

# Progress Report for MPhil Thesis

Tilman Graff – University of Oxford

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## Open Questions – What I need to discuss

Topics to be raised in my next supervisor meeting.

Below starts my latest progress report.

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## 1 Research Question

### **Which factors influence the global distribution of trade network optimality?**

In this thesis, I aim to create a (potentially) global – in any case African – dataset of trade network efficiency. Taking the spatial distribution of current economic activity and population as given, I use a model from a recent working paper to determine the optimal trade network for each country. I then compare each country's current road network to its optimal one and derive a measure of how far a country is currently away from its ideal self.

In a second step, I will then investigate the origins of this global distribution. Which factors led to the heterogeneities among countries today? Specifically, I will look at:

- Do networks with large colonial infrastructure investments do better or worse today?
- Does tribal favoritism explain why some areas are lacking lucrative investment?
- And many more. See below.

Ferdinand notes that the better these questions are, the more I will be scrutinised for the methodology. But that's what I want!

## 2 Research steps

In order to conduct this research, I will need to follow a series of steps and transfer data between multiple programming softwares. Here is a step-by-step guide, with progress as of December 12, 2017:

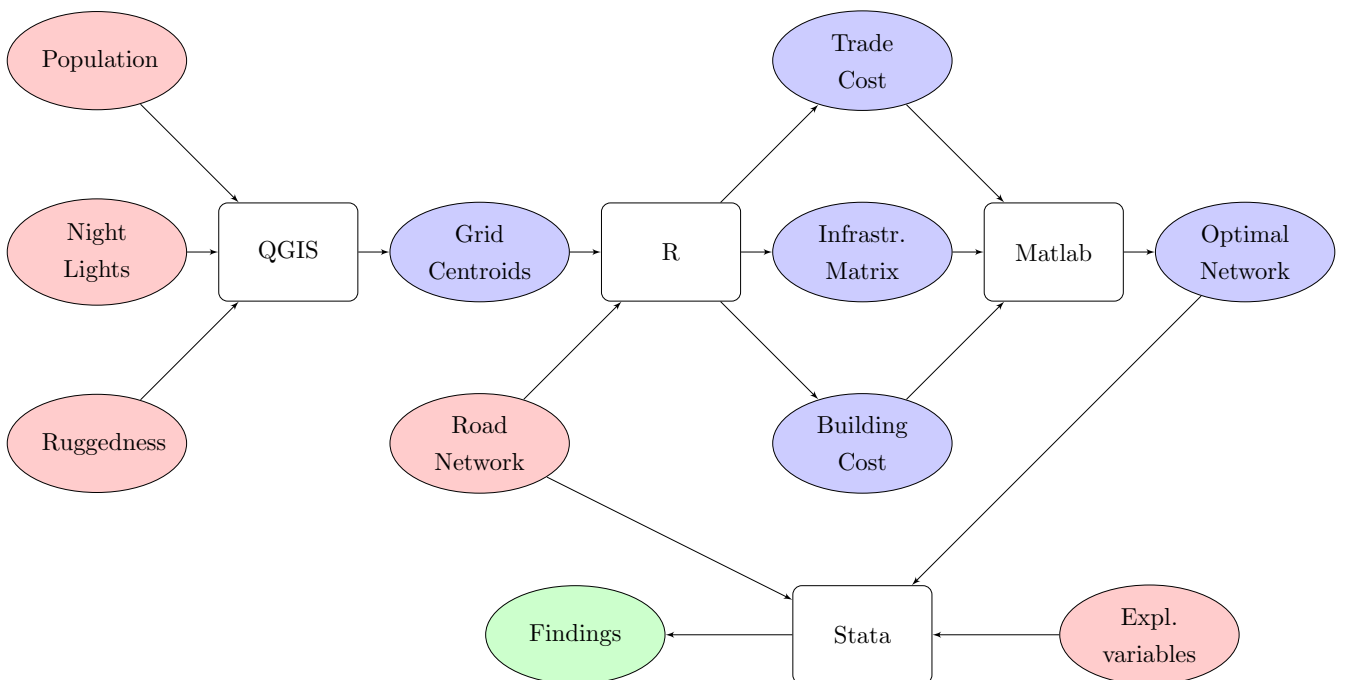
- ✓ Find global raster data on population, night-lights, ruggedness, and colonial infrastructure investments.

