

Network Science  
Spring 2024  
Problem sheet 4

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1. Assume that  $f(N)$  tends to zero as  $N \rightarrow \infty$  and take  $p(N) = f(N)/N$ . Prove that w.h.p.  $G \in G_{Np}$  has no “squares”, i.e. no  $(i, j, k, l)$  with links  $i-j-k-l-i$  and  $i, j, k, l$  all distinct.
2. Show that if we let  $p(N) = N^{-z}$  with  $z > 2$  then w.h.p. all nodes in graphs generated by the  $G_{Np}$  model will be isolated (they will not have any links).  
*This is a modified version of the last question on problem sheet 3*