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# Command Reference: ARMA()

## Lag and attenuate a time series using AutoRegressive Moving Average

Version 11.09.00, 2016-02-29

The ARMA ( ) command predicts output from an input time series (e.g., to route a streamflow time series downstream). By default this command will replace the original time series values (specify the NewTSID parameter to create a new output time series). The ARMA method preserves the “mass” of the data. The general equation for ARMA is:

$$O_t = a_1 * O_{t-1} + a_2 * O_{t-2} + \dots + a_p * O_{t-p} + b_0 * I_t + b_1 * I_{t-1} + \dots + b_q * I_{t-q}$$

Where:

$t$  = time step

$O_t$  = output value at time  $t$

$I_t$  = input value at time  $t$

$a$ ,  $b$  = ARMA coefficients

and the  $p$  and  $q$  values indicate the degree of the equation: ARMA( $p,q$ ).

The ARMA coefficients are determined by analyzing historical data and may be developed using a data interval that is different than the data interval of the time series that is being manipulated. The coefficients are typically computed by an external analysis program (TSTool does not perform this function).

The time series to process can have any interval. The  $a$  and  $b$  coefficients are listed in the dialog from left-most to right-most in the equation. Note that there are  $p$   $a$ -coefficients and  $(q + 1)$   $b$ -coefficients (because there is a  $b$ -coefficient at time  $t_0$ ). The interval used to compute the ARMA coefficients can be different from the data interval but the data and ARMA intervals must be divisible by a common interval. The ARMA algorithm is executed as follows:

1. The data and ARMA intervals are checked and if they not the same, the data are expanded by duplicating each value into a temporary array. For example, if the data interval is 6Hour and the ARMA interval is 2Hour, each data value is expanded to three data values (2Hour values). If the data interval is 6Hour and the ARMA interval is 10Hour, each data value is expanded to three data values (2Hour values).
2. The ARMA equation is applied at each point in the expanded data array. However, because the ARMA coefficients were developed using a specific interval, only the data values at the ARMA interval are used in the equation. For example, if the expanded data array has 2Hour data and the ARMA interval is 10Hour, then every fifth value will be used (e.g.,  $t$  corresponds to the “current” value and  $t - 1$  corresponds to the fifth value before the current value). Because the ARMA algorithm depends on a number of previous terms in both the input and output, there may be missing terms at the beginning of the data array and in cases where missing data periods are encountered. Ideally ARMA will be applied to filled data and only the initial conditions will be an issue. In this case the output period should ideally be less than the total period so that the initial part of the routed time series can be ignored. In cases where  $O$  values are missing, the algorithm first tries to use the  $I$  values. If any values needed for the result are missing, the result is set to missing. Use the InputInitialValues parameter to supply additional time series values at the start of the time series to overcome this issue.

- The final results are converted to a data interval that matches the original input, if necessary. If the original data interval and the ARMA interval are the same, no conversion is necessary. For example, if the original data interval is 6Hour and the ARMA interval is 10Hour, then the expanded data interval will be 2Hour. Consequently, three sequential expanded values are averaged to obtain the final 6Hour time series.

The following dialog is used to edit the command and illustrates the command syntax.

**Edit ARMA() Command**

Apply the ARMA (AutoRegressive Moving Average) method to predict future values from past values.  
 An example of ARMA application is to lag and attenuate a time series.  
 The adjusted output time series O is computed from the original input I using:  

$$O[t] = a_1*O[t-1] + a_2*O[t-2] + \dots + a_p*O[t-p] + b_0*I[t] + b_1*I[t-1] + \dots + b_q*I[t-q]$$
 where t = time, p = number of outflows to consider, and q = number of inflows to consider

Input **ARMA** Output

Specify the input time series to process. The input time series will be modified unless a NewTSID parameter is specified for output.  
 The output value is set to missing if one or more input values are missing (typically only filled data should be used). The period will not automatically be extended.  
 Specify initial input time series values to avoid missing values in output (leftmost value is earliest in time prior to time series start).

TS list: **AllMatchingTSID** Optional - indicates the time series to process (default=AllTS).

TSID (for TSList=AllMatchingTSID): **ts1**

EnsembleID (for TSList=EnsembleID):

Input initial values: Optional - input initial values (default - limited by input time series).

Command:  
`ARMA (TSList=AllMatchingTSID,TSID="ts1",ARMAInterval=Day,a=".25,.1,.075,.05,.025",b=".25,.25",Alias="ts1_routed",NewTSID="ts1_routed...Day",Description="New TSID description")`

Cancel OK

**ARMA() Command Editor for Input Parameters**

Input **ARMA** Output

ARMA a and b coefficients must be computed externally. The values for p and q will be determined from the number of coefficients.  
 The ARMA interval must be <= the time series interval.