- ✓ Grid the world on 50x50km squares and aggregate finer-resolution data into those grids.
- ~~Locate the maximum population point within each grid and call this the (population) centroid of the grid.~~ I decided against this additional step. Mostly because I cannot figure out how to do it in QGIS. (And it's probably not that important?). Instead, I investigate travel times and distances between unweighted geometric centroids.
- ✓ Use OpenStreetMap to find distance and average speed between neighboring gridcells.
- ✓ Use distance and ruggedness to calculate Infrastructure Building Cost Matrix  $\delta_{i,k}^I$  for every country.
- ✓ Use average speed to calculate current Infrastructure Matrix  $I_{i,k}$  for every country.
- ✓ Use distance to calculate (iceberg) Trade Constant Matrix  $\delta_{i,k}^\tau$  for every country.
- Use  $\delta_{i,k}^I$ ,  $\delta_{i,k}^\tau$ , and  $I_{i,k}$  to find the optimal trade network  $I_{i,k}^*$  and optimal trade flows  $Q_{i,k}^*$  for every country. This directly follows the Fajgelbaum and Schaal (2017) Working Paper. I know how to do this, I am however afraid that this might take too long.
- Compare  $I_{i,k}$  and  $I_{i,k}^*$  for every country to obtain a measure of network optimality  $\zeta_c$  for every country  $c$ .
- Investigate heterogeneity in  $\zeta_c$

The following flowchart visualises the process. It shows the path input data (red circles) take through various programming languages (white rectangles) and intermediate datasets (blue circles) into eventual findings (green circle).

### 3 Notes on individual steps

In this section, I provide a more detailed account of what I did in each of the above-mentioned steps.



### 3.1 Find global raster data

I use two datasources to create a global raster dataset of relevant variables:

- Data on night lights, ruggedness, land suitability, altitude, malaria index, and precipitation comes from Henderson et al. (2018). These are available on 25km x 25km grids. Most of the data are for the year 2010. These data are different from most used in the recent literature, as they are not top-coded at 65 but rather able to gain much finer differentiations in highly-lit areas. I follow the authors in bottom-coding the data at 0.00034 instead of zero to counteract noise at the bottom. Importantly, there are a couple of regions with NaN values for the Henderson et al. light data: most notably over a stretch of the Algerian Sahara and over Lake Victoria. Once aware of these, I am not too worried about these areas. I drop them from my here on.
- For census-level spatial population data, I use the Gridded Population of the World (GPW) database from the Socioeconomic Data and Applications Center (2016). These are available on much finer resolution. This database is for the year 2015.
- For later analysis, I will try to investigate heterogeneity on the ethnicity level. Which ethnic groups are significantly under/overinvested in and how does this correlate with political violence etc. Data for this comes from Michalopoulos and Papaioannou (2016).

Using GIS, I aggregated these datasets to a 1-by-1 degree global grid (roughly 50km x 50km), following Fajgelbaum and Schaal (2017). In doing so, I take spatial sums of population, and spatial averages of lights, ruggedness, malaria, and weather data.

### 3.2 Construct Centroids

For each of these gridcells, I calculate the geometric centroid. I do not weigh by population in constructing this centroid, as I have been unable to figure out how to do this. Ferdinand notes that this is not important.

I then crop all global centroids that are not over land. This leaves me with 59,059 gridcells. Doing this, I am aware that I will lose information: I cut gridcells that might be partially over land, as soon as their centroid is not over land. This approach will, however, create equidistant centroid locations, so I'm really just playing one disadvantage against the other.

I then attribute the centroids with the lights, population, and other data from the underlying gridcell. Thus, I act as if all people and all economic activity of a given cell were concentrated on the single centroid point. This is because Fajgelbaum and Schaal's model calculates trade between nodes, not areas. I find this to be a reasonable model simplification.

### 3.3 Construct Global Road database

I calculate the optimal route between any centroid and each of its eight surrounding neighbours. In doing so, I rely on the open source online project OPEN STREET MAPS (OSM), which is comparable to GOOGLE MAPS, but allows for unlimited use of its API. I scrape OSM with an R-Package called `osrmRoute`. This

package takes start and destination locations, sends them to OSM, and comes back with the optimal route, distance, and speed in virtually no time. I am amazed by how fast this is.

