Tsinghua-Berkeley Shenzhen Institute OPERATIONS RESEARCH Fall 2023

Homework 1

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- Acknowledgments: This assignment refers to the textbook: Introduction to Operations Research(10th).
- Collaborators: I finish this assignment by myself. 3.4.9 (b) and 3.4.11 (b) were solved with the help of Excel.

The answers below are arranged according to the order of the following questions in the textbook: 3.1-9 (a) (b), 3.1-10 (a) (b), 3.4-9 (a) (b), 3.4-11(a) (b).

1.1. 3.1-9

(a) SOLUTION Let x= the number of Special Risk and y= the number of Mortgage and z= the total profit. Objective:

$$Maximize \quad z = 5x + 2y, \tag{1}$$

subject to:

$$3x + 2y \le 2400\tag{2}$$

$$y \le 800 \tag{3}$$

$$2x \le 1200,\tag{4}$$

and $x \ge 0, y \ge 0$.

(b) As Figure 1 shown, $z_{max} = 5 \times 600 + 2 \times 300 = 3600$, when x = 600, y = -1.5x + 1200 = 300.

1.2. 3.1-10

(a) SOLUTION Let x= number of hot dogs per week and y= number of hot dog buns per week, and z= the total profit per week. Objective:

Maximize
$$z = 0.88x + 0.33y$$
. (5)

subject to:

$$0.1y \le 200 \tag{6}$$

$$0.25x \le 800$$
 (7)

$$3x + 2y \le 12000, (8)$$

and $x \ge 0, y \ge 0$.

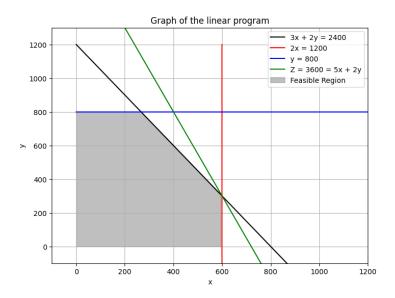


Figure 1: Graphical Solution to Question 3.1-9

(b) As Figure 2 shown, $z_{max} = 0.88 \times 3200 + 0.33 \times 1200 = 3212$, when x = 3200, y = -1.5x + 6000 = 1200.

1.3. 3.4-9

(a) SOLUTION Let x_{ij} = the number of space leased in moth i with a period of j (i = 1, 2, j = 1, 2, 3) and z = the total cost. Objective:

Minimize
$$z = 65 \sum_{i=1}^{5} x_{i1} + 100 \sum_{i=1}^{4} x_{i2} + 135 \sum_{i=1}^{3} x_{i3} + 160 \sum_{i=1}^{2} x_{i4} + 190x_{15},$$
 (9)

subject to:

$$\sum_{i=1}^{5} x_{1j} \ge 30000 \tag{10}$$

$$\sum_{j=1}^{4} x_{2j} + \sum_{j=2}^{5} x_{1j} \ge 20000 \tag{11}$$

$$\sum_{j=1}^{3} x_{3j} + \sum_{j=3}^{5} x_{1j} + \sum_{j=2}^{4} x_{2j} \ge 40000$$
 (12)

$$\sum_{i=1}^{2} x_{4j} + \sum_{i=4}^{5} x_{1j} + \sum_{i=3}^{4} x_{2j} + \sum_{i=2}^{3} x_{3j} \ge 10000$$
 (13)

$$x_{15} + x_{24} + x_{33} + x_{42} + x_{51} \ge 50000, \tag{14}$$

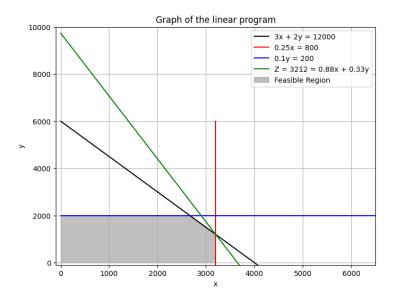


Figure 2: Graphical Solution to Question 3.1-10

and
$$x_{ij} \ge 0$$
 for $i = 1,...,5$ and $j = 1,...,6$ - i.

(b) The solution solved by Excel is shown in Figure 3, $z_{min}=7650000$, when $x_{15}=3000, x_{31}=10000, x_{51}=20000$ and $x_{others}=0$.

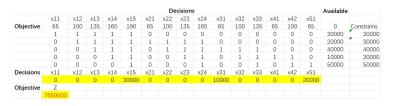


Figure 3: Graphical Solution to Question 3.4-9

1.4. 3.4-11

(a) SOLUTION Let x_{ij} = the number of the productions shipped from factory i to customer j, where i = 1, 2 and j = 1, 2, 3.

Minimize
$$z = 600x_{11} + 800x_{12} + 700x_{13} + 400x_{21} + 900x_{22} + 600x_{23},$$
 (15)

subject to:

$$x_{11} + x_{12} + x_{13} \le 400 \tag{16}$$

$$x_{21} + x_{22} + x_{23} \le 500 \tag{17}$$

$$x_{11} + x_{21} = 300 (18)$$

$$x_{12} + x_{22} = 200 (19)$$

$$x_{13} + x_{23} = 400, (20)$$

and $x_{ij} \ge 0$ for i = 1, 2 and j = 1, 2, 3.

(b) Solution found by Excel is shown in Figure 4, $z_{min}=540000$, when $x_{11}=0, x_{12}=200, x_{13}=200, x_{21}=300, x_{22}=0, x_{23}=200.$

| | Decisions | | | | | | Available | |
|-----------|-----------|-----|-----|-----|-----|-----|-----------|------------|
| | x11 | x12 | x13 | x21 | x22 | x23 | | |
| Objective | 600 | 800 | 700 | 400 | 900 | 600 | 0 | Constrains |
| | 1 | 1 | 1 | 0 | 0 | 0 | 400 | 400 |
| | 0 | 0 | 0 | 1 | 1 | 1 | 500 | 500 |
| | 1 | 0 | 0 | 1 | 0 | 0 | 300 | 300 |
| | 0 | 1 | 0 | 0 | 1 | 0 | 200 | 200 |
| | 0 | 0 | 1 | 0 | 0 | 1 | 400 | 400 |
| Decisions | x11 | x12 | x13 | x21 | x22 | x23 | | |
| | 0 | 200 | 200 | 300 | 0 | 200 | | |
| Objective | Z | | | | | | | |
| | 540000 | | | | | | | |

Figure 4: Graphical Solution to Question 3.4-11

A Relevant files

Relevant files can be found in my GitHub:

https://github.com/OpenGHz/TBSI-MyHomework.git.