

$$Z_a = g_\theta(X_a), Z_t = Z_a + \int_a^t f_\theta(Z_s) \mathrm{d}X_s$$