Two problems present itself:

1. OSM's data supply is user generated and hence biased towards more prosperous areas. However, since I mostly care about big highways, I doubt there are all too glaring omissions. Also, I care about relative inefficiencies within a country, not cross-section differences between countries.
2. I tell OSM to find the optimal route for a car. However, in many remote areas, cars don't get you from A to B. `osrmRoute` then desparately tries to locate the user onto the nearest street (which could be far away!). I hence scrape the entire loc-by-loc route, and calculate the walking distance to the nearest street (and the walking distance from the end of the supplied route to the actual endpoint). I do so by taking direct paths and imply a walking speed of 4 km/h. I then calculate whether walking the entire distance from A to B is faster (not shorter, but faster!) than the route supplied by `osrmRoute`. If so, I replace the route with the walking route.

**Figure 1:** Road Networks for different countries as scraped off OSM

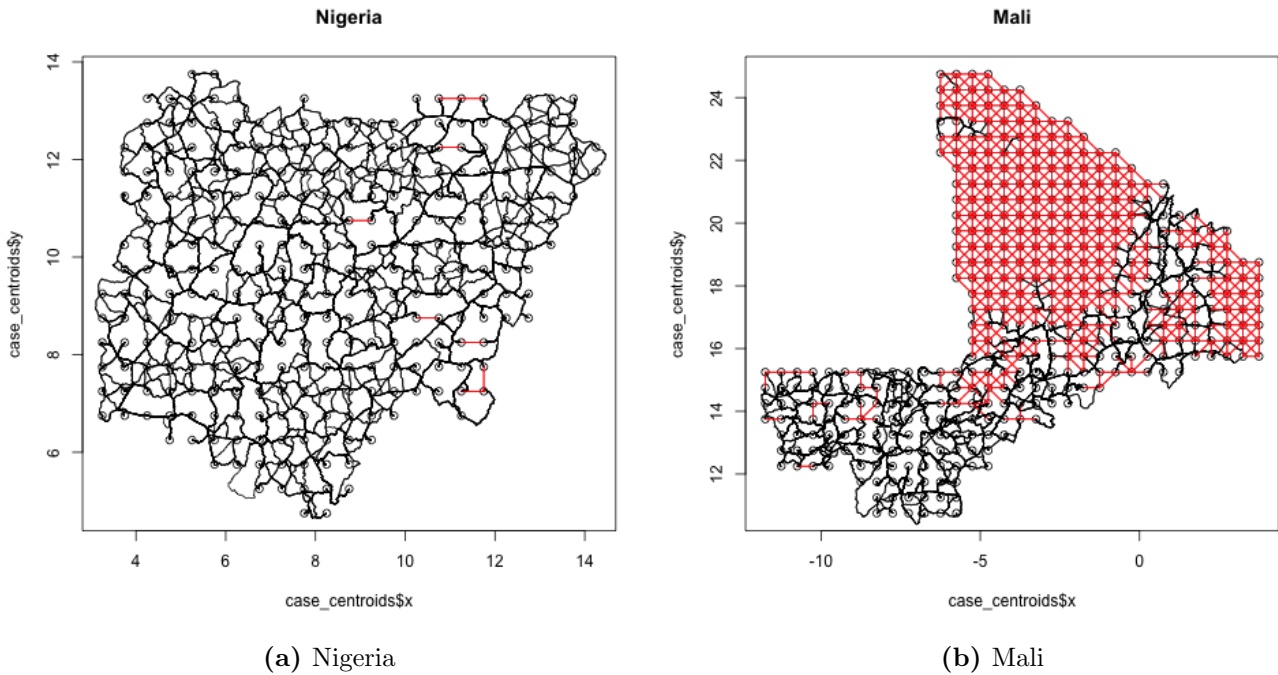


Figure 1a displays how this would look like for the country of Nigeria. In black are optimal routes from all 289 centroids to their up to eight closest neighbours. If walking were the preferred option, this direct route is plotted in red. In Nigeria, this is mostly the case in some areas of the (swampy) South and East and some observations in the desert ridden North.

This procedure seems to well capture notions of remoteness: Consider the same graph but for Mali (Figure 1b). For much of the Saharan parts of the country, walking straight lines through the sand is the best available option. I am actually not too worried about these areas. They will presumably have almost no population or night lights and hence I do not expect the later optimisation to yield unrealistic trans-Saharan highways.

