16-745: Optimal Control and Reinforcement Learning

Spring 2024

Course Description

This is a course about how to make robots move through and interact with their environment with speed, efficiency, and robustness. We will survey a broad range of topics from nonlinear dynamics, linear systems theory, classical optimal control, numerical optimization, state estimation, system identification, and reinforcement learning. The goal is to provide students with hands-on experience applying each of these ideas to a variety of robotic systems so that they can use them in their own research.

Prerequisites: Strong linear algebra skills, experience with a high-level programming language like Python, MATLAB, or Julia, and basic familiarity with ordinary differential equations.

Instructors

Prof. Zac Manchester	**Email:** zacm@cmu.edu
Head TA: Kevin Tracy	**Email:** ktracy@cmu.edu
TA: Jeong Hun (JJ) Lee	**Email:** jeonghunlee@cmu.edu
TA: Fausto Vega	**Email:** fvega@andrew.cmu.edu
TA: Arun Bishop	**Email:** arunleob@cmu.edu
TA: Sam Schoedel	**Email:** sschoede@andrew.cmu.edu

Logistics

- Lectures will be held Tuesdays and Thursdays 5:00–6:20 PM Eastern time in TEP 1403. Lectures will also be live streamed on zoom and recorded for later viewing.

- Recitation will be held Fridays on Zoom at 11 AM.

- Office hours will be TODO: based on survey.

- GitHub will be used to distribute assignments and GradeScope will be used for submissions.

- Piazza will be used for general discussion and Q&A outside of class and office hours.

- There will be no exams. Instead, students will form groups of up to five to complete a project on a topic of their choice.

Learning Objectives

By the end of this course, students should be able to do the following:

1. Analyze the stability of dynamical systems

2. Design LQR controllers that stabilize equilibria and trajectories

3. Use offline trajectory optimization to design trajectories for nonlinear systems

4. Use online convex optimization to implement model-predictive control

5. Understand the effects of stochasticity and model uncertainty

6. Directly optimize feedback policies when good models are unavailable

Learning Resources

There is no textbook required for this course. Video recordings of lectures and lecture notes will be posted online. Additional references for further reading will be provided with each lecture.

Homework

Four homeworks will be assigned during the semester. Students will have at least two weeks to complete each assignment. All homework will be distributed and collected using GitHub. Solutions and grades will be returned within one week of homework due dates.

Project Guidelines

Students should work in groups of 1–5 to complete a substantial final project. The goal is for students to apply the course content to their own research. Project proposals will be solicited on the first homework assignment, and topics will be selected in consultation with the instructors.

Project grades will be based on a short presentation given during the last week of class and a final report submitted by May 10. Reports should be written in the form of a 6–8 page conference paper using the standard two-column IEEE format.

Grading

Grading will be based on:

- 50% Project

- 40% Homework

- 10% Participation

Attendance during lectures is not required to earn a full participation grade. Students can also participate through any combination of office hours, Piazza discussions, project presentations, and by offering constructive feedback about the course to the instructors.

Course Policies

Late Homework: Students are allowed a budget of 6 late days for turning in homework with no penalty throughout the semester. They may be used together on one assignment, or separately on multiple assignments. Beyond these six days, no other late homework will be accepted.

Accommodations for Students with Disabilities: If you have a disability and are registered with the Office of Disability Resources, I encourage you to use their online system to notify me of your accommodations and discuss your needs with me as early in the semester as possible. I will work with you to ensure that accommodations are provided as appropriate. If you suspect that you may have a disability and would benefit from accommodations but are not yet registered with the Office of Disability Resources, I encourage you to contact them at access@andrew.cmu.edu.

Statement of Support for Students' Health & Well-Being: Take care of yourself. Do your best to maintain a healthy lifestyle this semester by eating well, exercising, avoiding drugs and alcohol, getting enough sleep, and taking some time to relax. This will help you achieve your goals and cope with stress.

If you or anyone you know experiences any academic stress, difficult life events, or feelings like anxiety or depression, we strongly encourage you to seek support. Counseling and Psychological Services (CaPS) is here to help: call 412-268-2922 and visit http://www.cmu.edu/counseling. Consider reaching out to a friend, faculty, or family member you trust for help getting connected to the support that can help.

If you or someone you know is feeling suicidal or in danger of self-harm, call someone immediately, day or night:
   CaPS: 412-268-2922
   Re:solve Crisis Network: 888-796-8226

If the situation is life threatening, call the police:
   On campus: CMU Police: 412-268-2323
   Off campus: 911

If you have questions about this or your coursework, please let me know. Thank you, and have a great semester.

Tentative Schedule

Week	Dates	Topics	Assignments
1	Jan 16	Course Overview, & Dynamics Intro	Survey
	Jan 18	Stability, Discrete-Time Dynamics	HW0 Out
2	Jan 23	Optimization Intro	HW0 Due
	Jan 25	Numerical Optimization Pt. 1	HW1 Out
3	Jan 30	Numerical Optimization Pt. 2 & Optimal Control Intro	
	Feb 1	Pontryagin, Shooting Methods, & LQR Intro	
4	Feb 6	LQR as a QP & Riccati Equation	HW 1 Due
	Feb 8	Dynamic Programming & Intro to Convexity	HW 2 Out
5	Feb 13	Convex Model-Predictive Control	
	Feb 15	Intro to Trajectory Optimization, Iterative LQR, & DDP	
6	Feb 20	DDP with Constraints and Free Final Time	HW2 Due
	Feb 22	Direct Trajectory Optimization, Collocation, & SQP	HW3 Out
7	Feb 27	Attitude Intro: SO(3) & Quaternions	
	Feb 29	Optimizing with Attitude	
8	Mar 5	No Class	
	Mar 7	No Class	
9	Mar 12	LQR with Attitude, Quadrotors, & Contact Intro	HW3 Due
	Mar 14	Trajectory Optimization for Hybrid Systems	HW4 Out
10	Mar 19	Data-Driven Methods & Iterative Learning Control	
	Mar 21	Stochastic Optimal Control & LQG	
11	Mar 26	Robust Control & Minimax DDP	HW4 Due
	Mar 28	RL from an Optimal Control Perspective	
12	Apr 2	Practical Tips & Tricks, Control History	
	Apr 4	Case Study: How to Land a Rocket	
13	Apr 9	Case Study: How to Drive a Car	
	Apr 11	No Class	
14	Apr 16	Case Study: How to Walk	
	Apr 18	TBD	
14	Apr 23	Project Presentations	
	Apr 25	Project Presentations	

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Project grades will be based on a short presentation given during the last week of class and a final report submitted via Google drive by May 10 Anywhere on Earth. Reports should be written in the form of a 6 page (plus references) ICRA or IROS conference paper using the standard two-column IEEE format. Sections should include an abstract, introduction and/or background to motivate your problem, 2–3 main technical sections on your contributions, conclusions, and references. Grading will be based on the following criteria:

10%	Class presentation
10%	Adherence to IEEE formatting and length requirements
10%	Innovation & Creativity: Is what you did new/cool/interesting? Convince me.
30%	Clarity of presentation: Can I understand what you did from your writing + plots?
40%	Technical correctness: Are your results reasonable? Is your code correct?