

6. Consider the integers \mathbb{Z} (an integral domain, right?). What does the notation $\langle 3 \rangle$ mean? What sort of thing is this? What is $\langle r \rangle$ in general?
7. What is $\mathbb{Q}[x]$? Then give an example of an ideal in $\mathbb{Q}[x]$, using proper notation and by listing out some of the elements in the ideal.
8. Give the definition of a **quotient ring** (i.e. a **factor ring**). What do elements of a quotient ring look like? How are the operations defined?
9. Illustrate what you wrote about quotient rings above using two examples: First, $\mathbb{Z}/\langle 3 \rangle$, and then $\mathbb{Q}[x]/\langle x^2 + 1 \rangle$. How many elements are in each of these quotient rings? What do the elements look like? Show how to add/multiply elements.