## 4 Calibration of $I_{i,k}$ , $\delta_{i,k}^\tau$ , $\delta_{i,k}^I$

Next up, I use the obtained matrices to construct underlying graph characteristics needed for the model to work. As rough guideline, I follow Fajgelbaum and Schaal (2017).

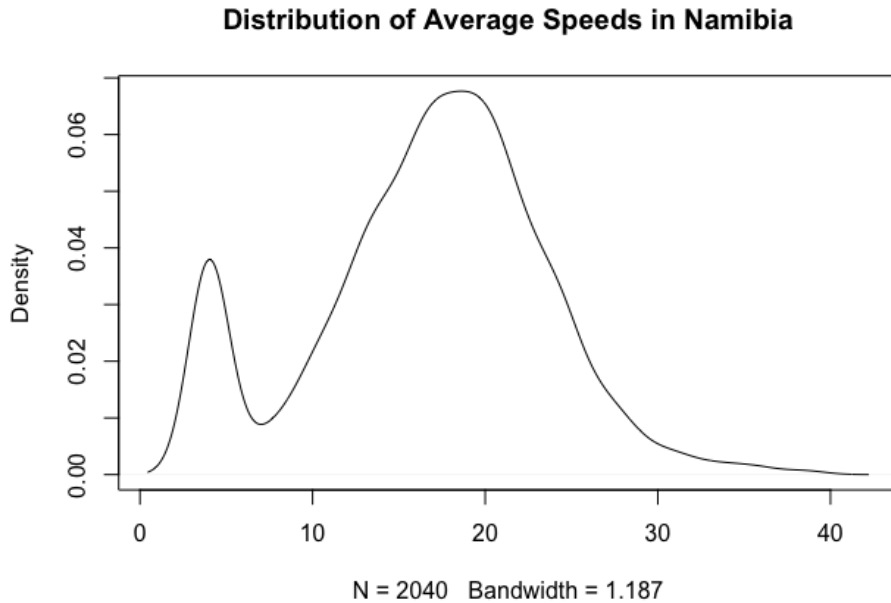
### 4.1 Current Infrastructure Network $I_{i,k}$

The matrix  $I_{i,k}$  discretises the road network obtained by `osrmRoute`. Basically, it attaches a value to each link between nodes, indicating “How much infrastructure” has been built into the edge. Fajgelbaum and Schaal (2017) do this by calculating the mean number of lanes a road has plus adding a dummy for national roads. I cannot do this, as I don’t have comprehensive data on road lanes. However, I believe that the derived speed matrix from `osrmRoute` actually serves as the much more significant statistic for what Fajgelbaum and Schaal want to capture. I hence propose

$$I_{i,k} = \text{Average Speed}_{i,k} \quad (1)$$

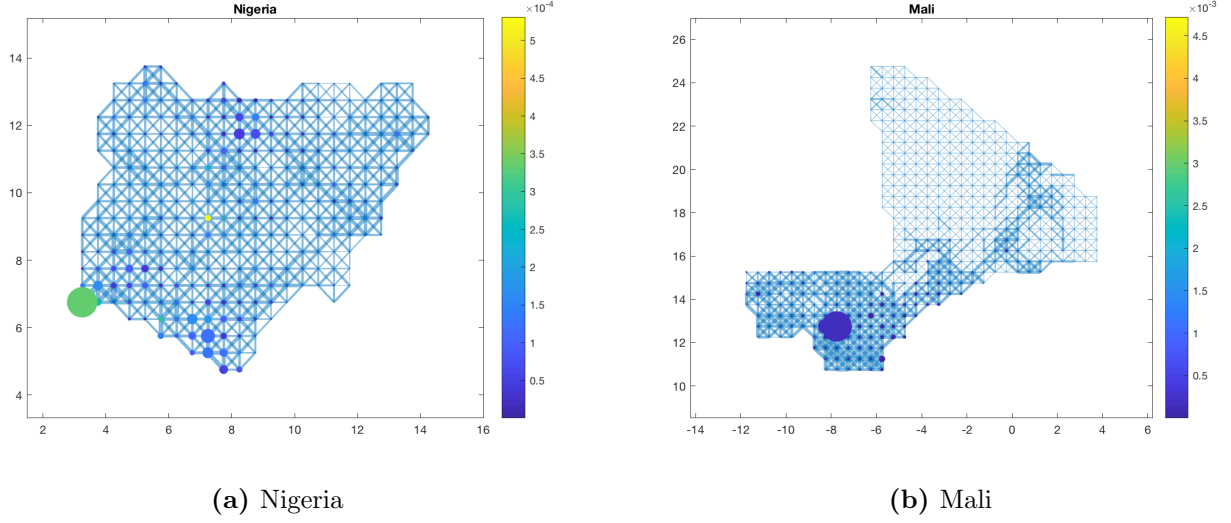
This is obviously a very simple calibration. But the general logic is clear: if a certain edge allows a car to drive faster on it, chances are that more investments had been made into it. In a sense, this captures the same notion Fajgelbaum and Schaal with their calibration based on lanes and national roads. Figure 2 shows a distribution of the average speeds (on travelled routes, in km/h) for Namibia. As can be seen, the distribution follows a nicely behaved shape, with an additional hump at 4 km/h for purely walked routes (see above).

