

$$g(t, Z_t) = f(Z_t) - \frac{dX_t}{dt}$$