

$\sim H_0$  : No one in the class  
can predict the future

$H_1$  : Someone can predict the future

6 tosses :

Let  $A$  be the event of someone  
guessing all 6 tosses correctly

$$P(A) = \frac{\text{card } A}{\text{Card } \Omega} = \frac{1}{2^6} = \frac{1}{64}$$

$\Omega$  - space of 6 tosses  $= 0.0156$

$$\frac{1}{32} = 0.03$$

$$\alpha = 0.05$$

$$p = 0.03 \quad p < \alpha$$

Class today has 58 students

Suppose there were 100 students  
there would be 100 p-values

$p \sim \text{Unif}(0,1)$  under  $H_0$  is true

So for 100 independent p-values

How many would you expect are less than 0.05?

Let  $Z$  be the number of p-values

less than  $\alpha$  ( $= 0.05$ )

$$Z = \sum_{i=1}^n I(x_i < \alpha) \stackrel{(n=100)}{=} A_i$$

each  $x_i$  is a p-value

$$I(x_i < \alpha) = \begin{cases} 1 & \text{if } x_i < \alpha \\ 0 & \text{otherwise} \end{cases}$$

$\xrightarrow{\sim \text{Unif}(0,1)}$

each  $I(x_i < \alpha) \sim \text{Bern}(\alpha)$

$$Z \sim \text{Bin}(n, \alpha) \quad n=100 \quad \alpha=0.05$$

$$E[Z] = n\alpha = 100 \cdot (0.05) = 5$$

$$\tilde{Z} \quad n=58 \quad \alpha=0.05$$

$$E[\Sigma] = 58 \cdot (0.05) = 2.9$$

$$\alpha = 0.03 = 58(0.03) \Rightarrow \underline{1.74}$$

Let  $A_i$  be a hypothesis test

$$\text{Let } A = \bigcup_{i=1}^n A_i$$

$$P(A) = P\left(\bigcup_{i=1}^n A_i\right) \leq \sum_{i=1}^n P(A_i)$$

Suppose  $P(A_i) = \alpha$  for  $i=1, 2, \dots, n$

$$\begin{aligned} P(A) &= P\left(\bigcup_{i=1}^n A_i\right) \leq \sum_{i=1}^n P(A_i) \\ &= \sum_{i=1}^n \alpha = n\alpha \end{aligned}$$

Need to adjust threshold  $\alpha$  when there are multiple hypotheses

$$P(A) = n\alpha$$

Let  $\tilde{\alpha} = \frac{\alpha}{n}$   $\leftarrow$  nominal threshold level  
adjusted significance level

Test  $H_0$  at level  $\tilde{\alpha} = \frac{\alpha}{n}$   
for multiple hypotheses  
then the probability that at least  
one individual hypothesis is rejected  
is  $\alpha$

## BONFERRONI CORRECTION

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$H_0$  : My colleague cannot see  
the future

$H_1$  : My colleague can see  
the future.

$\alpha = 0.02 \Rightarrow H_0$  rejected

## The exam

Chapter 1: Central tendency + dispersion

Chapter 2: EDA

Chapter 3: Normal random variables

Chapter 4: Hypothesis testing

Excluding one-sided hypothesis  
testing (Section 4.4.2)

Chapter 5: Pitfalls in Statistics

Chapter 6: Covariance + Correlation

Chapter 7: Statistical models

Chapter 8: (Maximum) likelihood

Chapter 9: Simple linear regression

Excluding 10. Bayesian inference

11. Bootstrap

A. Additional details

Formula sheet?

- Term 1      3 Q
- Term 2      3 Q

Revision class(es)    3 May (Wed)