With these calibrations, I can define country road networks as undirected graphs. Nodes correspond to centroid locations, edges correspond to their interconnections, with edgeweights defined by the average speed one reaches while driving (or walking) over the edge. Figure 3a and 3b display this discretisation



**Figure 2:** Average Speed for Namibia, in km/h, 288 centroid locations

**Figure 3:** Discretised Networks for different countries



of the road network for Nigeria and Mali. Node sizes correspond to populations, node colours to implied productivity (see below), edge widths correspond to average speeds.

#### 4.2 Infrastructure Building Cost Matrix $\delta_{i,k}^I$

I am still working on this one. The entries to this matrix represent the cost to building new infrastructure (think: one additional km/h to stay in the logic from above) onto a given edge from  $i$  to  $k$ . Fajgelbaum and Schaal use

$$\ln\left(\frac{\delta_{i,k}^I}{dist_{i,k}}\right) = \ln(\delta_0^I) - 0.11 * (dist_{i,k} > 50km) + 0.12 * \ln(ruggedness_{i,k}) \quad (2)$$

which comes from Collier et al. (2015).  $\delta_0^I$  is individual for every country. I have all the data to replicate this,<sup>1</sup> but was thinking of including measures on extra low soil quality (which is congruent to Saharan soil) and (maybe) the Malaria index in there (or is that too much a colonial, “white guys walk in, build a road, and get Malaria”, kind of thinking?). Update December 5th: I have now decided to just go with the Fajgelbaum and Schaal calibration. Collier et al. (2015) only have one additional variable in their dataset (which is population density), but that’s not an underlying cost parameter and rather an outcome corollary. I will thus not include it and stick to Fajgelbaum and Schaal.

#### 4.3 Iceberg Trade Constant Matrix $\delta_{i,k}^\tau$

I cannot follow Fajgelbaum and Schaal in this one, as their calibrations strike me as way to high. With their specification, I am basically stifling most trade as the cost is unbearable. To be fair, their parameters are calibrated on different measures for  $I_{i,k}$  and  $Y_i$ , so it’s not surprising that this does not work.

<sup>1</sup>Note that Henderson et al. slightly alter the ruggedness variable, compared to Nunn and Puga (2012), which also causes it to be on average a bit higher (about 20 per cent). Should not really matter.

In trying to come up with a different approach, I find the analysis by Atkin and Donaldson (2015), who estimate the trade cost elasticity to (log) distance as 0.0374 for Ethiopia and 0.0558 for Nigeria, using barcode-level spatial price data. I take the average value between the two and hence define

$$\delta_{i,k}^\tau = 0.466 * \log(\text{dist}_{i,k}) \quad (3)$$

The actual iceberg trade costs are then computed as

$$\tau_{i,k}(Q_{i,k}, I_{i,k}) = \delta_{j,k}^\tau * \frac{Q_{i,k}^\beta}{I_{i,k}^\gamma} \quad (4)$$

where  $Q_{i,k}$  represents trade flows between nodes (to capture notion of congestion),  $I_{i,k}$  is the existing Infrastructure Network (derived above),  $\beta = 1$  and  $\gamma = 1$  in the easiest calibration.