ARMA interval: **Day** Required (e.g., 2Hour, 15Minute).

"a" coefficients: **.25,.1,.075,.05,.025** Required - "a" coefficients to multiply input values.

"b" coefficients: **.25,.25** Required - "b" coefficients to multiply input values.

Require coefficients to sum to 1: ☐ Optional - require "a" and "b" coefficients to sum to 1 (default=True).

**ARMA() Command Editor for ARMA Parameters**

Input | **ARMA** | Output

Specify a new TSID and optionally alias to create a new output time series - otherwise original time series will be modified.  
The output period will default to the input time series but if specified will override the input period.  
The output minimum and maximum values are applied after the ARMA method is applied and therefore don't impact the ARMA calculations.

Alias to assign: -- Select Specifier -- => ts1\_routed

Required - use %L for location, etc.

New time series ID: ts1\_routed...Day

Required - specify unique TSID information to define time series.

Edit Clear

Description/Name: New TSID description

Optional - description for time series.

Output start:

Optional - override the global output start (default=input period).

Output end:

Optional - override the global output end (default=input period).

Output minimum value:

Optional - output minimum value (default - no minimum limit).

Output maximum value:

Optional - output maximum value (default - no maximum limit).

ARMA\_Output

### ARMA() Command Editor for Output Parameters

The command syntax is as follows:

```
ARMA (Parameter=Value, ...)
```

### Command Parameters

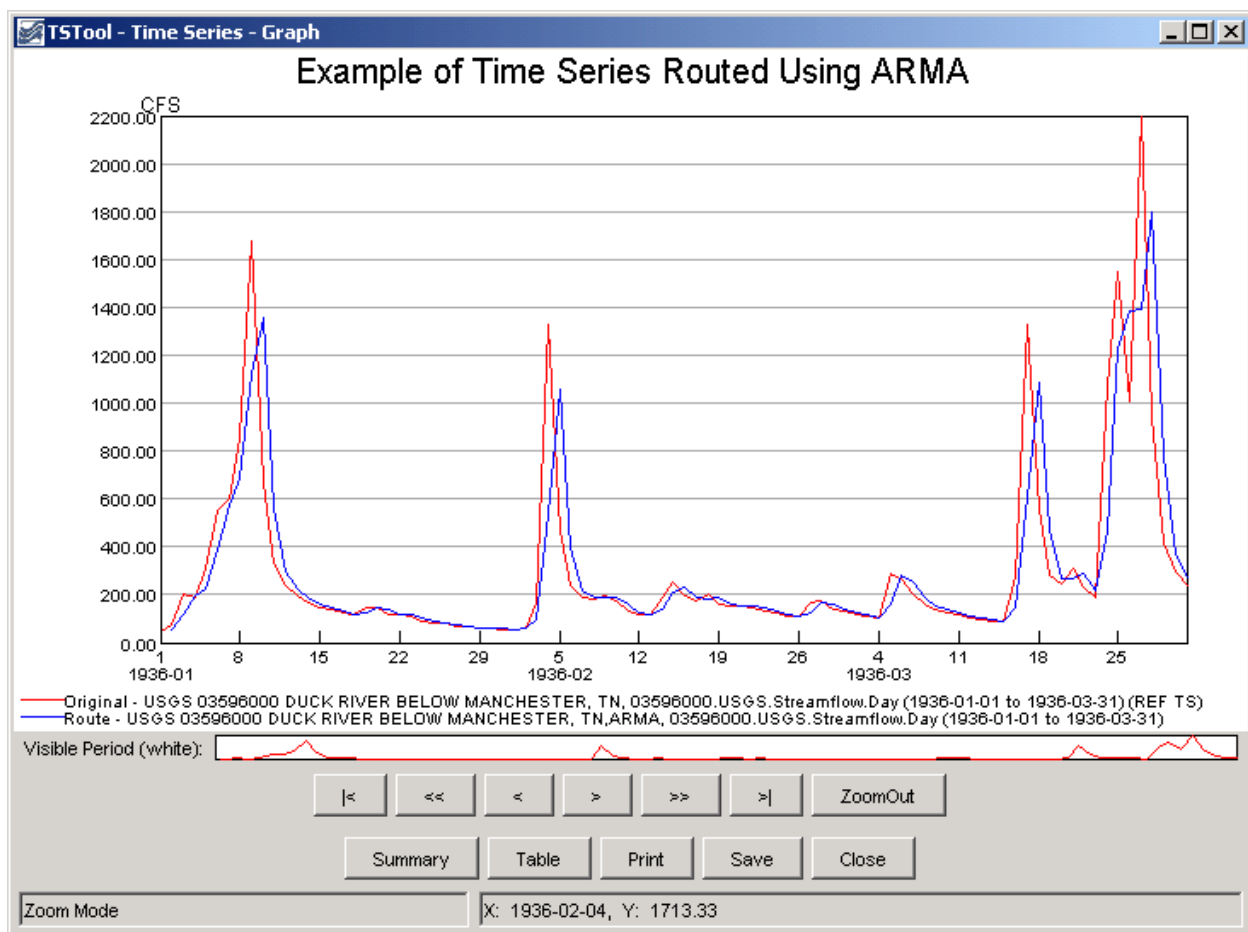
Parameter	Description	Default
TSList	Indicates the list of time series to be processed, one of: <ul style="list-style-type: none"> <li>AllMatchingTSID – all time series that match the TSID (single TSID or TSID with wildcards) will be modified.</li> <li>AllTS – all time series before the command.</li> <li>EnsembleID – all time series in the ensemble will be modified.</li> <li>FirstMatchingTSID – the first time series that matches the TSID (single TSID or TSID with wildcards) will be modified.</li> <li>LastMatchingTSID – the last time series that matches the TSID (single TSID or TSID with wildcards) will be modified.</li> <li>SelectedTS – the time series are those selected with the SelectTimeSeries() command.</li> </ul>	AllTS
TSID	The time series identifier or alias for the time series to be modified, using the * wildcard character to match multiple time series. Can be specified with \${Property}.	Required if TSList=*TSID.
EnsembleID	The ensemble to be modified, if processing an ensemble. Can be specified with \${Property}.	Required if TSList=EnsembleID.
ARMA Interval	The ARMA interval to use in the analysis. See discussion above for explanation when the ARMA interval is different from the input time series. Can be specified with \${Property}.	None – must be specified.
a	a coefficients, separated by commas. a and b coefficients must sum to 1.000000 unless	Optional.

