

**The  $\chi^2$  Hypothesis Tests for categorical variables:** chi-square statistic =  $\sum \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$

\*When comparing the distribution of **one categorical variable to a fixed/specified population distribution**

**IDENTIFY:**  $\chi^2$  Goodness of Fit Test

**CHECK:**

- Data come from a random sample or process.
- If sampling without replacement,  $n \leq 10\%$  of N
- All expected counts  $\geq 5$ . (To calculate expected counts for each category, multiply the sample size by the expected proportion under  $H_0$ .)

**CALCULATE:**

$$\chi^2 =$$

$$df = \# \text{ of categories} - 1$$

When comparing the distribution of **a categorical variable across 2 or more populations/treatments**

**IDENTIFY:**  $\chi^2$  Test for Homogeneity

**CHECK:**

- Data come from 2 or more independent random samples or 2 or more randomly assigned treatments.
- If sampling without replacement, each n should  $\leq 10\%$  of each corresponding N
- All expected counts  $\geq 5$ . (Calculate expected counts and verify this to be true.)

**CALCULATE:**

$$\chi^2 =$$

$$df = (\# \text{ of rows} - 1)(\# \text{ of cols} - 1)$$

When looking for **association or dependence between two categorical variables**

**IDENTIFY:**  $\chi^2$  Test for Independence

**CHECK:**

- Data come from a random sample or process.
- If sampling without replacement,  $n \leq 10\%$  of N
- All expected counts  $\geq 5$ . (Calculate expected counts and verify this to be true.)

**CALCULATE:**

$$\chi^2 =$$

$$df = (\# \text{ of rows} - 1)(\# \text{ of cols} - 1)$$

\*Not tested on the AP® Exam.