With this, my estimates of  $\tau_{i,k}(Q_{i,k}, I_{i,k})$  are much smaller than in Fajgelbaum and Schaal (2017), but the resulting trade flows seem to be ok. I will have to do some fine tuning on this.

#### 4.4 Derive productivity measures

I need a spatial distribution of innate productivity characteristics for each location. Since I have population and lights data, this should be relatively easy to back out. However, I initially confronted some problems with this. Firstly, I only have lights data and not GDP data. Is it fair to say that people produce lights and hence in a production function like

$$Y_i = z_i L_i^\alpha \quad (5)$$

lights can readily serve as  $Y_i$ ? And if so, how can I circumvent the inevitable outlier-cell with hardly any population, but some remnant of lights, that will immediately render it hyperproductive? I used a couple of steps:

1. All cells with no population are immediately coded as no productivity.
2. I decide on  $\alpha = 0.7$  to circumvent a problem of overvaluing the contribution of small populations.
3. Then,  $z_i = \frac{Y_i}{L_i^\alpha}$  and can be readily computed for the entire dataset.

Results are promising. Capital cities tend to be more productive (even when they are bigger) than less populous cells. I should be able to go from here.

#### 4.5 Heterogeneous goods

The original model allows for differentiated goods (which aggregated in canonical CES form). I think this is a very useful property. However, it also blows up computation time, as for every new good adds another price field over which to optimise. I tried various ways to have 5, 10, or even 20 different goods, but while they produce fancy graphs for small countries, they are just not computationally feasible in large countries.

I hence propose the following compromise:

1. I introduce two different goods, an *urban good* and an *agricultural good*. Cities only produce the former, rural areas only produce the later (i.e. the respective productivity on the other good is zero.)
2. To identify urban areas, I code the most densely populated gridcells as urban and the least densely populated as rural.
3. I iteratively define the cutoff point for this as to match a country's 2016 total urbanisation rate, as reported by The World Bank (2017).<sup>2</sup> With this procedure, 7.3 per cent of locations are urban, but are home to 40 per cent of the population in the sample. A ratio which neatly compares to recent figures from Lall et al. (2017).

## 5 Computation of Optimal Networks

After all this heavy data lifting and calibration, I can now finally start to actually get the Matlab Code up and running. Since it takes long for larger countries, I've started with the smaller ones. Over one night, the code can calculate the optimal reallocation of a given transport network for the 40 smallest African countries, or the three biggest. Below is how some of this looks for the country of Gabon.

From this, one can easily derive a measure of how much welfare a country or even region would gain under this optimal reallocation procedure. For starters, I just calculated welfare gains as

$$\zeta_c = \frac{\text{Welfare under the optimal Infrastructure}_c}{\text{Welfare under the current Infrastructure}_c} \quad (6)$$

Note that for entire countries,  $\zeta_c \geq 0$  by construction. For individual regions, however,  $\zeta_c$  can take on any positive value, really.

Figures 5a to 5c show the spatial distribution of these welfare gains and losses under the optimal reallocation scenario.

I can also now rank all countries by the cumulative welfare gain they would achieve under the perfect reallocation scenario. Table 1 does so.

## 6 Potential research alleyways

$\zeta_c$  is representing whether an area would gain or lose with infrastructure under the optimal scenario. Broadly, there are two different pots of potential research questions. One has  $\zeta_c$  on the LHS and one has it on the RHS:

