} A$$



$$\dot{U}_{A'N} = j3\dot{I}_A = 132\angle 53.1^{\circ} \text{V}$$

$$\dot{U}_{A'B'} = \sqrt{3} \ 132 \angle (30^{\circ} + 53.1^{\circ}) = \sqrt{3} \ 132 \angle 83.1^{\circ} V$$

$$\dot{U}_{A'C'} = -\dot{U}_{C'A'} = -\sqrt{3} \, 132 \angle (120^{\circ} + 83.1^{\circ}) = \sqrt{3} \, 132 \angle 23.1^{\circ} \, V$$



$$U_{A'C'}I_{A}\cos[23.1^{\circ} - (-36.9^{\circ})]$$
  
=  $\sqrt{3}132 \times 44\cos 60^{\circ} = 5029W$ 

$$\dot{U}_{AN} = 220 \angle 0^{\circ} V$$

$$\dot{I}_{A} = 44 \angle -36.9^{\circ} A$$

$$P = 3U_p I_p \cos \phi_p = 3 \times 220 \times 44 \cos 36.9^\circ = 23.2 \text{kW}$$

OR 
$$P = \sqrt{3}U_l I_l \cos \phi_p = \sqrt{3} \times \sqrt{3} \times 220 \times 44 \cos 36.9^\circ = 23.2 \text{kW}$$

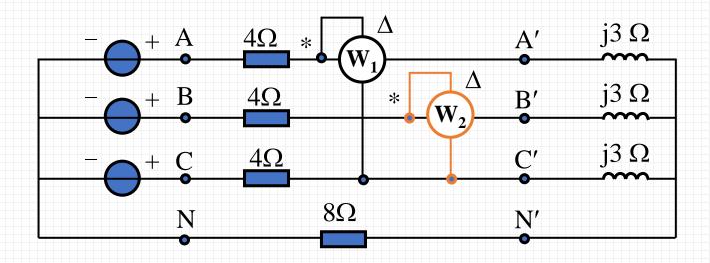
$$Q = 3U_p I_p \sin \phi_p = 3 \times 220 \times 44 \sin 36.9^\circ = 17.4 \text{kvar}$$

#### 另一种求法:

$$P = 3I_1^2 R = 3 \times 44^2 \times 4 = 23.2$$
kW

$$Q = 3I_l^2 X = 3 \times 44^2 \times 3 = 17.4$$
kvar

#### (4) 可以用两表法测负载功率



$$\dot{U}_{A'B'} = \sqrt{3} \ 132 \angle 83.1^{\circ} \text{V}$$

$$\dot{I}_{A} = 44 \angle -36.9^{\circ} \text{ A}$$

$$\dot{U}_{B'C'} = \sqrt{3} \ 132 \angle -36.9^{\circ} \text{ V}$$

$$\dot{I}_{\rm B} = 44 \angle -156.9^{\circ} \, {\rm A}$$

$$(\mathbf{W}_2)$$

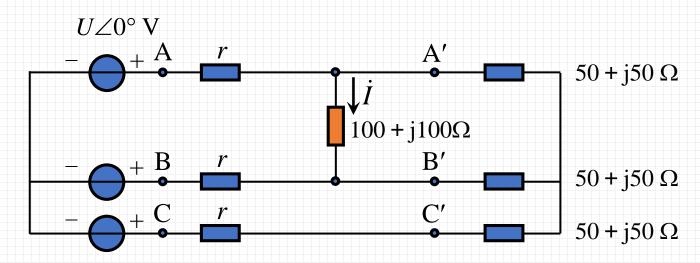
$$U_{\rm B'C'}I_{\rm B}\cos[(-36.9^{\circ})-(-156.9^{\circ})]$$

$$U_{\text{B'C'}}I_{\text{B}}\cos[(-36.9^{\circ}) - (-156.9^{\circ})]$$
  
=  $\sqrt{3}132 \times 44\cos 120^{\circ} = -5029\text{W}$ 

$$(\mathbf{W_1})$$

=5029W

9. 电源三相对称, r分别为0和10Ω时求 $\dot{I}$ 。



解: 
$$(1) r = 0$$

$$\dot{I} = \frac{\dot{U}_{AB}}{100 + j100} = 0.0122U \angle -15^{\circ}$$

(2) 
$$r = 10 \Omega$$

戴维南等效

开路电压: 抽单相  $\dot{U}_{\rm oc} = 1.56U \angle 35.2^{\circ}$ 

等效内阻抗: 交流电桥平衡  $Z_{eq} = 18.03 + j1.64\Omega$ 

$$\dot{I} = \frac{\dot{U}_{OC}}{Z_{eq} + 100 + j100} = 0.01U \angle -5.53^{\circ}$$

## 关于期末考试

#### • 考试范围

- 以期中以后内容为主(动态时域+正弦稳态)
- 节点、回路、叠加、戴维南、替代、二端口 (**考**)
- 非线性电阻、MOSFET、运放、特勒根定理、互易定理(不考)
- 一 冲激卷积、周期非正弦(不考)
- 考试时间: 6月24日 19:00 ~ 21:00
- 考试地点: 六教6A201、6A203
- 考试形式: 半开卷 (下发的盖 "电路" 章的A4纸随便写 (不得打印不得粘贴) + 计算器)
- · 答疑时间地点: 6月24日上午8: 30~11: 30, 西主楼1-316 (可网上)