Parameter	Description	Default
	RequireCoefficientSumTol=False. Can be specified with <code>\${Property}</code> .	
b	b coefficients, separated by commas. a and b coefficients must sum to 1.000000 unless RequireCoefficientSumTol=False. Can be specified with <code>\${Property}</code> .	None – must be specified.
Require Coefficients SumTol	If true, the sum of the a and b coefficients must sum to 1.000000 (remainder is ignored). The default enforces mass balance but using False is useful when evaluating analysis.	True
InputInitial Values	A list of comma-separated values to use for the input time series, to allow computation of output at the start of the period. The first value is the earliest in time and the last is the value prior to the start of the input time series. Can be specified with <code>\${Property}</code> .	
NewTSID	If specified, create a new time series as output, with this TSID. Can be specified with <code>\${Property}</code> .	Apply ARMA process and modify the input time series.
Alias	Alias for new output time series if NewTSID is specified. Can specify with %L, <code>\${ts:Property}</code> , and <code>\${Property}</code> .	No alias assigned to output time series.
OutputStart	The date/time for the start of the output as a date/time string or <code>\${Property}</code> . The period can only be lengthened if a new time series is created as output.	Use the global output period or input time series.
OutputEnd	The date/time for the end of the output as a date/time string or <code>\${Property}</code> . The period can only be lengthened if a new time series is created as output.	Use the global output period or input time series.
OutputMinimum	Minimum value allowed for output. Any computed output value less than the minimum will be set to the minimum value. The values are reset after the ARMA calculations occur and therefore do not impact the ARMA calculations. Can be specified with <code>\${Property}</code> .	None – use computed output value.
OutputMaximum	Maximum value allowed for output. Any computed output value greater than the minimum will be set to the maximum value. The values are reset after the ARMA calculations occur and therefore do not impact the ARMA calculations. Can be specified with <code>\${Property}</code> .	None – use computed output value.

A sample command file to process streamflow data from the USGS is as follows:

```
SetOutputPeriod(OutputStart="1936-01-01",OutputEnd="1936-03-31")
ReadUsgsNwisRdb(InputFile="Data/G03596000.rdb",Alias=Original)
Copy(TSID="Original",NewTSID="03596000.USGS.Streamflow.Day.Routed",Alias=Routed)
ARMA(TSList=AllMatchingTSID,TSID="Routed",ARMAInterval=2Hour,a="0.7325,
-0.3613,0.1345,0.5221,-0.2500,0.1381,-0.2643,0.0558",b="0.0263,0.0116,
-0.0146,-0.0081,0.0127,0.0798,0.0727,0.0523,0.0599")
```

The following figure shows the original and routed time series.

