

## Inverse, Converse and Contrapositive:

Say P and Q are propositions. Given the implication  $P \Rightarrow Q$ , or  $P \supset Q$

- its inverse is  $\neg P \Rightarrow \neg Q$ , or  $\sim P \supset \sim Q$
- The converse is  $Q \Rightarrow P$ , or  $Q \supset P$
- Its contrapositive is  $\neg Q \Rightarrow \neg P$  or  $\sim Q \supset \sim P$

Write the conditional statements for inverse, converse and contrapositive of the following implication:

1. If this book is interesting, then I am staying at home.

- ☐ P: This book is interesting
- ☐ Q: I am staying at home
- ☐  $\neg P \rightarrow \neg Q$ : If this book is not interesting, then I am not staying at home
- ☐  $Q \rightarrow P$ : If i am staying at home, then this book is interesting
- ☐  $\neg Q \rightarrow \neg P$ : If I am not staying at home, then this book is not interesting

2. If you are more than 60 years old, then you are entitled to a senior citizen's card.

- ☐ P: You are more than 60 years old
- ☐ Q: You are entitled to a senior citizen's card
- ☐  $\neg P \rightarrow \neg Q$ : If you are not more than 60 years old, then you are not entitled to a senior citizen's card
- ☐  $Q \rightarrow P$ : If you are entitled to a senior citizen's card, then you are more than 60 years old
- ☐  $\neg Q \rightarrow \neg p$ : If you are not entitled to a senior citizen's card, then you are not more than 60 years old