

Name: \_\_\_\_\_

1. Find the degrees of field extensions, and briefly explain (using polynomials).  
Then give a basis for each larger field over the smaller field.

(a)  $[\mathbb{Q}(\sqrt{2}) : \mathbb{Q}]$

(b)  $[\mathbb{Q}(\sqrt{2}, \sqrt[3]{5 + \sqrt{2}}) : \mathbb{Q}(\sqrt{2})]$

(c)  $[\mathbb{Q}(\sqrt{2}, \sqrt[3]{5 + \sqrt{2}}) : \mathbb{Q}(\sqrt[3]{5 + \sqrt{2}})]$

(d)  $[\mathbb{Q}(\sqrt[3]{5 + \sqrt{2}}) : \mathbb{Q}]$