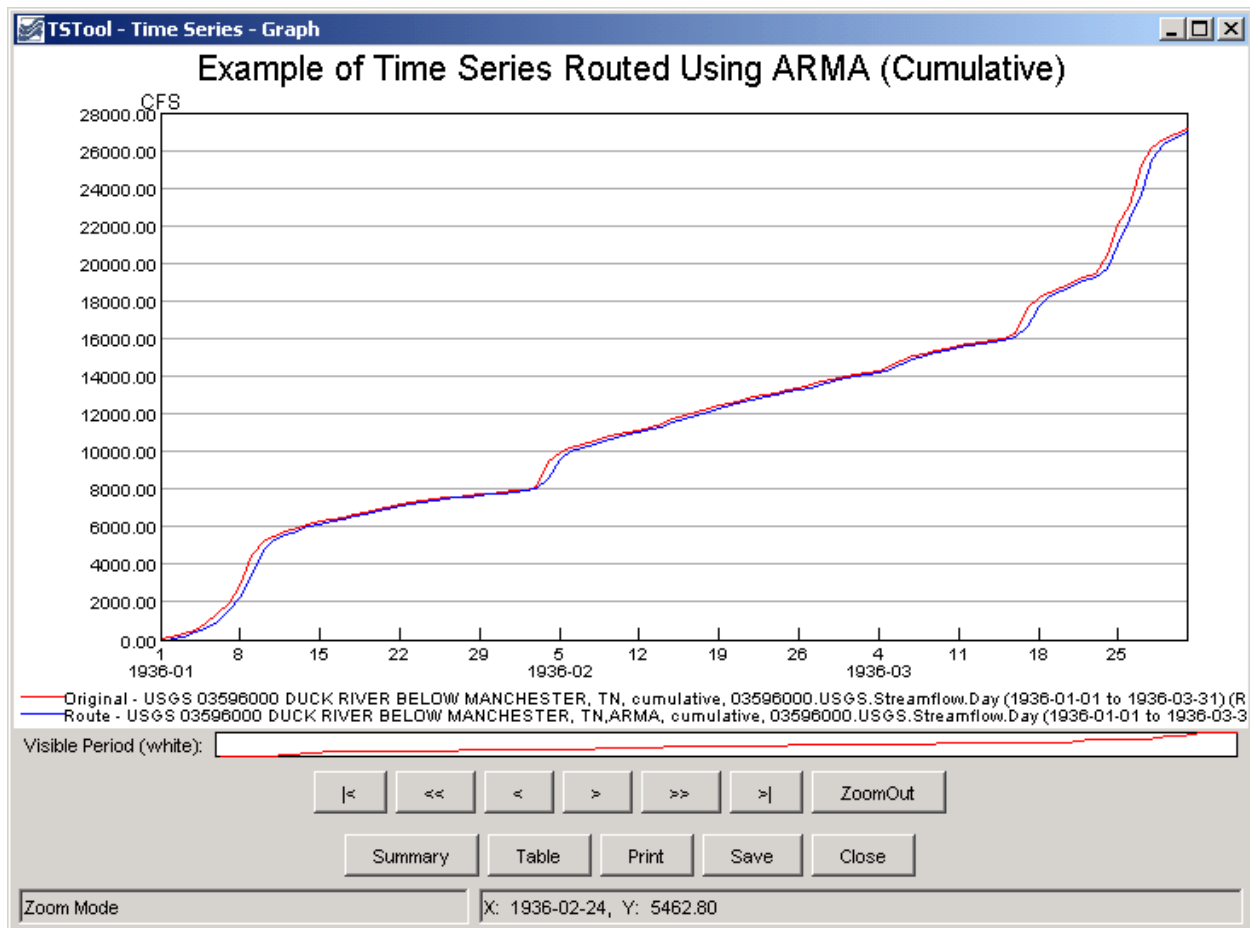


ARMA\_graph

**Example Graph Showing Original and ARMA-Routed Time Series**

The `Cumulate()` command can be used to verify mass balance of the original and routed time series (see the `Cumulate()` command discussion below). For example, insert a `Cumulate()` command near the end of a command file.

The following figure shows the time series from the previous graph, this time as cumulative time series.



**Example Graph Showing Original and ARMA-Routed Time Series as Cumulative Values**