### 6.1 $\zeta_c$ on the LHS

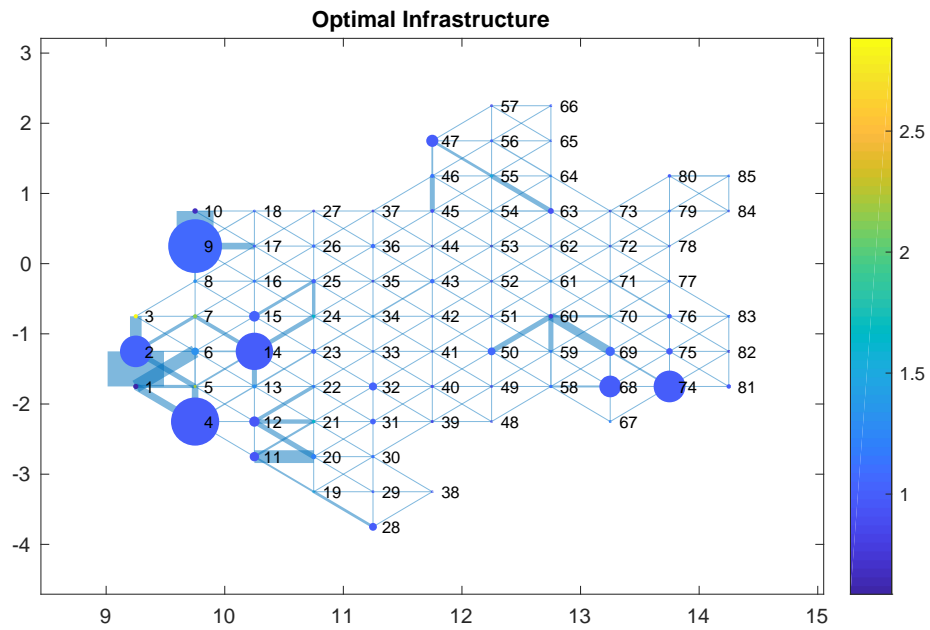
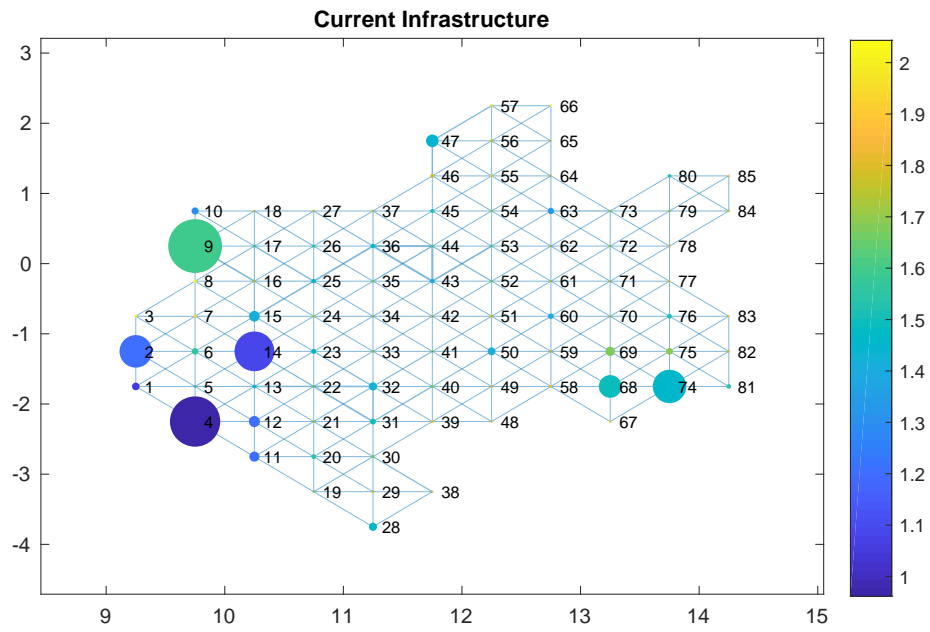
What determines why some areas are under-/overinvested in? Ideas could be

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<sup>2</sup>I start by assuming every location is a city and then gradually proceed to kick out the least densely populated locations, until the ratio of people living in urban areas to total population equals that of the WDI.

