

$$Z_a \doteq g_\theta(X_a), Z_t \doteq Z_a + \int_a^t f_\theta(Z_s) dX_s$$