#### **CONFIDENCE INTERVALS**

Use **confidence intervals** to **estimate** a parameter with a particular **confidence level, C**.

IDENTIFY: Identify the parameter and the confidence level.

CHOOSE: Choose and name the appropriate interval.

CHECK: Check that conditions for the procedure are met.

#### CALCULATE:

CI: point estimate  $\pm$  critical value  $\times$  SE of estimate

df = (if applicable)
( \_\_\_\_\_ , \_\_\_\_ )

#### **CONCLUDE:**

We are C% confident that the true [parameter] is between \_\_\_\_ and \_\_\_\_. (Put the parameter in *context*.)

We have evidence that [...], because [...]. OR We do not have evidence that [...], because [...].

# When the parameter is: a single proportion p

CHOOSE: **1-Proportion Z-Interval** to estimate p, or **1-Proportion Z-Test** to test  $H_0$ :  $p = p_0$ .

#### CHECK:

- Data come from a random sample or process.
- for CI:  $n\hat{p} \ge 10$  and  $n(1 \hat{p}) \ge 10$ . for Test:  $np_0 \ge 10$  and  $n(1 - p_0) \ge 10$ .

CALCULATE: (1-PropZInt or 1-PropZTest)

**point estimate**: sample proportion  $\hat{p}$ 

**SE** of estimate: for CI, use  $\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$ ; for Test, use  $\sqrt{\frac{p_0(1-p_0)}{n}}$ 

# When the parameter is: a difference of proportions $p_1-p_2$

CHOOSE: **2-Proportion Z-Interval** to estimate  $p_1 - p_2$ , or **2-Proportion Z-Test** to test  $H_0$ :  $p_1 = p_2$ .

#### CHECK:

- Data come from 2 independent random samples or 2 randomly assigned treatments.
- $n_1 \hat{p}_1 \ge 10$ ,  $n_1 (1 \hat{p}_1) \ge 10$ ,  $n_2 \hat{p}_2 \ge 10$ ,  $n_2 (1 \hat{p}_2) \ge 10$ .

### CALCULATE: (2-PropZInt or 2-PropZTest)

**point estimate**: difference of sample proportions  $\,\hat{p}_1 - \hat{p}_2\,$ 

**SE** of estimate: 
$$\hat{p}$$
 is the *pooled* proportion for CI, use  $\sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$ ; for Test, use  $\sqrt{\hat{p}(1-\hat{p})}$   $\sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$ 

#### **HYPOTHESIS TESTS**

Use **hypothesis tests** to **test**  $H_0$  versus  $H_A$  at a particular **significance level,**  $\alpha$ .

IDENTIFY: Identify the hypotheses and the significance level.

CHOOSE: Choose and name the appropriate test.

CHECK: Check that conditions for the procedure are met.

#### CALCULATE:

standardized test statistic =  $\frac{\text{point estimate} - \text{null value}}{SE \text{ of estimate}}$ df = (if applicable)

p-value =

### **CONCLUDE:**

p-value  $< \alpha$ , so we reject  $H_0$ .

We have evidence that  $[H_A]$ . (Put  $H_A$  in *context*.)

OR

p-value >  $\alpha$ , so we do NOT reject  $H_0$ .

We do NOT have evidence that  $[H_A]$ . (Put  $H_A$  in context.)

# When the parameter is: a single mean $\mu$

CHOOSE: **1-Sample T-Interval** to estimate  $\mu$ , or **1-Sample T-Test** to test  $H_0$ :  $\mu = \mu_0$ .

### CHECK:

- Data come from a random sample or process.
- $n \ge 30$ , OR population known to be nearly normal, OR population could to be nearly normal because data has no excessive skew or outliers (draw graph).

CALCULATE: (TInterval or T-Test)

**point estimate**: sample mean  $\bar{x}$ 

**SE** of estimate:  $\frac{s}{\sqrt{n}}$ 

df = n - 1

When the parameter is: a difference of means  $\mu_1$ - $\mu_2$ 

CHOOSE: **2-Sample T-Interval** to estimate  $\mu_1 - \mu_2$ , or **2-Sample T-Test** to test  $H_0$ :  $\mu_1 = \mu_2$ .

# CHECK:

- Data come from 2 independent random samples or 2 randomly assigned treatments.
- $n_1 \ge 30$  and  $n_2 \ge 30$ , OR *both* populations known to be nearly normal, OR *both* populations could be nearly normal because both data sets have no excessive skew or outliers (draw 2 graphs).

CALCULATE: (2-SampTInt or 2-SampTTest)

**point estimate**: difference of sample means  $\bar{x}_1 - \bar{x}_2$ 

**SE** of estimate:  $\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ 

df: use technology