

$$a_i = \frac{[t_i, t_{i+1}]f - m_i}{\Delta t_i} - b_i \Delta t_i$$