

6. List five elements in the quotient ring $\mathbb{Q}[x]/\langle p(x) \rangle$ (using the same $p(x)$ from the previous page). Remember, these will all be cosets.

7. The element $x^3 + \langle p(x) \rangle$ is an element of $\mathbb{Q}[x]/\langle p(x) \rangle$, but it can also be written as a “simpler” coset. How?

8. Describe $\mathbb{Q}[x]/\langle p(x) \rangle$ as a set using set builder notation. In other words, this quotient ring is the set of all cosets of the form ...

9. Wait: if we want to show that E is a field, and E is basically the same as $\mathbb{Q}[x]/\langle p(x) \rangle$, then we could just show $\mathbb{Q}[x]/\langle p(x) \rangle$ is a field. What would this mean? What do we need to verify?