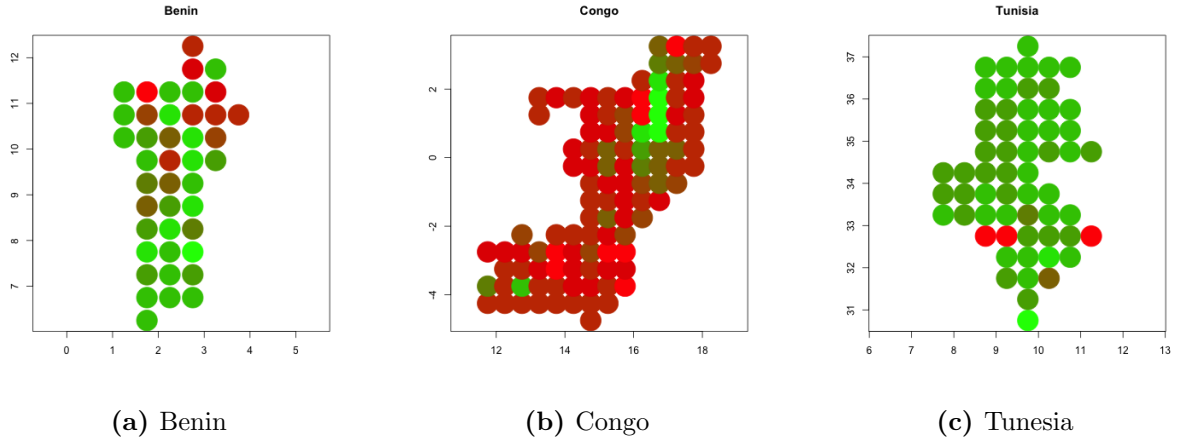


## Gabon



**Figure 4:** Optimal reallocation for Gabon

**Figure 5:** Spatial Distribution of  $\zeta_c$  for sample countries



- Colonial Legacies: do areas that had more colonial investment still enjoy more infrastructure than they should?
- Do areas from the ethnicity of the tribal leader enjoy too much infrastructure?

## 6.2 $\zeta_c$ on the RHS

This asks what the correlates / outcomes of being over/-underinvested in are. Michalopoulos and Papaioannou (2016) have a bunch of interesting outcomes like

- Political Violence in frequency, intensity, and kind from ACLED
- Ethnic power relations from EPR dataset
- Wellbeing from DHS dataset

For these, the unit of observation would be ethnicities. So I would have to aggregate my  $\zeta_c$  measure over the Murdock ethnicity map. Should be fine.

The trouble with both these approaches is that  $\zeta_c$  is obviously both an outcome and an effect in the intricate interplay of the political economy of African countries. I don't know to what extent I can actually do inference, or will just have to rely on correlations. We'll see.

## 7 Next steps

1. Optimise Matlab Code for better performance, or find better performance elsewhere (1 week)
2. Perform Network optimisations (1-2 weeks)

Immediate goal: Have optimal networks calculated by January 1, 2018.

**Table 1:** Sample Countries by  $\zeta_c$ 

Country	$\zeta_c$ in %
Guinea	2.81
Uganda	2.73
Ethiopia	2.68
Gabon	2.41
Sierra-Leone	2.16
Liberia	2.06
Zimbabwe	2.03
Eritrea	2.02
Burkina-Faso	1.88
Benin	1.64
Senegal	1.64
Lesotho	1.61
Cote-d'Ivoire	1.44
Equatorial-Guinea	1.35
Malawi	1.35
Togo	1.35
Guinea-Bissau	1.26
Ghana	1.09
Djibouti	1.05
Rwanda	0.84
Tunisia	0.53
Botswana	0.23
Western-Sahara	0.22
Burundi	0.13
Congo	0.12
Swaziland	0.00

## Past supervisor meetings; topics raised and answered

November 28, 2018

- Is it ok to use geometric centroids as opposed to population-weighted centroids? *Yes, it's fine. Ferdinand did this in Maurer et al. (2017).*
- Night Lights: do I have to translate them into GDP first? Fajgelbaum and Schaal (2017) use G-Econ, but that's only available for the year 1990 and in much coarser resolution. *Tough. But probably go for it just because it's easiest and no direct alternative comes to mind. Keep it at its easiest level. Kocornik-Mina et al. (2015) do use pure lights and cite Henderson et al. (2012) who find a Lights-GDP elasticity of 1.*
- Can I proceed to use Open Street Maps even though it has disadvantages as described below? *Yes.*
- Computational challenges looming. As soon as I'll start the Matlab bit, I will need either patience or better computing power. Does the department / chair grant access to remote desktops etc.? *Probably not.*
- Average speed a good proxy for Infrastructure Matrix  $I_{i,k}$ ? *Not really many other options.*

- The paper by Fajgelbaum and Schaal (2017) has been criticised for its heavy dependence on the congestion assumption (in words, that iceberg trade costs rely on current trade flows, or that  $\tau_{i,k}(Q_{i,k}, I_{i,k})$  is a function of  $Q_{i,k}$ ); namely by Allen and Arkolakis (2016). I think this criticism is overblown. Still worth keeping in mind. *Definitely cite and discuss this. But should be fine.*

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