

**Mathematics Pre-arrival course**

**Weekly Quiz 2 – Calculus: Integration and Differentiation**

Note in all problems that  $\log(x)$  represents the natural logarithm of  $x$  (sometimes written  $\ln(x)$ ).

1. The derivative of the function:

$$y = \sin(x^3)$$

is

- (a)  $y = 3x^2 \cos(x^3)$
- (b)  $y = 3x^2 \sin(x^3)$
- (c)  $y = -3x^2 \cos(x^3)$
- (d)  $y = -3x^2 \sin(x^3)$

2. The derivative of the function:

$$y = 2x^2 \cos(3x^2)$$

is

- (a)  $y = 4x(\cos(3x^2) + 3x^2 \sin(3x^2))$
- (b)  $y = 2x(2 \cos(3x^2) - x \sin(3x^2))$
- (c)  $y = 2x(2 - x^2) \cos(3x^2)$
- (d)  $y = 4x(\cos(3x^2) - 3x^2 \sin(3x^2))$

3. The derivative of the function:

$$y = \frac{e^{\sin(x)}}{1 + 2x}$$

is

- (a)  $y = \frac{-e^{\cos(x)}((1+2x)\cos(x)+2)}{(1+2x)^2}$
- (b)  $y = \frac{e^{\sin(x)}((1+2x)\cos(x)-2)}{(1+2x)^2}$
- (c)  $y = \frac{e^{\sin(x)}(2-(1+2x)\cos(x))}{(1+2x)^2}$
- (d)  $y = \frac{e^{\sin(x)}(1+2x)\cos(x)}{(1+2x)^2}$

4. The value of  $\frac{dy}{dx}$  when:

$$\sqrt{x^2y} + x = y, \quad x, y > 0$$

is

- (a)  $\frac{dy}{dx} = \frac{\sqrt{y}(1+\sqrt{y})}{\sqrt{y}-x}$
- (b)  $\frac{dy}{dx} = \frac{2\sqrt{y}(1-y)}{2\sqrt{y}+x^2}$
- (c)  $\frac{dy}{dx} = \frac{2\sqrt{y}(1+\sqrt{y})}{2\sqrt{y}-x}$
- (d)  $\frac{dy}{dx} = \frac{\sqrt{y}(1-\sqrt{y})}{\sqrt{y}+x}$

5. Find the value of

$$\int_0^1 (x^3 - 6x + 1)(x^2 - 2)dx$$

- (a) 1
- (b) -1
- (c)  $\frac{1}{12}$
- (d)  $\frac{5}{2}$

6. Find the value of

$$\int_0^{1/\sqrt{2}} \frac{1}{\sqrt{2x^2 + 1}} dx$$

- (a)  $\log |\sqrt{2}|$
- (b) 1
- (c)  $\frac{1}{\sqrt{2}} \log |\sqrt{2} + 1|$
- (d)  $\frac{1}{\sqrt{2}} \log |\sqrt{2}|$

7. Find the value of

$$\int_0^1 \frac{e^{2x}}{e^{2x} + 4} dx$$

- (a)  $\frac{1}{2} \log |\frac{e^2 + 4}{5}|$
- (b)  $1 - \log |5|$
- (c)  $\log |\frac{e^2 + 4}{5}|$
- (d)  $\frac{1}{2} \log |\frac{e^2 - 4}{5}|$

8. Find the value of

$$\int_0^1 \frac{1}{2x^2 + 4x + 4} dx$$

- (a)  $\arctan(3) - \frac{\pi}{4}$
- (b)  $\frac{1}{2} \arctan(2) - \frac{\pi}{8}$
- (c)  $\frac{1}{2} \arctan(2) - \frac{\pi}{4}$
- (d)  $\frac{1}{2} \arctan(3) - \frac{\pi}{8}$

9. Find the value of

$$\int_0^1 \frac{1}{x^2 + 3x + 2} dx$$

- (a)  $\frac{1}{2} \log |\frac{2}{3}|$
- (b)  $\frac{1}{2} \log |\frac{4}{3}|$
- (c)  $\log |\frac{2}{3}|$
- (d)  $\log |\frac{4}{3}|$

10. Find the value of

$$\int_0^1 \arcsin(x) dx$$

- (a)  $\pi$
- (b)  $\frac{\pi}{2} - 1$
- (c)  $\arcsin(2) - 1$
- (d)  $\arcsin(2)$

11. The solution to the equation

$$\cosh(3x) = 6 \cosh(x)$$

for  $x \in \mathbb{R}$  is

- (a)  $x = 1$
- (b)  $x = \log(2 + \sqrt{5})$
- (c)  $x = \log(3 + \sqrt{8})$
- (d)  $x = \log\left(\frac{3}{2} + \frac{\sqrt{5}}{2}\right)$

12. The value of the integral

$$\int_{\frac{1}{2}\log(3)}^{\log(3)} \frac{1}{5 \cosh(x) - 4 \sinh(x)} dx$$

is

- (a)  $\frac{\pi}{18}$
- (b)  $\frac{\pi}{9}$
- (c)  $\frac{1}{2} \log(3)$
- (d)  $\log(3)$